

Indications for particle physics from asymptotic safety

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in collaboration with E. M. Sessolo
and
A. Chikkaballi, S. Pramanick, D. Rizzo, Y. Yamamoto

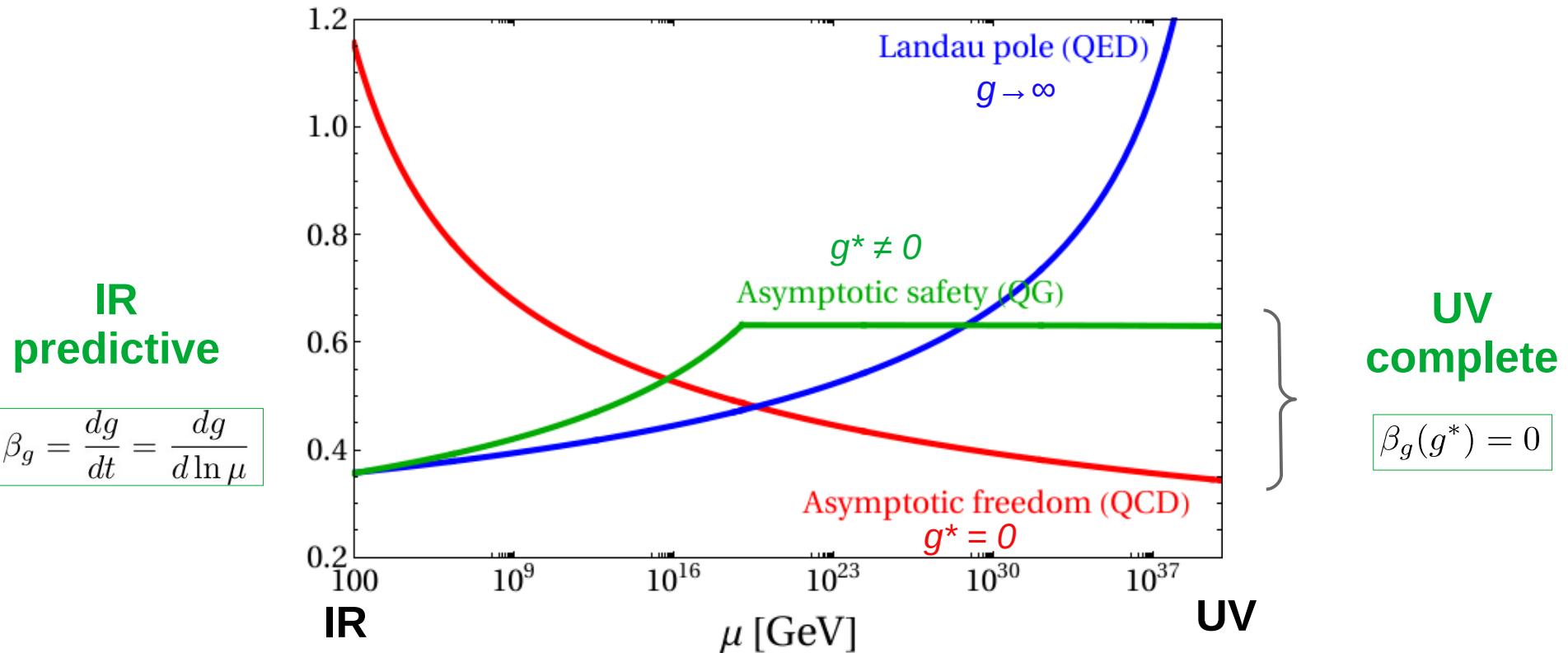
Mainly based on:
Eur.Phys.J.C 81 (2021) 4, 272 (arXiv: 2007.03567)
JHEP 08 (2022) 262 (arXiv: 2204.00866)
JHEP 11 (2023) 224 (arXiv: 2308.06114)
and work in progress

Quantum spacetime and the Renormalization Group 2025

Heidelberg, 31.03.2025

Asymptotic safety

... why we like it

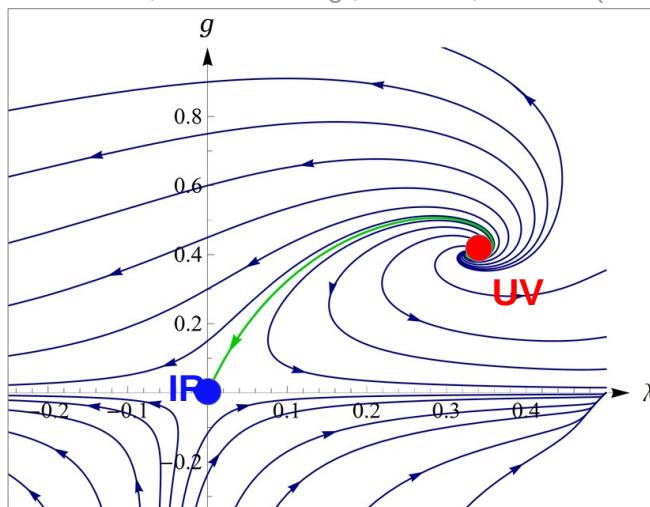


Asymptotic safety

... how we get it

Trans-Planckian fixed point for gravity (FRG)

M. Reuter, F. Saueressig , PRD 65, 065016 (2002)



Other possibility in 4D:

- Gauge-Yukawa (Li-Sa) models
(Litim, Sannino, JHEP 1412 (2014) 178)

Trans-Planckian corrections to matter RGes (FRG)

$$k > M_{\text{Pl}}$$

$$\beta_g = \beta_g^{\text{SM+NP}} - g f_g = 0$$
$$\beta_y = \beta_y^{\text{SM+NP}} - y f_y = 0$$

fixed points for
matter

parametric description of
(universal) gravity contributions

e.g. A. Eichhorn, A. Held, 1707.01107
A. Eichhorn, F. Versteegen, 1709.07252

heuristic approach: confront AS
with low-scale pheno

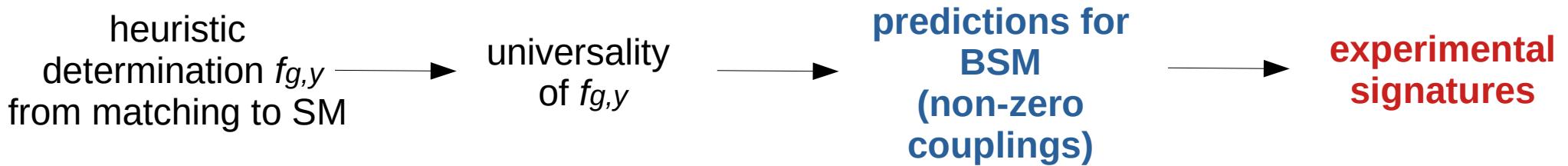
Asymptotic safety

... what we can learn

- **Predictions** for Beyond the Standard Model
- **Consistency** of the IR physics with the AS ansatz
- **Naturally small** parameters (eg. neutrino masses)
- **Forbidding couplings** allowed by symmetries
- Conclusions

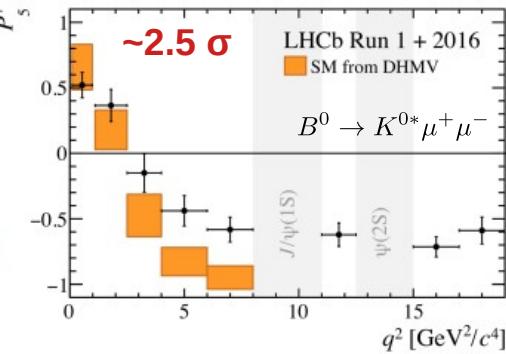
Predictions for BSM

Working assumption:
there is a UV interacting FP for (some) SM couplings

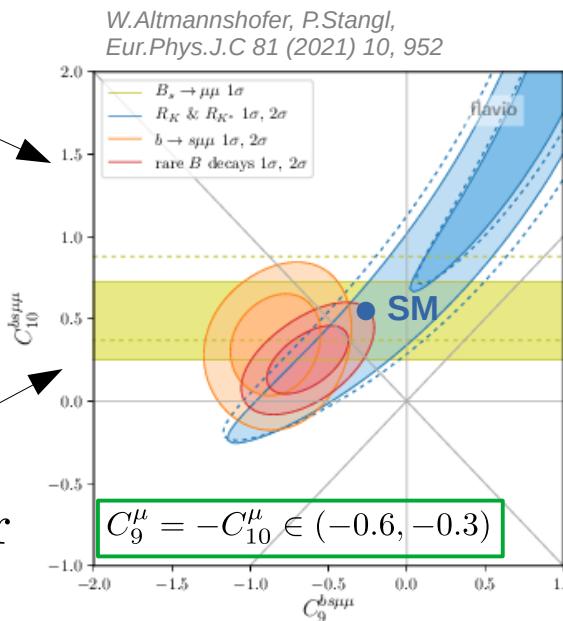


Particularly usefull for **experimental anomalies**:

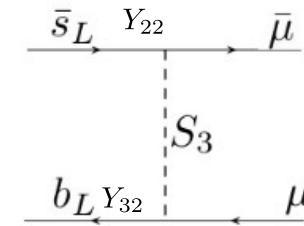
experimental data (eg. b to s anomalies)



$$\mathcal{C}_{\text{NP}} \approx \frac{c_i c_j}{m_{\text{NP}}^n} \times \text{loop factor}$$



BSM model (ex. leptoquarks)



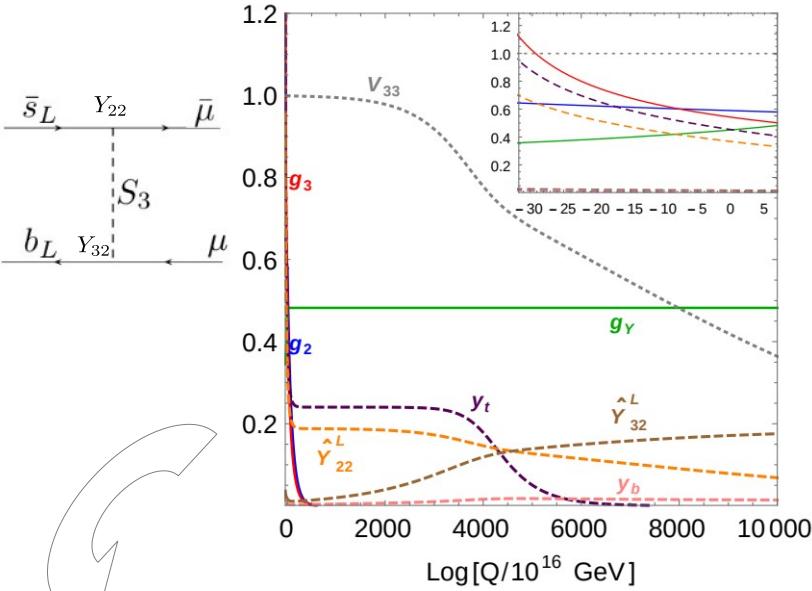
$$C_9^\mu = -C_{10}^\mu = \frac{\pi v_h^2}{V_{33} V_{32}^* \alpha_{\text{em}}} \frac{\hat{Y}_{32}^L \hat{Y}_{22}^{L*}}{m_{S_3}^2}$$

no precise prediction for the BSM mass

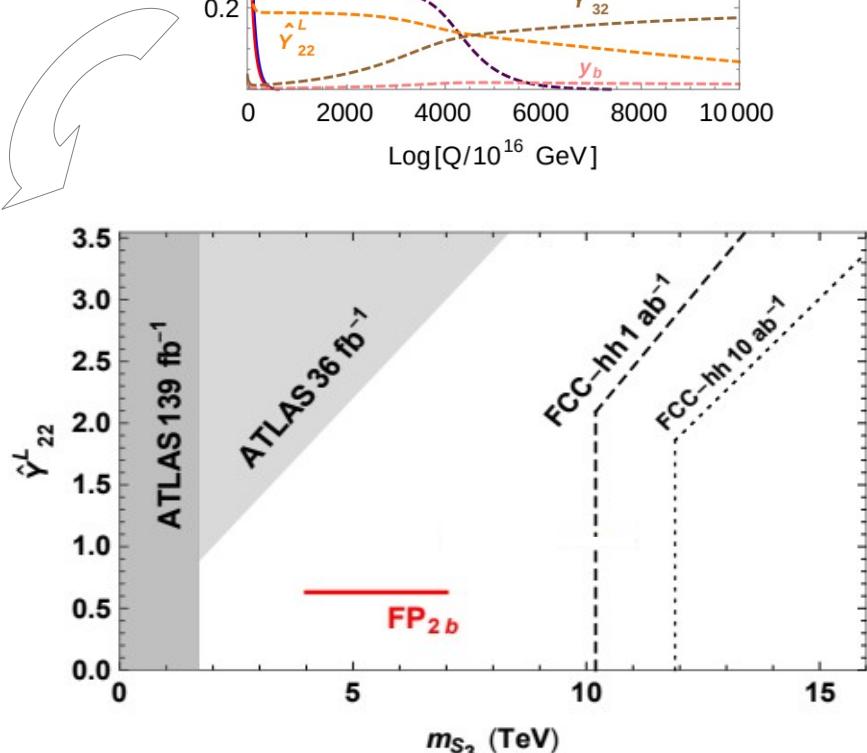
Example: leptoquark mass

KK, E.M.Sessolo, Y.Yamamoto,
Eur.Phys.J.C 81 (2021) 4, 272

SM + LQ + QG



**UV boundary conditions
conditions
from irrelevant
 g_Y and y_t**



mass predicted

$$M_{S_3} \in (4.5, 7) \text{ TeV}$$

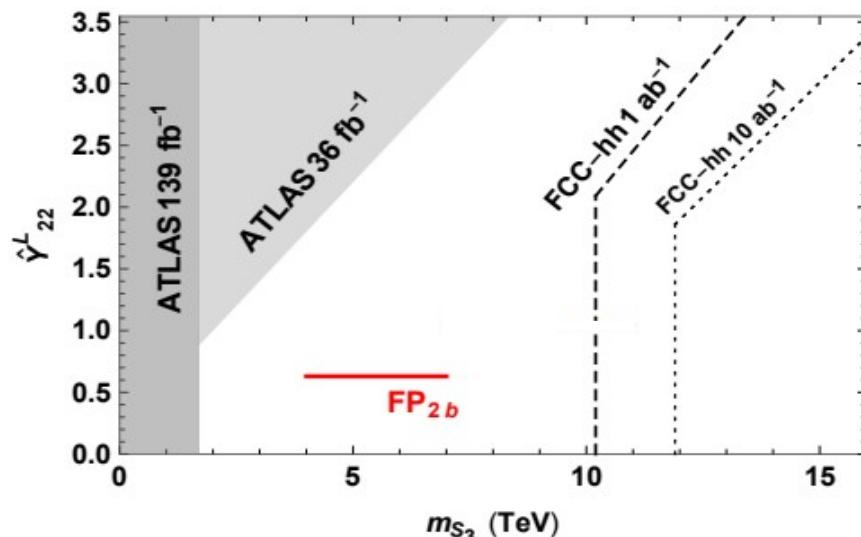
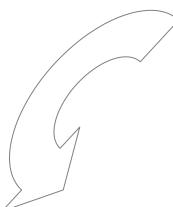
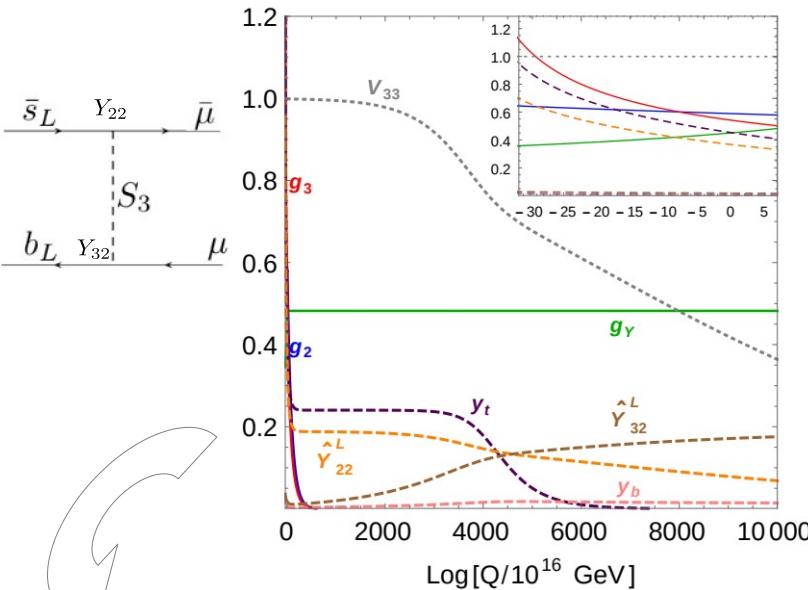
In the reach of the FCC!

also: complementary predictions in flavor: ex. D-meson decays

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KK, E.M.Sessolo, Y.Yamamoto,
Eur.Phys.J.C 81 (2021) 4, 272

SM + LQ + QG



also: complementary predictions in flavor: ex. D-meson decays

Some other works along this lines...

- anomalies in $b \rightarrow s$

A.Chikkaballi, W. Kotlarski, KK, D.Rizzo, E.M.Sessolo,
JHEP 01 (2023) 164

- anomalies in $b \rightarrow c$

KK, E.M.Sessolo, Y.Yamamoto,
Eur.Phys.J.C 81 (2021) 4, 272

- muon $g-2$

KK, E.M.Sessolo, Phys. Rev. D 103, (2021)

Other AS predictions for BSM

Reichert, Smirnov, 1803.04027; Grabowski, Kwapisz, Meissner, 1810.08461; Hamada, Tsumura, Yamada, 2002.03666, Eichhorn, Pauly, 2005.03661; de Brito, Eichhorn, Lino dos Santos, 2112.08972, Boos, Carone, Donald, Musser, 2206.02686, 2209.14268, Eichhorn, dos Santos, Miqueleto, 2306.17718

mass predicted

$$M_{S_3} \in (4.5, 7) \text{ TeV}$$

In the reach of the FCC!

Predictions for BSM

PROS:

- UV constraints on BSM (a priori free) couplings
- Allows to pinpoint BSM masses when confronted with data
- Predictions are (very) robust

W.Kotlarski, KK, D.Rizzo, E.M.Sessolo
EPJC '23, arXiv: 2304.08959

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CONS:

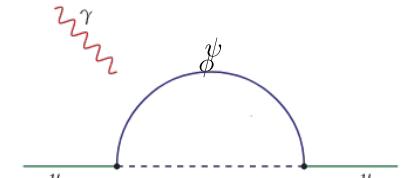
- Interactive fixed point in the SM needed but...  A. Pastor-Gutiérrez, J. M. Pawłowski, M. Reichert
SciPost Phys. 15 (2023) 3, 105
- Very specific values of f_g, f_y required  What about FRG?
- Only useful when there is experimental data
- No clear way of checking consistency with AS (case by case analysis needed)

Consistency between AS and pheno

VL fermions: 

$$\mathcal{L}_{\text{NP}} \supset (Y_R \mu_R E' S + Y_L F' S^\dagger l_\mu + Y_1 E h^\dagger F + Y_2 F' h E' + \text{H.c.})$$

$Y_R^* \neq 0, Y_L^* \neq 0, Y_1^* \neq 0, Y_2^* = 0$ *to explain g-2*



in the context of g-2

$$\frac{dy_\mu}{dt} = \frac{1}{16\pi^2} \left\{ \left[3y_t^2 + C_1 \left(Y_1^2 + Y_2^2 + \frac{1}{2}Y_L^2 + \frac{1}{2}Y_R^2 \right) - \frac{15}{4}g_Y^2 - \frac{9}{4}g_2^2 \right] y_\mu + C_2 Y_2 Y_R Y_L \right\} - f_y y_\mu$$

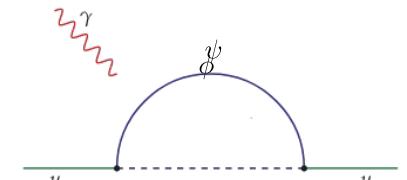
allows for $y_\mu^* = 0$ muon mass correct

Consistency between AS and pheno

VL fermions: ☺

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Leptoquark: ☹

$$\mathcal{L}_{NP} \supset Y_{ij}^L Q_i^T (-i\sigma_2) L_j S_1 + Y_{ij}^R u_{R\,i}^* e_{R\,j}^* S_1 + \text{H.c.}$$

$Y_{32}^{R*} \neq 0, Y_{32}^{L*} \neq 0$ to explain g-2

$$\frac{dy_\mu}{dt} \sim -6 y_t Y_{33}^R Y_{23}^L$$

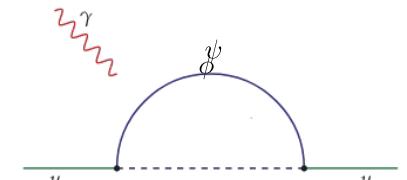
does not allow for $y_\mu^* = 0$ muon mass incorrect ~ top mass

Consistency between AS and pheno

VL fermions: 😊

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Leptoquark: 😢

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to explain g-2
NOT CONSISTENT WITH AS

$$\frac{dy_\mu}{dt} \sim -6 y_t Y_{33}^R Y_{23}^L$$

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Naturally small neutrino masses

NuFIT5.1 (2021) 2007.14792

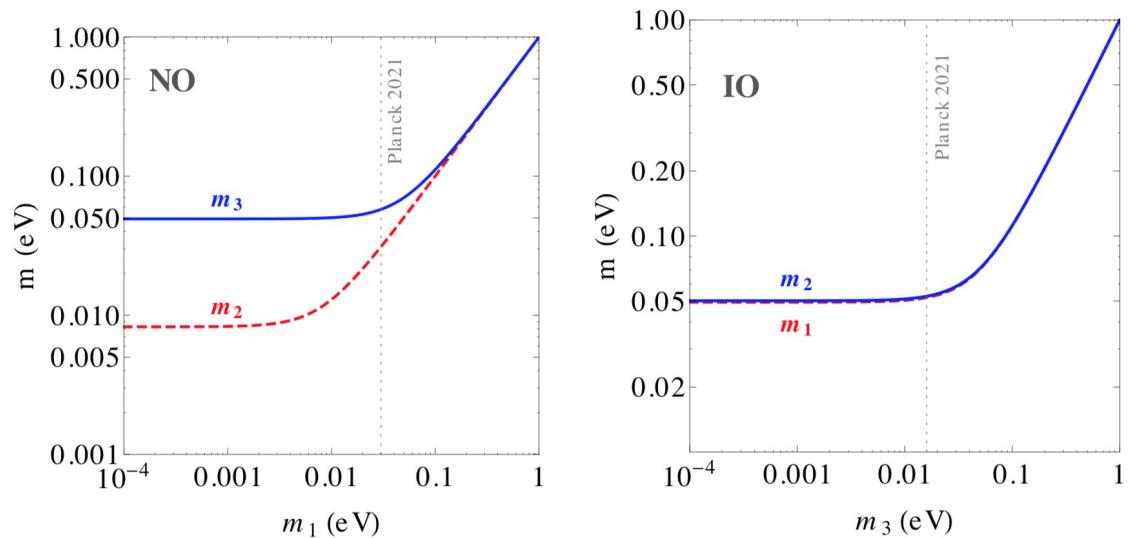
$$\Delta m_{21}^2 = 7.42^{+0.21}_{-0.20} \times 10^{-5} \text{ eV}^2,$$

NO: $\Delta m_{31}^2 = 2.515^{+0.028}_{-0.028} \times 10^{-3} \text{ eV}^2,$

IO: $\Delta m_{32}^2 = -2.498^{+0.028}_{-0.029} \times 10^{-3} \text{ eV}^2,$

Planck (2021) 1807.06209

$$\sum_{i=1,2,3} m_i < 0.12 \text{ eV}$$



either Dirac neutrino ...

... or Majorana neutrino

$$\mathcal{L}_D = -y_\nu^{ij} \nu_{R,i} (H^c)^\dagger L_j + \text{H.c.}$$

$$m_\nu = \frac{y_\nu v_H}{\sqrt{2}}$$

- 10^{-13} Yukawa coupling
- Lepton number is conserved

e.g. Type 1 see-saw

$$\mathcal{L}_M = \mathcal{L}_D - \frac{1}{2} M_N^{ij} \nu_{R,i} \nu_{R,j} + \text{H.c.}$$

$$m_\nu = \begin{pmatrix} 0 & m_D^T \\ m_D & M_N \end{pmatrix} \quad m_\nu = y_\nu^2 v_h^2 / (\sqrt{2} M_N)$$

- $O(1)$ Yukawa coupling
- Lepton number is violated

Naturally small neutrino masses

KK, S.Pramanick, E.Sessolo, JHEP 08 (2022) 262

SM + RHN:

$$\begin{aligned}\frac{dg_Y}{dt} &= \frac{g_Y^3}{16\pi^2} \frac{41}{6} - f_g g_Y = 0 \quad \text{get } f_g \\ \frac{dy_t}{dt} &= \frac{y_t}{16\pi^2} \left[\frac{9}{2}y_t^2 + y_\nu^2 - \frac{17}{12}g_Y^2 \right] - f_y y_t = 0 \quad \text{get } f_y \\ \frac{dy_\nu}{dt} &= \frac{y_\nu}{16\pi^2} \left[3y_t^2 + \frac{5}{2}y_\nu^2 - \frac{3}{4}g_Y^2 \right] - f_y y_\nu = 0 \quad \text{predict}\end{aligned}$$

$\longrightarrow g_Y^*, y_t^* \sim \mathcal{O}(1)$

$\beta_\nu \equiv \frac{dy_\nu}{dt} = 0 \rightarrow$ two IRR solutions for neutrino FP:

1. $y_\nu^{*2} = \frac{32\pi^2}{5}f_y + \frac{3}{10}g_Y^{*2} - \frac{6}{5}y_t^{*2}$ (interactive)

2. $y_\nu^* = 0$ (Gaussian)

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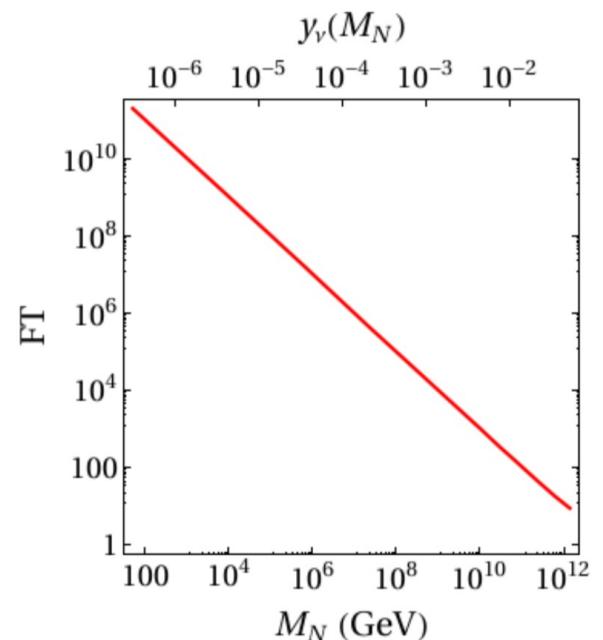
1. $y_\nu^{*2} = \frac{32\pi^2}{5} f_y + \frac{3}{10} g_Y^{*2} - \frac{6}{5} y_t^{*2}$ (interactive)

large fine tuning of f_y to get small Yukawa

large Yukawa coupling \rightarrow Majorana neutrino

$$m_\nu = y_\nu^2 v_h^2 / (\sqrt{2} M_N)$$

AS prediction for the Majorana mass



Naturally small neutrino masses

KK, S.Pramanick, E.Sessolo, JHEP 08 (2022) 262

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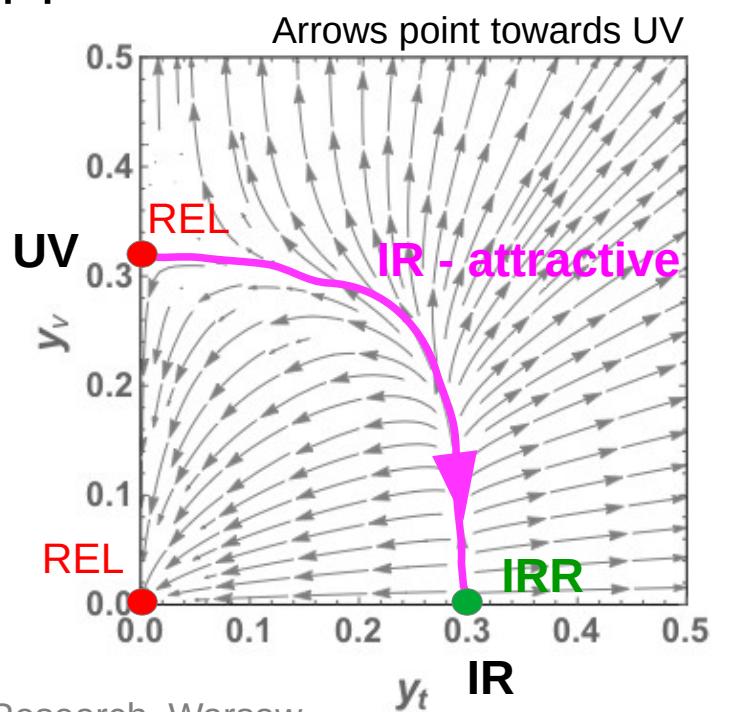
2. $y_\nu^* = 0$ (Gaussian)

Irrelevant if f_y is small enough!

$$f_y < f_{\nu,tY}^{\text{crit}} \approx 0.0008 \quad 16\pi^2 \theta_\nu \approx -\frac{2}{3} g_Y^{*2} + \frac{3}{2} y_t^{*2} < 0$$

small Yukawa coupling \rightarrow Dirac neutrino

Relevant FPs provide a UV completion



Naturally small neutrino masses

Integrated curve in blue :

$$y_\nu(t; \kappa) \approx \left(\frac{16\pi^2 f_y}{e^{f_y(\kappa-t)} + 5/2} \right)^{1/2}$$

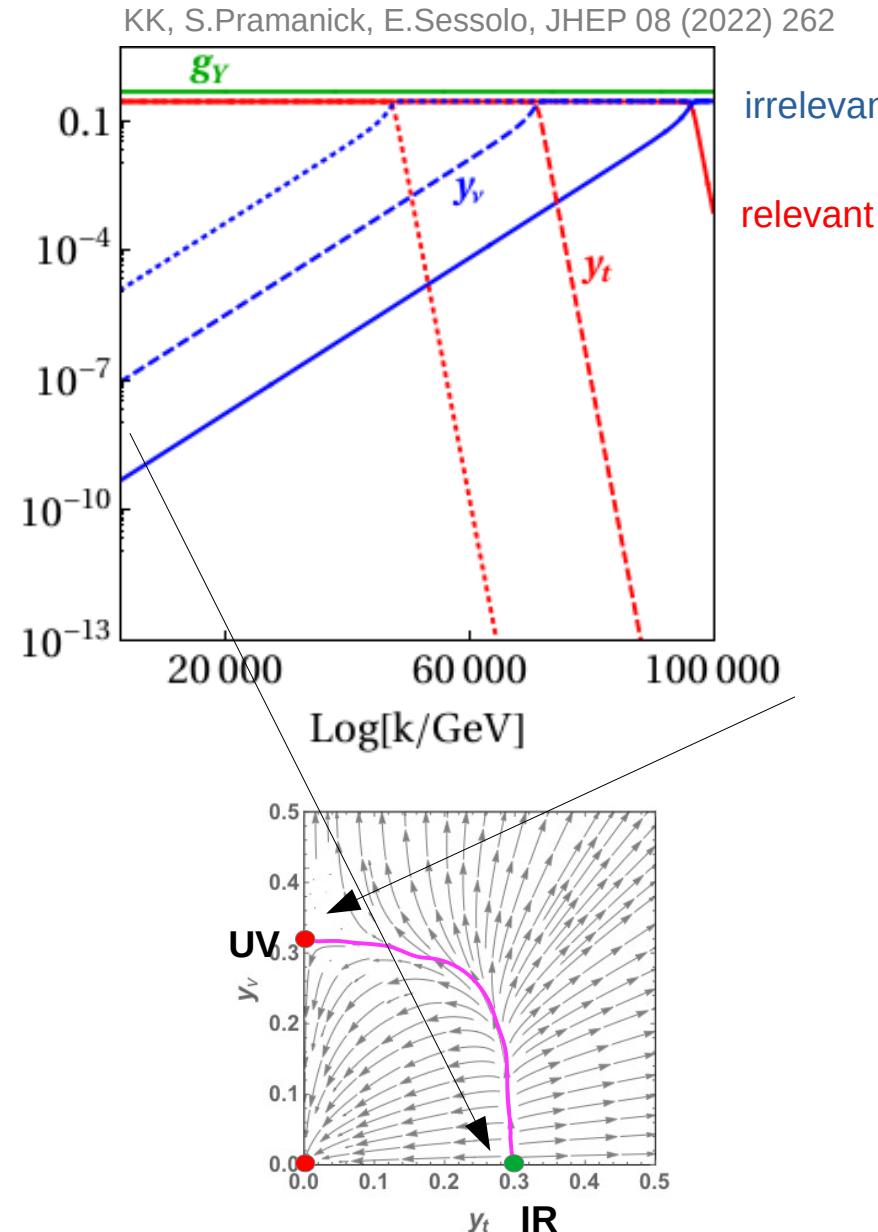
κ = “distance” in e-folds

No fine tuning:

Smallness of the neutrino Yukawa due to the “distance” of the Planck scale from infinity

Neutrinos can be Dirac naturally

Alternative to the see-saw mechanism



The mechanism is more generic...

In pairs of Yukawa interactions one can use the “large” Y_L to drive down the “small” Y_S ...

$$\mathcal{L} \supset Y_S \chi_R \Phi \chi_L + Y_L \psi_R \Phi \psi_L + \text{H.c.}$$

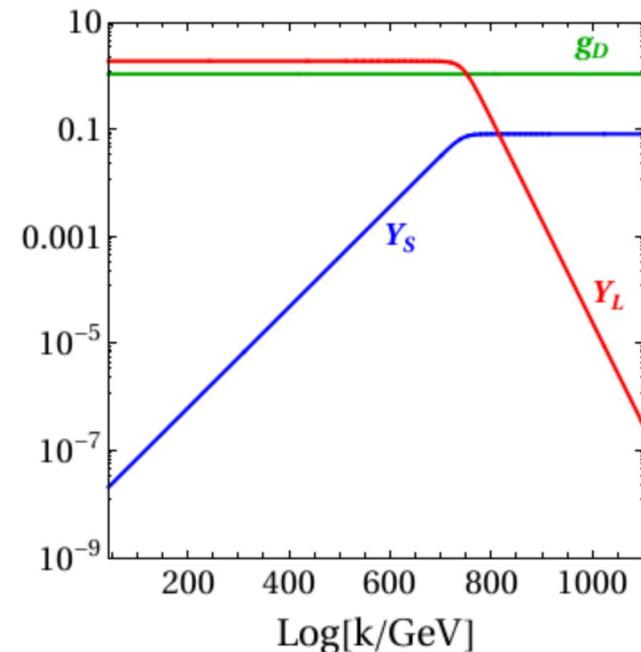
Recall that...

$$\frac{dy_X}{dt} = \frac{y_X}{16\pi^2} [\alpha_X y_X^2 + \alpha_Z y_Z^2 - \alpha_Y g_Y^2] - f_y y_X$$

$$\frac{dy_Z}{dt} = \frac{y_Z}{16\pi^2} [\alpha'_X y_X^2 + \alpha'_Z y_Z^2 - \alpha'_Y g_Y^2] - f_y y_Z$$

... thus we want ...

$$f_{Z,XY}^{\text{crit}} = \frac{g_Y^{*2}}{16\pi^2} \frac{\alpha'_X \alpha_Y - \alpha'_Y \alpha_X}{\alpha_X - \alpha'_X} > f_y \text{ (from UV)}$$



... it happens often (but not always) if $Q_\psi \gg Q_\chi$ (gauge charge)

Can use it to justify freeze-in, feebly interacting models, etc...

Connections to FRG

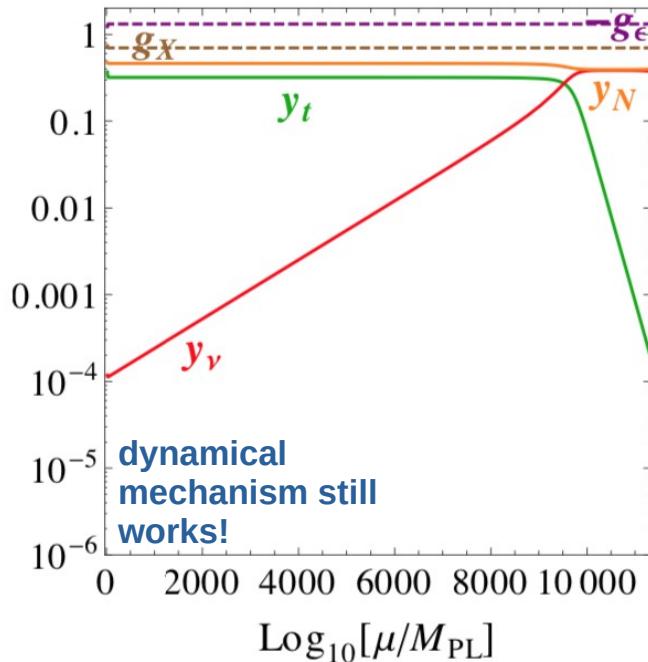
A. Chikkaballi, KK, E. Sessolo, 2308.06114

SM + gauged $U(1)_{B-L}$ + QG:

$$g_Y^* = 0 \dots$$

... but its role played by

$$g_X^* \neq 0, \quad g_\epsilon^* \neq 0$$



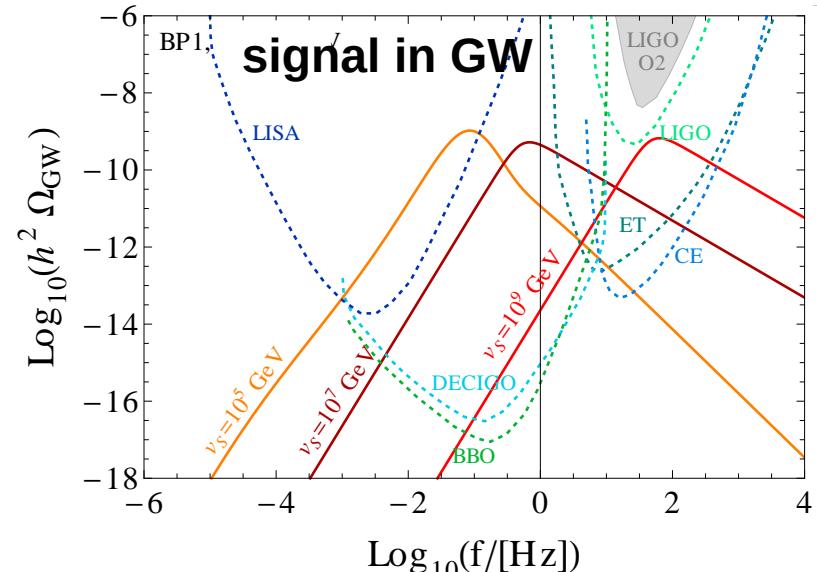
Extra info: FP analysis provides predictions for g_X, g_ϵ

extended gauge sector

$$\mathcal{L} \supset -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{4}X_{\mu\nu}X^{\mu\nu} - \frac{\epsilon}{2}B_{\mu\nu}X^{\mu\nu} \\ + i\bar{f}\left(\partial^\mu - ig_Y Q_Y \tilde{B}^\mu - ig_{B-L} Q_{B-L} \tilde{X}^\mu\right)\gamma_\mu f$$

easier to make consistent with the FRG calculations

	f_g	f_y	g_X^*	g_ϵ^*	$g_X (10^{5,7,9} \text{ GeV})$
BP1	0.01	0.0005	0.10	-0.55	0.29, 0.29, 0.30
BP2	0.05	-0.005	0.70	-1.32	0.40, 0.41, 0.44
BP3	0.02	-0.0015	0.10	-0.75	0.12, 0.12, 0.12
BP4	0.03	-0.004	0.10	0.75	0.09, 0.09, 0.09



Forbidding (allowed) couplings

A. Chikkaballi, KK, R. Lino dos Santos, E. Sessolo,
work in progress

Motivation: stability of the dark matter particle

SU(N) dark matter: stabilizing Z_2 added “by hand” ex. E. Ma, Phys. Rev. D 103, 051704 (2021)

ex. SU(6) minimal anomaly free setup: $15_Q, \bar{6}_D, \bar{6}_P$

$$\underbrace{\text{SM}}_{\text{dark sector}} \quad \bar{6}_P = \bar{5}_P + \underbrace{1_P}_{\text{DM}}$$

$$\begin{aligned} \mathcal{L} \supset & Y_D 15_Q \bar{6}_D \bar{6}_{H_1} + Y_{\text{mix}} 15_Q \bar{6}_P \bar{6}_{H_1} + Y'_D 15_Q \bar{6}_D \bar{6}_{H_3} + Y'_{\text{mix}} 15_Q \bar{6}_P \bar{6}_{H_3} \\ & + Y_U 15_Q 15_Q 15_{H_2} + Y_1 \bar{6}_D \bar{6}_D 15_{H_2} + Y_2 \bar{6}_P \bar{6}_P 15_{H_2} + Y_{12} \bar{6}_D \bar{6}_P 15_{H_2} \\ & + Y_3 \bar{6}_D \bar{6}_D 21_{H_4} + Y_4 \bar{6}_P \bar{6}_P 21_{H_4} + Y_{34} \bar{6}_D \bar{6}_P 21_{H_4} + \text{H.c.} \end{aligned}$$

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Z_2 symmetry forbids the dark-SM mixing

Y_1 small to forbid decay $\text{DM} \rightarrow h \nu_L$

} **(META) STABLE DM**

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$$+ Y_U 15_Q 15_Q 15_{H_2} + Y_1 \bar{6}_D \bar{6}_D 15_{H_2} + Y_2 \bar{6}_P \bar{6}_P 15_{H_2} + Y_{12} \bar{6}_D \bar{6}_P 15_{H_2}$$

$$+ Y_3 \bar{6}_D \bar{6}_D 21_{H_4} + Y_4 \bar{6}_P \bar{6}_P 21_{H_4} + Y_{34} \bar{6}_D \bar{6}_P 21_{H_4} + \text{H.c.}$$

Allowed FP:

$g_6^* = 0 (\text{R})$ compatible with AF

$Y'_D^* = 0 (\text{IR}), Y_{\text{mix}}^* = 0 (\text{IR})$ no SM-dark mixing in the quark sector

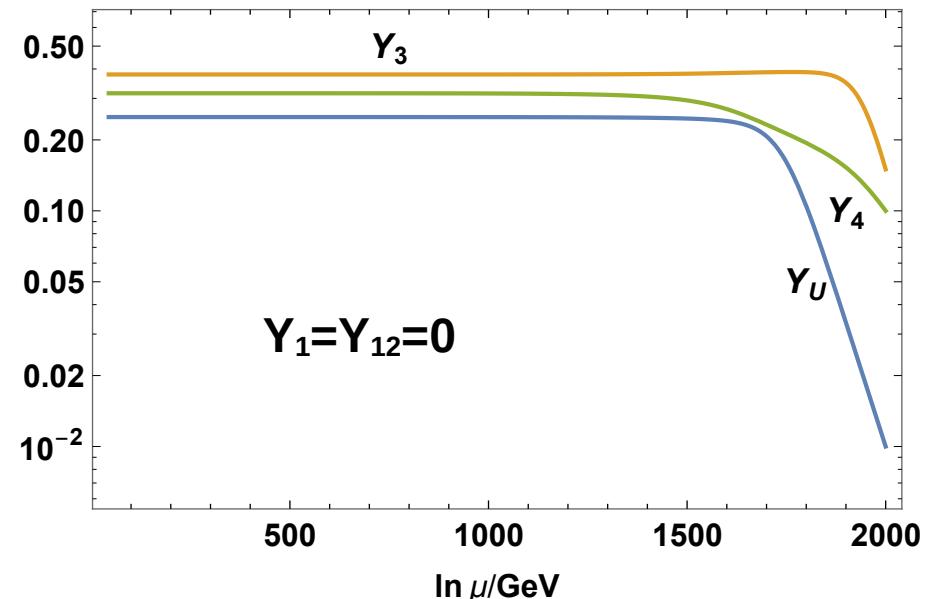
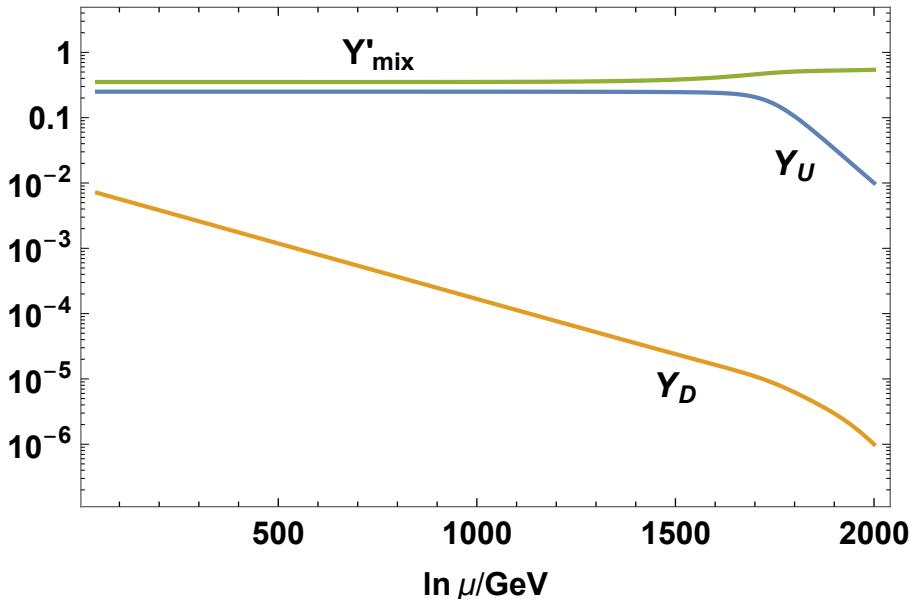
$Y_{12}^* = 0 (\text{IR}), Y_{34}^* = 0 (\text{IR})$ no SM-dark mixing in the neutrino sector

$Y_1^* = 0 (\text{IR})$ no decay into the SM neutrino

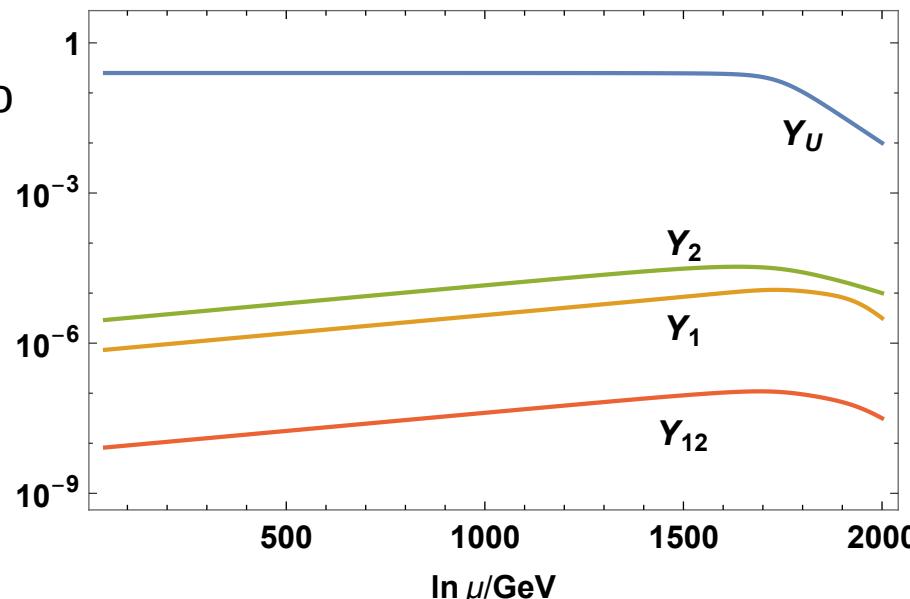
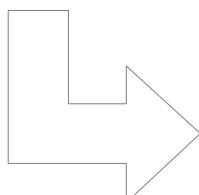
STABLE DM

Forbidding (allowed) couplings

A. Chikkaballi, KK, R. Lino dos Santos, E. Sessolo,
preliminary



$Y_1=0$: massless neutrino



(META) STABLE DM

Conclusions

- ASQG-inspired boundary conditions allow for specific predictions for the BSM physics.
- The bottleneck of the heuristic approach: UV interactive FPs for the SM couplig(s).
- In the realizations pertinent to naturalness, AF of the SM gauge couplings can be accommodated.
- Question for the future: can the identified mechanisms be applied in different settings (ex. slow-walk instead of a fixed point).