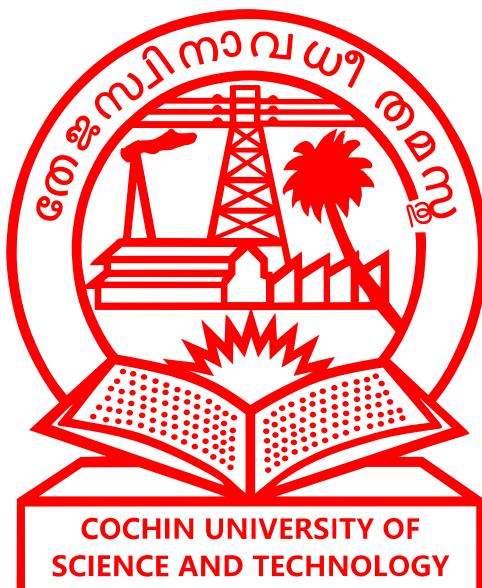


Python Project 1:

Discrete-time Signal Classifier: Energy Vs. Power



Submitted by

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Signal Classifier: Energy Vs. Power

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Aim

The aim is to classify a given real-valued signal into energy signal or power signal, or neither of them, using numeric integration, and also to find their energy and power. The signal may be given as a Python function, and the test is done by calling the classifier function..

Tools used

- Python 3.14
- Jupyter notebook
- Numpy and Math module

Method of Classification (Convergence)

The given discrete time signal's energy (E) and power (P) are computed using the summation of squares of samples as:

$$E = \sum_{n=-\infty}^{\infty} |x[n]|^2$$
$$P = \lim_{N \rightarrow \infty} \frac{1}{2N+1} \sum_{n=-N}^{N} |x[n]|^2$$

To classify the signal into either category, the summation has to be evaluated and checked if it converges to a non-zero value. The signal is energy signal if $0 < E < \infty$ and it is power signal $0 < P < \infty$. To test for the convergence of the signal, the energy and power are computed within various increasing upper limits L ($L = 10^2, 10^3, \dots, 10^6$), ie. in $(-10^2, 10^2), \dots, (-10^6, 10^6)$. From this, a sequence containing differences between each successive limit (energy or power) is obtained and checked if it tends to decrease. Additionally, to account for any rounding error which may result in an oscillatory pattern in the sequence of differences, it is also checked whether each difference is within the average of the whole difference sequence, ie. thus converges to a finite value.

- **Energy Signal:** If the energy converges to a finite value ($0 < E < \infty$) and the average power $P = 0$.
- **Power Signal:** If the energy diverges ($E \rightarrow \infty$) but the average power converges to a finite non-zero constant ($0 < P < \infty$).
- **Neither:** If both energy and power diverge, as seen in growing exponential signals that trigger numerical overflows.

Source Code

```
1 #jupyter python program to classify discrete time signals as energy or power usinfg convergence
2
3 import numpy as np
4 from math import inf
5
6 '''3. It utilises convergence, by iterating over the list of all energies/powers (read as sequence) where the seq is unstable
7 - the differences of consecutive elements (form a list of that) is inc and any diff in the list is
8 greater than avg diff of elements (ie energies are finite ie not tends to inf/0 on inc interval windows) or
9 - the list of energies contain 0 or infinity or
10 - the length of energy/power list is <2.
11 Thus returning the respective boolean.'''
12
13 def is_stable(sequence):
14     #Checks if a sequence approaches a non-zero, non-infinite limit.
15     if len(sequence) < 2: return False
16     if 0 in sequence or inf in sequence: return False
17
18     # Calculate differences between successive calculation steps
19     diffs = [abs(sequence[i] - sequence[i-1]) for i in range(1, len(sequence))]
20     avg_diff = sum(diffs) / len(diffs)
21
22     for i in range(1, len(diffs)):
23         # If the gap between steps grows and is larger than average, hasn't converged
24         if diffs[i] > diffs[i-1] and diffs[i] > avg_diff:
25             return False
26     return True
27
28 '''2. Generate energies and powers of intervals from -10^2 to 10^2, -10^3 to 10^3, ..... -10^7 to 10^7 for the signal_fn
29 and pass the lists to is_stable() to check stability of energies/powers hence return the classified o/p accordingly.
30 (stable energies = energy signal and viceversa)'''
31
32 def classify_dt_signal(signal_func):
33     energies = []
34     powers = []
35
36     # Test for increasing 'N' (Number of samples)
37     # We check the signal from N=100 to N=1,000,000
38     for i in range(2, 7):
39         N = 10**i
40         n = np.arange(-N, N)
41         x_n = signal_func(n)
42
43         # 1. Compute Signal Energy: Sum of squares
44         E = np.sum(np.abs(x_n)**2)
45
46         # 2. Compute Average Power: Energy / Total Duration
47         P = E / len(n)
48
49         energies.append(E)
50         powers.append(P)
51
52     # Classification Logic
53     if is_stable(energies):
54         return f"Energy Signal (E {energies[-1]:.4f})"
55     elif is_stable(powers):
56         return f"Power Signal (P {powers[-1]:.4f})"
57     else:
58         return "Neither Energy nor Power Signal"
```

Validation against test signals

```
1  ''' 1. Representation of discrete time signals as fns'''
2
3  # Rectangular Pulse (Energy Signal)
4  def rect(n): return np.where((n >= 0) & (n <= 10), 1, 0)
5
6  # Unit Step (Power Signal)
7  def unit_step(n): return np.where(n >= 0, 1, 0)
8
9  def dc_signal(n):
10     # Constant value of 2 for all indices
11     return np.full_like(n, 2, dtype=float)
12
13  '''
14  def growing_exp(n):
15      # Returns e^n for n >= 0
16      # Note: We cap n to avoid float overflow errors
17      return np.where((n >= 0) & (n < 20), np.exp(n), 0)
18  '''
19  def growing_exp(n):
20      try:
21          # A slower growth like 1.1^n helps avoid instant overflow
22          # so you can actually see the instability.
23          val = 1.1**n
24          return np.where(n >= 0, val, 0)
25      except:
26          return float('inf')
27
28  #Decaying Exponential (Energy Signal)
29  # As n increases, value decreases; energy sum converges.
30  def decaying_exp(n):
31      return np.where(n >= 0, (0.5)**n, 0)
32
33  #Discrete Impulse / Kronecker Delta (Energy Signal)
34  # Only has a value at n=0.
35  def impulse(n):
36      return np.where(n == 0, 1, 0)
37
38  #Unit Ramp (Neither Energy nor Power)
39  # Grows linearly; both E and P will diverge to infinity.
40  def unit_ramp(n):
41      return np.where(n >= 0, n, 0)
42
43  # Signum Function (Power Signal)
44  # Similar to a DC signal but changes polarity at n=0.
45  def signum_sig(n):
46      return np.sign(n)
47
48  print(f"Rect Pulse: {classify_dt_signal(rect)}")
49  print(f"Unit Step: {classify_dt_signal(unit_step)}")
50  print(f"sine wave: {classify_dt_signal(np.sin)}")
51  print(f"dc/constant signal: {classify_dt_signal(dc_signal)}")
52  print(f"growing exponential signal: {classify_dt_signal(growing_exp)}")
53  print(f"Decaying Exp: {classify_dt_signal(decaying_exp)}")
54  print(f"Impulse: {classify_dt_signal(impulse)}")
55  print(f"Unit Ramp: {classify_dt_signal(unit_ramp)}")
56  print(f"Signum: {classify_dt_signal(signum_sig)}")
```

Output

Rect Pulse: Energy Signal ($E \approx 11.0000$)
Unit Step: Power Signal ($P \approx 0.5000$)
sine wave: Power Signal ($P \approx 0.5000$)
dc/constant signal: Power Signal ($P \approx 4.0000$)
growing exponential signal: Neither Energy nor Power Signal
Decaying Exp: Energy Signal ($E \approx 1.3333$)
Impulse: Energy Signal ($E \approx 1.0000$)
Unit Ramp: Neither Energy nor Power Signal
Signum: Power Signal ($P \approx 1.0000$)