

$$u(t) = K_p e(t) + K_i \int_0^t e(\tau) d\tau + K_d \frac{de(t)}{dt} \quad (1a)$$

$$u(t) = K_p (br(t) - y(t)) + K_i \int_0^t e(\tau) d\tau + K_d \frac{d}{dt} (cr(t) - y(t)) \quad (1b)$$

$$D(s) = \frac{K_d s}{1 + \frac{1}{N}s} (cR(s) - Y(s)) \quad (2a)$$

$$(N + s) D(s) = K_d N s (cR(s) - Y(s)) \quad (2b)$$

$$ND(t) + \frac{dD(t)}{dt} = K_d N \frac{d}{dt} (cr(t) - y(t)) \quad (2c)$$

$$P[k] = K_p (br[k] - y[k]) \quad (3a)$$

$$I[k] = I[k - 1] + K_i T_s (r[k] - y[k]) \quad (3b)$$

$$ND[k] + \frac{D[k] - D[k - 1]}{T_s} = K_d N \frac{cr[k] - y[k] + cr[k - 1] - y[k - 1]}{T_s} \quad (4a)$$

$$(1 + NT_s) D[k] = D[k - 1] + K_d N ((cr - y)[k] - (cr - y)[k - 1]) \quad (4b)$$

$$D[k] = \frac{1}{1 + NT_s} \left( D[k - 1] + K_d N ((cr - y)[k] - (cr - y)[k - 1]) \right) \quad (4c)$$

$$P[k] = K_p e[k] \quad (5a)$$

$$I[k] = I[k - 1] + K_i T_s e[k] \quad (5b)$$

$$D[k] = K_d f_s (e[k] - e[k - 1]) \quad (5c)$$