

# Package ‘temStaR’

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**Title** Tempered Stable Distribution

**Version** 0.90

**Author** Aaron Y.S. Kim [aut, cre]

**Maintainer** Aaron Y.S. Kim <aaron.kim@girininst.com>

**Description** This package provides useful tools to use the multivariate normal tempered stable distribution and process

**License** `use\_mit\_license()`

**Encoding** UTF-8

**LazyData** true

**Roxygen** list(markdown = TRUE)

**RoxygenNote** 7.2.1

**Imports** functional,  
nloptr,  
pracma,  
spatstat,  
evmix,  
Matrix,  
mvtnorm,  
doParallel,  
foreach

**Suggests** functional,  
nloptr,  
pracma,  
spatstat,  
evmix,  
Matrix,  
mvtnorm,  
doParallel,  
foreach

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changeCovMtx2Rho	<i>changeCovMtx2Rho</i>
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## Description

Change covariance matrix to Rho matrix.

**Usage**

```
changeCovMtx2Rho(CovMtx, alpha, theta, betaVec, PDFlag = TRUE)
```

---

chf_NTS	<i>chf_NTS</i>
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---

**Description**

chf\_NTS calculates Ch.F of the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If a time parameter value is given, it calculates Ch.F of the NTS process  $\phi(u) = E[\exp(iu(X(t+s) - X(s)))] = \exp(t \log(E[\exp(iuX(1))]))$ , where X is the NTS process generated by the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ .

**Usage**

```
chf_NTS(u, param)
```

**Arguments**

u	An array of u
ntsparam	A vector of the NTS parameters $(\alpha, \theta, \beta, \gamma, \mu)$ . For NTS process case it is a vector of parameters $(\alpha, \theta, \beta, \gamma, \mu, t)$ .

**Value**

Characteristic function of the NTS distribution

**Examples**

```
library(functional)
library(nloptr)
library(pracma)
library(spatstat)
library(Matrix)
library("temStaR")
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparam <- c(alpha, theta, beta, gamma, mu)
u <- seq(from = -2*pi, to = 2*pi, length.out = 101)
phi <- chf_NTS(u, ntsparam)
```

```
#Annual based parameters
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
#scaling annual parameters to one day
dt <- 1/250 #one day
```

```
ntsparm <- c(alpha, theta, beta, gamma, mu, dt)
u <- seq(from = -2*pi, to = 2*pi, length.out = 101)
phi <- chf_NTS(u, ntsparm)
```

---

chf\_stdNTS

*chf\_stdNTS*


---

## Description

chf\_stdNTS calculates Ch.F of the standard NTS distribution with parameters  $(\alpha, \theta, \beta)$ . If a time parameter value is given, it calculates Ch.F of the standard NTS process  $\phi(u) = E[\exp(iu(X(t+s) - X(s)))] = \exp(t \log(E[\exp(iuX(1))]))$ , where  $X$  is the standard NTS process generated by the standard NTS distribution with parameters  $(\alpha, \theta, \beta)$ .

## Usage

```
chf_stdNTS(u, param)
```

## Arguments

u	An array of u
ntsparm	A vector of the standard NTS parameters $(\alpha, \theta, \beta)$ . For the standard NTS process case it is a vector of parameters $(\alpha, \theta, \beta, t)$ .

## Value

Characteristic function of the standard NTS distribution

## Examples

```
#' library(functional)
library(nloptr)
library(pracma)
library(spatstat)
library(Matrix)
library("temStaR")
alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparm <- c(alpha, theta, beta)
u <- seq(from = -2*pi, to = 2*pi, length.out = 101)
phi <- chf_stdNTS(u, ntsparm)

#Annual based parameters
alpha <- 1.2
theta <- 1
beta <- -0.2
#scaling annual parameters to one day
dt <- 1/250 #one day
ntsparm <- c(alpha, theta, beta, gamma, mu, dt)
u <- seq(from = -2*pi, to = 2*pi, length.out = 101)
phi <- chf_stdNTS(u, ntsparm)
```

---

copulaStdNTS	<i>copulaStdNTS</i>
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---

**Description**

copulaStdNTS calculates the stdNTS copula values

**Usage**

```
copulaStdNTS(u, st, subTS = NULL)
```

**References**

Y. S. Kim, D. Volkmann (2013), Normal Tempered Stable Copula, Applied Mathematics Letters, 26(7), 676-680 <https://www.sciencedirect.com/science/article/pii/S0893965913000384>

---

cvaretns	<i>cvaretns</i>
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---

**Description**

cvaretns calculates Conditional Value at Risk (CVaR, or expected shortfall ES) of the NTS market model with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If only three parameters are given, it calculates CVaR of the standard NTS distribution with parameter  $(\alpha, \theta, \beta)$

**Usage**

```
cvaretns(eps, ntsparm)
```

**Arguments**

eps	the significant level for CVaR. Real value between 0 and 1.
ntsparm	A vector of the NTS parameters $(\alpha, \theta, \beta, \gamma, \mu)$ . A vector of the standard NTS parameters $(\alpha, \theta, \beta)$ .

**Value**

CVaReturn of the NTS distribution.

**References**

Y. S. Kim, S. T. Rachev, M. L. Bianchi, and F. J. Fabozzi (2010), Computing VaR and AVaR in infinitely divisible distributions, Probability and Mathematical Statistics, 30 (2), 223-245.  
 S. T. Rachev, Y. S. Kim, M. L. Bianchi, and F. J. Fabozzi (2011), Financial Models with Levy Processes and Volatility Clustering, John Wiley & Sons

**Examples**

```

library("temStaR")
alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparm <- c(alpha, theta, beta)
u <- c(0.01, 0.05)
q <- cvaretnts(u, ntsparm)

alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparm <- c(alpha, theta, beta, gamma, mu)
u <- c(0.01, 0.05)
q <- cvaretnts(u, ntsparm)

#Annual based parameters
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
#scaling annual parameters to one day
dt <- 1/250 #one day
ntsparm <- c(alpha, theta, beta, gamma, mu, dt)
u <- c(0.01, 0.05)
q <- cvaretnts(u, ntsparm)

```

---

cvarGauss

*cvarGauss*


---

**Description**

Calculate the CVaR for the normal distributed market model. Developer's version.

**Usage**

```
cvarGauss(eta, mu = 0, sigma = 1)
```

---

cvarmarginalmnts

*cvarmarginalmnts*


---

**Description**

cvarmarginalmnts calculates the CVaR of the  $n$ -th element of the multivariate NTS distributed random variable.

**Usage**

```
cvarmarginalmnts(eta, n, st)
```

**Arguments**

eta	the significant level for CVaR. Real value between 0 and 1.
n	the $n$ -th element to be calculated.
st	Structure of parameters for the $n$ -dimensional NTS distribution.

---

cvarnts	<i>cvarnts</i>
---------	----------------

---

**Description**

cvarnts calculates Conditional Value at Risk (CVaR, or expected shortfall ES) of the NTS market model with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If only three parameters are given, it calculates CVaR of the standard NTS distribution with parameter  $(\alpha, \theta, \beta)$

**Usage**

```
cvarnts(eps, ntsparm)
```

**Arguments**

eps	the significant level for CVaR. Real value between 0 and 1.
ntsparm	A vector of the NTS parameters $(\alpha, \theta, \beta, \gamma, \mu)$ . A vector of the standard NTS parameters $(\alpha, \theta, \beta)$ .

**Value**

CVaR of the NTS distribution.

**References**

Y. S. Kim, S. T. Rachev, M. L. Bianchi, and F. J. Fabozzi (2010), Computing VaR and AVaR in infinitely divisible distributions, *Probability and Mathematical Statistics*, 30 (2), 223-245.

S. T. Rachev, Y. S. Kim, M. L. Bianchi, and F. J. Fabozzi (2011), *Financial Models with Levy Processes and Volatility Clustering*, John Wiley & Sons

**Examples**

```
library("temStaR")
alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparm <- c(alpha, theta, beta)
u <- c(0.01, 0.05)
q <- cvarnts(u, ntsparm)

alpha <- 1.2
theta <- 1
```

```

beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparm <- c(alpha, theta, beta, gamma, mu)
u <- c(0.01, 0.05)
q <- cvarnts(u, ntsparm)

#Annual based parameters
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
#scaling annual parameters to one day
dt <- 1/250 #one day
ntsparm <- c(alpha, theta, beta, gamma, mu, dt)
u <- c(0.01, 0.05)
q <- cvarnts(u, ntsparm)

```

---

dBeta

*dBeta*


---

### Description

The first derivative of the beta. Developer's version.

### Usage

```
dBeta(n, w, betaArray, covMtx)
```

---

dcopulaStdNTS

*dcopulaStdNTS*


---

### Description

dcopulaStdNTS calculates density of the stdNTS copula.

### Usage

```
dcopulaStdNTS(u, st, subTS = NULL)
```

### References

Y. S. Kim, D. Volkmann (2013), Normal Tempered Stable Copula, Applied Mathematics Letters, 26(7), 676-680 <https://www.sciencedirect.com/science/article/pii/S0893965913000384>



---

dCVaRstdNTS_numint	<i>dCVaRstdNTS_numint</i>
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---

**Description**

Calculate the marginal contribution to CVaR for the multivariate stdNTS Model. Developer's version.

**Usage**

```
dCVaRstdNTS_numint(
    eta,
    alpha,
    theta,
    beta,
    cv = NULL,
    v = NULL,
    N = 20,
    rho = 1e-04
)
```

---

dCVaR_numint	<i>dCVaR_numint</i>
--------------	---------------------

---

**Description**

The first derivative of CVaR for the beta parameter of the stdNTS. Developer's version.

**Usage**

```
dCVaR_numint(eta, alpha, theta, beta, N = 200, rho = 0.1)
```

---

dinvCdf_stdNTS_int	<i>dinvCdf_stdNTS_int</i>
--------------------	---------------------------

---

**Description**

The first derivative of inverse CDF for the beta parameter of the stdNTS. Developer's version.

**Usage**

```
dinvCdf_stdNTS_int(eta, x = NULL, alpha, theta, beta)
```

---

dmarginalmnts	<i>dmarginalmnts</i>
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---

### Description

dmarginalmnts calculates the marginal density of the  $n$ -th element of the multivariate NTS distributed random variable.

### Usage

```
dmarginalmnts(x, n, st)
```

### Arguments

x	the $x$ such that $f(x) = \frac{d}{dx}P(X_n < x)$
n	the $n$ -th element to be calculated.
st	Structure of parameters for the $n$ -dimensional NTS distribution.

---

dmnts	<i>dmnts</i>
-------	--------------

---

### Description

dmnts calculates the density of the multivariate NTS distribution:  $f(x_1, \dots, x_n) = \frac{d^n}{dx_1 \dots dx_n} P(x_n < R_1, \dots, x_n < R_n)$ . The multivariate NTS random vector  $R = (R_1, \dots, R_n)$  is defined

$$R = \mu + \text{diag}(\sigma)X,$$

where

$X$  follows  $\text{stdNTS}_n(\alpha, \theta, \beta, \Sigma)$

### Usage

```
dmnts(x, st, subTS = NULL)
```

### Arguments

x	array of the $(x_1, \dots, x_n)$
st	Structure of parameters for the $n$ -dimensional NTS distribution. <code>st\$ndim</code> : dimension <code>st\$mu</code> : $\mu$ mean vector (column vector) of the input data. <code>st\$sigma</code> : $\sigma$ standard deviation vector (column vector) of the input data. <code>st\$alpha</code> : $\alpha$ of the std NTS distribution (X). <code>st\$theta</code> : $\theta$ of the std NTS distribution (X). <code>st\$beta</code> : $\beta$ vector (column vector) of the std NTS distribution (X). <code>st\$Rho</code> : $\rho$ matrix of the std NTS distribution (X).
numofsample	number of samples.

**Value**

Simulated NTS random vectors

**References**

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

**Examples**

```
library("temStaR")
library(mvtnorm)
strPMNTS <- list(ndim = 2,
  mu = c( 0.5, -1.5 ),
  sigma = c( 2, 3 ),
  alpha = 0.1,
  theta = 3,
  beta = c( 0.1, -0.3 ),
  Rho = matrix( data = c(1.0, 0.75, 0.75, 1.0),
    nrow = 2, ncol = 2)
)
dmnts(c(0.6, -1.0), st = strPMNTS)

strPMNTS <- list(ndim = 2,
  mu = c( 0, 0, 0 ),
  sigma = c( 1, 1, 1 ),
  alpha = 0.1,
  theta = 3,
  beta = c( 0.1, -0.3, 0 ),
  Rho = matrix(
    data = c(1.0, 0.75, 0.1, 0.75, 1.0, 0.2, 0.1, 0.2, 1.0),
    nrow = 3, ncol = 3)
)
pmnts(c(0,0,0), st = strPMNTS)
dmnts(c(0,0,0), st = strPMNTS)
```

---

dnts

dnts

---

**Description**

dnts calculates pdf of the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If only three parameters are given, it calculates pdf of the standard NTS distribution with parameter  $(\alpha, \theta, \beta)$ . If a time parameter value is given, it calculates pdf of the NTS process  $f(x)dx = d(P((X(t+s) - X(s)) < x))$ , where  $X$  is the NTS process generated by the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ .

**Usage**

```
dnts(xdata, ntsparm)
```

**Arguments**

xdata	An array of x
ntsparam	A vector of the NTS parameters $(\alpha, \theta, \beta, \gamma, \mu)$ . For the NTS process case it is a vector of parameters $(\alpha, \theta, \beta, \gamma, \mu, t)$ . A vector of the standard NTS parameters $(\alpha, \theta, \beta)$ .

**Value**

Density of NTS distribution

**References**

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

**Examples**

```
#
library(functional)
library(nloptr)
library(pracma)
library(spatstat)
library(Matrix)
library("temStaR")

alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparam <- c(alpha, theta, beta)
x <- seq(from = -6, to = 6, length.out = 101)
d <- dnts(x, ntsparam)
plot(x,d,type = 'l')

alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparam <- c(alpha, theta, beta, gamma, mu)
x <- seq(from = -2, to = 2, by = 0.01)
d <- dnts(x, ntsparam)
plot(x,d,type = 'l')

#Annual based parameters
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
#scaling annual parameters to one day
dt <- 1/250 #one day
ntsparam <- c(alpha, theta, beta, gamma, mu, dt)
x <- seq(from = -0.02, to = 0.02, length.out = 101)
d <- dnts(x, ntsparam)
plot(x,d,type = 'l')
```

fitmnts

*fitmnts***Description**

fitmnts fit parameters of the n-dimensional NTS distribution.

$$r = \mu + \text{diag}(\sigma)X$$

where

$X$  follows  $\text{stdNTS}_n(\alpha, \theta, \beta, \Sigma)$

**Usage**

```
\code{res <- fitmnts( returndata, n)}
\code{res <- fitmnts( returndata, n, alphaNtheta = c(alpha, theta))}
\code{res <- fitmnts( returndata, n, stdflag = TRUE ) }
\code{res <- fitmnts( returndata, n, alphaNtheta = c(alpha, theta), stdflag = TRUE)}
```

**Arguments**

returndata	Raw data to fit the parameters. The data must be given as a matrix form. Each column of the matrix contains a sequence of asset returns. The number of row of the matrix is the number of assets.
n	Dimension of the data. That is the number of assets.
alphaNtheta	If $\alpha$ and $\theta$ are given, then put those numbers in this parameter. The function fixes those parameters and fits other remaining parameters. If you set alphaNtheta = NULL, then the function fits all parameters including $\alpha$ and $\theta$ .
stdflag	If you want only standard NTS parameter fit, set this value be TRUE.

**Value**

Structure of parameters for the n-dimensional NTS distribution.

res\$mu :  $\mu$  mean vector of the input data.

res\$sigma :  $\sigma$  standard deviation vector of the input data.

res\$alpha :  $\alpha$  of the std NTS distribution (X).

res\$theta :  $\theta$  of the std NTS distribution (X).

res\$beta :  $\beta$  vector of the std NTS distribution (X).

res\$Rho :  $\rho$  matrix of the std NTS distribution (X), which is correlation matrix of epsilon.

res\$CovMtx : Covariance matrix of return data  $r$ .

**References**

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

**Examples**

```

library(functional)
library(nloptr)
library(pracma)
library(spatstat)
library(eymix)
library(Matrix)
library(quantmod)
library(temStaR)

getSymbols("^GSPC", src="yahoo", from = "2016-1-1", to = "2020-08-31")
pr1 <- as.numeric(GSPC$GSPC.Adjusted)
getSymbols("^DJI", src="yahoo", from = "2016-1-1", to = "2020-08-31")
pr2 <- as.numeric(DJI$DJI.Adjusted)

returndata <- matrix(data = c(diff(log(pr1)),diff(log(pr2))),
                     ncol = 2, nrow = (length(pr1)-1))
res <- fitmnts( returndata = returndata, n=2 )

#Fix alpha and theta.
#Estimate alpha and theta from DJIA and use those parameter for IBM, INTC parameter fit.
getSymbols("^DJI", src="yahoo", from = "2016-1-1", to = "2020-08-31")
prDJ <- as.numeric(DJI$DJI.Adjusted)
ret <- diff(log(prDJ))
ntsparam <- fitnts(ret)
getSymbols("IBM", src="yahoo", from = "2016-1-1", to = "2020-08-31")
pr1 <- as.numeric(IBM$IBM.Adjusted)
getSymbols("INTC", src="yahoo", from = "2016-1-1", to = "2020-08-31")
pr2 <- as.numeric(INTC$INTC.Adjusted)

returndata <- matrix(data = c(diff(log(pr1)),diff(log(pr2))),
                     ncol = 2, nrow = (length(pr1)-1))
res <- fitmnts( returndata = returndata,
               n = 2,
               alphaNtheta = c(ntsparam["alpha"], ntsparam["theta"]) )

```

---

fitmnts\_par

---

*fitmnts\_par*


---

**Description**

fitmnts\_par fit parameters of the n-dimensional NTS distribution. A parallel version of fitmnts()

**Usage**

```

fitmnts_par(
  returndata,
  n,
  alphaNtheta = NULL,
  stdflag = FALSE,
  parallelSocketCluster = NULL,
  PDflag = TRUE
)

```

## Examples

```
library(functional)
library(nloptr)
library(pracma)
library(spatstat)
library(evmix)
library(Matrix)
library(foreach)
library(doParallel)
library(quantmod)
library(temStaR)

getSymbols("^GSPC", src="yahoo", from = "2016-1-1", to = "2020-08-31")
pr1 <- as.numeric(GSPC$GSPC.Adjusted)
getSymbols("^DJI", src="yahoo", from = "2016-1-1", to = "2020-08-31")
pr2 <- as.numeric(DJI$DJI.Adjusted)

returndata <- matrix(data = c(diff(log(pr1)),diff(log(pr2))),
                      ncol = 2, nrow = (length(pr1)-1))

numofcluster <- detectCores()
cl <- makePSOCKcluster(numofcluster)
registerDoParallel(cl)
res <- fitmnts_par( returndata = returndata, n=2, parallelSocketCluster = cl )
stopCluster(cl)
```

---

fitnts

*fitnts*


---

## Description

fitnts fit parameters  $(\alpha, \theta, \beta, \gamma, \mu)$  of the NTS distribution. This function using the curvefit method between the empirical cdf and the NTS cdf.

## Usage

```
\code{fitnts(rawdat)}
\code{fitnts(rawdat), ksdensityflag = 1}
\code{fitnts(rawdat, initialparam = c(alpha, theta, beta, gamma, mu))}
\code{fitnts(rawdat, initialparam = c(alpha, theta, beta, gamma, mu)), ksdensityflag = 1}
\code{fitnts(rawdat, initialparam = c(alpha, theta, beta, gamma, mu)), maxeval = 100, ksdensityflag
```

## Arguments

rawdat	Raw data to fit the parameters.
initialparam	A vector of initial NTS parameters. This function uses the nloptr package. If it has a good initial parameter then estimation performs better. If users do not know a good initial parameters, then just set it as initialparam=NaN, that is default. The function cffitnts() may be helpful to find the initial parameters.
maxeval	Maximum evaluation number for nloptr. The iteration stops on this many function evaluations.

`ksdensityflag` This function fit the parameters using the curvefit method between the empirical cdf and the NTS cdf. If `ksdensityflag = 1` (default), then the empirical cdf is calculated by the kernel density estimation. If `ksdensityflag = 0`, then the empirical cdf is calculated by the empirical cdf.

### Value

Estimated parameters

### References

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

### Examples

```
library(evmix)
library(spatstat)
library("temStaR")
library("quantmod")
getSymbols("^GSPC", src="yahoo", from = "2013-1-1", to = "2023-12-31")
pr <- as.numeric(GSPC$GSPC.Adjusted)
ret <- diff(log(pr))
ntsparm <- fitnts(ret)

Femp = ecdf(ret)
x = seq(from=min(ret), to = max(ret), length.out = 100)
cemp = Femp(x)
ncdf = pnts(x, c(ntsparm))
plot(x,ncdf,type = 'l', col = "red")
points(x,cemp, type = 'l', col = "blue")
a = density(ret)
p = dnts(x,ntsparm)
plot(x,p,type = 'l', col = "red")
lines(a,type = 'l', col = "blue")
```

---

fitstdnts

*fitstdnts*

---

### Description

`fitstdnts` fit parameters  $(\alpha, \theta, \beta)$  of the standard NTS distribution. This function using the curvefit method between the empirical cdf and the standard NTS cdf.

### Usage

```
\code{fitstdnts(rawdat)}
\code{fitstdnts(rawdat), ksdensityflag = 1}
\code{fitstdnts(rawdat, initialparam = c(alpha, theta, beta))}
\code{fitstdnts(rawdat, initialparam = c(alpha, theta, beta)), ksdensityflag = 1}
\code{fitstdnts(rawdat, initialparam = c(alpha, theta, beta)), maxeval = 100, ksdensityflag = 1}
```



## Arguments

rawdat	Raw data to fit the parameters.
initialparam	A vector of initial standard NTS parameters. This function uses the <code>nloptr</code> package. If it has a good initial parameter then estimation performs better. If users do not know a good initial parameters, then just set it as <code>initialparam=NaN</code> , that is default.
maxeval	Maximum evaluation number for <code>nloptr</code> . The iteration stops on this many function evaluations.
ksdensityflag	This function fit the parameters using the curvefit method between the empirical cdf and the standard NTS cdf. If <code>ksdensityflag = 1</code> (default), then the empirical cdf is calculated by the kernel density estimation. If <code>ksdensityflag = 0</code> , then the empirical cdf is calculated by the empirical cdf.

## Value

Estimated parameters

## References

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

## Examples

```
library(functional)
library(nloptr)
library(pracma)
library(spatstat)
library(evmix)
library(Matrix)
library(quantmod)
library("temStaR")
library("quantmod")
getSymbols("^GSPC", src="yahoo", from = "2013-1-1", to = "2023-12-31")
pr <- as.numeric(GSPC$GSPC.Adjusted)
ret <- diff(log(pr))
stdret <- (ret-mean(ret))/sd(ret)
stdntsparam <- fitstdnts(stdret)

Femp = ecdf(stdret)
x = seq(from=min(stdret), to = max(stdret), length.out = 100)
cemp = Femp(x)
ncdf = pnts(x, c(stdntsparam))
plot(x,ncdf,type = 'l', col = "red")
lines(x,cemp, type = 'l', col = "blue")
a = density(stdret)
p = dnts(x,stdntsparam)
plot(x,p,type = 'l', col = "red", ylim = c(0, max(a$y, p)))
lines(a,type = 'l', col = "blue")
```

---

fitstdntsFixAlphaThata

*fitstdntsFixAlphaThata*


---

### Description

Fit beta of stdNTS distribution with fixed alpha and theta.

### Usage

```
fitstdntsFixAlphaThata(
  rawdat,
  alpha,
  theta,
  initialparam = NaN,
  maxeval = 100,
  ksdensityflag = 1
)
```

---

gensamplepathnts

*gensamplepathnts*


---

### Description

gensamplepathnts generate sample paths of the NTS process with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If only three parameters are given, it generate sample paths of the standard NTS process with parameters  $(\alpha, \theta, \beta)$ .

### Usage

```
gensamplepathnts(npath, nimestep, ntsparm, dt)
```

### Arguments

npath	Number of sample paths
nimestep	number of time step
ntsparm	A vector of the NTS parameters $(\alpha, \theta, \beta, \gamma, \mu)$ . A vector of the standard NTS parameters $(\alpha, \theta, \beta)$ .
dt	the time length of one time step by the year fraction. "dt=1" means 1-year.

### Value

Structure of the sample path. Matrix of sample path. Column index is time.

**Examples**

```

library("temStaR")
#standard NTS process sample path
alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparam <- c(alpha, theta, beta)
npath <- 5
ntimestep <- 250
dt <- 1/250
simulation <- gensamplepathnts(npath, ntimestep, ntsparam, dt)
matplot(colnames(simulation), t(simulation), type = 'l')

#NTS process sample path
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparam <- c(alpha, theta, beta, gamma, mu)
npath <- 5
ntimestep <- 250
dt <- 1/250
simulation <- gensamplepathnts(npath, ntimestep, ntsparam, dt)
matplot(colnames(simulation), t(simulation), type = 'l')

```

getGammaVec

*getGammaVec***Description**

beta to gamma in StdNTS

**Usage**

```
getGammaVec(alpha, theta, betaVec)
```

getPortNTSPParam

*getPortNTSPParam***Description**

Portfolio return with capital allocation weight is  $R_p = \langle w, r \rangle$ , which is a weighted sum of elements in the N-dimensional NTS random vector.  $R_p$  becomes an 1-dimensional NTS random variable. getPortNTSPParam find the parameters of  $R_p$ .

**Usage**

```

\code{res <- setPortfolioParam(strPMNTS,w)}
\code{res <- setPortfolioParam(strPMNTS,w, FALSE)}

```

## Arguments

strPMNTS	Structure of parameters for the n-dimensional NTS distribution. strPMNTS\$ndim : dimension strPMNTS\$mu : $\mu$ mean vector (column vector) of the input data. strPMNTS\$sigma : $\sigma$ standard deviation vector (column vector) of the input data. strPMNTS\$alpha : $\alpha$ of the std NTS distribution (X). strPMNTS\$theta : $\theta$ of the std NTS distribution (X). strPMNTS\$beta : $\beta$ vector (column vector) of the std NTS distribution (X). res\$Rho : $\rho$ matrix (Correlation) of the std NTS distribution (X). res\$Sigma : Covariance $\Sigma$ matrix of return data $r$ .
w	Capital allocation weight vector.
stdform	If stdform is FALSE, then the return parameter has the following representation $R_p = < w, r > = \mu + \text{diag}(\sigma)X$ , where $X$ follows $\text{stdNTS}_1(\alpha, \theta, \beta, 1)$ . If stdform is TRUE, then the return parameter has the following representation $R_p = < w, r >$ follows $\text{NTS}_1(\alpha, \theta, \beta, \gamma, \mu, 1)$

## Value

The weighted sum follows 1-dimensional NTS.

$$R_p = < w, r > = \mu + \text{diag}(\sigma)X,$$

where

$X$  follows  $\text{stdNTS}_1(\alpha, \theta, \beta, 1)$ .

Hence we obtain

res\$mu :  $\mu$  mean of  $R_p$ .

res\$sigma :  $\sigma$  standard deviation of  $R_p$ .

res\$alpha :  $\alpha$  of  $X$ .

res\$theta :  $\theta$  of  $X$ .

res\$beta :  $\beta$  of  $X$ .

## References

Proposition 2.1 of Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk <https://arxiv.org/pdf/2007.13972.pdf>

## Examples

```
library("temStaR")
strPMNTS <- list(ndim = 2,
  mu = c( 9.876552e-05, 4.747343e-04 ),
  sigma = c( 0.01620588, 0.02309643 ),
  alpha = 0.1888129 ,
  theta = 0.523042,
  beta = c( -0.04632938, 0.04063555 ),
  Rho = matrix( data = c(1.0, 0.469883,
    0.469883, 1.0),
```

```

                                nrow = 2, ncol = 2)
CovMtx = matrix( data = c(0.0002626304, 0.0001740779,
                           0.0001740779, 0.0005334452),
                  nrow = 2, ncol = 2)
)
w <- c(0.3, 0.7)
res <- getPortNTSPParam(strPMNTS,w)

```

---

importantSampling	<i>importantSampling</i>
-------------------	--------------------------

---

### Description

importantSampling do the important sampling for the TS Subordinator.

### Usage

```
importantSampling(alpha, theta)
```

---

ipnts	<i>ipnts</i>
-------	--------------

---

### Description

ipnts calculates inverse cdf of the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If only three parameters are given, it calculates inverse cdf of the standard NTS distribution with parameter  $(\alpha, \theta, \beta)$

### Usage

```
ipnts(u, ntsparm, maxmin = c(-10, 10), du = 0.01)
```

### Arguments

u	Real value between 0 and 1
ntsparm	A vector of the NTS parameters $(\alpha, \theta, \beta, \gamma, \mu)$ . A vector of the standard NTS parameters $(\alpha, \theta, \beta)$ .

### Value

Inverse cdf of the NTS distribution. It is the same as qnts function.

### References

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

**Examples**

```

library("temStaR")
alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparam <- c(alpha, theta, beta)
u <- seq(from = 0.01, to = 0.99, length.out = 99)
q <- ipnts(u, ntsparam)
plot(u, q, type = 'l')

alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparam <- c(alpha, theta, beta, gamma, mu)
u <- seq(from = 0.01, to = 0.99, length.out = 99)
q <- ipnts(u, ntsparam)
plot(x, q, type = 'l')

#Annual based parameters
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
#scaling annual parameters to one day
dt <- 1/250 #one day
ntsparam <- c(alpha, theta, beta, gamma, mu, dt)
u <- seq(from = 0.01, to = 0.99, length.out = 99)
q <- ipnts(u, ntsparam)
plot(x, q, type = 'l')

```

---

mctCVaR\_MNTS

---

*mctCVaR\_MNTS*


---

**Description**

Calculate the marginal contribution to CVaR for the multivariate NTS market model: the random vector  $r$  is

$$r = \mu + \text{diag}(\sigma)X$$

where

$X$  follows  $\text{stdNTS}_N(\alpha, \theta, \beta, \Sigma)$

**Usage**

```
\code{mctCVaR_MNTS(eta, n, w, stmnts)}
```

## Arguments

n	The target stock to calculate the mctCVaR
eta	Significant level of CVaR.
w	The capital allocation rate vector for the current portfolio
stmnts	Structure of parameters for the N-dimensional NTS distribution.
CVaRstd	CVaR Value of StdNTS residual. If NULL, the function automatically find it. The default value is NULL
dCVaRstd	The first derivative of the stdNTS CVaR for beta. If NULL, the function automatically find it. The default value is NULL
iCDFstd	The inverse cdf of stdNTS at the significant level eta. If NULL, the function automatically find it. The default value is NULL
	st\$ndim : Dimension of the model. Here st\$ndim=N.
	st\$mu : $\mu$ mean vector (column vector) of the input data.
	st\$sigma : $\sigma$ standard deviation vector (column vector) of the input data.
	st\$alpha : $\alpha$ of the std NTS distribution (X).
	st\$theta : $\theta$ of the std NTS distribution (X).
	st\$beta : $\beta$ vector (column vector) of the std NTS distribution (X).
	st\$Rho : $\rho$ matrix of the std NTS distribution (X), which is correlation matrix of epsilon.
	st\$CovMtx : Covariance matrix of return data $r$ .

## References

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

## Examples

```
library(functional)
library(nloptr)
library(pracma)
library(spatstat)
library(Matrix)
library(quantmod)
library(mvtnorm)
library("temStaR")

#Fix alpha and theta.
#Estimate alpha and theta from DJIA and use those parameter for IBM, INTL parameter fit.
getSymbols("^DJI", src="yahoo", from = "2020-8-25", to = "2020-08-31")
prDJ <- as.numeric(DJI$DJI.Adjusted)
ret <- diff(log(prDJ))
ntsparam <- fitnts(ret)
getSymbols("IBM", src="yahoo", from = "2016-1-1", to = "2020-08-31")
pr1 <- as.numeric(IBM$IBM.Adjusted)
getSymbols("INTL", src="yahoo", from = "2016-1-1", to = "2020-08-31")
pr2 <- as.numeric(INTL$INTL.Adjusted)

returndata <- matrix(data = c(diff(log(pr1)),diff(log(pr2))),
                     ncol = 2, nrow = (length(pr1)-1))
st <- fitmnts( returndata = returndata,
```

```

n = 2,
alphaNtheta = c(ntsparam["alpha"], ntsparam["theta"]) )
w <- c(0.3, 0.7)
eta <- 0.01

mctCVaR_MNTS(1, eta, w, st) #MCT-CVaR for IBM
mctCVaR_MNTS(2, eta, w, st) #MCT-CVaR for INTL

```

---

mctStdDev	<i>mctStdDev</i>
-----------	------------------

---

### Description

Morginal contribution to Risk for Standard Deviation.

### Usage

```
mctStdDev(n, w, covMtx)
```

### Arguments

n	The targer stock to calculate the mctStdDev
w	The capital allocation rate vector for the current portfolio
CovMtx	Covariance matrix of return data.

---

mctVaR_MNTS	<i>mctVaR_MNTS</i>
-------------	--------------------

---

### Description

Calculate the marginal contribution to VaR for the multivariate NTS market model: the random vector  $r$  is

$$r = \mu + \text{diag}(\sigma)X$$

where

$X$  follows  $\text{stdNTS}_N(\alpha, \theta, \beta, \Sigma)$

### Usage

```
\code{mctVaR_MNTS(n, eta, w, st)}
```



## Arguments

n	The target stock to calculate the mctVaR
eta	Significant level of VaR.
w	The capital allocation rate vector for the current portfolio
iCDFstd	The invert cdf of stdNTS at the significant level eta. If NULL, the function automatically find it. The default value is NULL st\$ndim : Dimension of the model. Here st\$ndim=N. st\$mu : $\mu$ mean vector (column vector) of the input data. st\$sigma : $\sigma$ standard deviation vector (column vector) of the input data. st\$alpha : $\alpha$ of the std NTS distribution (X). st\$theta : $\theta$ of the std NTS distribution (X). st\$beta : $\beta$ vector (column vector) of the std NTS distribution (X). st\$Rho : $\rho$ matrix of the std NTS distribution (X), which is correlation matrix of epsilon. st\$CovMtx : Covariance matrix of return data $r$ .
st	Structure of parameters for the N-dimensional NTS distribution.

## References

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

## Examples

```
library(functional)
library(nloptr)
library(pracma)
library(spatstat)
library(Matrix)
library(quantmod)
library(mvtnorm)
library(temStaR)

#Fix alpha and theta.
#Estimate alpha and theta from DJIA and use those parameter for IBM, INTL parameter fit.
getSymbols("^DJI", src="yahoo", from = "2020-8-25", to = "2020-08-31")
prDJ <- as.numeric(DJI$DJI.Adjusted)
ret <- diff(log(prDJ))
ntsparam <- fitnts(ret)
getSymbols("IBM", src="yahoo", from = "2016-1-1", to = "2020-08-31")
pr1 <- as.numeric(IBM$IBM.Adjusted)
getSymbols("INTL", src="yahoo", from = "2016-1-1", to = "2020-08-31")
pr2 <- as.numeric(INTL$INTL.Adjusted)

returndata <- matrix(data = c(diff(log(pr1)),diff(log(pr2))),
                     ncol = 2, nrow = (length(pr1)-1))
st <- fitmnts( returndata,
              n = 2,
              alphaNtheta = c(ntsparam["alpha"], ntsparam["theta"]) )
w <- c(0.3, 0.7)
eta <- 0.01
```

```
mctVaR_MNTS(1, eta, w, st) #MCT-VaR for IBM
mctVaR_MNTS(2, eta, w, st) #MCT-VaR for INTL
```

---

moments_NTS	<i>moments_NTS</i>
-------------	--------------------

---

### Description

moments\_NTS calculates mean, variance, skewness, and excess kurtosis of the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ .

### Usage

```
moments_NTS(param)
```

### Arguments

param                      A vector of the NTS parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ .

### Value

First 4 moments (Mean, Variance, Skewness, Excess Kurtosis) of NTS distribution. The mean is always the same as the parameter  $\mu$ .

### References

Kim, Y.S, K-H Roh, R. Douady (2020) Tempered Stable Processes with Time Varying Exponential Tails <https://arxiv.org/pdf/2006.07669.pdf>

### Examples

```
library("temStaR")
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparam <- c(alpha, theta, beta, gamma, mu)
moments_NTS(param = ntsparam)
```

---

moments_stdNTS	<i>moments_stdNTS</i>
----------------	-----------------------

---

**Description**

moments\_stdNTS calculates mean, variance, skewness, and excess kurtosis of the standard NTS distribution with parameters  $(\alpha, \theta, \beta)$ .

**Usage**

```
moments_stdNTS(param)
```

**Arguments**

param                      A vector of the standard NTS parameters  $(\alpha, \theta, \beta)$ .

**Value**

First 4 moments (Mean, Variance, Skewness, Excess Kurtosis) of NTS distribution. Of course, the mean and variance are always 0 and 1, respectively.

**References**

Kim, Y.S, K-H Roh, R. Douady (2020) Tempered Stable Processes with Time Varying Exponential Tails <https://arxiv.org/pdf/2006.07669.pdf>

**Examples**

```
library("temStaR")
alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparam <- c(alpha, theta, beta)
moments_stdNTS(param = ntsparam)
```

---

pmarginalmnts	<i>pmarginalmnts</i>
---------------	----------------------

---

**Description**

pmarginalmnts calculates the marginal cdf of the  $n$ -th element of the multivariate NTS distributed random variable.

**Usage**

```
pmarginalmnts(x, n, st)
```

**Arguments**

x                              the  $x$  such that  $F(x) = P(X_n < x)$   
n                                the  $n$ -th element to be calculated.  
st                                Structure of parameters for the  $n$ -dimensional NTS distribution.

pmnts

*pmnts***Description**

pmnts calculates the cdf values of the multivariate NTS distribution:  $F(x_1, \dots, x_n) = P(x_n < R_1, \dots, x_n < R_n)$ . The multivariate NTS random vector  $R = (R_1, \dots, R_n)$  is defined

$$R = \mu + \text{diag}(\sigma)X,$$

where

$X$  follows  $\text{stdNTS}_n(\alpha, \theta, \beta, \Sigma)$

**Usage**

```
pmnts(x, st, subTS = NULL)
```

**Arguments**

x	array of the $(x_1, \dots, x_n)$
st	Structure of parameters for the n-dimensional NTS distribution. <code>st\$ndim</code> : dimension <code>st\$mu</code> : $\mu$ mean vector (column vector) of the input data. <code>st\$sigma</code> : $\sigma$ standard deviation vector (column vector) of the input data. <code>st\$alpha</code> : $\alpha$ of the std NTS distribution (X). <code>st\$theta</code> : $\theta$ of the std NTS distribution (X). <code>st\$beta</code> : $\beta$ vector (column vector) of the std NTS distribution (X). <code>st\$Rho</code> : $\rho$ matrix of the std NTS distribution (X).
numofsample	number of samples.

**Value**

Simulated NTS random vectors

**References**

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

**Examples**

```
library(mvtnorm)
library(temStaR)

strPMNTS <- list(ndim = 2,
  mu = c( 0.5, -1.5 ),
  sigma = c( 2, 3 ),
  alpha = 0.1,
  theta = 3,
  beta = c( 0.1, -0.3 ),
  Rho = matrix( data = c(1.0, 0.75, 0.75, 1.0),
    nrow = 2, ncol = 2)
```

```

)
pmnts(c(0.6, -1.0), st = strPMNTS)

strPMNTS <- list(ndim = 2,
                 mu = c( 0, 0, 0 ),
                 sigma = c( 1, 1, 1 ),
                 alpha = 0.1,
                 theta = 3,
                 beta = c( 0.1, -0.3, 0 ),
                 Rho = matrix(
                     data = c(1.0, 0.75, 0.1, 0.75, 1.0, 0.2, 0.1, 0.2, 1.0),
                     nrow = 3, ncol = 3)
)
pmnts(c(0,0,0), st = strPMNTS)
dmnts(c(0,0,0), st = strPMNTS)

```

pnts

*pnts*

## Description

pnts calculates cdf of the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If only three parameters are given, it calculates cdf of the standard NTS distribution with parameter  $(\alpha, \theta, \beta)$ . If a time parameter value is given, it calculates cdf of the process  $F(x) = P((X(t+s) - X(s)) < x)$ , where  $X$  is the NTS process generated by the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ .

## Usage

```
pnts(xdata, ntsparm, dz = 2^-8, m = 2^12)
```

## Arguments

xdata	An array of x
ntsparm	A vector of the NTS parameters $(\alpha, \theta, \beta, \gamma, \mu)$ . For the NTS process case it is a vector of parameters $(\alpha, \theta, \beta, \gamma, \mu, t)$ . A vector of the standard NTS parameters $(\alpha, \theta, \beta)$ .

## Value

Cumulative probability of the NTS distribution

## References

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

**Examples**

```

library(functional)
library(nloptr)
library(pracma)
library(spatstat)
library(Matrix)
library("temStaR")

alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparm <- c(alpha, theta, beta)
x <- seq(from = -6, to = 6, length.out = 101)
p <- pnts(x, ntsparm)
plot(x,p,type = 'l')

alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparm <- c(alpha, theta, beta, gamma, mu)
x <- seq(from = -2, to = 2, by = 0.01)
p <- pnts(x, ntsparm)
plot(x,p,type = 'l')

#Annual based parameters
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
#scaling annual parameters to one day
dt <- 1/250 #one day
ntsparm <- c(alpha, theta, beta, gamma, mu, dt)
x <- seq(from = -0.02, to = 0.02, length.out = 101)
p <- pnts(x, ntsparm)
plot(x,p,type = 'l')

```

---

portfolioCVaRETmnts	<i>portfolioCVaRETmnts</i>
---------------------	----------------------------

---

**Description**

Calculate portfolio conditional value at Return on the NTS market model

**Usage**

```
portfolioCVaRETmnts(strPMNTS, w, eta)
```

**Arguments**

strPMNTS	Structure of parameters for the n-dimensional NTS distribution. strPMNTS\$ndim : dimension strPMNTS\$mu : $\mu$ mean vector (column vector) of the input data. strPMNTS\$sigma : $\sigma$ standard deviation vector (column vector) of the input data. strPMNTS\$alpha : $\alpha$ of the std NTS distribution (X). strPMNTS\$theta : $\theta$ of the std NTS distribution (X). strPMNTS\$beta : $\beta$ vector (column vector) of the std NTS distribution (X). res\$Rho : $\rho$ matrix (Correlation) of the std NTS distribution (X). res\$Sigma : Covariance $\Sigma$ matrix of return data $r$ .
w	Capital allocation weight vector.
eta	significantlt level

**Value**

portfolio value at Return on the NTS market model

---

portfolioCVarMnts	<i>portfolioCVarMnts</i>
-------------------	--------------------------

---

**Description**

Calculate portfolio conditional value at risk (expected shortfall) on the NTS market model

**Usage**

```
portfolioCVarMnts(strPMNTS, w, eta)
```

**Arguments**

strPMNTS	Structure of parameters for the n-dimensional NTS distribution. strPMNTS\$ndim : dimension strPMNTS\$mu : $\mu$ mean vector (column vector) of the input data. strPMNTS\$sigma : $\sigma$ standard deviation vector (column vector) of the input data. strPMNTS\$alpha : $\alpha$ of the std NTS distribution (X). strPMNTS\$theta : $\theta$ of the std NTS distribution (X). strPMNTS\$beta : $\beta$ vector (column vector) of the std NTS distribution (X). res\$Rho : $\rho$ matrix (Correlation) of the std NTS distribution (X). res\$Sigma : Covariance $\Sigma$ matrix of return data $r$ .
w	Capital allocation weight vector.
eta	significantlt level

**Value**

portfolio value at risk on the NTS market model

---

portfolioVaRETMnts	<i>portfolioVaRETMnts</i>
--------------------	---------------------------

---

### Description

Calculate portfolio value at return on the NTS market model

### Usage

```
portfolioVaRETMnts(strPMNTS, w, eta)
```

### Arguments

strPMNTS	Structure of parameters for the n-dimensional NTS distribution. strPMNTS\$ndim : dimension strPMNTS\$mu : $\mu$ mean vector (column vector) of the input data. strPMNTS\$sigma : $\sigma$ standard deviation vector (column vector) of the input data. strPMNTS\$alpha : $\alpha$ of the std NTS distribution (X). strPMNTS\$theta : $\theta$ of the std NTS distribution (X). strPMNTS\$beta : $\beta$ vector (column vector) of the std NTS distribution (X). res\$Rho : $\rho$ matrix (Correlation) of the std NTS distribution (X). res\$Sigma : Covariance $\Sigma$ matrix of return data $r$ .
w	Capital allocation weight vector.
eta	significanlt level

### Value

portfolio value at Return on the NTS market model

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portfolioVaRmnts	<i>portfolioVaRmnts</i>
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### Description

Calculate portfolio value at risk on the NTS market model

### Usage

```
portfolioVaRmnts(strPMNTS, w, eta)
```



## Arguments

strPMNTS	Structure of parameters for the n-dimensional NTS distribution. strPMNTS\$ndim : dimension strPMNTS\$mu : $\mu$ mean vector (column vector) of the input data. strPMNTS\$sigma : $\sigma$ standard deviation vector (column vector) of the input data. strPMNTS\$alpha : $\alpha$ of the std NTS distribution (X). strPMNTS\$theta : $\theta$ of the std NTS distribution (X). strPMNTS\$beta : $\beta$ vector (column vector) of the std NTS distribution (X). res\$Rho : $\rho$ matrix (Correlation) of the std NTS distribution (X). res\$Sigma : Covariance $\Sigma$ matrix of return data $r$ .
w	Capital allocation weight vector.
eta	significant level

## Value

portfolio value at risk on the NTS market model

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qmarginalmnts	<i>qmarginalmnts</i>
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## Description

qmarginalmnts calculates the quantile value of the  $n$ -th element of the multivariate NTS distributed random variable.

## Usage

```
qmarginalmnts(u, n, st)
```

## Arguments

u	vector of probabilities.
n	the $n$ -th element to be calculated.
st	Structure of parameters for the n-dimensional NTS distribution.

qnts

*qnts***Description**

qnts calculates quantile of the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If only three parameters are given, it calculates quantile of the standard NTS distribution with parameter  $(\alpha, \theta, \beta)$ . If a time parameter value is given, it calculates quantile of NTS process. That is it finds  $x$  such that  $u = P((X(t+s) - X(s)) < x)$ , where  $X$  is the NTS process generated by the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ .

**Usage**

```
qnts(u, ntsparm)
```

**Arguments**

**u** vector of probabilities.

**ntsparm** A vector of the NTS parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . For the NTS process case it is a vector of parameters  $(\alpha, \theta, \beta, \gamma, \mu, t)$ . A vector of standard NTS parameters  $(\alpha, \theta, \beta)$ .

**Value**

The quantile function of the NTS distribution

**Examples**

```
library(functional)
library(nloptr)
library(pracma)
library(spatstat)
library(Matrix)
library("temStaR")

alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparm <- c(alpha, theta, beta)
u <- c(0.01, 0.05, 0.25, 0.5, 0.75, 0.95, 0.99)
q <- qnts(u, ntsparm)

alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparm <- c(alpha, theta, beta, gamma, mu)
u <- c(0.01, 0.05, 0.25, 0.5, 0.75, 0.95, 0.99)
q <- qnts(u, ntsparm)
```

```
#Annual based parameters
```

```

alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
#scaling annual parameters to one day
dt <- 1/250 #one day
ntsparam <- c(alpha, theta, beta, gamma, mu, dt)
u <- c(0.01,0.05,0.25,0.5, 0.75, 0.95, 0.99)
q <- qnts(u, ntsparam)

```

rmnts

*rmnts*

### Description

rmnts generates random vector following the n dimensional NTS distribution using subordination.

$$r = \mu + \text{diag}(\sigma)X,$$

where

$X$  follows  $\text{stdNTS}_n(\alpha, \theta, \beta, \Sigma)$

### Usage

```
rmnts(strPMNTS, numofsample, rW = NULL, rTau = NULL)
```

### Arguments

strPMNTS	Structure of parameters for the n-dimensional NTS distribution. strPMNTS\$ndim : dimension strPMNTS\$mu : $\mu$ mean vector (column vector) of the input data. strPMNTS\$sigma : $\sigma$ standard deviation vector (column vector) of the input data. strPMNTS\$alpha : $\alpha$ of the std NTS distribution (X). strPMNTS\$theta : $\theta$ of the std NTS distribution (X). strPMNTS\$beta : $\beta$ vector (column vector) of the std NTS distribution (X). strPMNTS\$Rho : $\rho$ matrix of the std NTS distribution (X).
numofsample	number of samples.

### Value

Simulated NTS random vectors

### References

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

## Examples

```
strPMNTS <- list(ndim = 2,
                 mu = c( 0.00011, 0.00048 ),
                 sigma = c( 0.0162, 0.0231 ),
                 alpha = 1.23,
                 theta = 3.607,
                 beta = c( -0.1209, 0.0905 ),
                 Rho = matrix( data = c(1.0, 0.55, 0.55, 1.0), nrow = 2, ncol = 2)
                 )
gensim <- rmnts( strPMNTS, 100 )
plot(gensim)
```

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rnts	<i>rnts</i>
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## Description

`rnts` generates random numbers following NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If only three parameters are given, it generates random numbers of standard NTS distribution with parameter  $(\alpha, \theta, \beta)$ . If a time parameter value is given, it generates random numbers of increments of NTS process for time interval  $t$ .

## Usage

```
rnts(n, ntsparm, u = NULL)
```

## Arguments

<code>n</code>	number of random numbers to be generated.
<code>ntsparm</code>	A vector of NTS parameters $(\alpha, \theta, \beta, \gamma, \mu)$ . For NTS process case it is a vector of parameters $(\alpha, \theta, \beta, \gamma, \mu, t)$ . A vector of standard NTS parameters $(\alpha, \theta, \beta)$ .

## Value

NTS random numbers

## References

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

## Examples

```
library(functional)
library(nloptr)
library(pracma)
library(spatstat)
library(Matrix)
library("temStaR")

alpha <- 1.2
theta <- 1
```

```

beta <- -0.2
ntsparam <- c(alpha, theta, beta)
r <- rnts(100, ntsparam) #generate 100 NTS random numbers
plot(r)

alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparam <- c(alpha, theta, beta, gamma, mu)
r <- rnts(100, ntsparam) #generate 100 NTS random numbers
plot(r)

#Annual based parameters
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
#scaling annual parameters to one day
dt <- 1/250 #one day
ntsparam <- c(alpha, theta, beta, gamma, mu, dt)
r <- rnts(100, ntsparam) #generate 100 NTS random numbers
plot(r)

```

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setPortfolioParam	<i>setPortfolioParam</i>
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## Description

Please use getPortNTSParm instead of setPortfolioParam.

Portfolio return with capital allocation weight is  $R_p = \langle w, r \rangle$ , which is a weighted sum of elements in the N-dimensional NTS random vector.  $R_p$  becomes an 1-dimensional NTS random variable. setPortfolioParam find the parameters of  $R_p$ .

## Usage

```
\code{res <- setPortfolioParam(strPMNTS,w)}
```

## Arguments

strPMNTS	Structure of parameters for the n-dimensional NTS distribution. strPMNTS\$ndim : dimension strPMNTS\$mu : $\mu$ mean vector (column vector) of the input data. strPMNTS\$sigma : $\sigma$ standard deviation vector (column vector) of the input data. strPMNTS\$alpha : $\alpha$ of the std NTS distribution (X). strPMNTS\$theta : $\theta$ of the std NTS distribution (X). strPMNTS\$beta : $\beta$ vector (column vector) of the std NTS distribution (X). strPMNTS\$Rho : $\Sigma$ matrix of the std NTS distribution (X).
w	Capital allocation weight vector.

**Value**

The weighted sum follows 1-dimensional NTS.

$$R_p = \langle w, r \rangle = \mu + \text{diag}(\sigma)X,$$

where

$X$  follows  $\text{stdNTS}_1(\alpha, \theta, \beta, 1)$ .

Hence we obtain

`res$mu` :  $\mu$  mean of  $R_p$ .

`res$sigma` :  $\sigma$  standard deviation of  $R_p$ .

`res$alpha` :  $\alpha$  of  $X$ .

`res$theta` :  $\theta$  of  $X$ .

`res$beta` :  $\beta$  of  $X$ .

**References**

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

**Examples**

```
library("temStaR")
strPMNTS <- list(ndim = 2,
  mu = c( 9.876552e-05, 4.747343e-04 ),
  sigma = c( 0.01620588, 0.02309643 ),
  alpha = 0.1888129 ,
  theta = 0.523042,
  beta = c( -0.04632938, 0.04063555 ),
  Rho = matrix( data = c(1.0, 0.469883,
    0.469883, 1.0),
    nrow = 2, ncol = 2)
  CovMtx = matrix( data = c(0.0002626304, 0.0001740779,
    0.0001740779, 0.0005334452),
    nrow = 2, ncol = 2)
)
w <- c(0.3, 0.7)
res <- setPortfolioParam(strPMNTS,w)
```

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VaRetnts

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*VaRetnts*


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**Description**

VaRetnts calculates Conditional Value at Risk (CVaR, or expected shortfall ES) of the NTS market model with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If only three parameters are given, it calculates CVaR of the standard NTS distribution with parameter  $(\alpha, \theta, \beta)$

**Usage**

VaRetnts(`eps`, `ntsparam`)

**Arguments**

eps	the significant level for CVaR. Real value between 0 and 1.
ntsparam	A vector of the NTS parameters $(\alpha, \theta, \beta, \gamma, \mu)$ . A vector of the standard NTS parameters $(\alpha, \theta, \beta)$ .

**Value**

Value at Return of the NTS distribution.

**References**

Y. S. Kim, S. T. Rachev, M. L. Bianchi, and F. J. Fabozzi (2010), Computing VaR and AVaR in infinitely divisible distributions, *Probability and Mathematical Statistics*, 30 (2), 223-245.

S. T. Rachev, Y. S. Kim, M. L. Bianchi, and F. J. Fabozzi (2011), *Financial Models with Levy Processes and Volatility Clustering*, John Wiley & Sons

**Examples**

```
library("temStaR")
alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparam <- c(alpha, theta, beta)
u <- c(0.01, 0.05)
q <- VaRetnts(u, ntsparam)

alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparam <- c(alpha, theta, beta, gamma, mu)
u <- c(0.01, 0.05)
q <- VaRetnts(u, ntsparam)

#Annual based parameters
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
#scaling annual parameters to one day
dt <- 1/250 #one day
ntsparam <- c(alpha, theta, beta, gamma, mu, dt)
u <- c(0.01, 0.05)
q <- VaRetnts(u, ntsparam)
```

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