2.14 a.

$$\begin{bmatrix}
1 & 0 & 1 \\
1 & -2 & -1 \\
2 & 1 & 3 \\
1 & 0 & 1
\end{bmatrix}
-R_1$$

$$\begin{bmatrix}
1 & 0 & 1 \\
0 & -2 & -2 \\
0 & 1 & 1 \\
0 & 0 & 0
\end{bmatrix}$$

$$\begin{bmatrix}
1 & 0 & 1 \\
0 & -2 & -2 \\
0 & 1 & 1 \\
0 & 0 & 0
\end{bmatrix}$$

rank (A,) = 2 => dim (U,1 = 2

rank  $(A_1) = 2$ => dim  $(v_1) = 2$ 

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$$\dim (V_1 \wedge V_2) = \dim (V_1) + \dim (V_2) - \dim (V_1 + V_2) = 2 + 2 - 3 = 1$$

let w & (v, n v2)

There exists solutions to

where a E IR

Ey is linearly dependent on (1, (2, (5 => dy is a gree variable.

set dy = 1

$$\Rightarrow w = 3 \begin{bmatrix} 1 \\ 1 \\ 2 \end{bmatrix} + \begin{bmatrix} 0 \\ -2 \\ 7 \\ 0 \end{bmatrix} = \begin{bmatrix} 3 \\ 1 \\ 7 \\ 3 \end{bmatrix}$$