

Prospects for scalar-tensor cosmology in ASQG

Quantum
gravity

Cosmology

Fabian Wagner



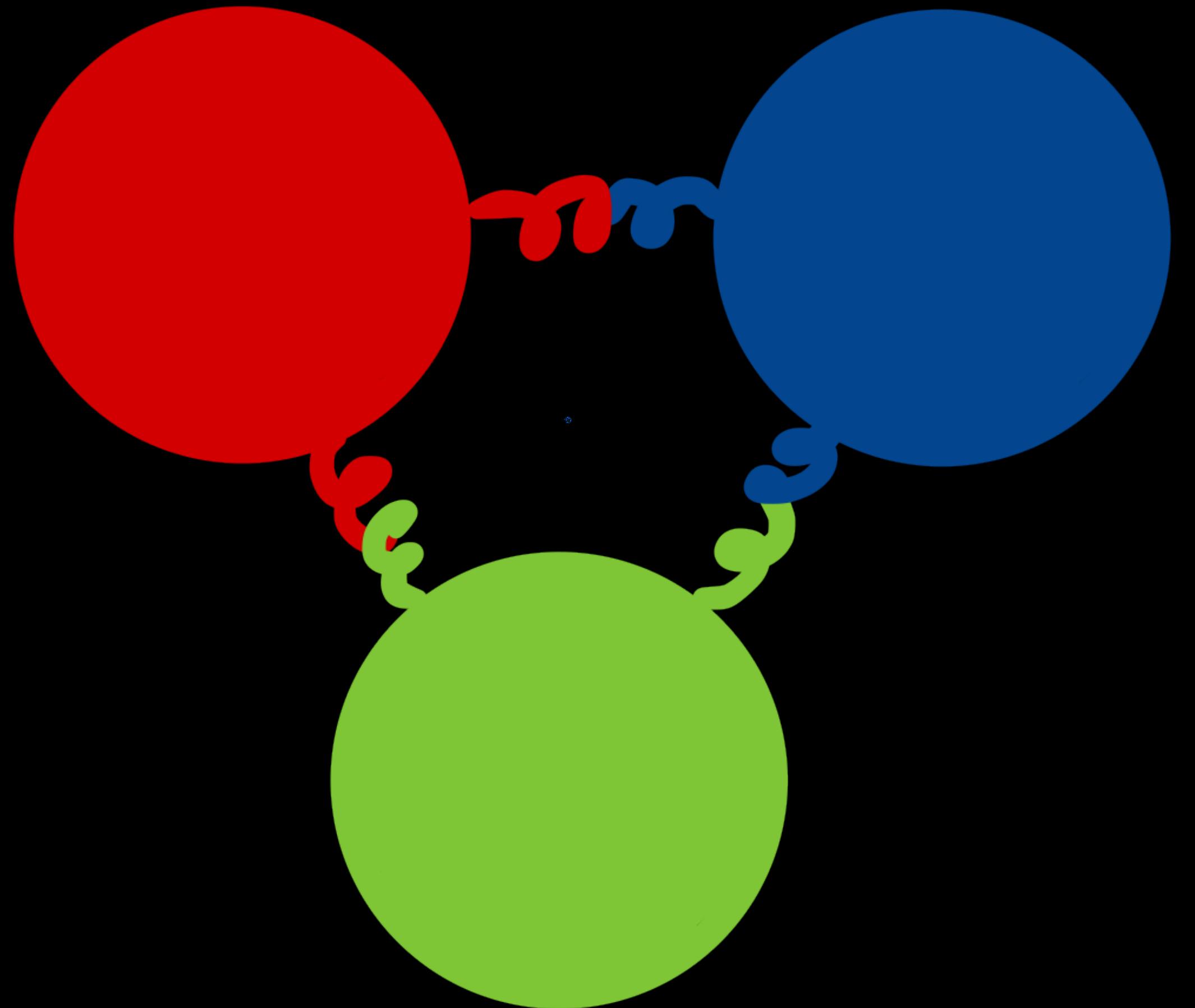
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UV assumption: Quantum scale invariance



g_{UV}

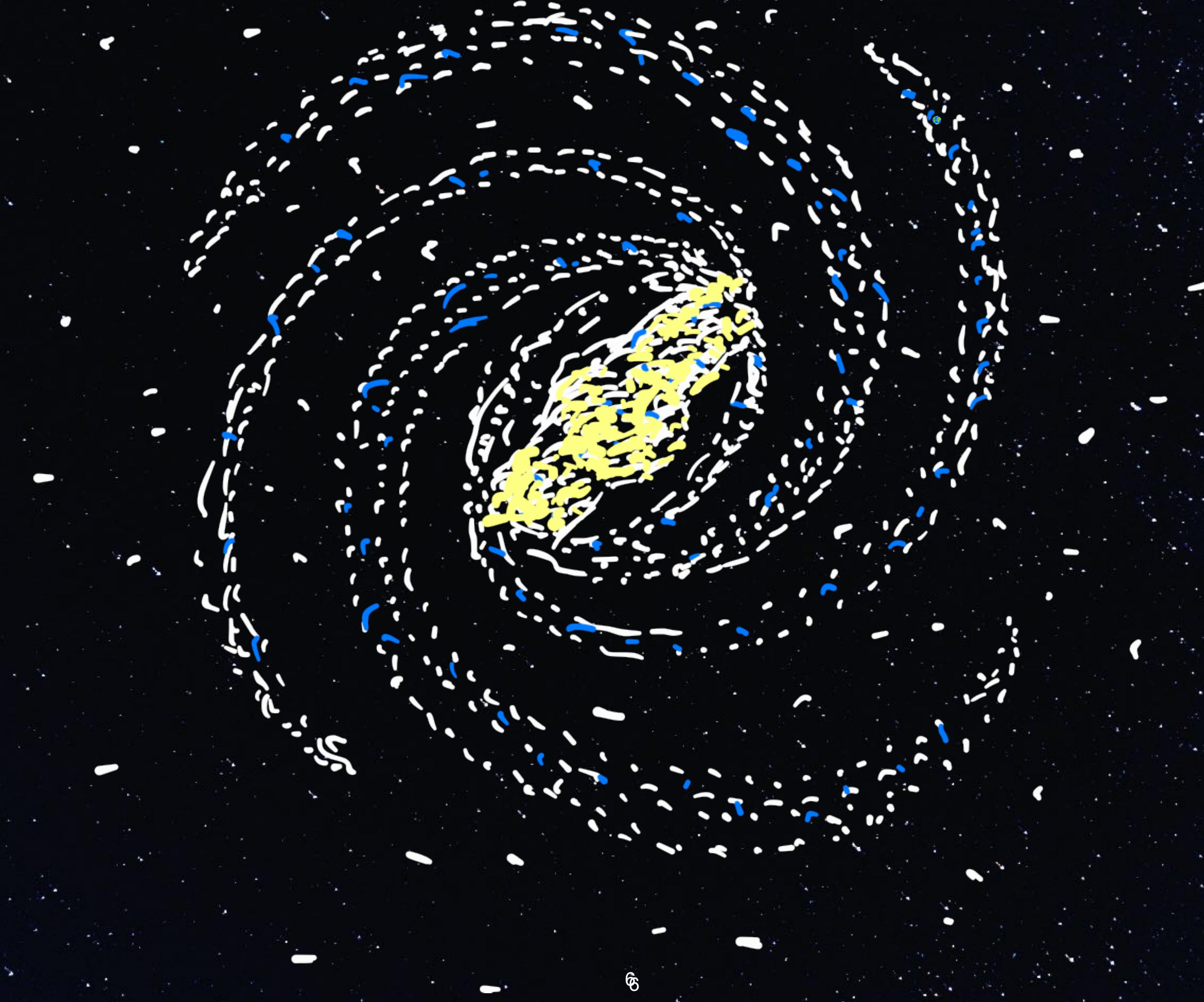






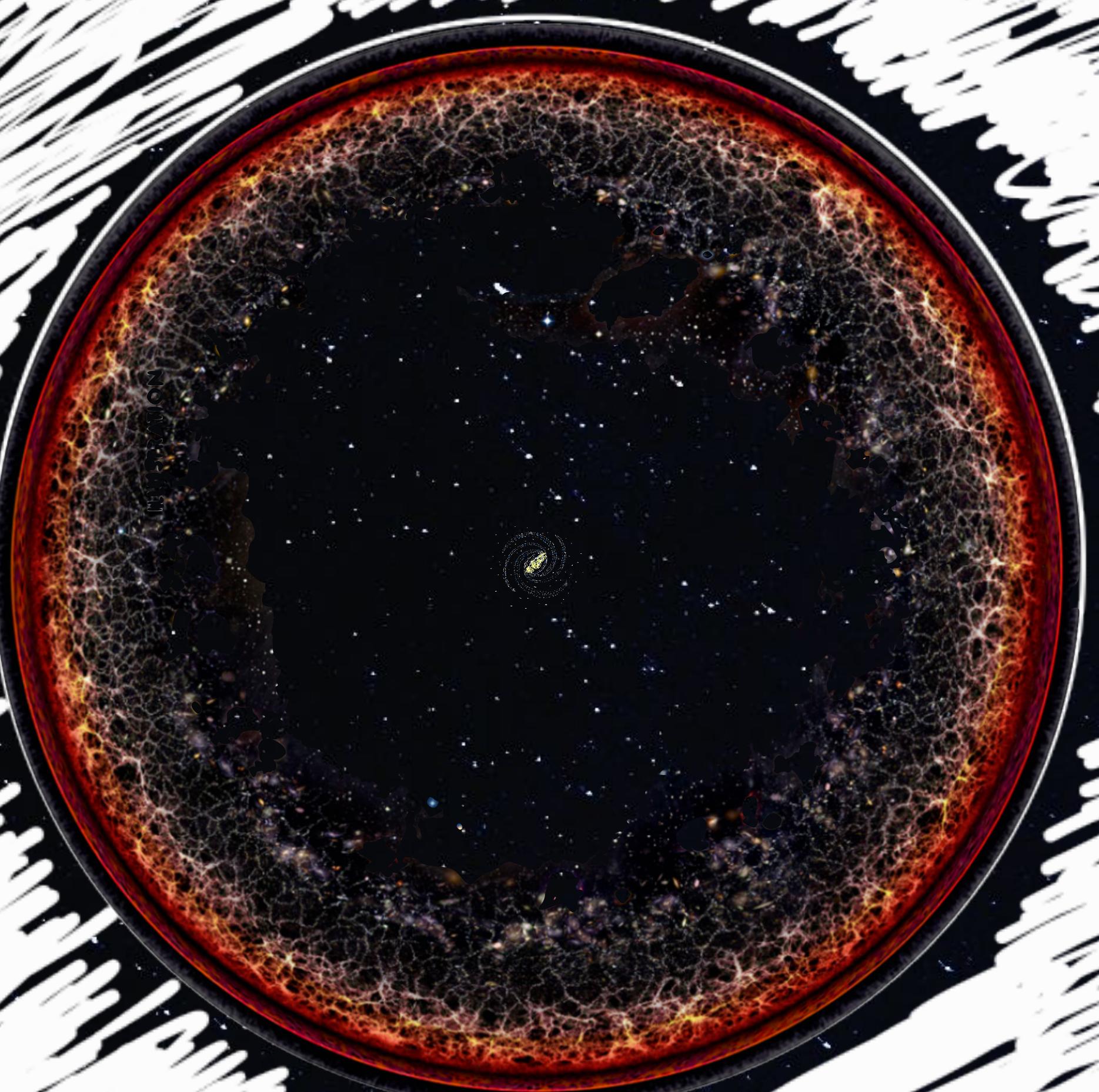
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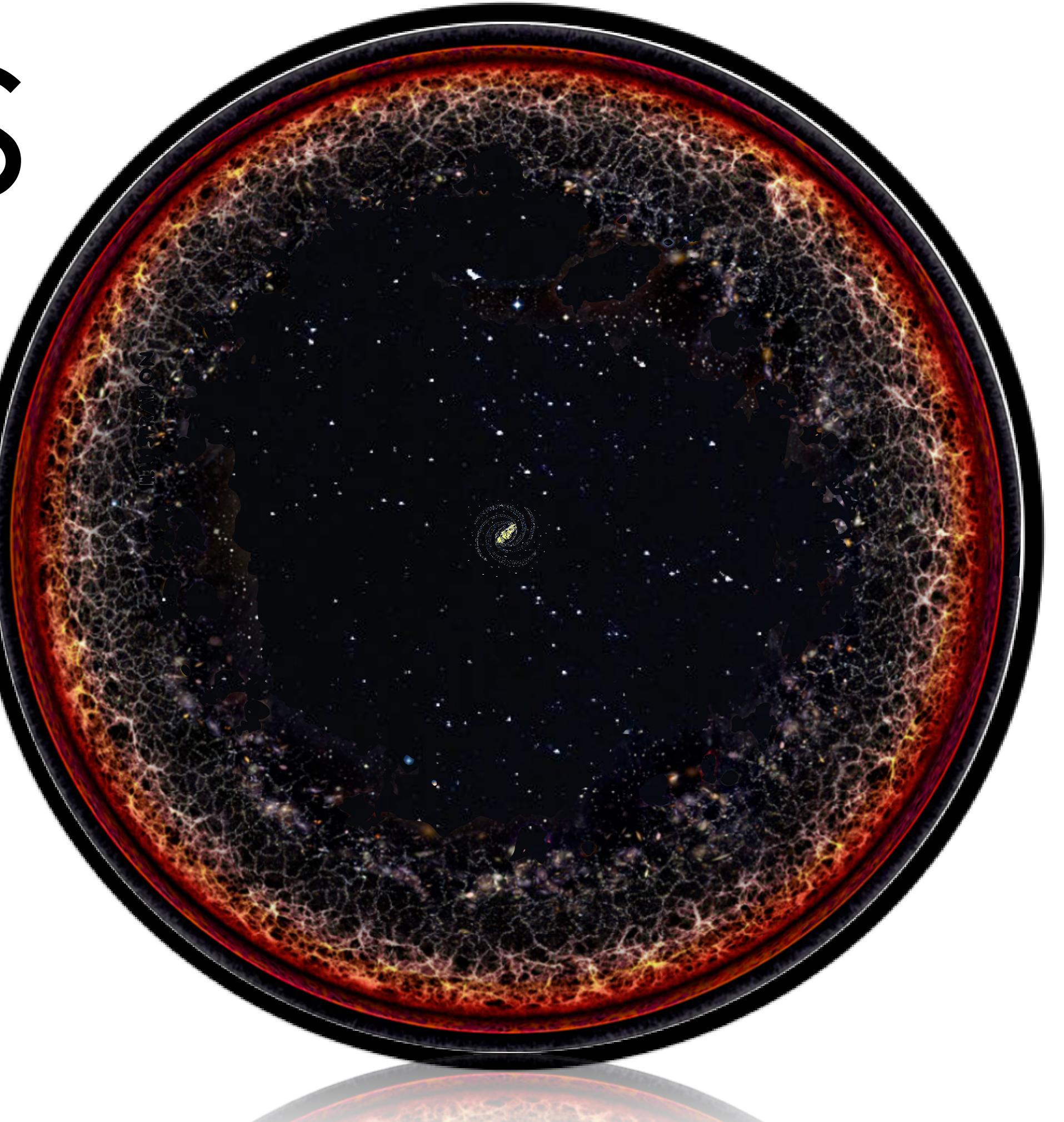


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IR predictions

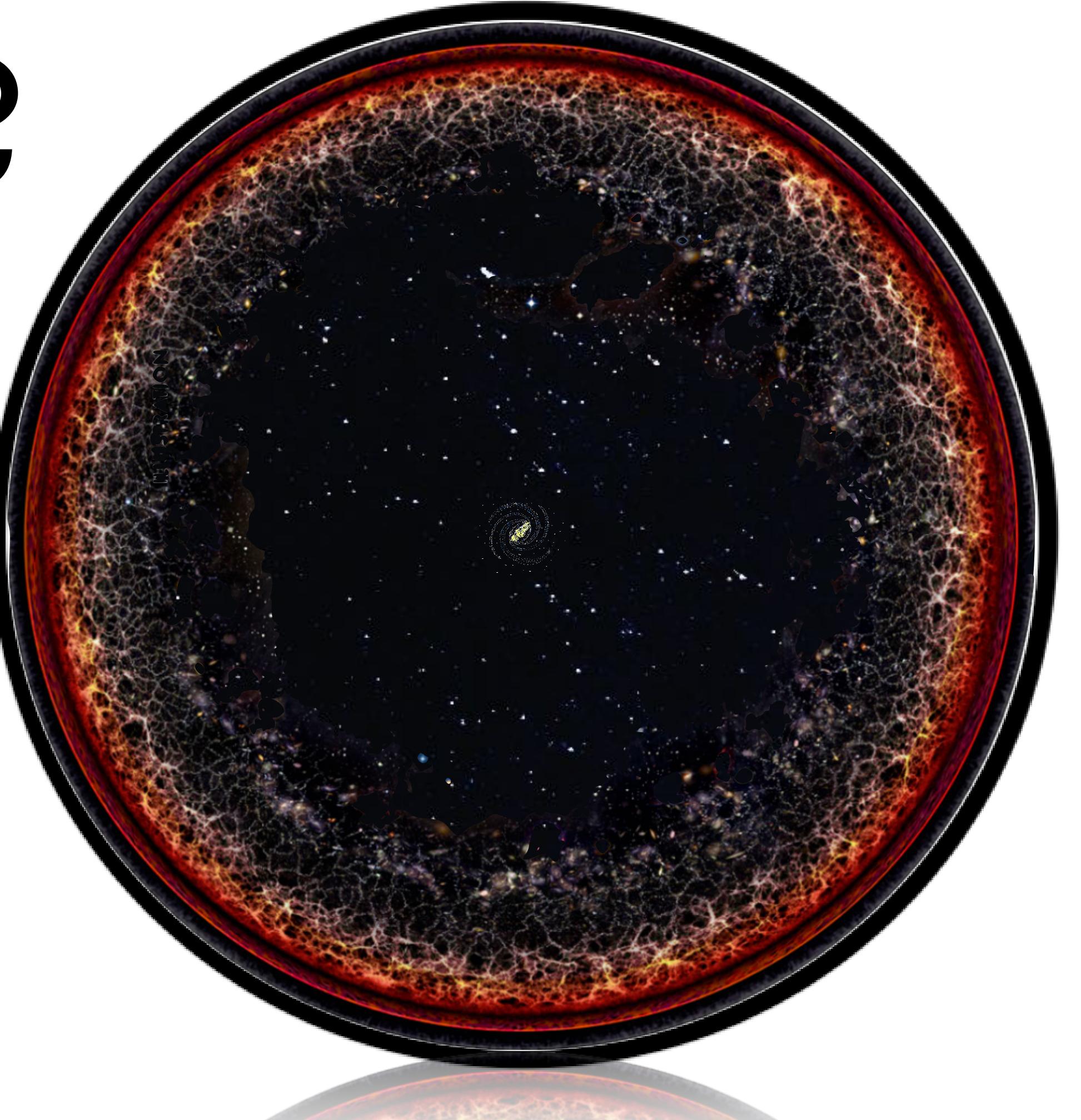
g_{IR}



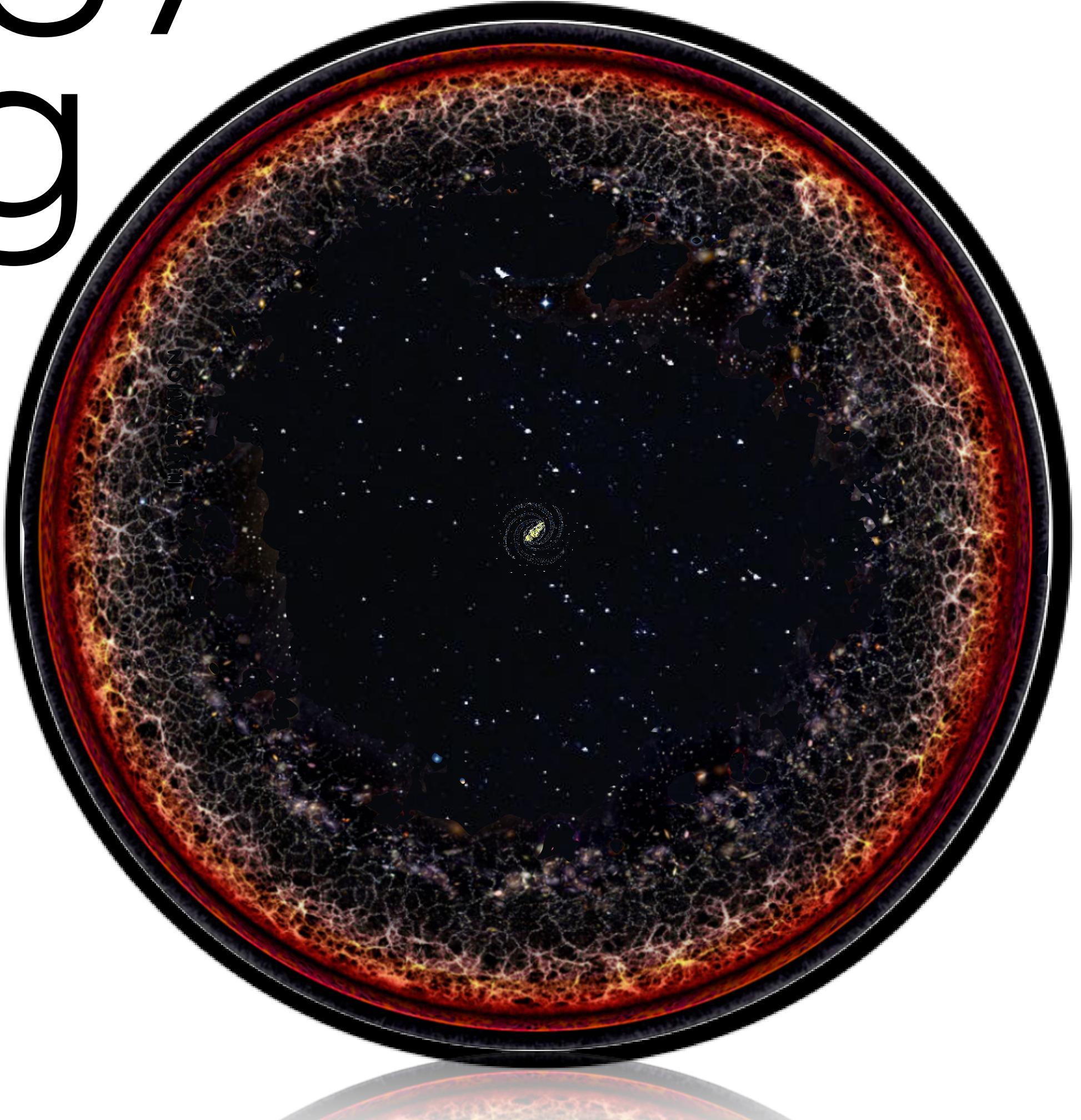


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How constrained is theory space?

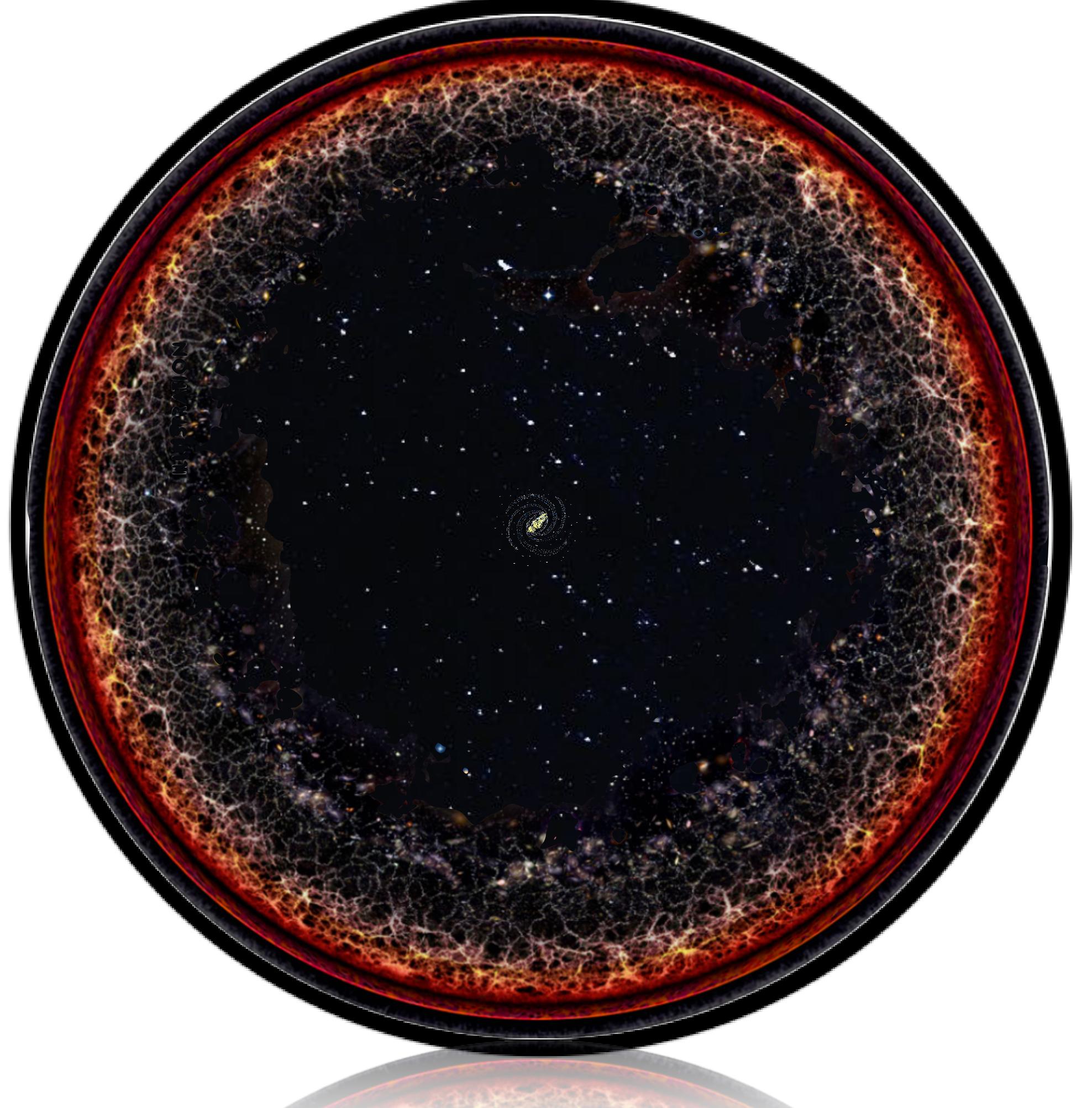


Can cosmology be a good testing ground?



Outline

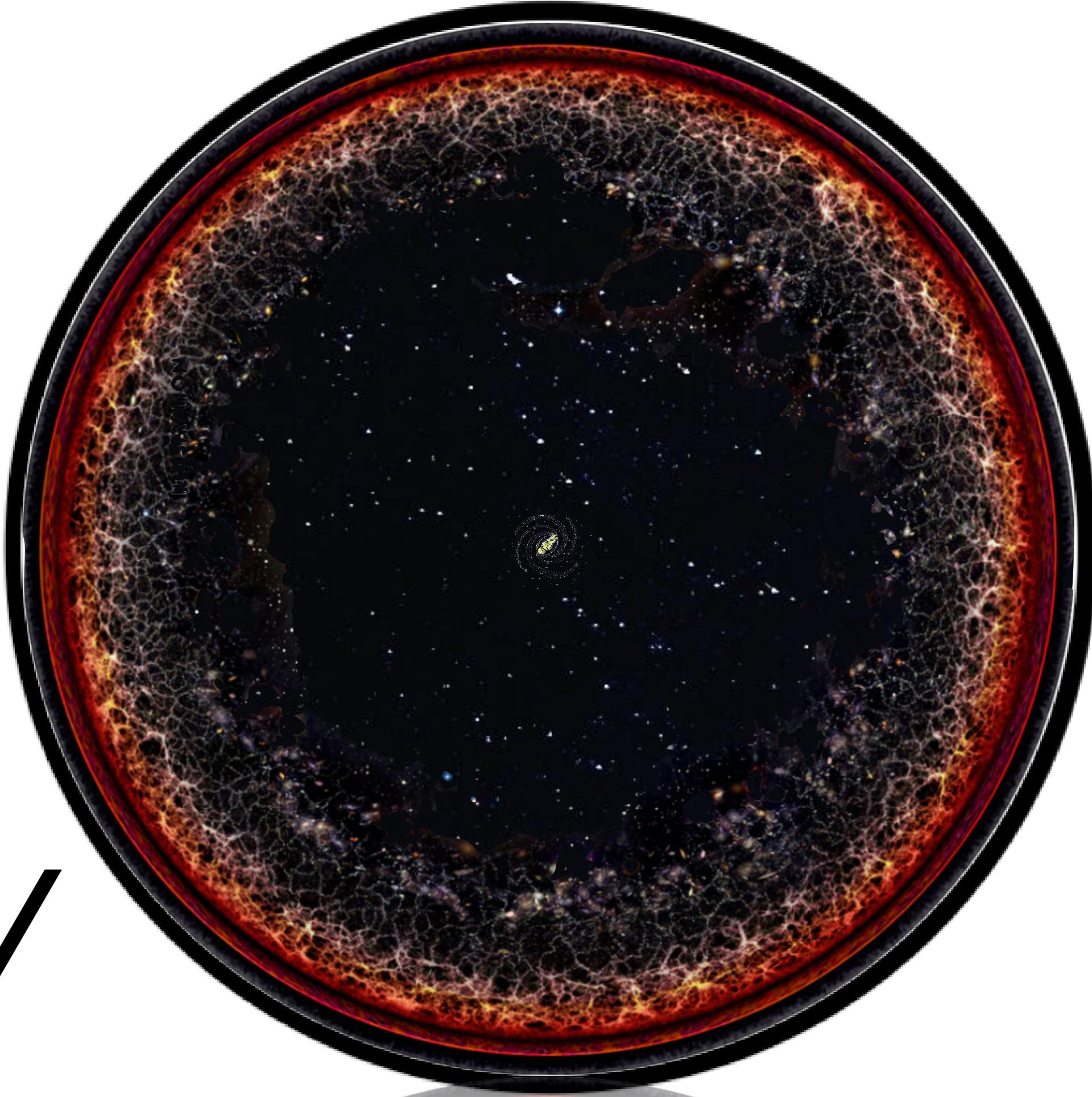
1. Cosmological tensions
2. Asymptotically safe scalar-tensor gravity
3. Outlook





Cosmological tensions

Why
cosmology





Recent breakthroughs

- accelerated expansion
Riess et al '98, Perlmutter et al '98
- neutrino oscillations
Super-Kamiokande '98
- gravitational waves
LIGO/Virgo '16
- ▶ GW170817
LIGO/Virgo '17



Big questions

Λ CDM: FLRW with 6 free parameters

What is...

- dark energy?
- dark matter?
- inflation?

$$\Omega_\Lambda$$

$$\Omega_c$$

$$n_s, A_s$$

Era of precision cosmology



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Redshift distortions

DESI, Euclid, MSE, Rubin Obs.

Supernovae 1A

SHOES, DES, Pantheon+, Rubin Obs.

CMB

LiteBird, CMB-S4

Baryon acoustic
oscillations

DESI, Euclid, MSE, Rubin Obs.

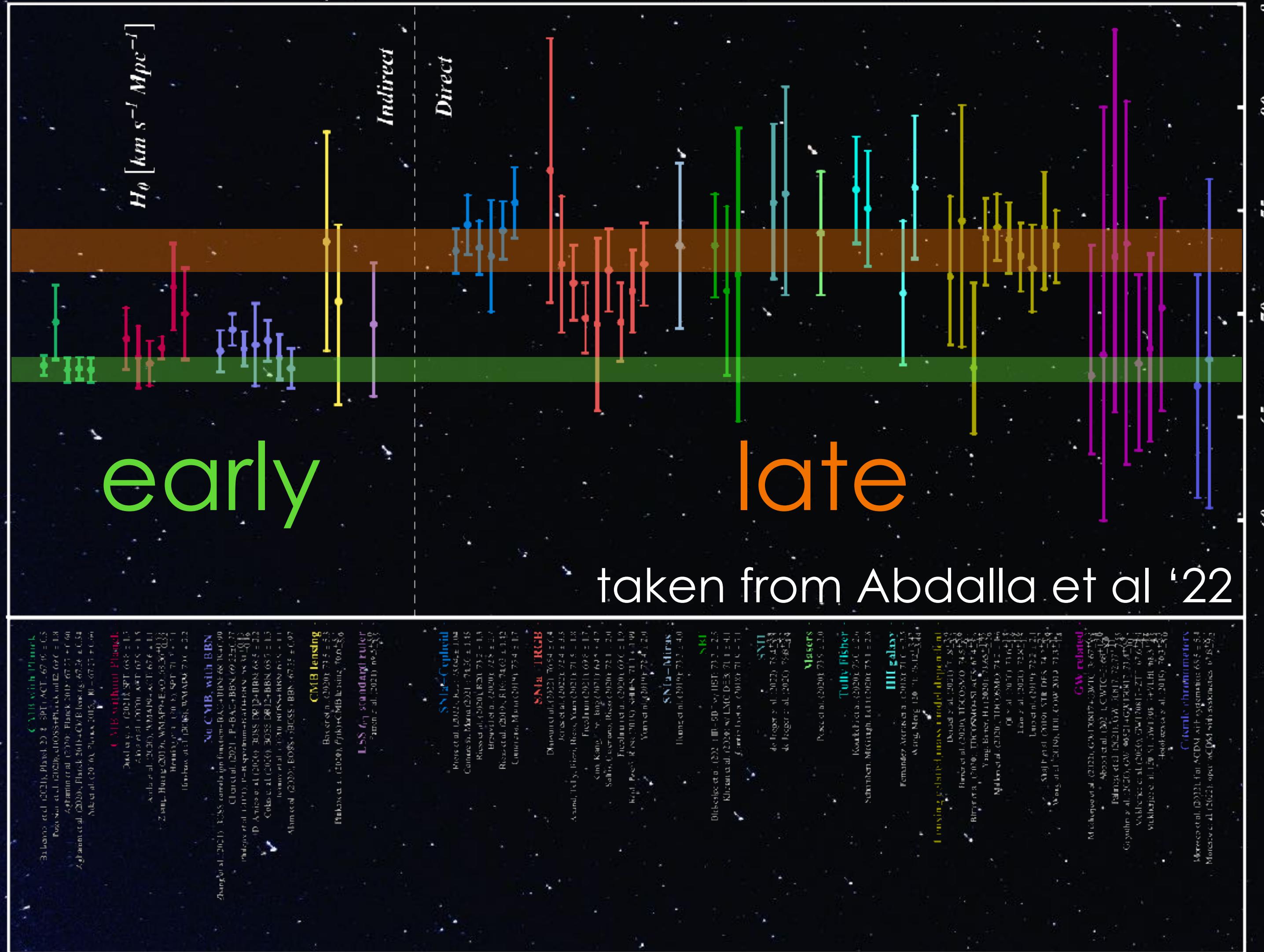
Lensing

DES, KiDS, Euclid, Rubin Obs.

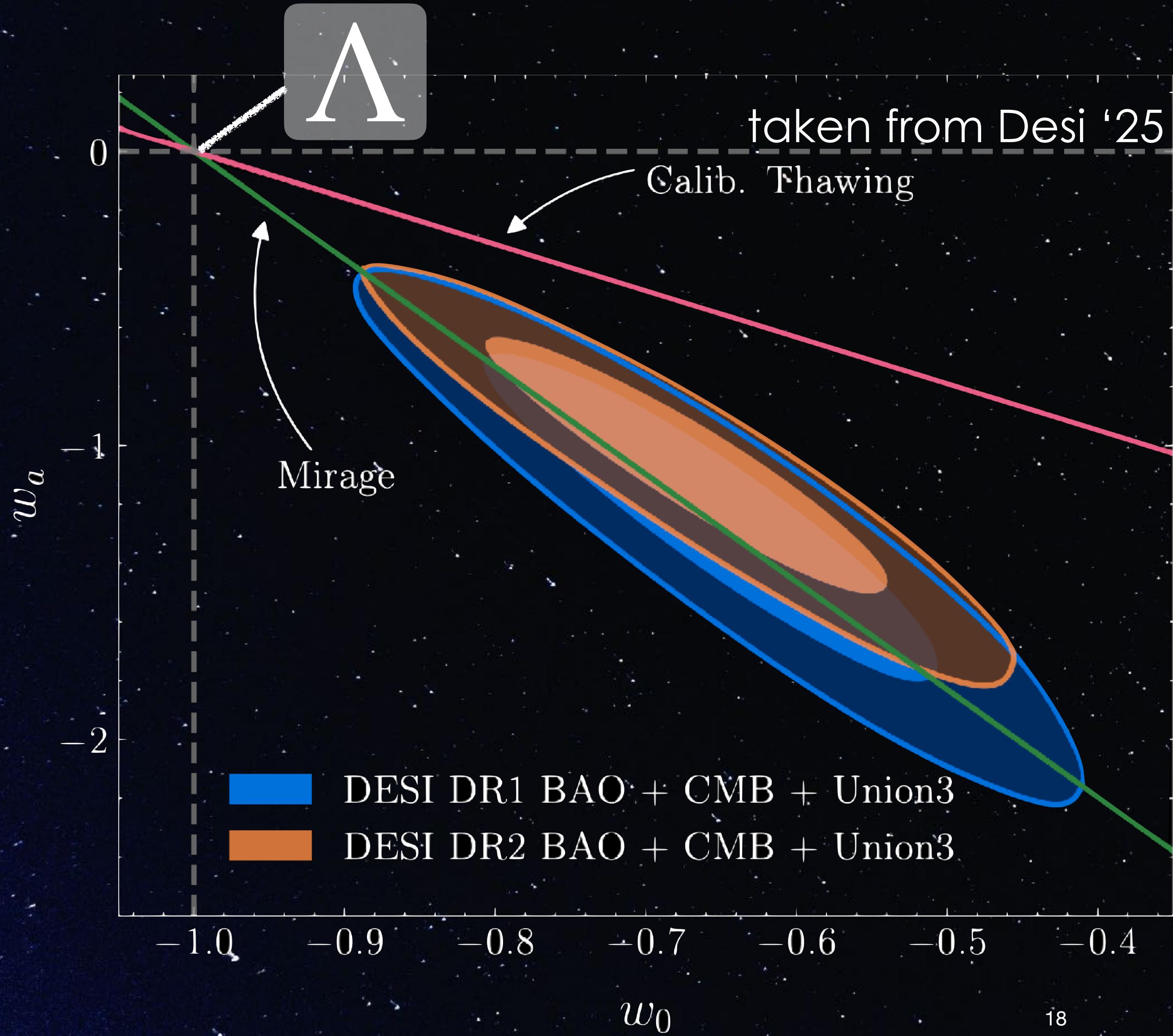
Galaxy clusters

DES, KiDS, JWST, Rubin Obs.

Cracks in the model: H_0



Cracks in the model: ω_a



related to
 H_0 -tension
Poulin et al '24, Pang et al '25



Bottom line

- many open questions
 - steady influx of data
- new physics to explore



Scalar-tensor theory

- field content: $g_{\mu\nu}, \phi$





Elephant in the room

“With four parameters I can fit an elephant, and with five I can make him wiggle his trunk”
v. Neumann

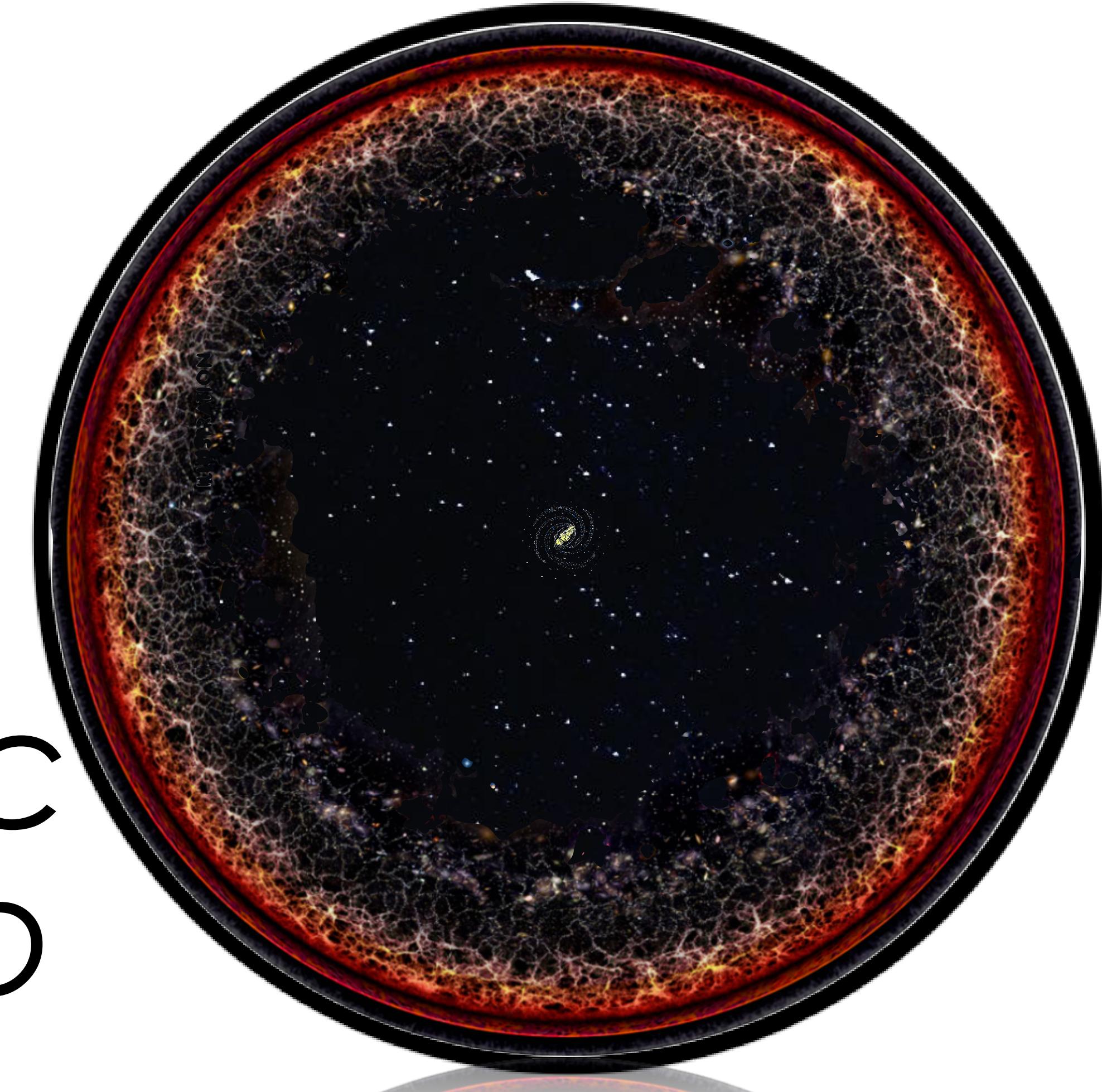
Dyson ‘04



see Wikipedia - von Neumann's elephant

Asymptotically safe scalar-tensor gravity

How asymptotic
safety may help





Scalar-tensor theory

quantum field

- field content: $g_{\mu\nu}, \phi$
- Reuter fixed point persists Percacci, Perini '03, many studies since
- ~~Reuter fixed point~~ "Gaussian" fixed point Eichhorn '12
- space of shift-sym. monomials is closed under RG-evolution Laporte et al '21

$$\text{NGFP}^{\text{ASQGM}} = \text{NGFP}^{\text{Reuter+shiftsym. mon.}} \otimes \text{GFP}^{\text{matter}}$$

Laporte et al '21

Horndeski theory

Horndeski '74



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- field content: $g_{\mu\nu}, \phi$ (kinetic term χ)
- at most 2nd-order field equations

$$\mathcal{L}_2 = -G_2(\phi, \chi)$$

$$\mathcal{L}_3 = G_3(\phi, \chi) \square \phi$$

$$\mathcal{L}_4 = -G_4(\phi, \chi)R + G_{4,\chi} \left[(\square\phi)^2 - \nabla_\mu \nabla_\nu \phi \nabla^\mu \nabla^\nu \phi \right]$$

$$\mathcal{L}_5 = G_5(\phi, \chi) G_{\mu\nu} \nabla^\mu \nabla^\nu \phi$$

$$-\frac{G_{5,\chi}}{6} \left[(\square\phi)^3 - 3 \square\phi \nabla_\mu \nabla_\nu \phi \nabla^\mu \nabla^\nu \phi + 2 \nabla_\mu \nabla_\nu \phi \nabla^\mu \nabla^\rho \phi \nabla_\rho \nabla^\nu \phi \right]$$



Horndeski theory

Horndeski '74

- field content: $g_{\mu\nu}, \phi$ (kinetic term χ)
- at most 2nd-order field equations

Ligo/Virgo '17

$$\mathcal{L}_2 = -G_2(\phi, \chi)$$

$$\frac{c_T - c}{c} \leq 10^{-15} (\text{GW170817})^*$$

$$\mathcal{L}_3 = G_3(\phi, \chi) \square \phi$$

*if EFT applies de Rham, Melville '18

$$\mathcal{L}_4 = -G_4(\phi, \chi)R + G_{4,\chi} \left[(\square\phi)^2 - \nabla_\mu \nabla_\nu \phi \nabla^\mu \nabla^\nu \phi \right]$$

$$\mathcal{L}_5 = G_5(\phi, \chi) G_{\mu\nu} \nabla^\mu \nabla^\nu \phi$$

$$-\frac{G_{5,\chi}}{6} \left[(\square\phi)^3 - 3 \square\phi \nabla_\mu \nabla_\nu \phi \nabla^\mu \nabla^\nu \phi + 2 \nabla_\mu \nabla_\nu \phi \nabla^\mu \nabla^\rho \phi \nabla_\rho \nabla^\nu \phi \right]$$

Example: kinetic braiding

Deffayet et al '10

shift-symmetric Horndeski dark energy with $c_T = c$

Shift-symmetric Horndeski gravity in the asymptotic-safety paradigm

Astrid Eichhorn,^a Rafael R. Lino dos Santos^a
and Fabian Wagner^{a,b,c}

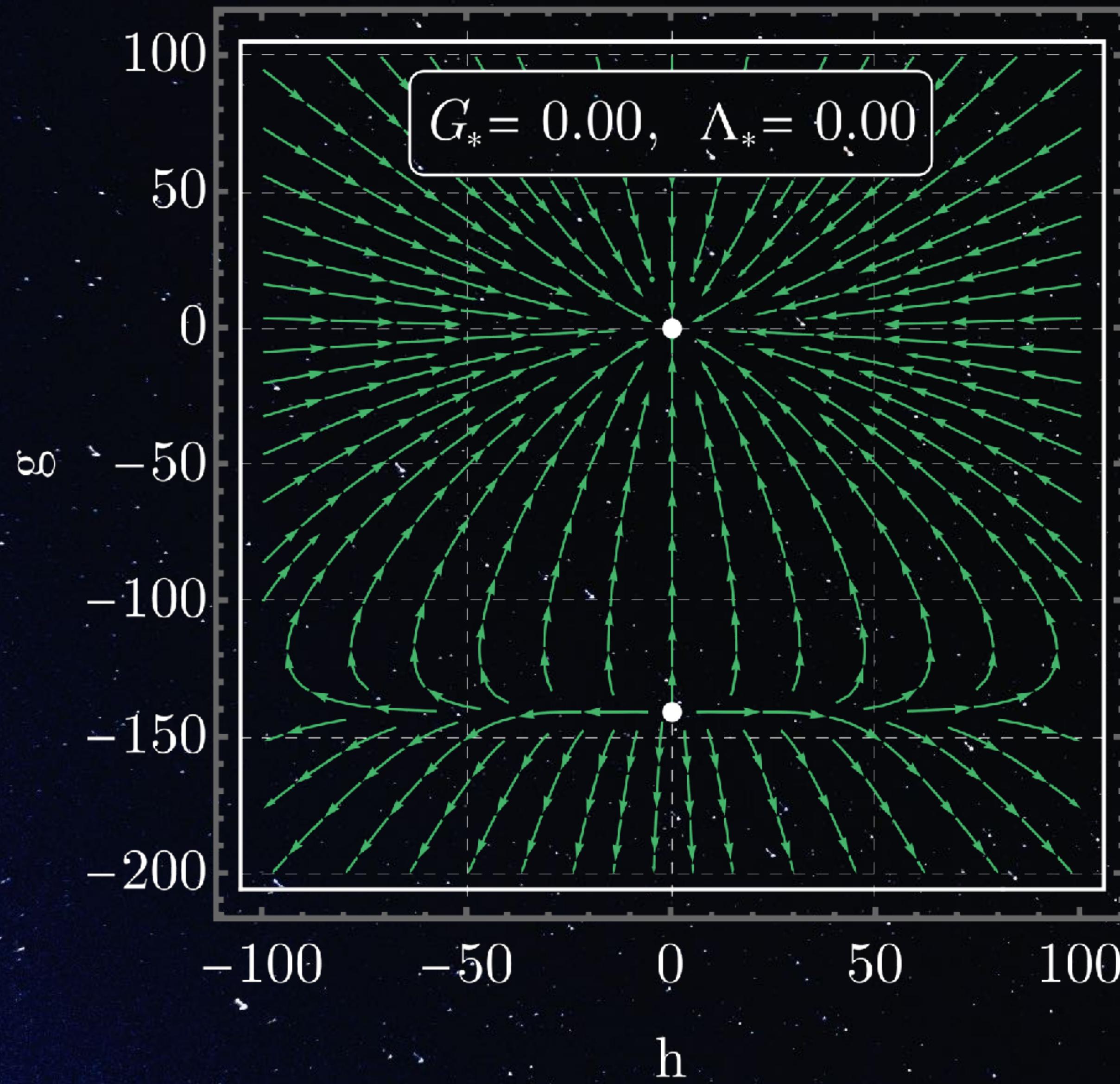
2023), 052,
2.08441 [gr-qc]

$$\mathcal{L}_2 = -G_2(\chi), \quad \mathcal{L}_3 = G_3(\chi) \square \phi, \quad \mathcal{L}_4 = -R/16\pi\bar{G}$$

$$\Gamma_k = \int_x \left(\frac{\bar{\Lambda}}{8\pi\bar{G}} - Z_\phi \chi + \bar{g} \chi^2 - \bar{h} \chi \square \phi - \frac{R}{16\pi\bar{G}} \right)$$

Example: kinetic braiding

Deffayet et al '10



- one physical fixed-point candidate
- free fixed point shifted by gravity
 $\rightarrow h_* = 0, g_* < 0$
- both g and h not free

prediction: $h_0 = 0$

Dark energy?

prediction: $h_0 = 0$

dark energy: $|\bar{h}_0| > 0$



model for dark energy incompatible
with asymptotic safety



Elephant in the room

“With four parameters I can fit an elephant, and with five I can make him wiggle his trunk”
v. Neumann

Dyson ‘04



see Wikipedia - von Neumann's elephant

Solution

Gravity alone: 3 free parameters ($\Lambda, G, \mathcal{R}^2$ -coupling)
scalar (ϕ) adds parameters dependent on symmetries

$\mathbb{Z}_2 + \text{shift}$
~~probably
not useful~~

 \mathbb{Z}_2
 ≥ 1

$m\phi^2, \xi\phi^2R, \lambda\phi^4$

none

 ≥ 3

$m\phi^2, \lambda_{(3)}\phi^3, \xi_{(3)}\phi R$

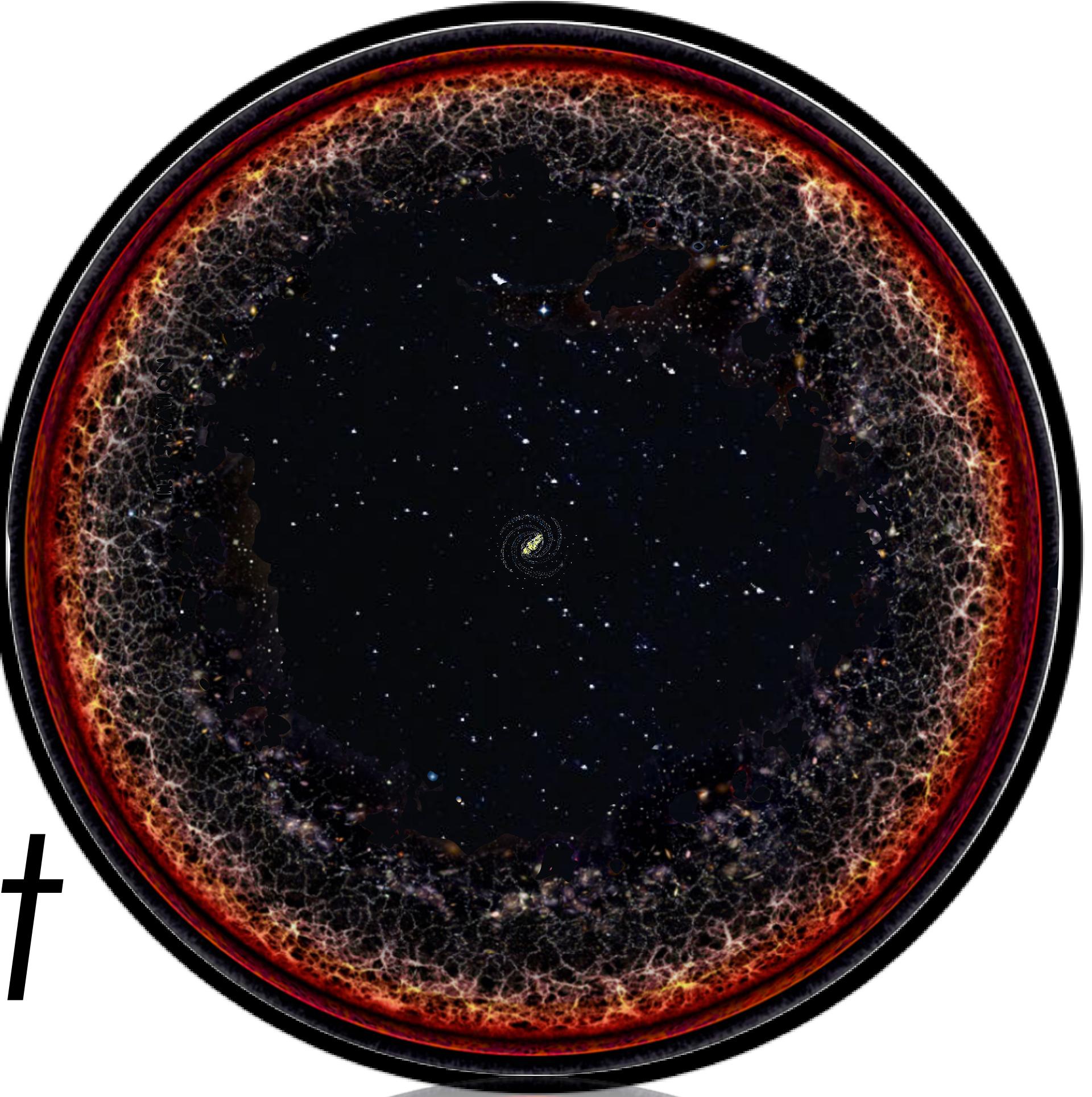
$\xi\phi^2R, \lambda\phi^4$

Outlook



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What's next





What's next

$$\mathbb{Z}_2$$

$$\geq 1$$

$$m\phi^2, \xi\phi^2R, \lambda\phi^4$$



What's next

Dark energy

$$\mathbb{Z}_2$$

$$\geq 1$$

$$m\phi^2, \xi\phi^2R, \lambda\phi^4$$



$c_T = c?$ Eichhorn, FW WIP

generate $G_4(\chi)R \sim \Lambda_{\text{UV}}^{-2}$

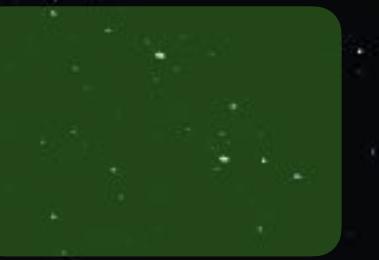
$c_T = c_\gamma \neq c?$ Mironov et al '24

generate $G_4(\chi)F^2, \dots$

leave Horndeski?

generate $\phi f(\square)\phi, \dots$

What's next



none

≥ 3

$m\phi^2, \lambda_{(3)}\phi^3, \xi_{(3)}\phi R$

$\xi\phi^2R, \lambda\phi^4$



What's next

Inflation

none

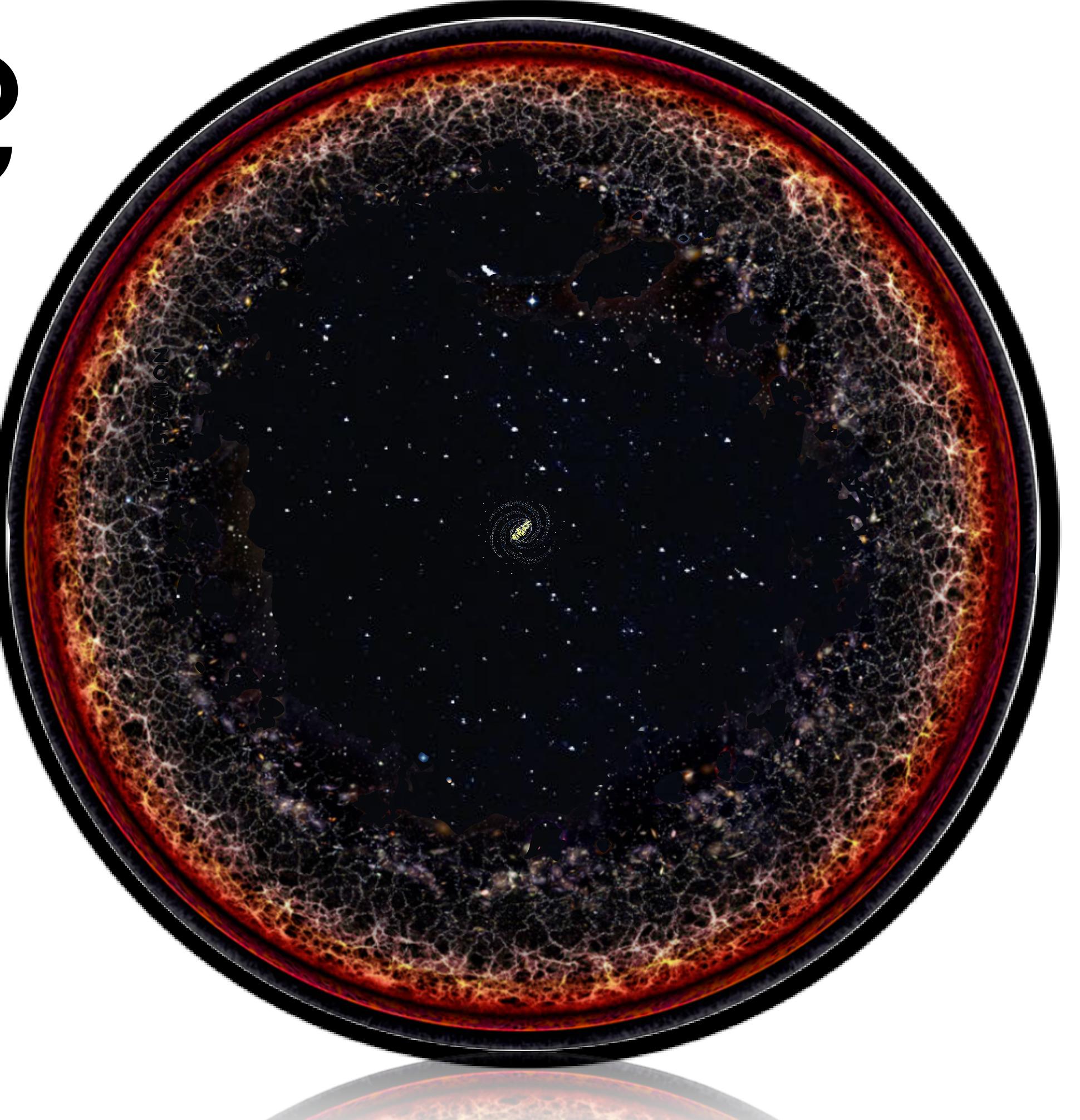
≥ 3

$m\phi^2, \lambda_{(3)}\phi^3, \xi_{(3)}\phi R$

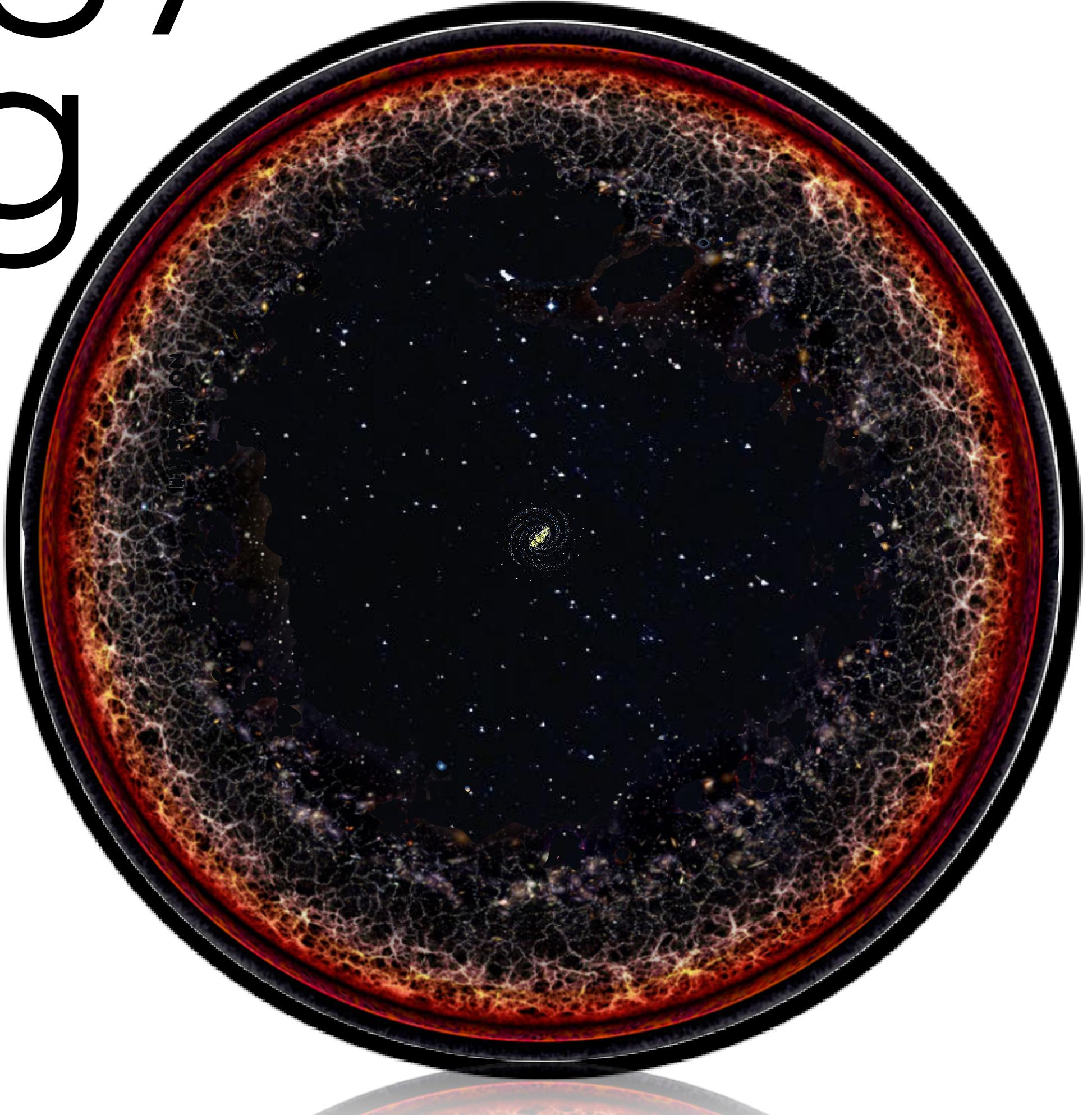
$\xi\phi^2R, \lambda\phi^4$

- reconstruct $V(\phi)$ and $F(\phi)R$ from free parameters Silva '25
- primordial black holes?
Bauer, Eichhorn, Knorr, FW WIP

How constrained is theory space?



Can cosmology be a good testing ground?



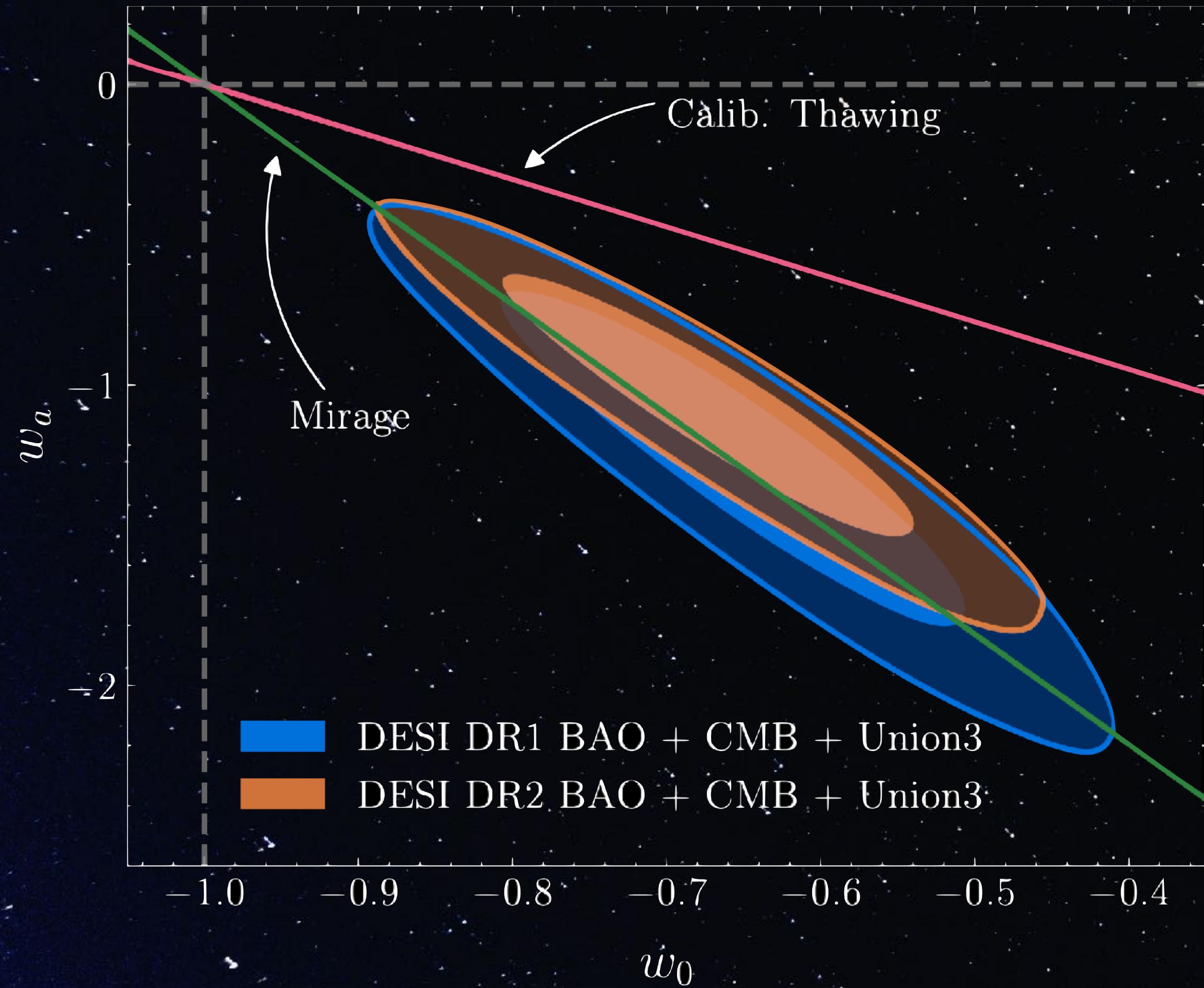
Summary

quantum-
gravity
constraints

cosmological
constraints

no wiggle room

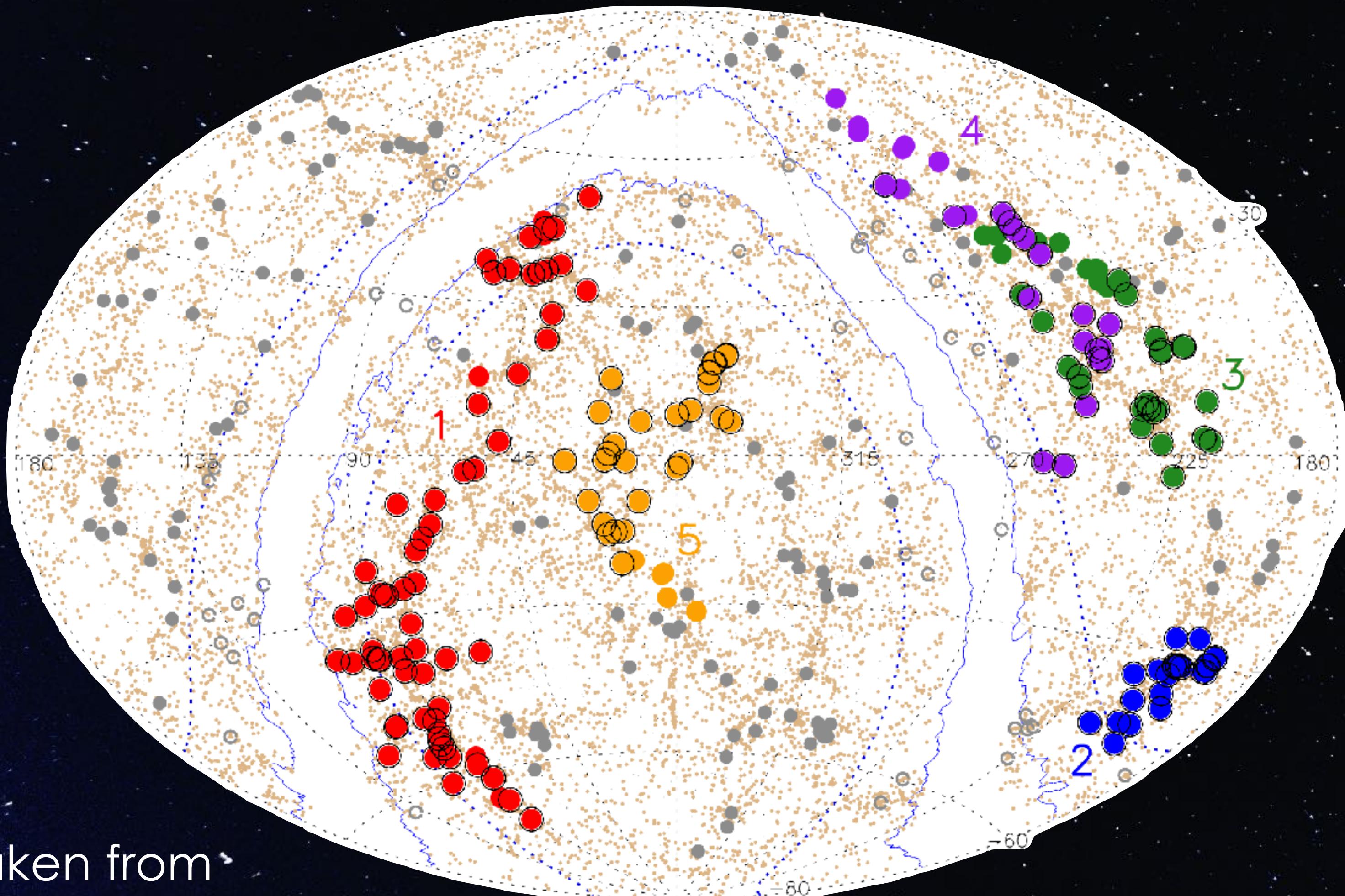
Cracks in the model: ω_a



$$\omega_{\Lambda} = \omega_0 + \omega_a \frac{z}{z+1}$$

$> 3\sigma$

Cracks in the model: Cosmological principle



structures
 $>400\text{Mpc}$

taken from
Böhringer et al '25