

# Horizontal Translation

I use the attached GeoGebra sketch to demonstrate to students why horizontal translations seem to go opposite to the direction you would expect. The explanation goes something like this:

- When we graph a function  $y=f(x)$ , we are plotting the set of points  $(x, f(x))$ . That is, for each specific  $X$ , we calculate its corresponding  $y$ -coordinate and plot all of these. (Show Step 1 on the graph. You can also drag point  $X$  to illustrate the various points on the graph.)
- To find the value of  $X-k$ , we go  $k$  units *left* from our specific  $X$ . We can calculate the corresponding  $y$ -coordinate  $f(X-k)$  also. (Show Step 2.)
- If we were to plot all the points  $(X-k, f(X-k))$ , we would NOT be plotting  $y = f(x-k)$ , we would still be plotting  $y = f(x)$ . (Drag  $X$  to show that all of the points from Step 2 still lie on the original graph of  $y = f(x)$ .)
- But the key idea is, when we graph  $y = f(x-k)$ , we are plotting the  $y$ -coordinate  $f(X-k)$  above the *original*  $x$ -coordinate  $X$ . (Show Step 3.) That is, we are plotting the set of points  $(X, f(X-k))$ . Effectively, this pulls the  $y$ -value that was above  $X-k$ , back over to  $X$ , that is,  $k$  units to the *right* of its location on the graph of  $y = f(x)$ .
- In effect, each specific  $X$ -coordinate "steals" the  $y$ -coordinate from the point  $k$  units to its left, pulling this  $y$ -coordinate  $k$  units to the right of its original location. (Drag point  $X$  to see the graph of  $y=f(x-k)$  traced out.)