

# 3D Random Walk

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PHYS3061: Lab Report 1

## Contents

<b>1</b>	<b>Introduction</b>	<b>2</b>
1.1	Random Number Generator . . . . .	2
1.2	Random Walk . . . . .	2
<b>2</b>	<b>Code</b>	<b>2</b>
2.1	Linear Congruential Generator . . . . .	2
2.2	3D Random Walk . . . . .	3
<b>3</b>	<b>Application</b>	<b>3</b>
3.1	Pólya's Random Walk Problem . . . . .	3
<b>4</b>	<b>Results and Analysis</b>	<b>3</b>
<b>5</b>	<b>Conclusion</b>	<b>3</b>

# 1 Introduction

## 1.1 Random Number Generator

The random number generator implemented here is a simple Linear Congruential Generator(LCG), which is generally a recursive mapping within a certain integer domain. for a set of parameters (a,c,m):

$$x_{N+1} = (x_N * a + c) \mod m$$
$$\xi: \{1, 2, 3, \dots, m-1\} \rightarrow \{1, 2, 3, \dots, m-1\}$$

Some special sets of (a,c,m) give seemingly very random and uniform distribution of results in recursive mapping. Based on this feature, we consider this recursive method as a random number generator.

In this experiment (a=1559, c=647, m=13229) are chosen. The main characteristic of these parameters is that they are all primes, in order to try to avoid periodicity behaviors in the random sequence. This special set is chosen by testing different combinations of (a,c,m) in a small parameter space.

## 1.2 Random Walk

A random walk, in simple terms, is a random sequence representing the accumulative sum of a random variable. In a simple 3D case:

$$\vec{X}_N = \sum_{i=1}^n \vec{s}_i$$

where  $\vec{s} \in V = \{(1, 0, 0), (-1, 0, 0), (0, 1, 0), (0, -1, 0), (0, 0, 1), (0, 0, -1)\}$

Assigning  $P(\vec{v}) \equiv 1/6$  for  $\vec{v} \in V$

Probability analysis give this famous relationship:

$$\langle |\vec{X}_N|^2 \rangle = \sqrt{N}$$

This relationship can be verified by a Monte Carlo Method, averaging the results over a large number of samples. Alternatively, we can use it to evaluate the randomness of our LCG generator.

# 2 Code

## 2.1 Linear Congruential Generator

```
def LCG():
    '''LCG Random Number generator'''
    # seed, a, c, m are all prime numbers, to avoid periodicity
    a = 1559
    c = 647
    m = 13229

    t = time.time() #Using current time to set the seed
    state = int( (t - int(t)) * 10000 ) % m

    logging_dict(locals()) #Recording the parameters in results.log

    '''LCG is a generator object'''
    while True:
        yield state / m
        state = (a*state+c) % m
```

## 2.2 3D Random Walk

## 3 Application

### 3.1 Pólya's Random Walk Problem

## 4 Results and Analysis

## 5 Conclusion