

Theory of Computation (TCP)

- nature of computation - systematic application of mathematical and logical methods to describe and model algorithms, computational processes and their efficiency.
- design of computing machines, understanding the limitations of computation, classifying problems based on their complexity and study of automata and formal languages.

Module 1:- Fundamentals.

a^* ^{aka power} = $\overbrace{aaa \dots}^{\text{atleast one } a}$ 0 or n numbers of a
 Kleene closure $[a^+]$ Turing Machine

Basics :-

1) Alphabet - An alphabet (Σ) is defined as finite set of input symbols

$$\text{eg: } \Sigma = \{0, 1, 2\}$$

where 0, 1, 2 are symbols or letters.

2) Strings / sentence / word :- Finite sequence of symbols over given alphabet.

$$0, 1, 2, 01, 02, 12, \text{etc over } \Sigma \{0, 1, 2\}$$

word / string length :- No. of symbols present in given string

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Empty string - string of length 0 or null or empty
is called epsilon (ϵ)

Null transition - jump from one state to two
without taking inputs.

Language - set of strings which ~~are~~ over
alphabet.

eg:- $L = \{x \mid x \text{ ends in } 'ba' \text{ over } \Sigma = \{a, b\}\}$

should have condition.

Power of Alphabet - $(\Sigma^*)^k$

$$\Sigma^1 = \{a, b\}$$

$$\Sigma^2 = \{aa, ab, ba, bb\}$$

$$\Sigma^0 = \{\} = \{\epsilon\}$$

Substring :- String U is substring, if U occurs
as it is in same order.

$$W = GATE$$

$$U = \{\epsilon, G, A, T, E, GA, GT, GE, AT, AE, TE, GAT, GTE, GAE, ATE, GATE\}$$

Proper substrings. = 9

Complete word and ϵ not counted in
proper substring.

$$\text{Improper } n = 11$$

$$\text{Proper} = n \frac{(n+1)}{2}$$

$$\text{Improper} = \frac{n(n+1)}{2} + 1$$

Types of languages

~~regular~~
Regular
languages

Context
Free
language

Context
Sensitive
language

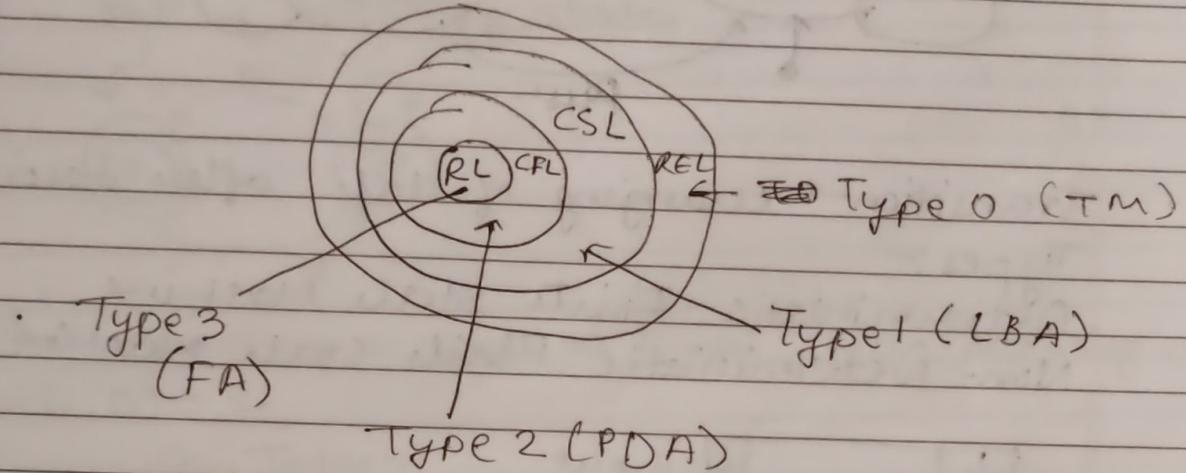
Recursively
Enumerable
language

↓
Finite
Automata

↓
Push Down
Automata

↓

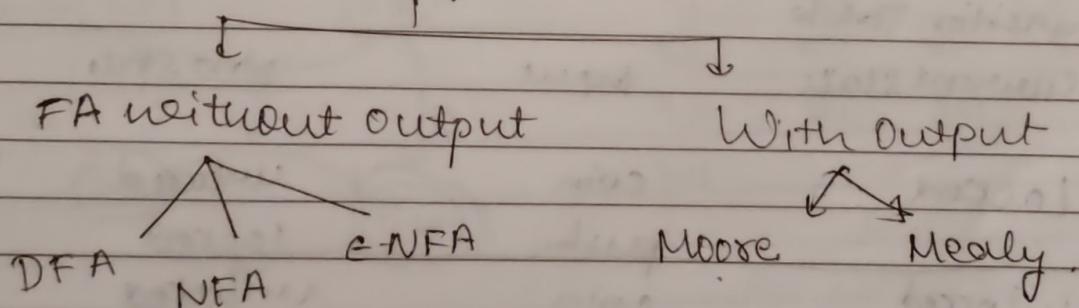
Turing
Machines



$TM > LBA > PDA > FA$

$T_0 > T_1 > T_2 > T_3$

Finite State Machine Classification



$1/0 - [FSM] - 0/p$

3 Tuples =

I - Input

O - Output

S - State

$\Sigma \rightarrow [FA] \rightarrow F$

5 Tuples =

• Σ - Input

Q - States

q_0 - Initial State

F - Final state

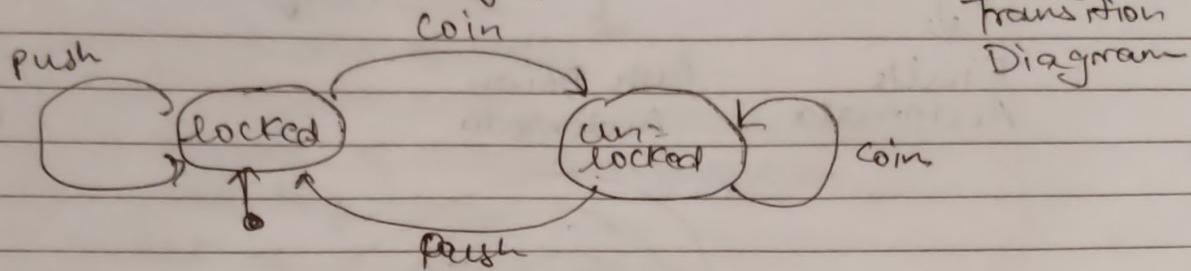
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8 - Transitions

Basics of FSM

1) Finite State Machine or Finite state Automata

- abstract Model of any problem

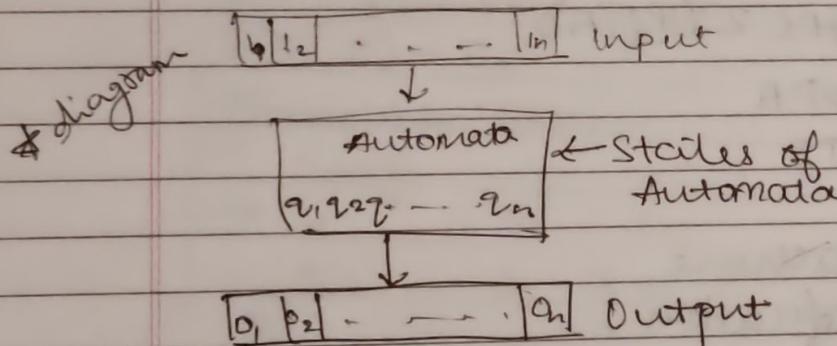


Transition → changing of state after receiving input

Types :-

Deterministic Finite State Machine

Non-Deterministic Finite State Machine



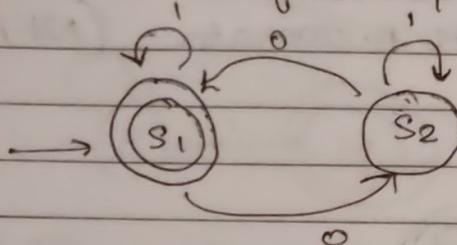
Transition Table

Current State	Input	Next State	Output
Locked	coin	unlocked	unlocks
unlocked	push	locked	None
unlocked	coin	unlocked	None
unlocked	push	locked	locks

No. of rows = No. of Transitions.

Deterministic FSM.

- Specific Output - Does not accept epsilon as input
- Five element Tuple
- Q - finite set of states
- Σ - Finite, non empty input alphabet.
- δ - series of transition function
- q_0 - starting state
- F - set of accepting states

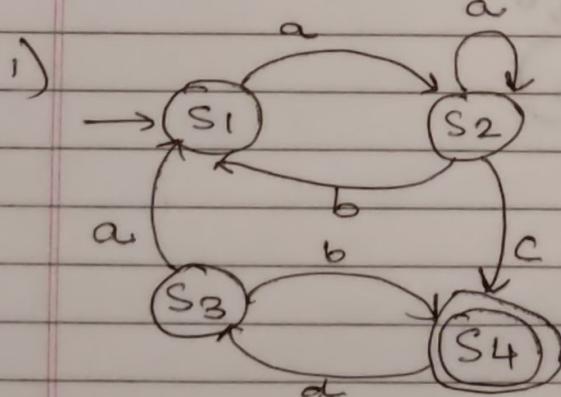


① → starting as well as final state / Accepting state
 $\delta(S_1, 0) = S_2$

Transition Table:-

state	0	1
s_1^*	s_2	s_1
s_2	s_1	s_2

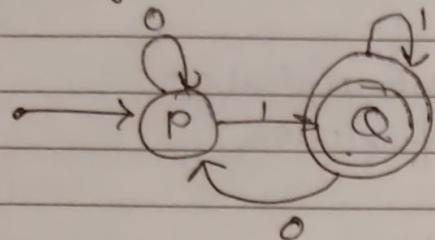
4 elements - 4 transitions



a	b	c	d
s_1	s_2		
s_2	s_2	s_1	s_4
s_3	s_1	s_4	
s_4			s_3

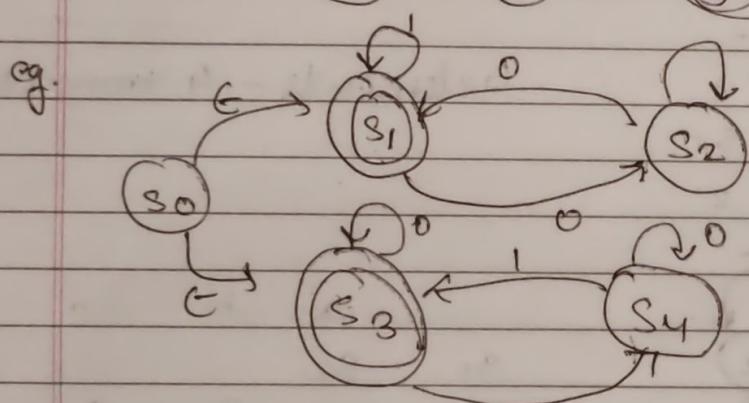
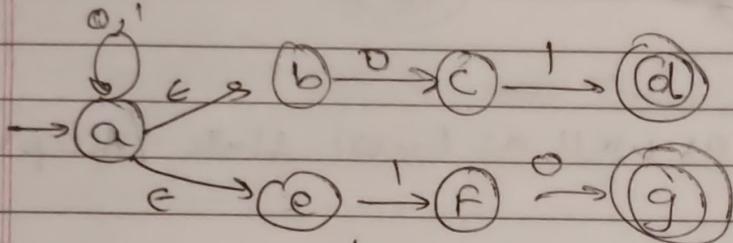
abacdaac	✓
abae	✓
aaaaac	✓
aaaacd	✗

2) Draw a diagram for DFA. Language of all strings that end with 1.

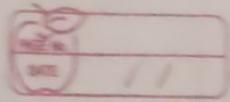


2) Non-Deterministic Finite Automata - (NFA)

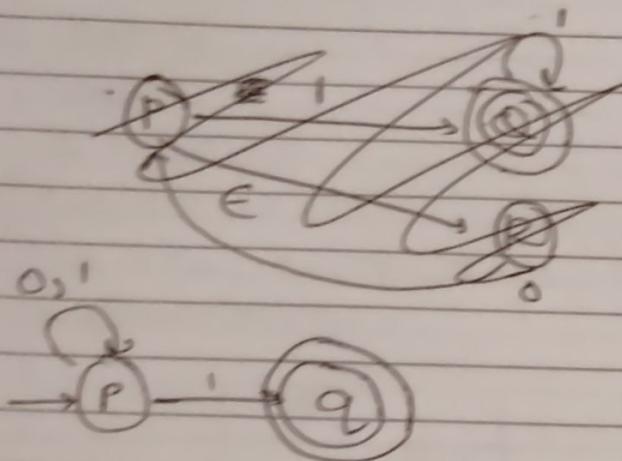
- Accept epsilon as input
- Five element tuple



- a) 1 ✓
- b) 01001 ✓
- c) 1011101 ✓
- d) 1000 X
- e) 0 ✓

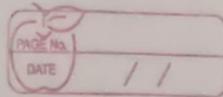


2) Language of all strings that end with 1.



Type 3) NFA with epsilon ~~not~~ transitions [Not compulsory]

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Type 2: \rightarrow Ending with .

//

Design a FSM to accept strings which are ending with '110' over the $\Sigma = \{0, 1\}$

 \rightarrow

1. Theory

2. Logic

$$I = \{0, 1\}$$

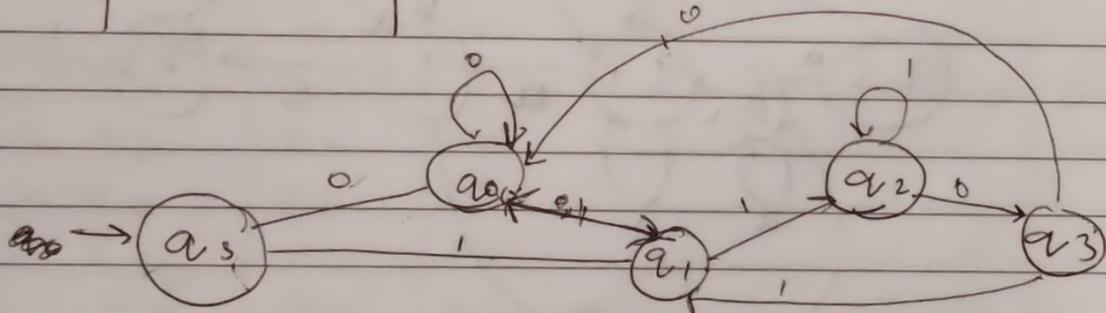
$$\Sigma = \{0, 1\}$$

$$S = \{q_0, q_1, q_2, q_3\}$$

3. Implementation.

$$0-0'-0'-0''$$

	\circ	+	$\frac{00}{11} = \frac{01}{11}$
$\rightarrow q_3$	$q_0 \cdot 1N^*$	$q_1 \cdot 1N$	$\xrightarrow{\frac{00}{11}} \xleftarrow{\frac{01}{11}}$
$0 q_0$	$q_0 \cdot 1N^*$	$q_1 \cdot 1N$	
$1 q_1$	$q_0 \cdot 1N^*$	$q_2 \cdot 1N$	
$11 q_2$	$q_3 \cdot 1N$	$q_2 \cdot 1N$	
<u>$110 q_3 *$</u>	<u>$q_0 \cdot 1N$</u>	<u>$q_1 \cdot 1N$</u>	
q₄			



6. Simulation.

- ($q_0, 011010$)
- + ($q_0, 11010, N$)
- + ($q_1, 1010, NN$)
- + ($q_2, 010, NNN$)
- + ($q_3, 10, NNNN$)
- + ($q_1, 0, NNNN$)
- + ($q_0, NNNN$)
- Reject

2) 'babbb' over $\Sigma = \{a, b\}$.

→ 1. Theory

2. Logic

$$I = \{a, b\}$$

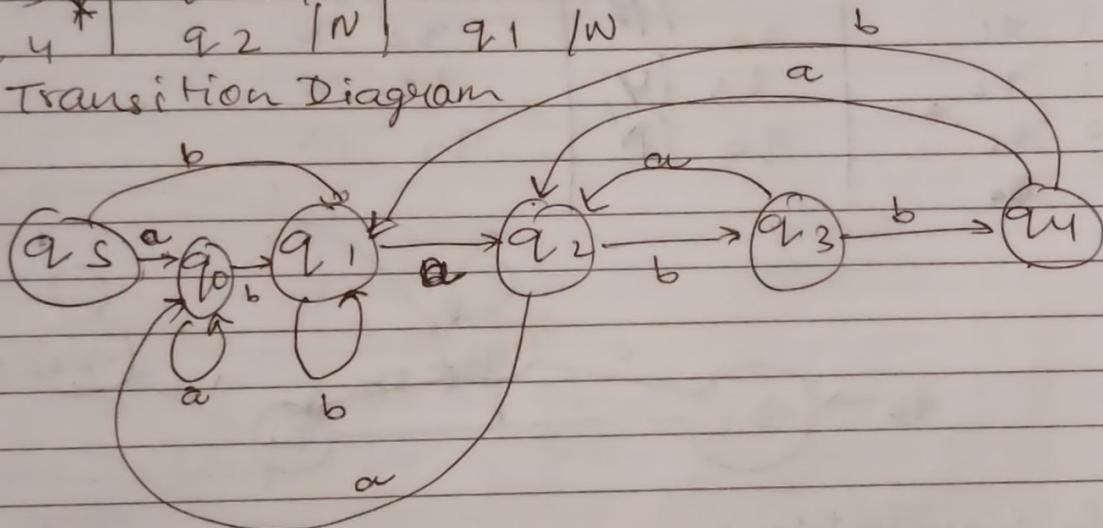
$$O = \{q_0, q_1, q_2, q_3, q_4\}$$

$$S = \{q_{25}, q_1, q_2, q_3, q_4\}$$

3. Implementation.

	a	b	<u>babba</u>
→ q_0	$q_0 N$	$q_1 N$	
q_0	$q_0 N$	$q_1 N$	
b q_1	$q_2 N$	$q_1 N$	
ba q_2	$q_0 N$	$q_3 N$	
bab q_3 *	$q_2 N$	$q_4 Y$	
$babb$ q_4 *	$q_2 N$	$q_1 N$	

4. Transition Diagram



5. Simulation

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Type 3:- Strings containing ^{Type}_{Trap State}

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1) Design a FSM to accept strings which contains '1011' over inputs $\Sigma = \{0, 1\}$

- 1. Theory (Remains same)
- 2. Logic

	0	1
→ q_0	q_0/N	q_1/N
0 q_0	q_0/N	q_1/N
1 q_1	q_2/N	q_1/N
10 q_2	q_0/N	q_3/N
101 q_3	q_2/N	q_4/Y
1011 q_4^*	q_4/Y	q_4/Y

2) 'bba' $\Sigma = \{a, b\}^3$

1.

2.

3.

	a	b
→ q_0	q_0	q_1
a q_0	q_0	q_1
b q_1	q_0	q_2
bb q_2	q_3	q_1
bba q_3^*	q_3	q_3

Type 4:- String Not containing Type

Type 4:- Does not contain

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i) Does not contain consecutive b's over $\Sigma = \{a, b\}$

	a	b
q_5^*	$q_0/4$	$q_1/4$
q_0^*	$q_0/4$	$q_1/4$
q_1^*	$q_0/4$	$q_2/4$
q_2^*	$q_0/4$	q_3/N
q_3	q_3/N	q_3/N

Trap State or Dead State

Accepting state or Final State ↑
 Not final or
 Not Accepting State

Type 5 :- Strings containing ODD/EVEN SEQUENCE

1. FSM to accept strings containing odd number of a's.

	a	b
$\rightarrow q_5$	q_0	q_1
Odd q_0^*	q_1	q_0
Even q_1	q_0	q_1

Type 6 :- EVEN AND ODD.

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- Design string containing even number of a's and odd number of b's.

	a	b
→ q_0	q_1	q_1 q_1
odd odd q_0	q_2	q_1
odd even q_1	q_3	q_0
even odd q_2 *	q_0	q_3
even even q_3	q_1	q_2

abbaab X

{ q_1 baab } \checkmark

{ q_1 aab } \checkmark

{ }

bababb. ✓

Type 7 :- Strings containing mixed sequence of a's and b's

Final states

- FSM :- a) Exactly 3a's $\rightarrow q_3$
- b) Atleast 3a's $\rightarrow q_3, q_4$
- c) Atmost 3a's $\rightarrow q_5, q_1, q_2, q_3$

	a	b
q_5	q_1	q_0
① q_0	q_1	q_0
→ q1 q_1	q_2	q_1
→ aa q_2	q_3	q_2
→ aaaa q_3	q_4	q_3
More than 3a's q_4	q_4	q_4

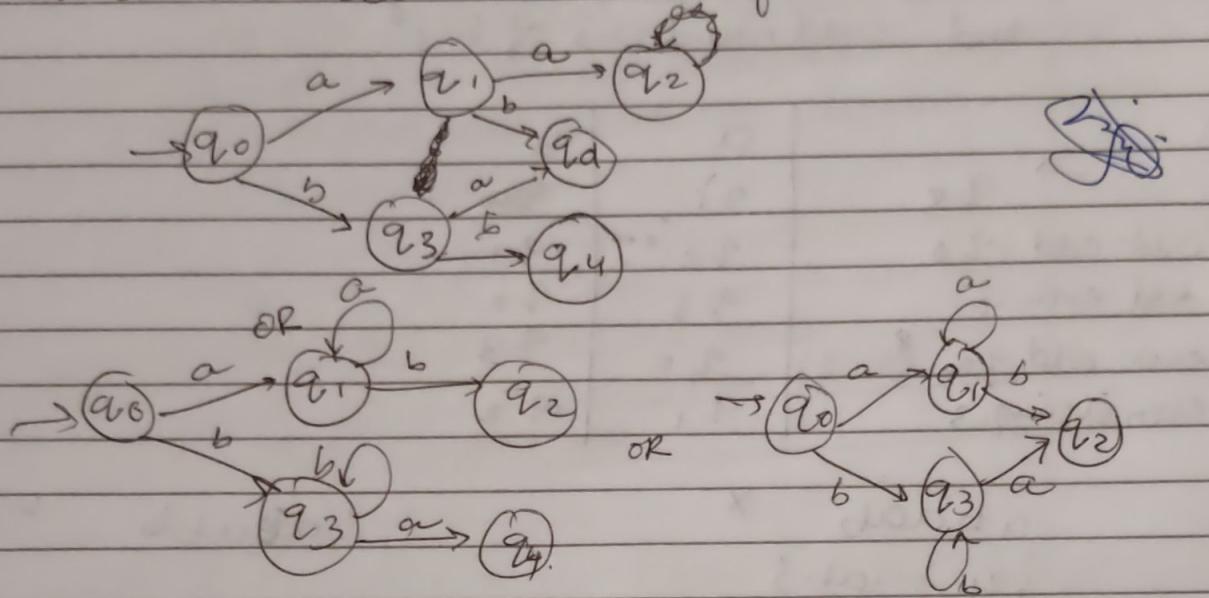
Type 8:- Misc. Examples .

* Start with "

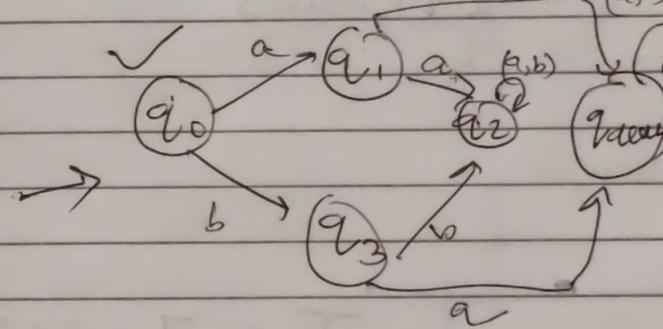
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DFA

- Starts with aa or with bb from {a, b}



	a	b
q_0	q_1	q_3
q_1	q_2	qdead
q_3	qdead	q_2
q_{dead}	q_{dead}	q_{dead}



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Module 2:-

Regular Languages and Expressions.

The set of strings accepted by finite automata is known as Regular expression language. Expression used to describe regular language is known as Regular Expression.

$+$ \rightarrow OR / Union

$*$ \rightarrow Closure / All combi

\cdot \rightarrow Concatenation / AND

\emptyset \Rightarrow Empty set

Σ \Rightarrow Σ^3

Kleene's Closure

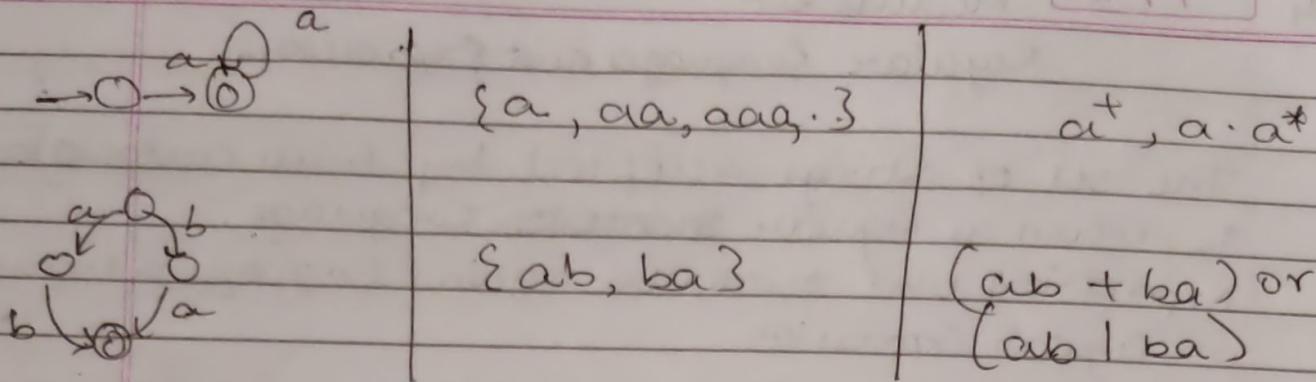
$$a^* = \{\epsilon, a^0, a^1, a^2, \dots\}$$

$$\text{we can say that } a^+ = a \cdot a^*$$

Additive Closure

$$a^+ = \{a^0, a^1, a^2, a^3, \dots\}$$

Automata	Language	Regular Expression
$\xrightarrow{\epsilon} \textcircled{0}$	$\{\epsilon\}$	ϵ
$\xrightarrow{a} \textcircled{0} \xrightarrow{a} \textcircled{0}$	$\{aa\}$	a
$\xrightarrow{a} \textcircled{0} \xrightarrow{b} \textcircled{0}$	$\{a, b\}$	$a+b, a b$
$\xrightarrow{\epsilon} \textcircled{0} \leftarrow \textcircled{0}$ or $\xrightarrow{\epsilon} \textcircled{0}$	ϕ	ϕ
$\xrightarrow{a} \textcircled{0}$	$\{\epsilon, a, aa, aaa, \dots\}$	a^*



- 1.) Set of all the strings that start with "a" over $\Sigma = \{a, b\}$

$$R.E = a \cdot (a+b)^*$$

$$L(R) = \{a, aa, ab, aaa, \dots\}$$

2. Set of all strings ends with 0 or 1.

$$\Sigma = \{0, 1\}$$

$$R.E = \cancel{(0+1)^*} \cdot (0+1) \text{ or } (0+1)^* \cdot 0 + (0+1)^* \cdot 1$$

$$L(R) = \{0, 1, 00, 01, 10, 11, \dots\}$$

3. Strings that starts with a and ends with b.

$$\text{Over } \Sigma = \{a, b\}$$

$$\rightarrow R.E = a \cdot (a+b)^* \cdot b$$

$$L(R) = \{ab, aab, abb, \dots\}$$

4. String start with x and ends with xy over

$$\Sigma = \{x, y\}$$

merge pattern

$$\rightarrow R.E = x \cdot (x+y)^* \cdot (x,y) + xy$$

$$L(R) = \{xx, xy, axyxy, axxyyxy, \dots\}$$

5. starts with abb, ends with bba

\rightarrow $abb(a+b)^*bba + abba + abbbba$

$R \cdot E \rightarrow FA$

Rules of Conversion.

Rule 1:- $\rightarrow O \quad \textcircled{O} \quad \text{For } R \cdot E = \emptyset$

Rule 2:- $\xrightarrow{\text{start}} \textcircled{O} \quad \text{For } RE = E$

Rule 3:- Start $\rightarrow O \xrightarrow{a} \textcircled{O}$ $\text{For } RE = a$

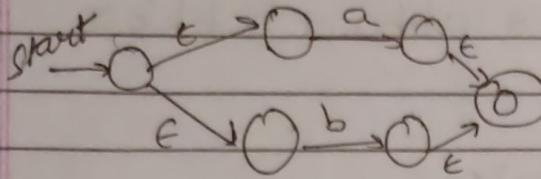
Rule 4:- $\rightarrow O \xrightarrow{} \textcircled{O R_1 O} \xrightarrow{} \textcircled{O}$ $\xrightarrow{} \textcircled{O R_2 O} \xrightarrow{} \textcircled{O}$ $\text{For } R \cdot E = R_1 + R_2$

Rule 5:- $\rightarrow (\textcircled{O R_1 O}) \xrightarrow{} (\textcircled{O R_2 O}) \quad \text{For } R \cdot E \Rightarrow R_1 \cdot R_2$

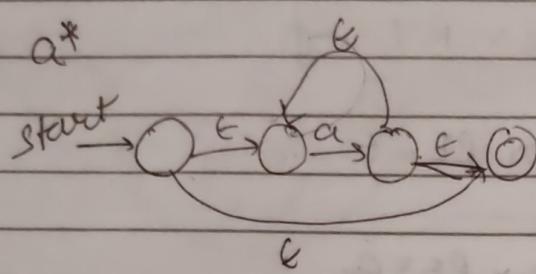
Rule 6:- $\rightarrow O \xrightarrow{E} \textcircled{O R_1 O} \xrightarrow{E} \textcircled{O} \xrightarrow{E} \textcircled{O} \quad \text{For } R \cdot E \Rightarrow R_1^*$

1. Convert :-

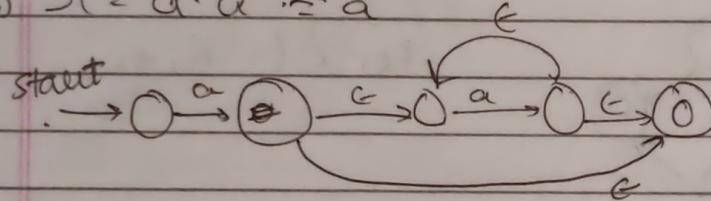
i) $\sigma_1 = a + b$



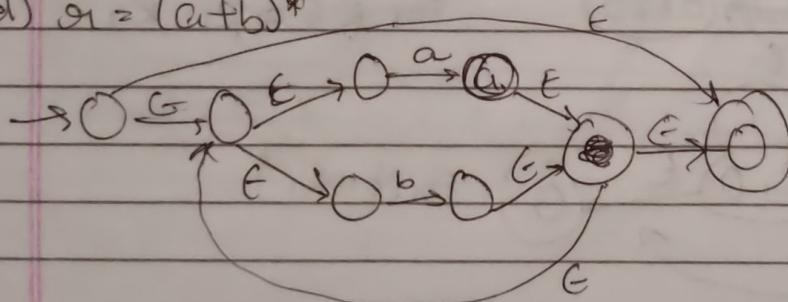
b) $\sigma_1 = a^*$



c) $\sigma_1 = a \cdot a^* = a^+$



d) $\sigma_1 = (a+b)^*$

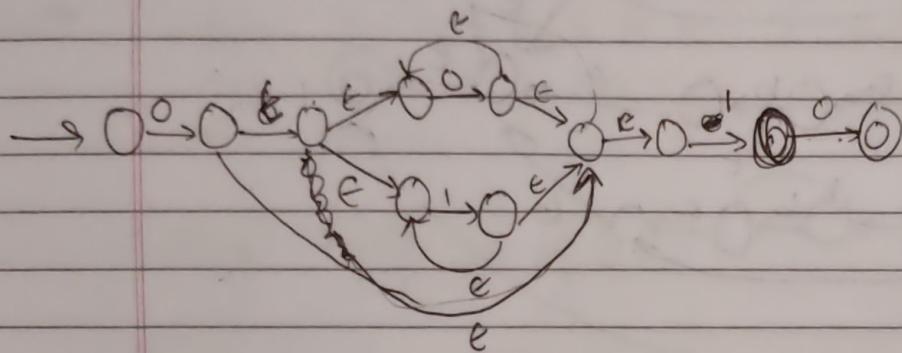


2. Construct F.A.

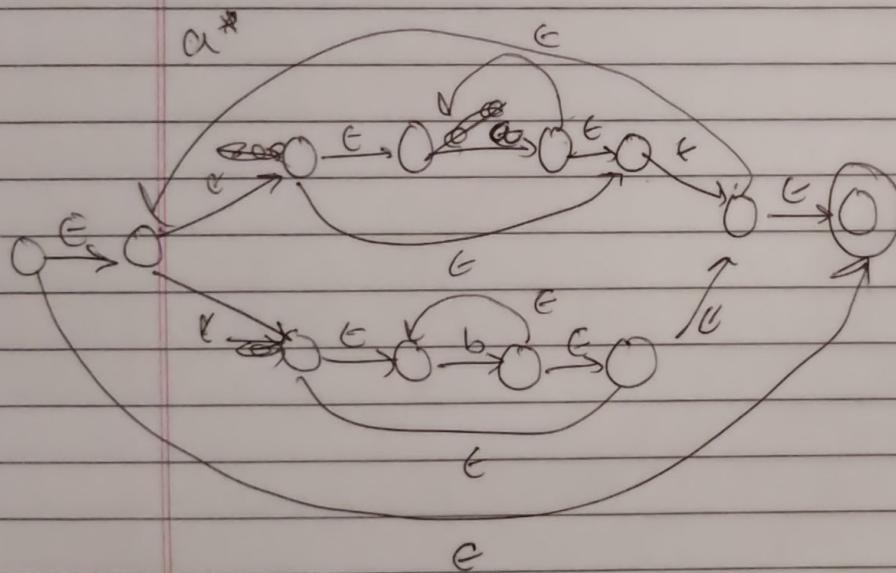
$$O.(O+A)^*.10$$

$\downarrow \quad \downarrow \quad \downarrow$
A B C

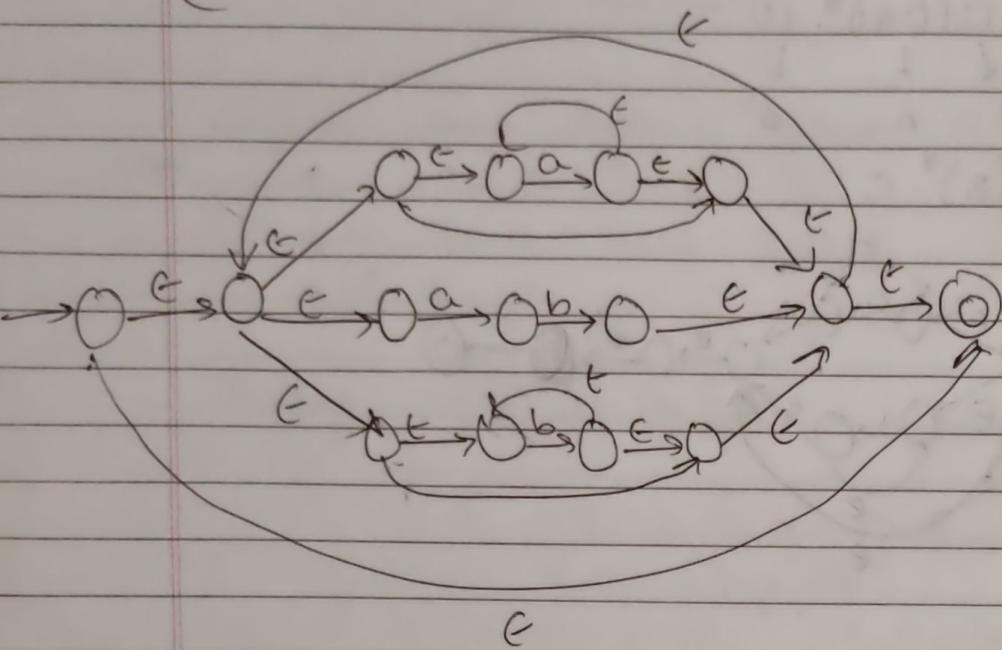
$$A.(B)^*.C$$



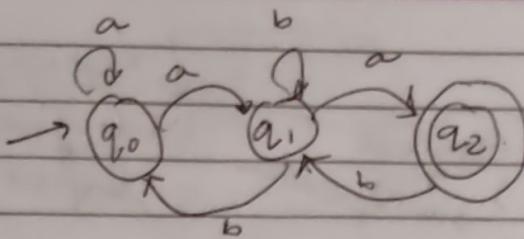
3) $r = (a^* + b^*)^*$ $c = (A+B)^*$



$$(a^* + ab + b^*)^4$$



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Solve using Döder's Theorem. FA to R.E

$$\rightarrow \begin{aligned} q_0 &= q_0 \cdot a + q_1 \cdot b + \epsilon & -① \\ q_1 &= q_0 \cdot a + q_1 \cdot b + q_2 \cdot b & -② \\ q_2 &= q_1 \cdot a & -③ \end{aligned}$$

Putting eq ③ in eq ②

$$q_1 = q_0 \cdot a + q_1 \cdot b + q_1 \cdot a \cdot b$$

$$\therefore = q_0 \cdot a + q_1 (b + ab)$$

$$q_1 = q_0 \cdot a + (b + ab)^* \rightarrow \text{Further solve for } [q_0, a]$$

$$R = Q + RB$$

DFA Minimization.

↓ Myhill-Nerode
Theorem (Box method)

Classical method
involving ϵ moves

Direct method
(no ϵ)

subset generation

DFA given as
input

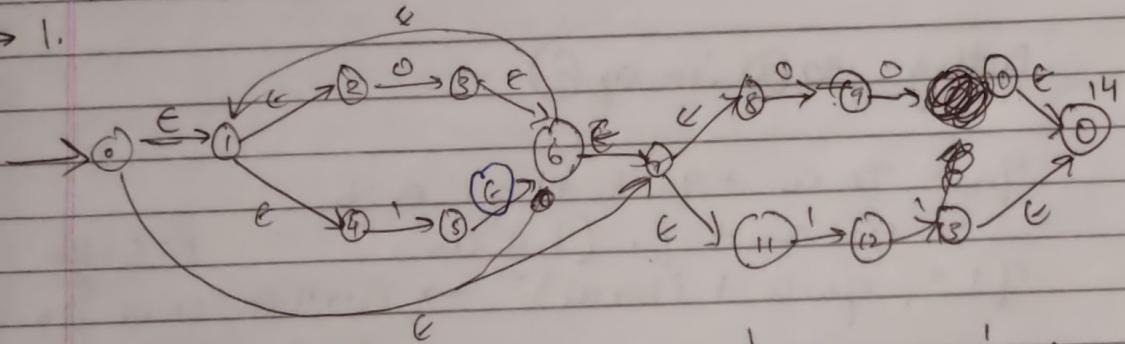
1. RE to NFA
2. NFA to DFA
3. DFA to Min DFA

1. NFA to DFA

2. DFA to Min DFA

$$1. \text{ RE} = (0+1)^* (00 + 11)$$

→ 1.



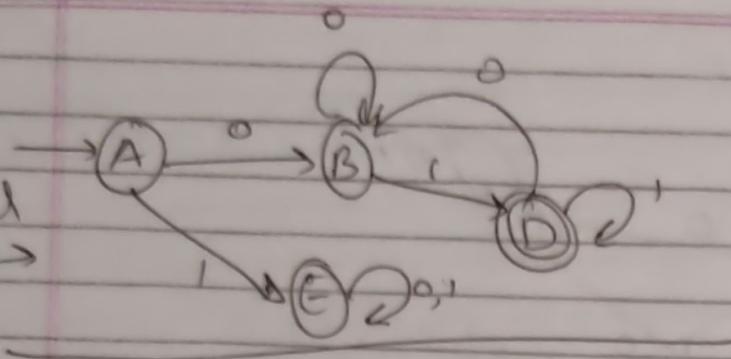
ϵ -closure Table

x	$y = \epsilon - \text{closure}(x)$	$\delta(y, 0)$	$\delta(y, 1)$
A $\{0\}$	$\{0, 1, 2, 4, 7, 8, 11\}$	$\{3, 9\}$	$\{5, 12\}$
B $\{3, 9\}$	$\{3, 6, 7, 8, 11, 1, 2, 4, 9\}$	$\{3, 9, 10\}$	$\{5, 12\}$
C $\{5, 12\}$	$\{5, 6, 7, 8, 11, 1, 2, 4, 13\}$	$\{3, 9\}$	$\{5, 12, 13\}$
D $\{3, 9, 10\}$	$\{1, 2, 3, 4, 6, 7, 8, 9, 11, 10, 14\}$	$\{3, 9, 10\}$	$\{5, 12\}$
E $\{5, 12, 13\}$	$\{1, 2, 4, 5, 6, 7, 8, 11, 12, 13, 14\}$	$\{3, 9\}$	$\{5, 12, 13\}$

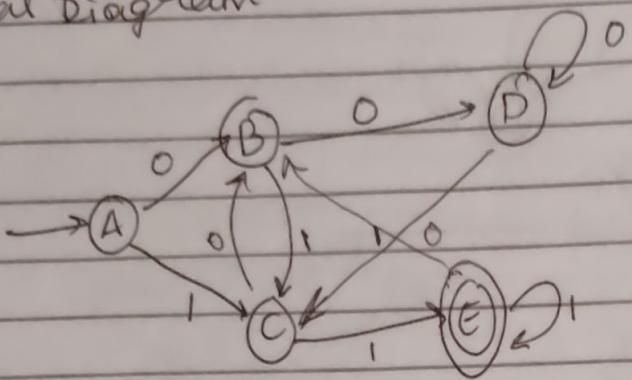
Q	ϵ	0	1
A		B	C
B		D	C
C		B	E
D*		D	C
E*		B	E

↓ 14 initial final
states
 ϵ -closure me
14 Dar ϵ me
hai

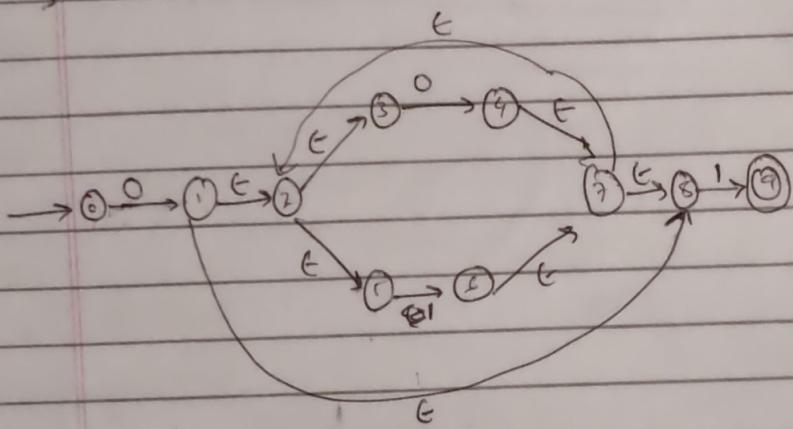
Final DFA



Final diagram.



2) RE to DFA $\Rightarrow 0(0+1)^* 1$



x	$y = \epsilon\text{-closure}(x)$	$\delta(y, 0)$	$\delta(y, 1)$
A $\{0\}$	$\{0\}$	$\{1\}$	$\{3\}$
B $\{1\}$	$\{0, 1, 2, 5, 8\}$	$\{4\}$	$\{6, 9\}$
C $\{4\}$	$\{4, 7, 2, 3, 5, 8\}$	$\{4\}$	$\{6, 9\}$
D $\{6, 9\}$	$\{6, 7, 8, 2, 3, 5, 9\}$	$\{4\}$	$\{6, 9\}$
E $\{3\}$	$\{3\}$	$\{3\}$	$\{3\}$

\rightarrow	A	B	E	A	B	E
[B	C	D	B	B	D
C	C	D	D	D*	B	D
D*	C	D	D	E	E	E
E	E	E	E	(A)	(B)	(E)

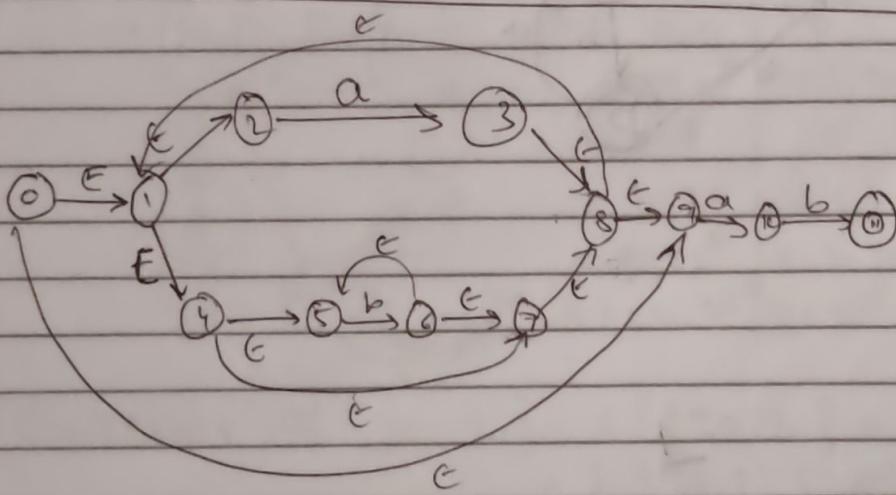
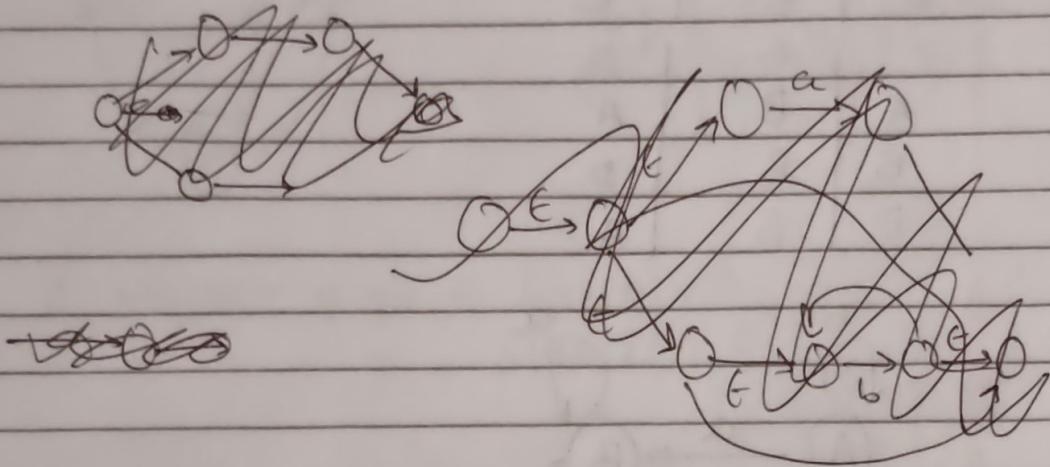
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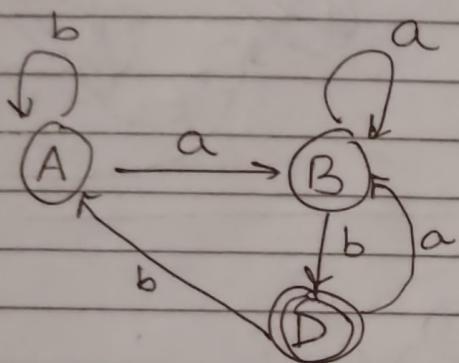
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$$1) R.E (a+b^*)^* ab.$$



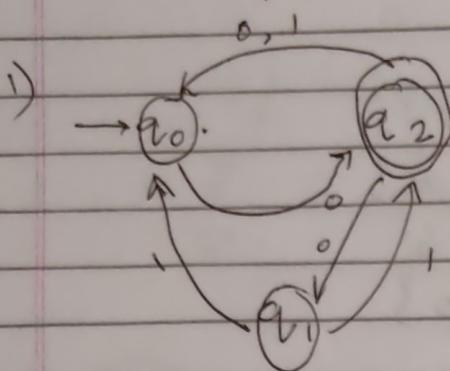
x	$y = E - \text{closure}(x)$	$\delta(y, a)$	$\delta(y, b)$
A $\{0\}$	$\{0, 1, 2, 4, 5, 7, 8, 9\}$	$\{3, 10\}$	$\{6\}$
B $\{3, 10\}$	$\{3, 8, 9, 1, 2, 4, 5, 7, 10\}$	$\{3, 10\}$	$\{6, 11\}$
C $\{6\}$	$\{5, 6, 7, 8, 1, 2, 4, 5, 9\}$	$\{3, 10\}$	$\{6\}$
D* $\{6, 11\}$	$\{6, 5, 7, 8, 9, 1, 2, 4, 5, 10\}$	$\{3, 10\}$	$\{6\}$

	a	b
→	A'	B
B	B	D
C	B	C
D*	B	C
	a	b
A	B	A
B	B	D
D	B	A



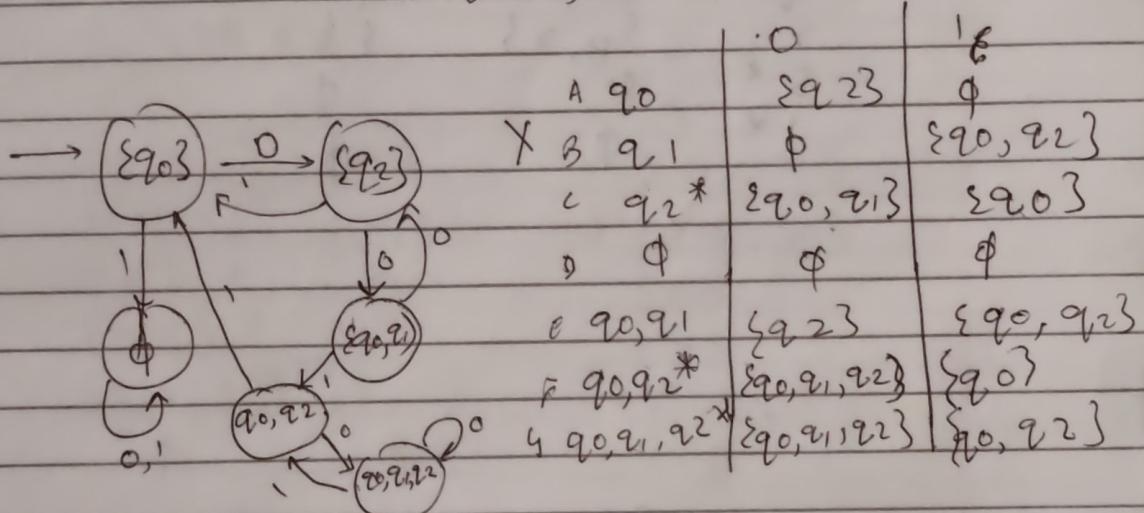
• 17/08/24

Subset generation or Direct Method.



	0	1
$\rightarrow q_0$	$\{q_2\}$	\emptyset
q_1	\emptyset	$\{q_0, q_2\}$
q_2^*	$\{q_0, q_1\}$	$\{q_0\}$

Step 1. 0 successor of $q_0 \Rightarrow S(q_0, 0) = q_2$
 1 " $S(q_0, 1) = \emptyset$



$$\begin{aligned}
 &\text{successor of } \{q_0, q_1\} - S(\{q_0, q_1\}, 0) \\
 &= S(q_0, 0) \cup S(q_1, 0) \\
 &= q_2 \cup \emptyset \\
 &= \{q_2\}
 \end{aligned}$$

HW

2) NPA to DPA

	O	I
$\epsilon_P \}$	$\{\epsilon_q, \epsilon_t \}$	$\{\epsilon_q \}$
ϵ_q^*	$\{\epsilon_r \}$	$\{\epsilon_q, \epsilon_t \}$
ϵ_r	$\{\epsilon_s \}$	$\{\epsilon_p \}$
ϵ_s^*	\emptyset	$\{\epsilon_p \}$

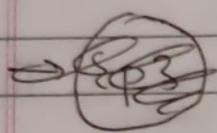
3)

	O	I
ϵ_P	$\{\epsilon_P, \epsilon_q \}$	$\{\epsilon_P \}$
ϵ_q	$\{\epsilon_r, \epsilon_s \}$	$\{\epsilon_t \}$
ϵ_r	$\{\epsilon_P, \epsilon_r \}$	$\{\epsilon_t \}$
ϵ_s^*	\emptyset	\emptyset
ϵ_t^*	\emptyset	\emptyset

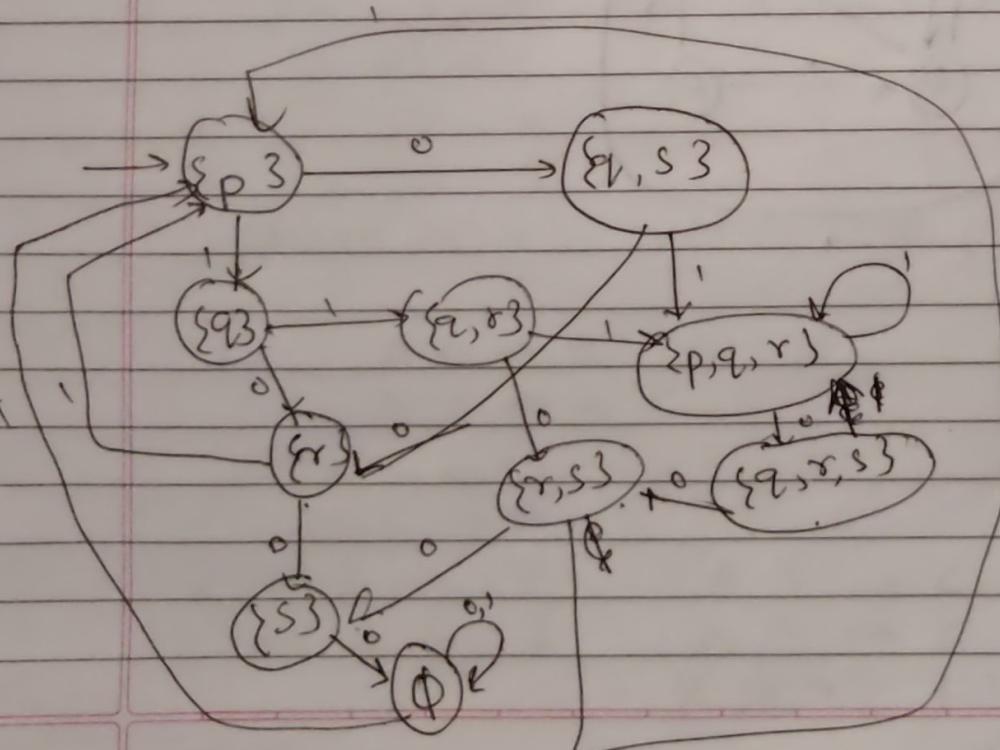
NFA TO DFA

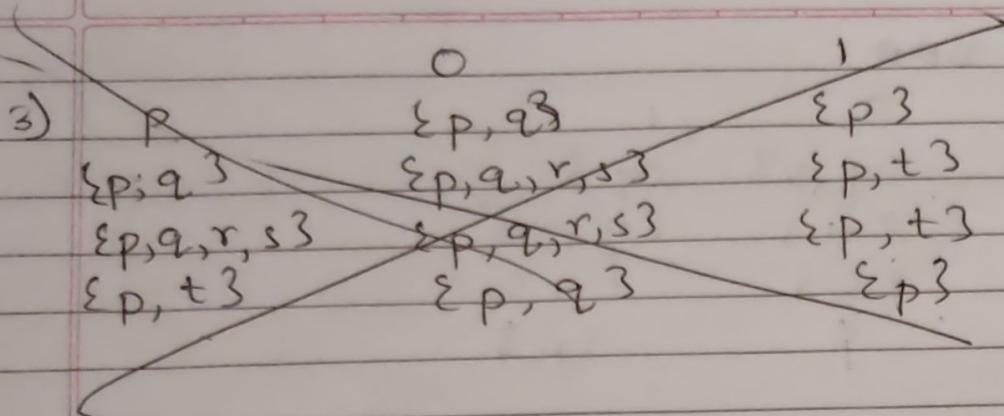
1.

	0	1
$\epsilon_P \}$	$\epsilon_q, s \}$	$\epsilon_q \}$
q^*	$\epsilon_{q,s} \}$	$\epsilon_{q,r} \}$
r	$\epsilon_s \}$	$\epsilon_p \}$
s^*	\emptyset	$\epsilon_p \}$



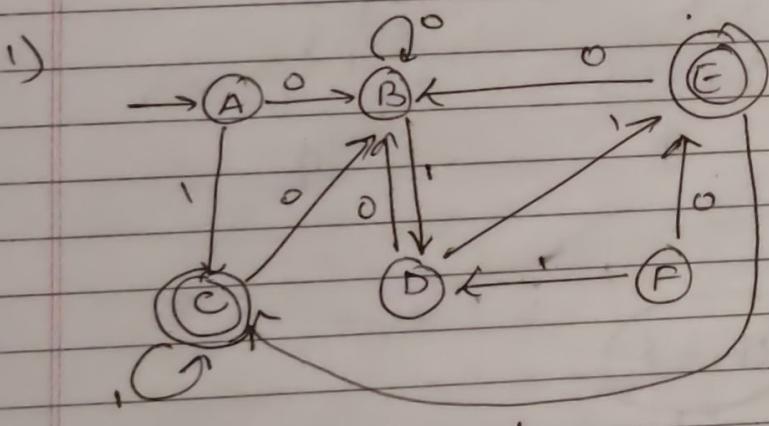
	0	1
$\epsilon_P \}$	$\epsilon_q, s \}$	$\epsilon_q \}$
$\epsilon_q \}$	$\epsilon_{q,r} \}$	$\epsilon_{q,r} \}$
$\epsilon_q, s \}$	$\epsilon_{q,r} \}$	$\epsilon_{p,q,r} \}$
$\epsilon_{q,r} \}$	$\epsilon_s \}$	$\epsilon_p \}$
$\epsilon_s \}$	\emptyset	$\epsilon_p \}$
$\epsilon_{p,q,r} \}$	$\epsilon_{q,r} \}$	$\epsilon_{p,q,r} \}$
$\epsilon_{p,q,r} \}$	\emptyset	\emptyset





Box Method (Myhill-Nerode Theorem)

1. Remove all states which are not reachable from start.
2. Create tables such that rows or columns can be identified by state numbers.
3. All those cells in which 1 state is final & other is non-final should be marked ①.



Step1:- Eliminate F (not reachable)

2:- Table:-

A, E	O	I	
$\rightarrow A$	B	C	[omit first row]
B*	B	D	for col
C*	B	E	[omit last row]
D*	B		for last rows
E*	B	C	

3.	B	2		
*	C	1	1	
*	D	X	2	1
*	E	1	1	X*
	A	B	C	D

one final
one nonfinal move

4. a is input $\{p, q\}$ state
 $\{p, a\} = r \quad]$ No decision
 $\{q, a\} = s \quad]$

if $\{p, a\} = r$

$\{q, a\} = s$

check $\{r, s\}$ if marked then $\{p, q\}$ as ②

like $A, O \rightarrow B$
 $B, O \rightarrow B$

$A, I \rightarrow C$

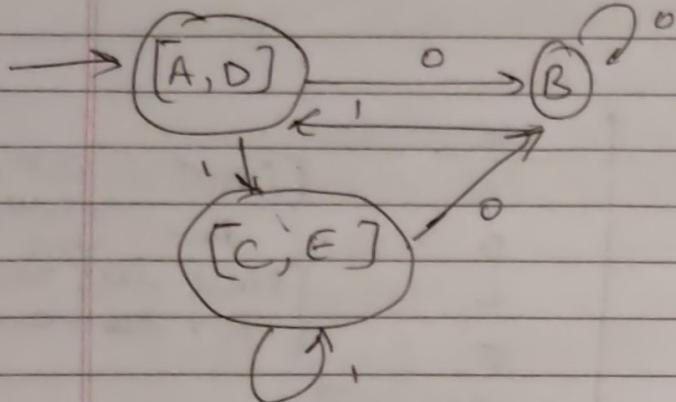
$B, I \rightarrow D$

$A, O - B \quad]$
 $D, O - B \quad]$

$A, I \rightarrow C \quad]$ Not marked
 $D, I \rightarrow E \quad]$ list them together
 $(A, D) \Rightarrow (C, E) \rightarrow$ may merge

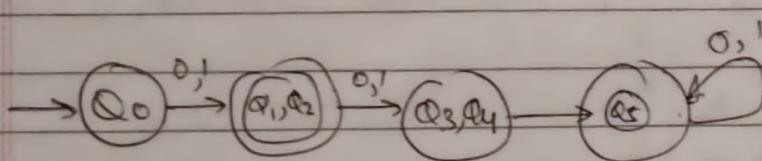
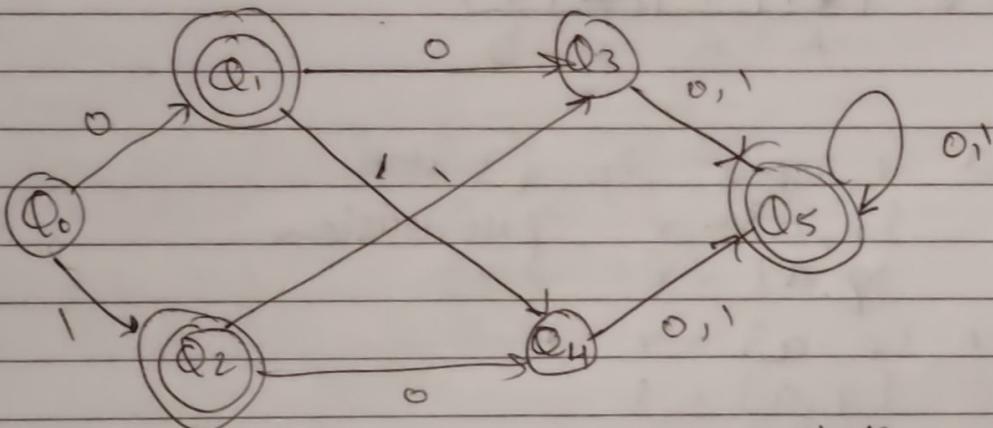
$$\begin{array}{l} B, 0 \rightarrow B \\ D, 0 \rightarrow B \end{array}$$

$$\begin{array}{l} B, 1 - D \\ D, 1 = E \end{array}$$



	0	1
$\rightarrow A, D$	B	C, E
C, E^*	B	C, E
B	B	A, D

~~HW~~



states	inputs
Q_0	Q_1, Q_2 Q_1, Q_2
Q_1Q_2	Q_3Q_4 Q_3Q_4
Q_3Q_4	Q_5 Q_5
Q_5	Q_5 Q_5

24/08/24

FA with output: Moore & Mealy Machines.

- No final states

1. Moore \rightarrow output depends on each state
2. Mealy \rightarrow Associated with Transitions.

Mealy machine. ($Q, \Sigma, O, \delta, X, q_0$)

$Q \rightarrow$ Finite set of states

$\Sigma \rightarrow$ Input

$O \rightarrow$ Output

$\delta \rightarrow$ input transition function $\delta: Q \times \Sigma \rightarrow Q$

$X \rightarrow$ output $\dots \dots \dots X: Q \times \Sigma \rightarrow O$

$q_0 \rightarrow$ initial state

1. Design a mealy machine to output X , if the i/p ends in 101, otherwise Y over $\Sigma = \{0, 1\}$

→

Step 1. Theory.

Step 2. Logic

$$M = (Q, \Sigma, O, \delta, X, q_0)$$

$$\Sigma = \{0, 1\} \quad \delta: Q \times \Sigma \rightarrow Q$$

$$O = \Sigma \times \{X, Y\}$$

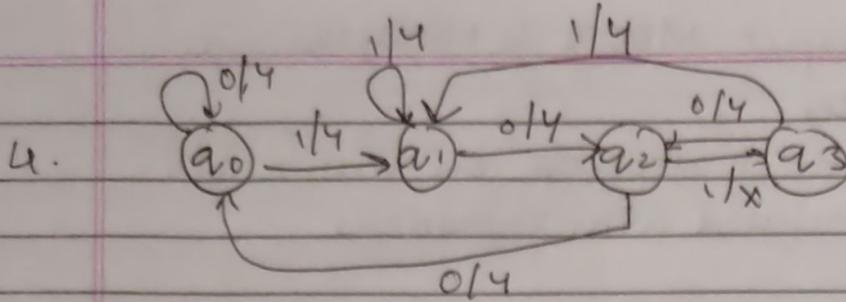
$$X = Q \times \Sigma \rightarrow O \quad Y = \Sigma \times \{X, Y\}$$

3: Transition Table.

!!

$\delta \Rightarrow Q \setminus \Sigma$	0	1	
$\rightarrow q_0$	$q_0 Y$	$q_1 Y$] merge
0 q_0	$q_0 Y$	$q_1 Y$	
1 q_1	$q_2 Y$	$q_1 Y$	
10 q_2	$q_0 Y$	$q_3 X$	
101 q_3	$q_2 Y$	$q_1 Y$	

MAP $X: Q \times \Sigma \rightarrow O \rightarrow q_0$	0	1
1 q_1	Y	Y
10 q_2	Y	X
101 q_3	Y	Y



5.	$s(q_0, 10110_1)$	$s(q_0, 110100)$
	$s(q_1, 01101)_Y$	$s(q_1, 10100)_Y$
	$s(q_2, 1101)_YY$	$s(q_1, 0100)YY$
	$s(q_3, 101)YYX$	$s(q_2, 100)YYYY$
	$s(q_1, 01)YYXY$	$s(q_3, 00)YYYYX$
	$s(q_2, 1)YYXY$	$s(q_2, 0)YYYYX$
	$s(q_3, \Sigma)YYXY$	$s(q_3, \Sigma)YYYYX$

2) Design a mealy m/c to change each occurrence of abb to aba.

→ Table:-

	a	b	
→ q_s	q_0	q_1 — merge	
$a q_0$	q_0	q_2	
$b q_1$	q_0	q_1 — merge	
$abb q_2$	q_0	q_3^*	
$abb q_3$	q_0	q_1	

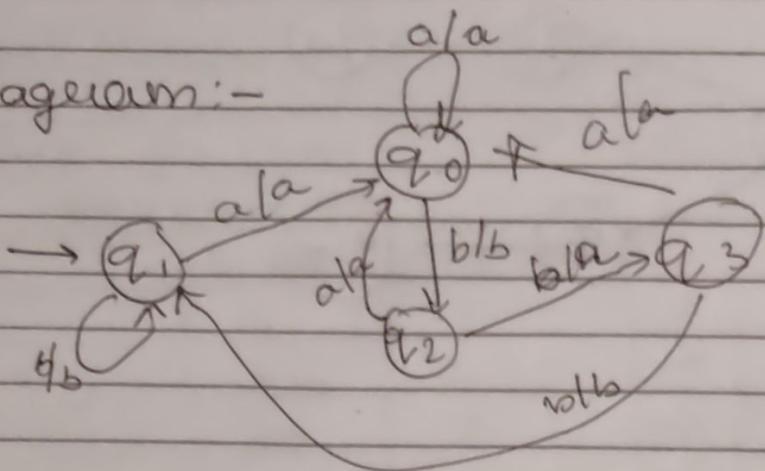
a	q_0	q_0	q_2
b → q_1	q_0	q_1	q_1
ab	q_2	q_0	q_3
absb	q_3	q_0	q_1

MAF

q_0	a	b
q_1	a	b
q_2	a	a
q_3	a	b

Sirf yaha
change
baki jo input
wahi output

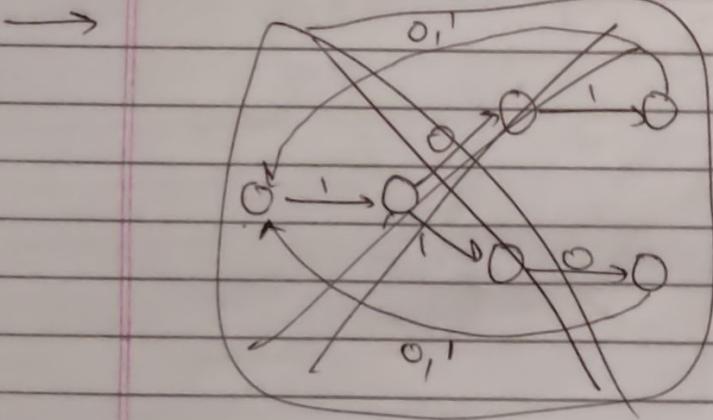
Diagram:-

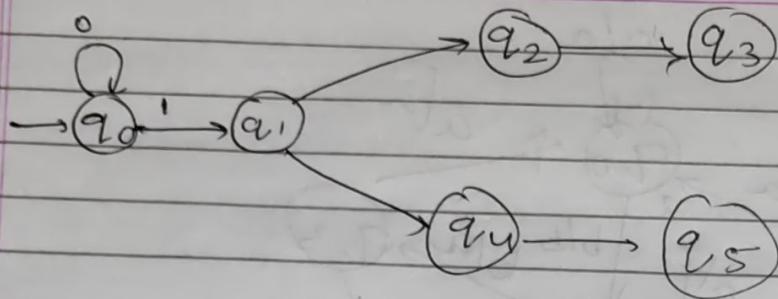


Example.

- $s(q_1, ababb)$
- $(q_0, babb) a$
- $(q_2, abb) ab$
- (q_0, abbb) .

- 3) binary I/P sequence such that if it has substring 110, m/c should output A
 if it has 101, m/c should output B.
 otherwise C.





Moore Machine \rightarrow State

$n+1 \rightarrow \text{output}$

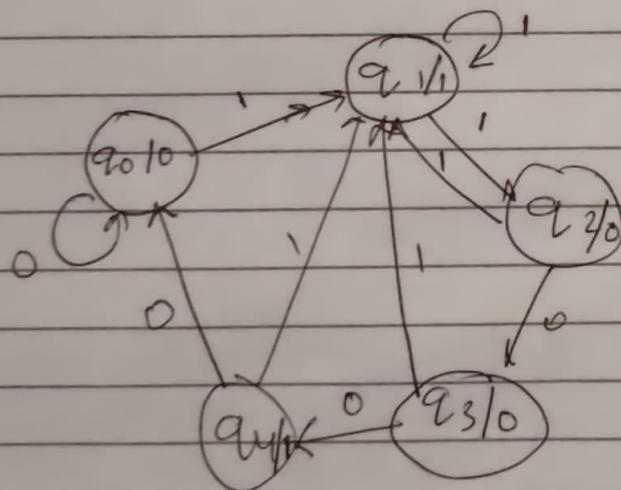
1) each $1000 \rightarrow 1001 \quad \Sigma = \{0, 1\}$

2) $n \rightarrow 120 \rightarrow 122 \quad \{0, 1, 2\}$

3) $n \text{ aab} \rightarrow \Sigma \{a, b\}$

q_s	0	1	λ
0 q_0	q_0	q_1	$\lambda(q_0) = 0$
1 q_1	q_2	q_1	$\lambda(q_1) = 1$
10 q_2	q_3	q_1	$\lambda(q_2) = 0$
100 q_3	q_4	q_1	$\lambda(q_3) = 0$
(1000) q_4	q_0	q_1	$\lambda(q_4) = 1$

	0	1	λ
0 q_0	q_0	q_1	0
1 q_1	q_2	q_1	1
10 q_2	q_3	q_1	0
100 q_3	q_4	q_1	0
(1000) q_4	q_0	q_1	1



$s(q_s, 101101) \ 0$
 $s(q_1, 01101) \ 01$
 $s(q_2, 1101) \ 010$
 $s(q_3, 101) \ 0101$
 $s(q_4, 0) \ 01011$
 $(q_2, 1) \ 010110$
 $(q_1, 1) \ 0101101$
 No change