

MP3 Test Plan

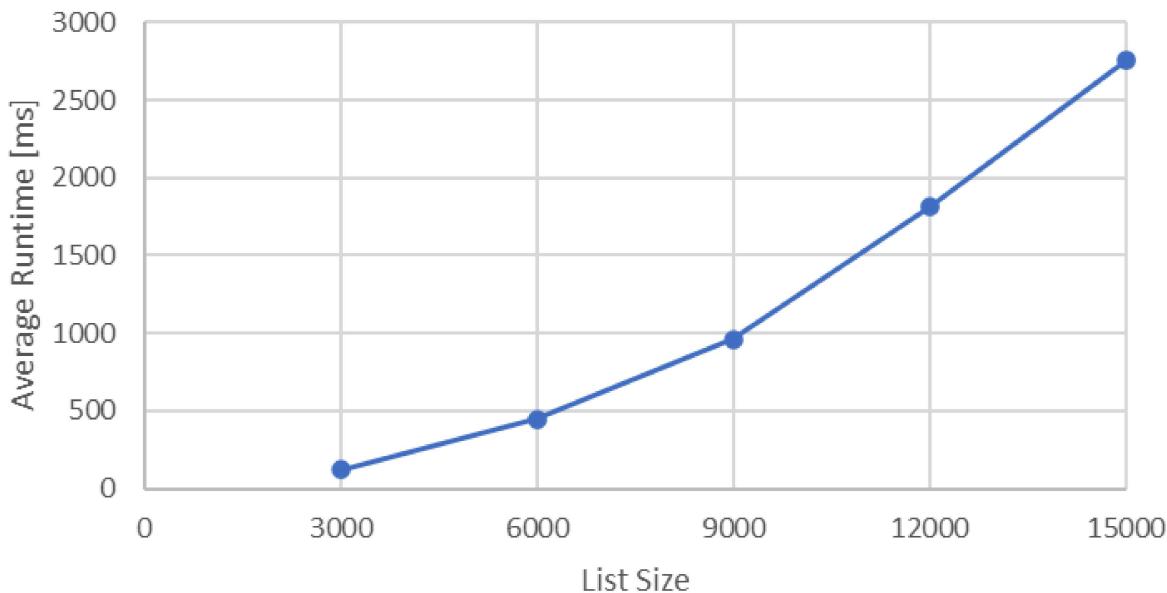
Test Type Performances

This section outlines the test cases designated for each of the 5 sorting functions implemented in MP3. Each function undergoes testing with randomly ordered input, ascending input, and descending input. Across each input scenario, 5 different input sizes are tested, carefully selected to provide a diverse range of runtime values, ranging from less than a hundred milliseconds to over 1 second. Due to runtime variability, each case is tested three times, and the average runtime of these iterations is presented.

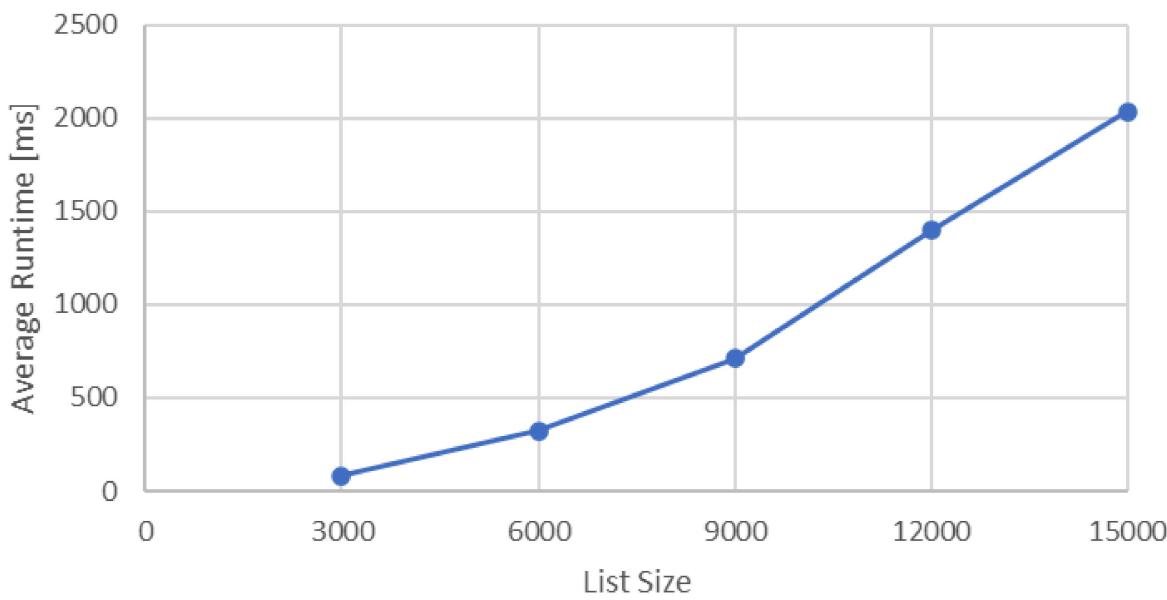
1. Bubble Sort

| List Type and Size | 1st Runtime | 2nd Runtime | 3rd Runtime | Average Runtime |
|--------------------|-------------|-------------|-------------|-----------------|
| Random 3000 | 116.48 | 123.08 | 115.55 | 118.37 |
| Random 6000 | 428.64 | 479.00 | 429.02 | 445.55 |
| Random 9000 | 963.96 | 956.91 | 957.28 | 959.38 |
| Random 12000 | 1819.42 | 1820.68 | 1802.20 | 1814.10 |
| Random 15000 | 2720.81 | 2770.35 | 2776.62 | 2755.92 |
| Ascending 3000 | 80.03 | 81.03 | 82.74 | 81.27 |
| Ascending 6000 | 321.29 | 325.03 | 321.15 | 322.49 |
| Ascending 9000 | 707.96 | 713.85 | 709.45 | 710.42 |
| Ascending 12000 | 1439.44 | 1404.05 | 1356.30 | 1399.93 |
| Ascending 15000 | 2027.35 | 2036.35 | 2043.60 | 2035.77 |
| Descending 3000 | 113.00 | 113.38 | 114.86 | 113.75 |
| Descending 6000 | 420.91 | 413.11 | 407.80 | 413.94 |
| Descending 9000 | 900.89 | 909.06 | 903.88 | 904.61 |
| Descending 12000 | 1697.42 | 1818.87 | 1718.07 | 1744.79 |
| Descending 15000 | 2651.01 | 2587.02 | 2595.03 | 2611.02 |

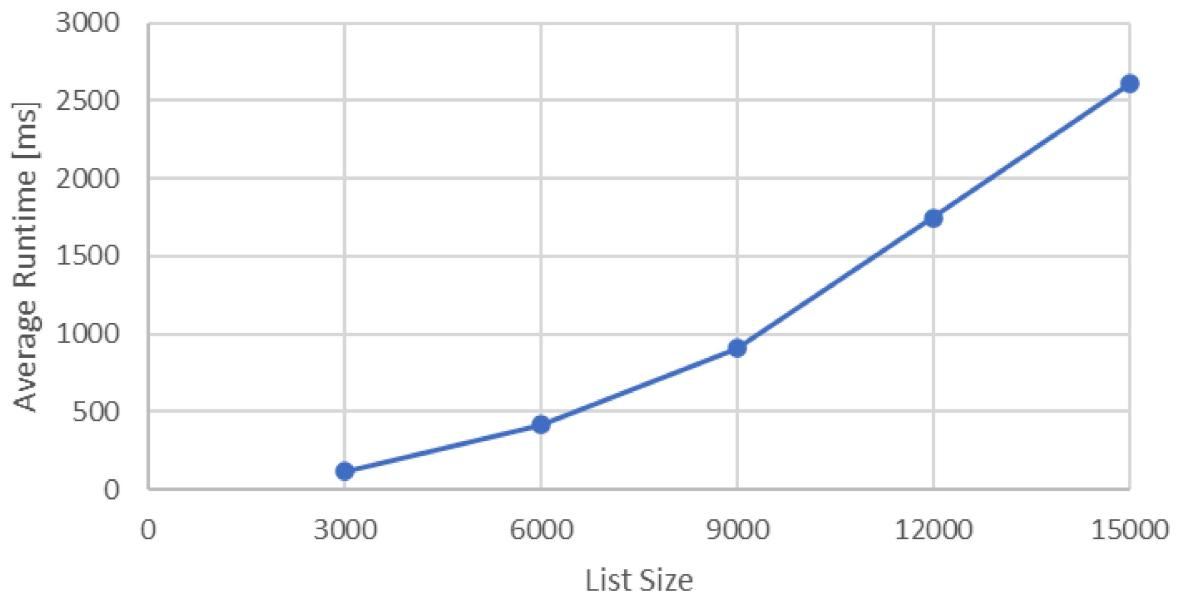
Random



Ascending



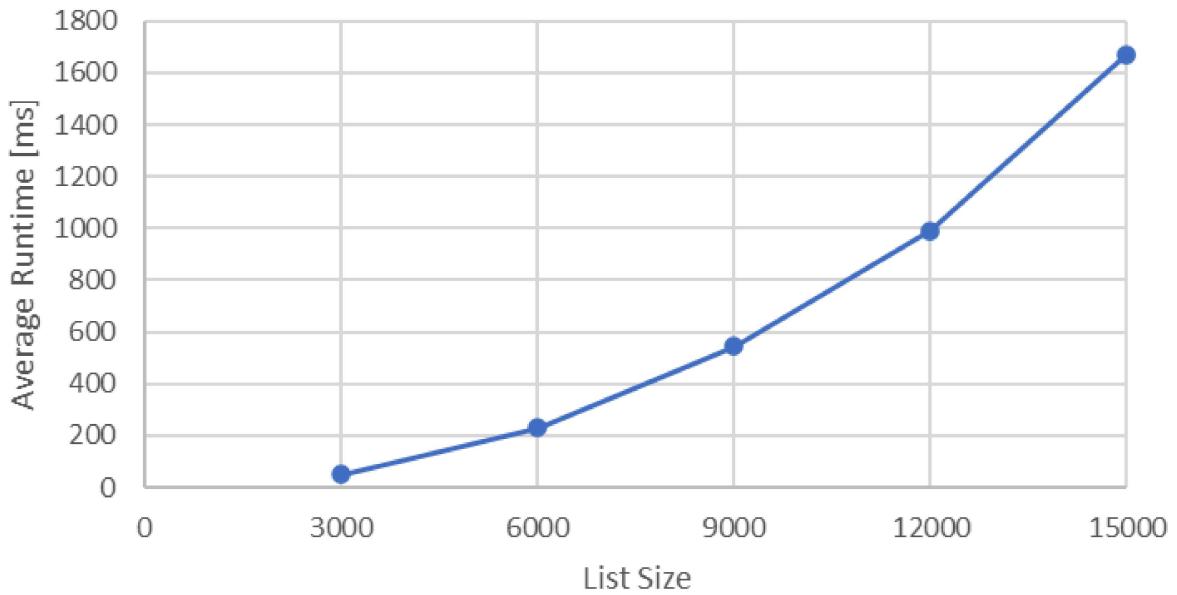
Descending



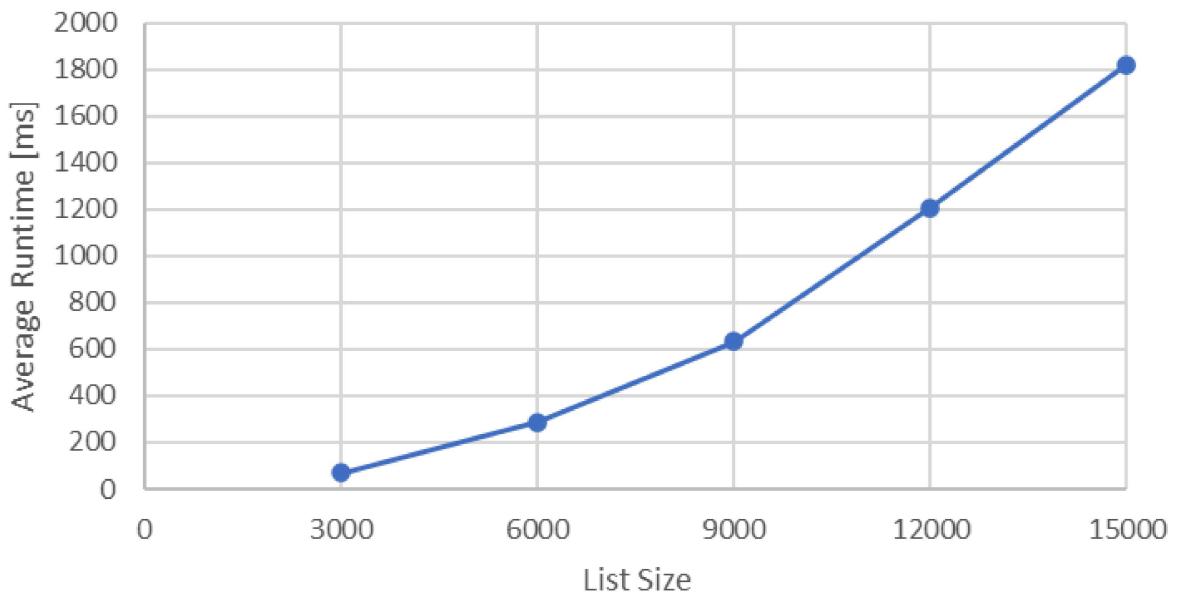
2. Insertion Sort

| List Type and Size | 1st Runtime | 2nd Runtime | 3rd Runtime | Average Runtime |
|--------------------|-------------|-------------|-------------|-----------------|
| Random 3000 | 48.74 | 47.93 | 50.32 | 49.00 |
| Random 6000 | 235.26 | 227.58 | 229.12 | 230.65 |
| Random 9000 | 543.90 | 531.80 | 554.33 | 543.34 |
| Random 12000 | 1000.98 | 993.84 | 979.43 | 991.42 |
| Random 15000 | 1678.48 | 1678.97 | 1655.57 | 1671.01 |
| Ascending 3000 | 70.66 | 69.51 | 70.11 | 70.09 |
| Ascending 6000 | 288.27 | 283.71 | 291.83 | 287.94 |
| Ascending 9000 | 622.87 | 645.42 | 627.52 | 631.94 |
| Ascending 12000 | 1205.02 | 1202.88 | 1213.76 | 1207.22 |
| Ascending 15000 | 1832.75 | 1824.92 | 1806.51 | 1821.39 |
| Descending 3000 | 0.32 | 0.27 | 0.30 | 0.30 |
| Descending 6000 | 0.72 | 0.55 | 0.67 | 0.65 |
| Descending 9000 | 0.99 | 1.04 | 0.88 | 0.97 |
| Descending 12000 | 1.33 | 1.24 | 1.09 | 1.22 |
| Descending 15000 | 1.69 | 1.63 | 1.46 | 1.59 |

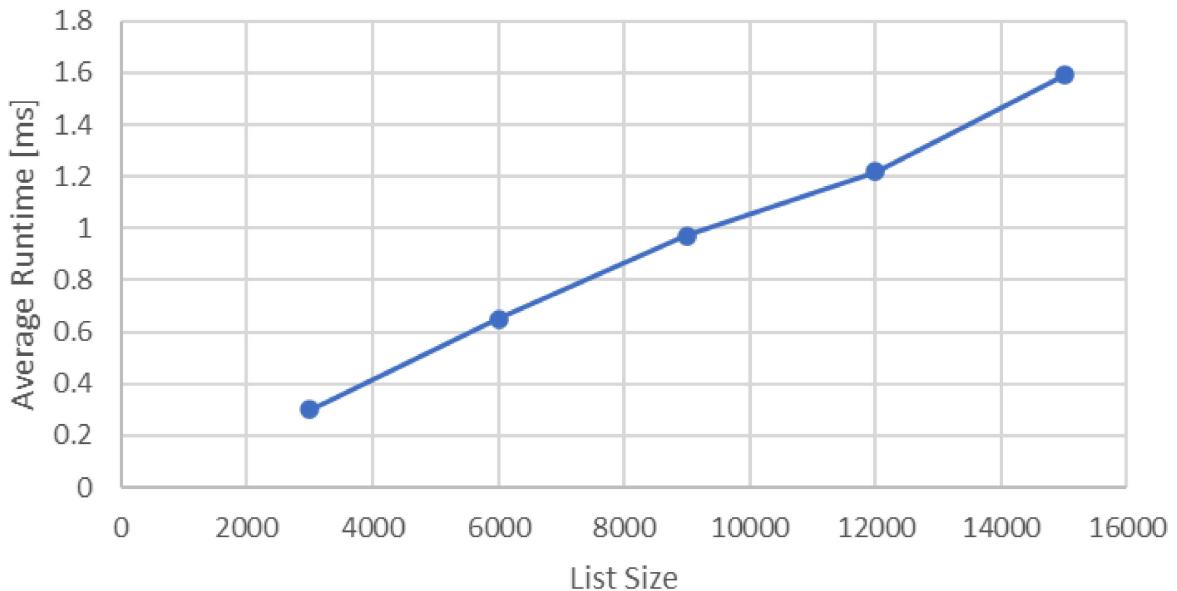
Random



Ascending



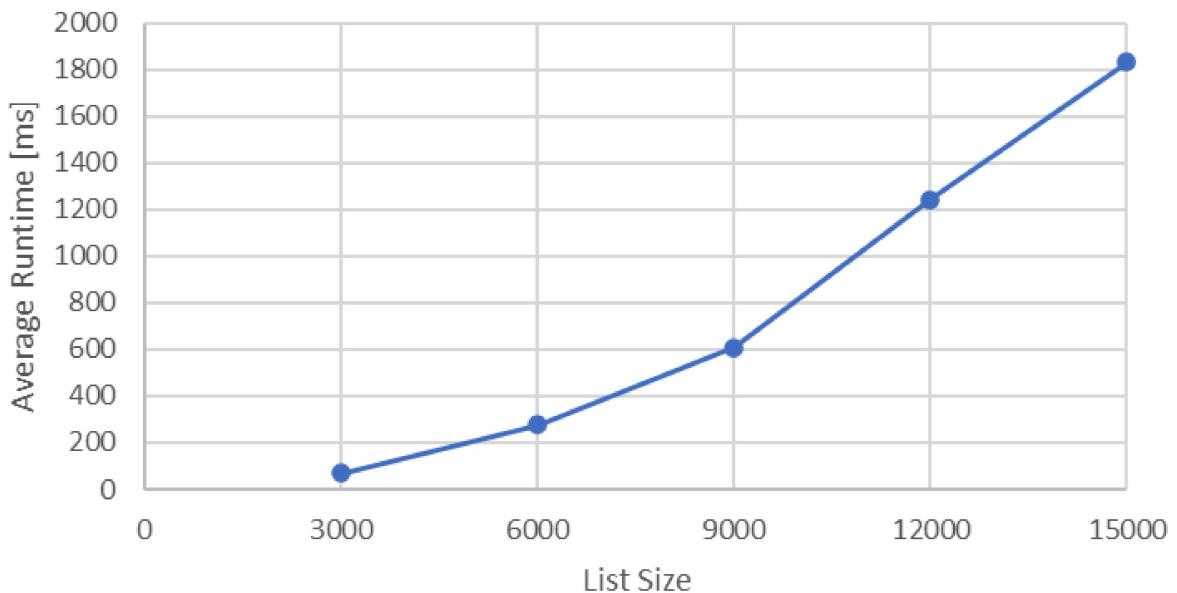
Descending



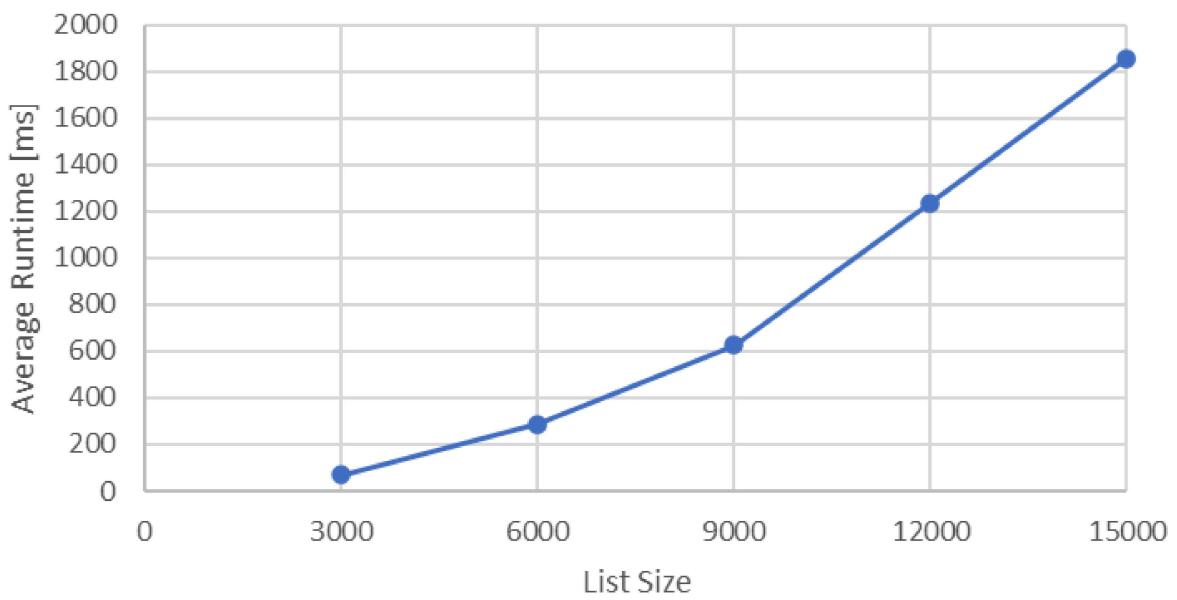
3. Recursive Selection Sort

| List Type and Size | 1st Runtime | 2nd Runtime | 3rd Runtime | Average Runtime |
|--------------------|-------------|-------------|-------------|-----------------|
| Random 3000 | 70.18 | 68.66 | 69.32 | 69.39 |
| Random 6000 | 275.69 | 274.90 | 278.20 | 276.26 |
| Random 9000 | 600.08 | 607.55 | 611.78 | 606.47 |
| Random 12000 | 1164.82 | 1253.27 | 1310.0 | 1242.69 |
| Random 15000 | 1771.32 | 1942.08 | 1778.60 | 1830.67 |
| Ascending 3000 | 71.66 | 69.14 | 70.17 | 70.32 |
| Ascending 6000 | 282.44 | 289.15 | 283.90 | 285.16 |
| Ascending 9000 | 619.70 | 626.50 | 626.76 | 624.32 |
| Ascending 12000 | 1191.18 | 1213.71 | 1301.27 | 1235.39 |
| Ascending 15000 | 1897.88 | 1812.38 | 1860.96 | 1857.07 |
| Descending 3000 | 73.71 | 70.79 | 71.83 | 72.11 |
| Descending 6000 | 283.73 | 282.77 | 286.53 | 284.34 |
| Descending 9000 | 627.03 | 620.14 | 624.94 | 624.04 |
| Descending 12000 | 1196.48 | 1233.62 | 1210.43 | 1213.51 |
| Descending 15000 | 1781.01 | 1802.50 | 1803.96 | 1795.82 |

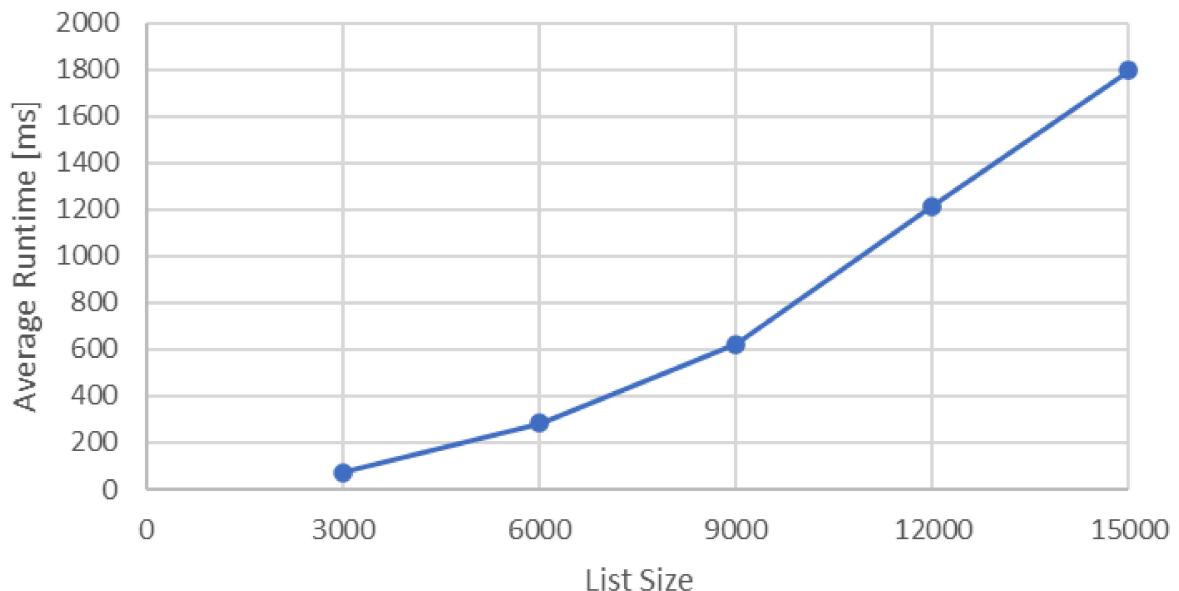
Random



Ascending



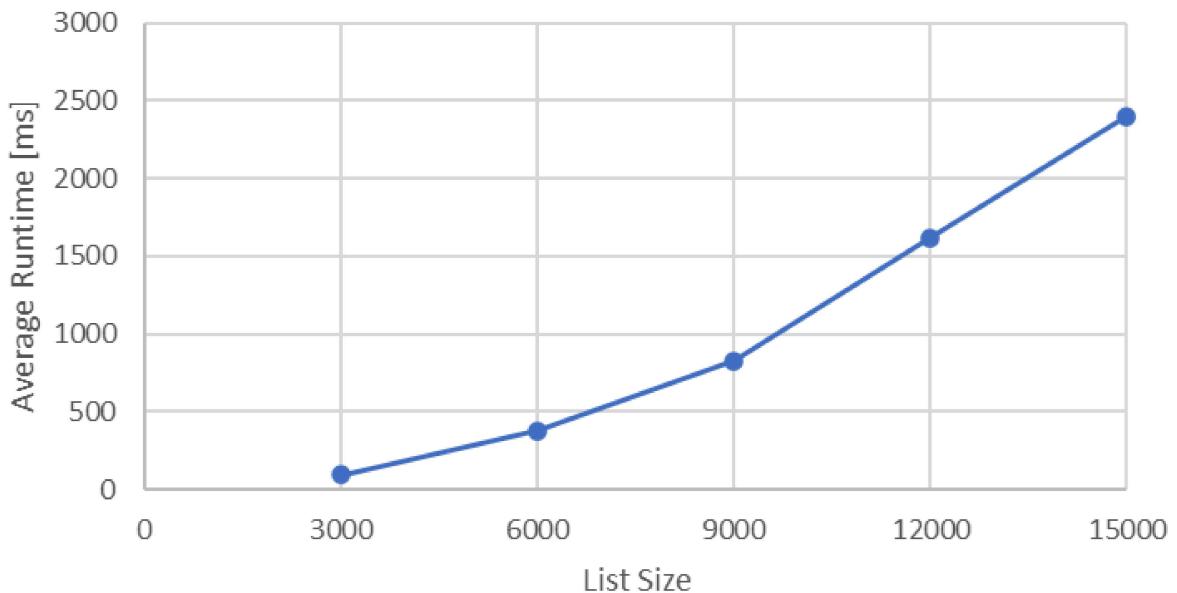
Descending



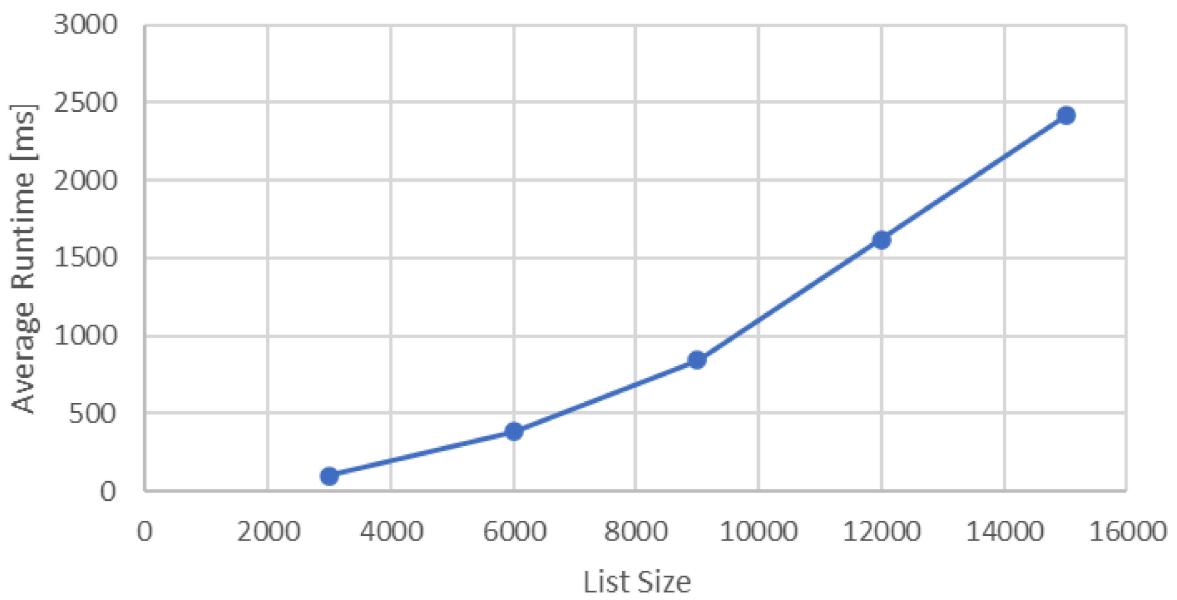
4. Iterative Selection Sort

| List Type and Size | 1st Runtime | 2nd Runtime | 3rd Runtime | Average Runtime |
|--------------------|-------------|-------------|-------------|-----------------|
| Random 3000 | 95.38 | 93.65 | 93.29 | 94.11 |
| Random 6000 | 379.74 | 373.55 | 378.14 | 377.14 |
| Random 9000 | 831.86 | 820.23 | 820.23 | 824.11 |
| Random 12000 | 1576.31 | 1719.56 | 1566.65 | 1620.84 |
| Random 15000 | 2401.68 | 2394.73 | 2399.79 | 2398.73 |
| Ascending 3000 | 95.13 | 98.05 | 97.63 | 96.94 |
| Ascending 6000 | 380.78 | 381.24 | 378.84 | 380.29 |
| Ascending 9000 | 840.44 | 842.09 | 840.16 | 840.89 |
| Ascending 12000 | 1692.96 | 1588.77 | 1580.30 | 1620.67 |
| Ascending 15000 | 2401.79 | 2428.87 | 2413.38 | 2414.68 |
| Descending 3000 | 95.22 | 95.59 | 96.41 | 95.74 |
| Descending 6000 | 382.91 | 379.04 | 394.23 | 385.39 |
| Descending 9000 | 837.24 | 865.49 | 833.70 | 845.48 |
| Descending 12000 | 1581.31 | 1583.44 | 1581.95 | 1582.23 |
| Descending 15000 | 2456.07 | 2401.92 | 2409.70 | 2422.56 |

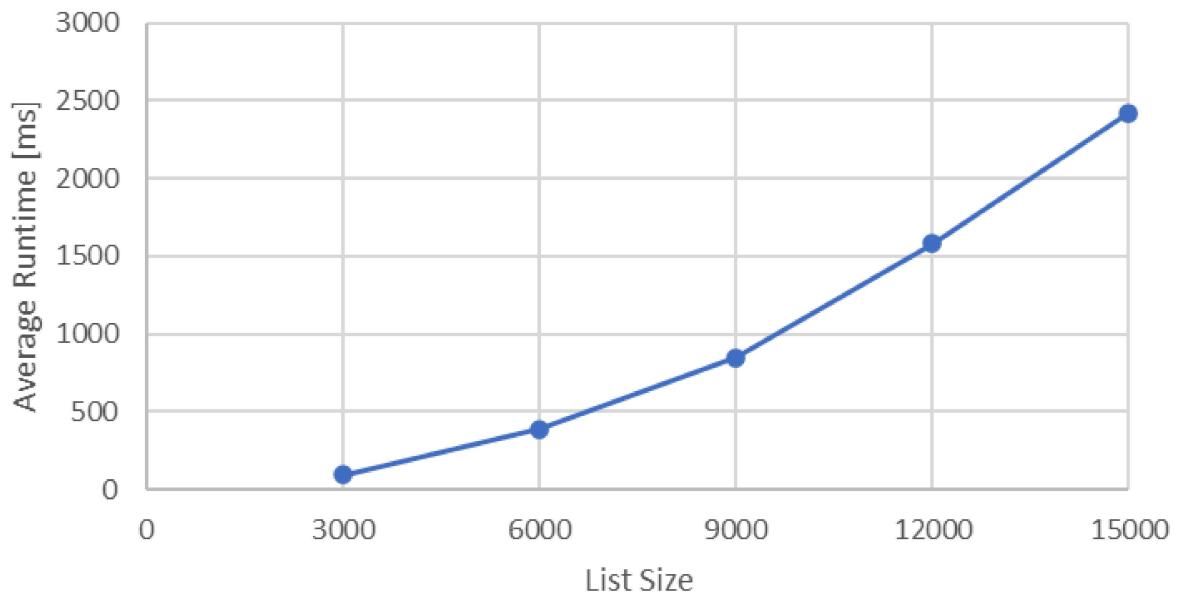
Random



Ascending



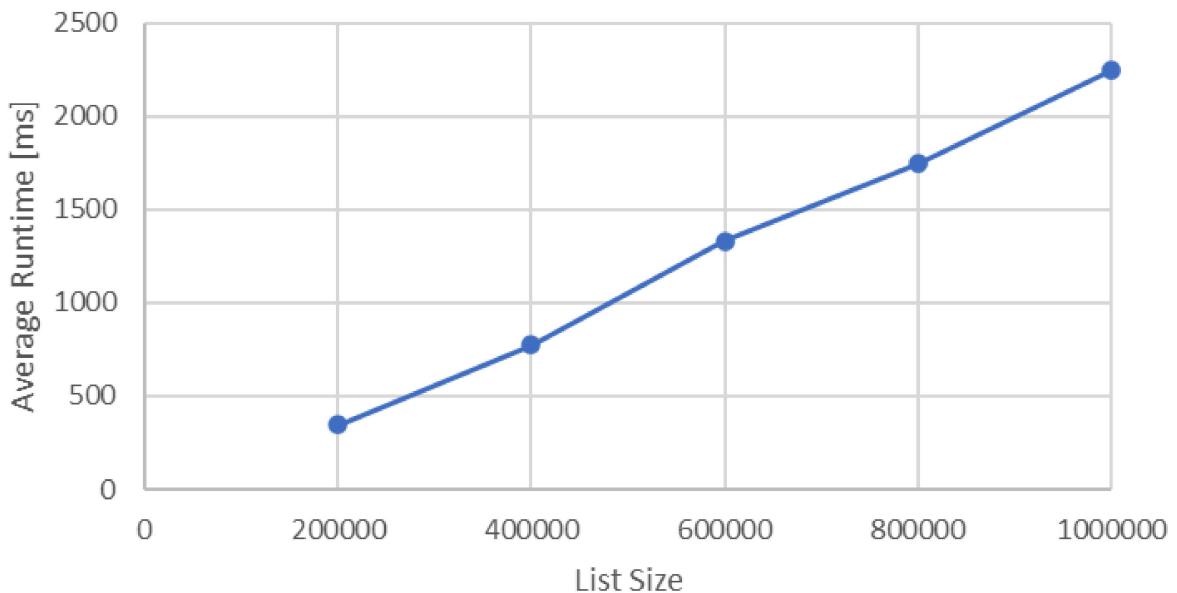
Descending



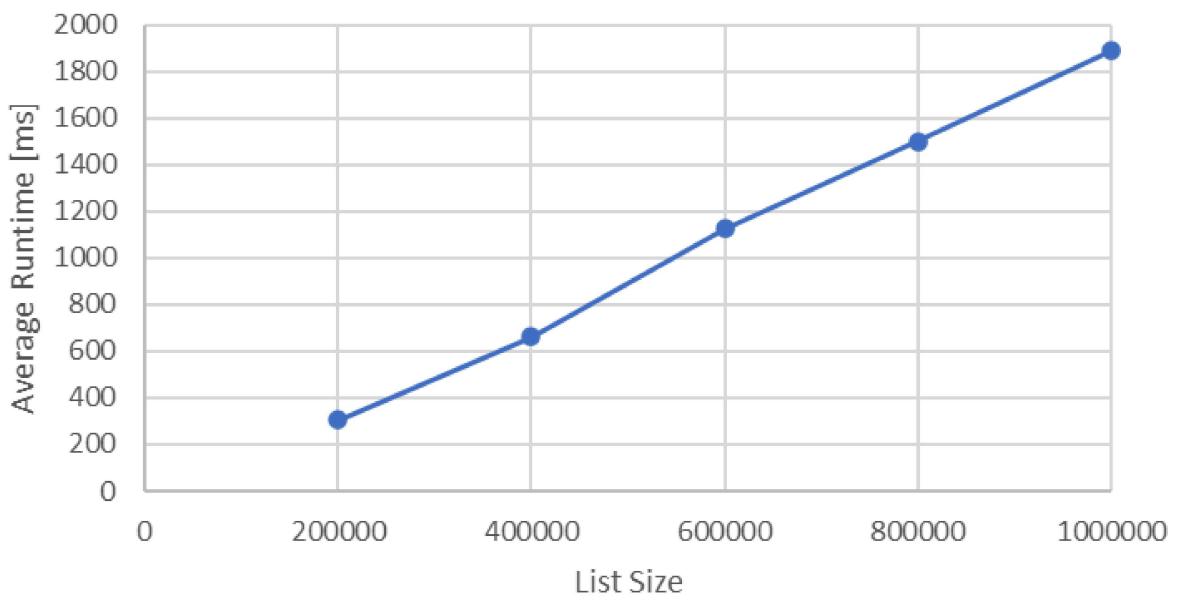
5. Merge Sort

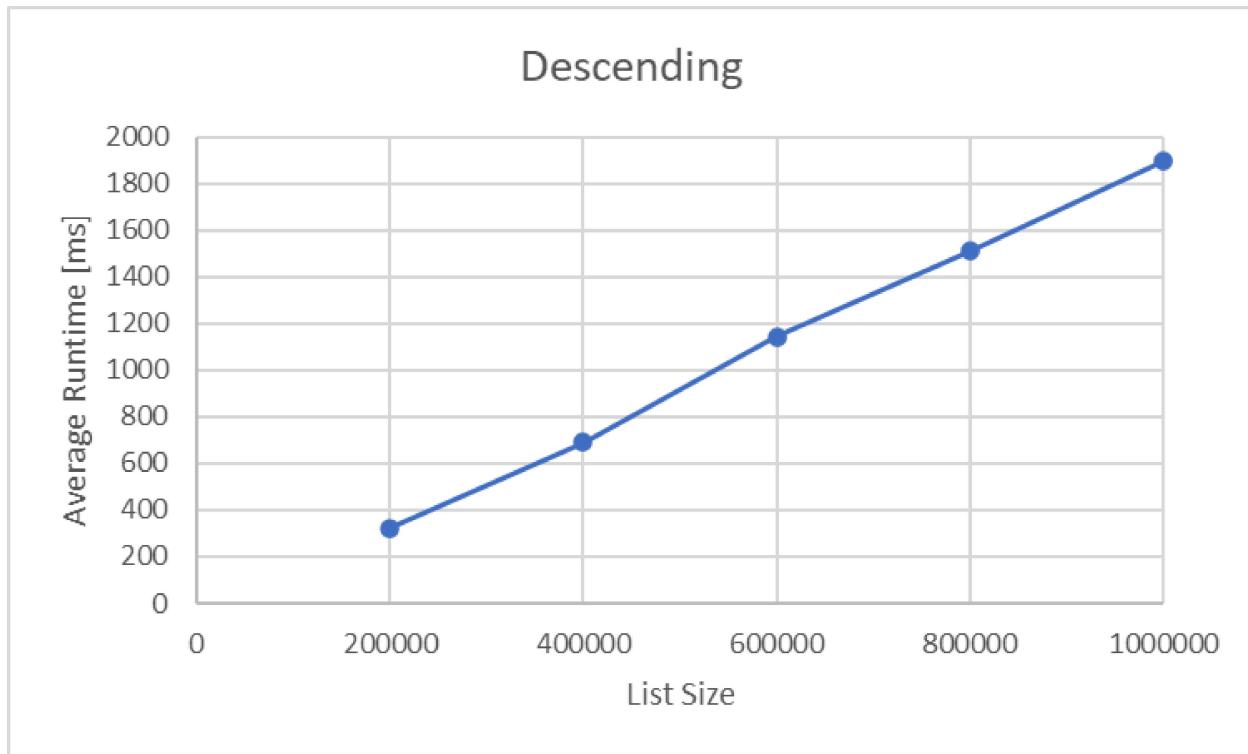
| List Type and Size | 1st Runtime | 2nd Runtime | 3rd Runtime | Average Runtime |
|--------------------|-------------|-------------|-------------|-----------------|
| Random 200000 | 344.47 | 346.67 | 345.31 | 345.48 |
| Random 400000 | 765.37 | 780.83 | 772.30 | 772.83 |
| Random 600000 | 1318.98 | 1322.70 | 1348.39 | 1330.02 |
| Random 800000 | 1772.31 | 1662.75 | 1808.92 | 1747.99 |
| Random 1000000 | 2254.37 | 2245.91 | 2241.72 | 2247.33 |
| Ascending 200000 | 309.03 | 303.07 | 303.47 | 305.19 |
| Ascending 400000 | 653.58 | 672.83 | 653.66 | 660.02 |
| Ascending 600000 | 1123.30 | 1126.36 | 1123.80 | 1124.49 |
| Ascending 800000 | 1503.30 | 1496.84 | 1500.38 | 1500.17 |
| Ascending 1000000 | 1861.58 | 1918.21 | 1886.63 | 1888.81 |
| Descending 200000 | 311.71 | 306.51 | 350.219 | 322.81 |
| Descending 400000 | 668.29 | 689.01 | 712.41 | 689.90 |
| Descending 600000 | 1128.38 | 1146.92 | 1157.90 | 1144.4 |
| Descending 800000 | 1502.87 | 1509.22 | 1523.57 | 1511.89 |
| Descending 1000000 | 1899.14 | 1878.20 | 1909.10 | 1895.48 |

Random



Ascending





Analysis of Results

For initially randomized lists, the first 4 functions show similar runtimes, around 100 milliseconds for 3000 elements and 1.5-2 seconds for 15000 elements. Both recursive and iterative selection sort perform comparably. Despite differing implementations, their time complexities remain $O(n^2)$, resulting in similar runtimes. In contrast, merge sort exhibits a substantial improvement, being much faster due to its $O(n\log_n)$ complexity. This allows it to handle much larger lists within the same timeframe.

Bubble sort shows slight performance gains when the input list is already sorted. In insertion sort, a significant runtime decrease occurs when sorting a descending list into ascending order due to reduced comparisons. No notable runtime differences are observed in selection sort or merge sort based on the input list's initial sorting.