

# CS 137

## PART 1

### INTRO

`#include <stdio.h>`  $\Rightarrow$  Header file w/ preprocessing command  
`int main () {`  
 `printf ("Hello world\n");`  $\Rightarrow$  Prints output  
 `return 0;`  $\hookrightarrow$  Newline  
`}`  $\hookrightarrow$  Successful  $\Rightarrow$  0 or EXIT\_SUCCESS

### COMPILER

`scc my-file.c`  $\Rightarrow$  Compile  
`/a.out`  $\Rightarrow$  execution

### EUCLIDEAN ALGO

Pseudocode:

1. Find bigger num
2. Find remainder ( $a \geq b$ )
3. Make  $a = b$ ,  $b = \underline{\underline{a \% b}}$   $\rightarrow$  should be before update
4. Repeat until  $b=0, a = \text{gcd}$

Iterative:

```
While ( $b \neq 0$ ) {  
    r =  $a \% b$   
    a = b  
    b = r  
}  
return a
```

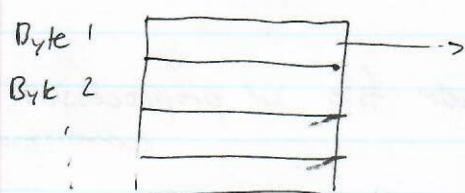
Recursive:

```
int recursive (int a, int b) {  
    if ( $b == 0$ )  
        return a;  
    else {  
        swap = a  
        b = a  $\% b$   $\leftarrow a = b$   
        return recursive (a, b);  
    }  
}
```

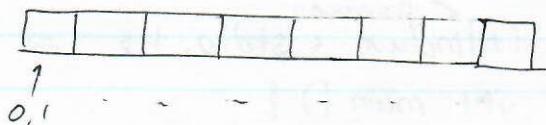
### INPUT/OUTPUT

`printf ("...", variable)`  
 $\hookleftarrow$  Variable input: %d, %lu, %c  
`scanf ("...", &variable);`  
 $\stackrel{\text{format input}}{\uparrow}$

## MEMORY



1 byte = 8 bits:



Representation:  $(2^8 - 1, 0)$

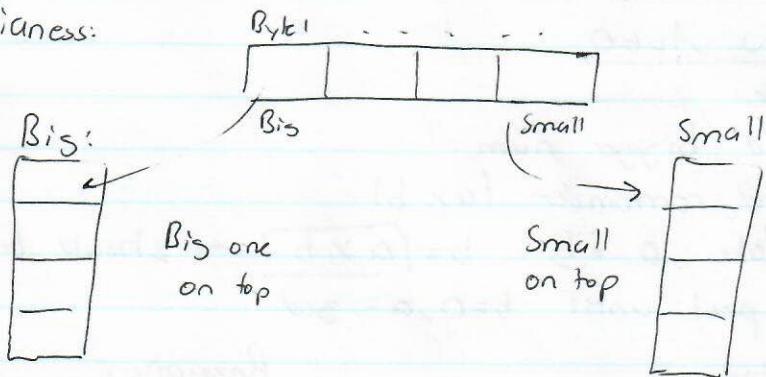
- Conversion:

Decimal  $\rightarrow$  binary: split into powers of 2:

$$123_{10} = (10^0 \times 3) + (10^1 \times 2) + (10^2 \times 1)$$

$$123_{10} \Rightarrow 123_2 \Rightarrow (1 \times 2^6) + (1 \times 2^5) + (1 \times 2^4) + (1 \times 2^3) + (1 \times 2^2) + (1 \times 2^1) + (1 \times 2^0) = 1111011_2$$

- Endianness:



- Signed int: binary way of notations  $\oplus$  and  $\ominus$

$$\begin{array}{c} 0100 \\ \downarrow \oplus \\ \end{array} \quad \begin{array}{c} 1100 \\ \downarrow \ominus \\ \end{array}$$

▫ Short cut of converting from  $\oplus$  to  $\ominus$  representation (negation)

1. Write in binary
2. Find right-most 1 bit
3. Invert all bits to left of that

- Binary arithmetic:

▫ Ex: Do  $-4 - 3$  in binary:

$$4 = 0000 \ 0000 \Rightarrow -4: 1111 \ 1100$$

$$3 = 0000 \ 0011 \Rightarrow -3: 1111 \ 1101$$

$$\begin{array}{r} 1111 \ 1100 \\ + 1111 \ 1101 \\ \hline \end{array}$$

$$+ \underline{1111 \ 1101}$$

$$1111 \ 1001 \Rightarrow \text{Throw away last carry over}$$

$$- (1111 \ 1001) = 0000 \ 0111$$

▫ Overflow = undefined behaviour (underflow)

↳ Know limit of variables (e.g. unsigned > 0)

## OPERATIONS

$\text{BEDMAS}$ : left associative

$$\hookrightarrow 6 - 2 \times 3 = (6-2) \times 3 \quad (\text{evaluates left expression})$$

Assignment: right associative ( $/=$ ,  $-=$ ,  $+=$ )

Incremental:

- ↳ Prefix:  $++var$   $\Rightarrow$  increment then use } Effect on while loop
- ↳ Suffix:  $var++$   $\Rightarrow$  use it then increment } loop

↳ Suffix:  $var++ \Rightarrow$  Use it, then increment } loop

Relational:  $\leq$ ,  $\leq^*$

Equality: ==, !=      Boolean

logical: & 8, 11 }

## Bit wise Operations:

$$a = 101100, b = 001110$$

NOT: ~a : 010011

AND:  $a \& b = 001100$  (1 if both 1)

OR:  $a \mid b$  : 101110 (1 if either 1)

XOR:  $a \text{ } \wedge \text{ } b: 100010 \Rightarrow (1 \text{ if strictly either 1})$

Left shift:  $a >> 2 = 001011$

Right shift:  $a \ll 3$ :  $1011000000000000$

## IF / ELSE

Dans l'île : if ( - - )

if (- ..) ↑  
else (- ..) ↑ b/c of lack of brackets

Ternary: boolean-expr? val1 : val2

Switch: switch (expr) {

case expr-value: break;

car expr-value: - ..

default: . . . break; next case.

## PART 2

### Loops:

1. while (condition) { - - }
2. do { - - } while (condition);  $\Rightarrow$  Executes at least once
3. for (initializer; condition; update) { - - }

- o Commands:

1. break;  $\Rightarrow$  exit loop
2. continue;  $\Rightarrow$  skip to next iteration
3. goto .

label: . . . . .  
goto label } } Looping potential

### FINDING PRIMES

1. Read in number
2. If  $n \leq 1 \Rightarrow$  Not prime
3. Else:

while ( $div + div \leq number \Rightarrow div = 2 \rightarrow \sqrt{n}$

if ( $n \times div == 0$ )

Not prime; break;

else :

$div++$ ;

if ( $div + div \leq number \{$  } If the number is a prime,  
Not prime; }  $div + div > \sqrt{n}$  by  
} else { prime } } while loop increment

### FUNCTIONS

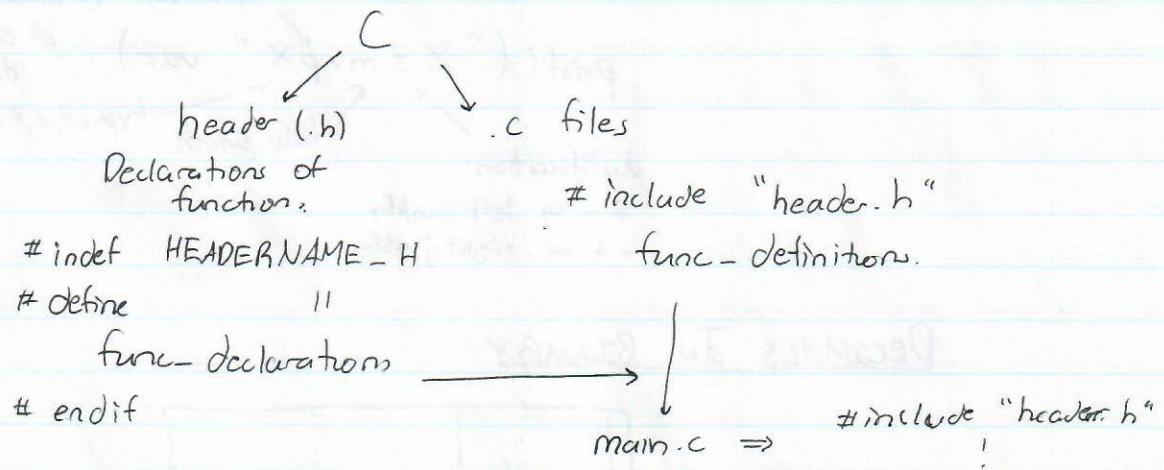
#### declaration

return\_type func\_name (parameters) { - - }

- o Function stack is gone when it hits 'return'

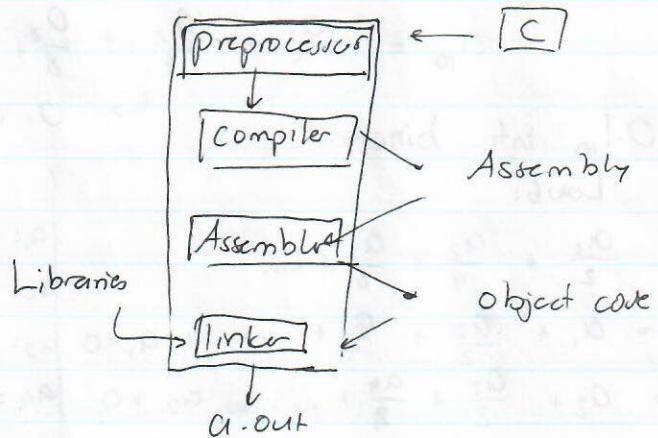
- o Pass by values: creates from array, not changing variables

## MODULES



o Compilation:

gcc -o powers powers.c-files  $\Rightarrow$  gcc main.c header.c



## MACROS

#define PI 3.1415...

↳ Constant name

## RECURSION

- o Iterative  $\rightarrow$  recursive (useful if no while, for, do-while, etc. allowed)
- o 2 rules:
  1. Base case (0, 1, ...)
  2. Progression towards base case.

PART 3

printf ("%.<sup>e</sup> m. p x", var)

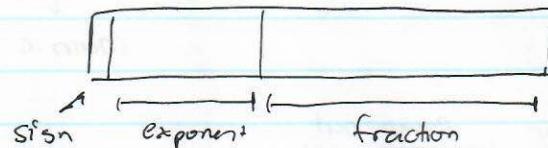
precision (# of decimal points (e-f), # of digits (d), # of significant digits (s))

field width type(d,e,f,s)

Justification:

- $\Rightarrow$  left justify
- +  $\Rightarrow$  right justify

## DECIMALS IN BINARY



$$(-1)^{\text{sign}} \cdot \text{fraction} \cdot 2^{\text{exponent}}$$

$$a_{10} = \frac{a_1}{2} + \frac{a_2}{4} + \frac{a_3}{8} + \dots$$

- Ex:// 0.1<sub>10</sub> into binary:

Long:

$$\begin{aligned} 0.1 &= \frac{a_1}{2} + \frac{a_2}{4} + \frac{a_3}{8} + \dots \\ \times 2 \quad &0.2 = a_1 + \frac{a_2}{2} + \frac{a_3}{4} + \dots \Rightarrow a_1 = 0 \\ \times 2 \quad &0.4 = a_2 + \frac{a_3}{2} + \frac{a_4}{4} + \dots \Rightarrow a_2 = 0 \\ &\vdots \end{aligned}$$

EASY:

$a_1:$	$0.1 \times 2 = 0.2 \Rightarrow a_1 = 0$
$a_2:$	$0.2 \times 2 = 0.4 \Rightarrow a_2 = 0$
$a_3:$	$0.4 \times 2 = 0.8 \Rightarrow a_3 = 0$
$a_4:$	$0.8 \times 2 = 1.6 \Rightarrow a_4 = 1$
$a_5:$	$0.6 \times 2 = 1.2 \Rightarrow a_5 = 1$

0.2

Notice repeating pattern

$$0.1_{10} = 0.0\overline{011}_2$$

## ERRORS

Absolute:  $| \text{decimal} - \text{actual} |$

Relative:  $\frac{| \text{decimal} - \text{actual} |}{| \text{actual} |}$

- Comparisons + equality check is no good for decimals  
 $\hookrightarrow$  Use tolerance/epsilon:  $x == y \Rightarrow (x-y) < \epsilon$

- Division:  $\frac{\text{float}}{\text{int}}$  or  $\frac{\text{int}}{\text{float}}$  or  $\frac{(\text{float})a}{b}$   $\leftarrow$  typecasting

## ARRAYS

int arr[5] = { 000, 004, 008, , 000 }  
 arr[0] = 000, arr[1] = 004, arr[2] = 008, arr[3] = , arr[4] = 000

Size  $\left\{ \begin{array}{l} \text{sizeof}(\text{var}) = \# \text{ of bytes of that var} \\ \hookrightarrow \text{sizeof(int)} = 4 \\ \# \text{ of elements in array: } \text{sizeof(array)} / \text{sizeof(element\_in\_array)} \end{array} \right.$

Passing:

Most things pass by value. Not arrays: pass by reference

func(array)  $\Rightarrow$  function gets the address of the array

↳ `func (a[ ])` ⇒ `a` in address to 1<sup>st</sup> element in arr.

Pointer decay: reverting from full array in main to just memory address in function  $\Rightarrow$  lose information (size)

Copying:

copy value 1 by 1 into new array. ( $a[0]$  returns value)

## MULTIDIMENSIONAL ARRAYS

int arr [ ] [2] = { {3, 43}, {4, 3}, {5, 93} } ;  $\Rightarrow$  3  $\times$  2 array

↳ q: arr[2][1] OR arr[0][row \* sizeof(row) + col]

$$a[0] = arr[0][2 \times 2 + 1]$$

Diagram illustrating a list  $a$  with elements  $a[0]$  and  $a[1]$ . The list is shown as a horizontal line with brackets indicating its structure. The first element  $a[0]$  is at the start, and the second element  $a[1]$  is indicated by an arrow pointing to the next position. The list ends with a closing bracket. Below the list, the elements  $a[0]$  and  $a[1]$  are shown again, with arrows pointing to their respective positions in the list above. To the right, the text "Reason behind why this works!" is written with an arrow pointing to the list structure.

Reason behind why  
this works!

## MATH.H

fabs(x), pow(x, y) =  $x^y$ , log( $\frac{x}{a}$ ) =  $\ln x$

## Root FINDING

### ① Bisection method:

1. Get some  $a$  and  $b$  s.t.  $f(a) > 0$  and  $f(b) < 0$
2. Find midpoint:  $m = \frac{a+b}{2}$
3. If  $f(m) < 0$ :  $b = m$
4. If  $f(m) > 0$ :  $a = m$
5. Loop until  $|m_{n-1} - m_n| < \epsilon$  / # of iterations.

### ② Fixed point:

Works if looking at function:  $s(x_0) = x_0 \Rightarrow$  Fixed point

↳ Ex: Root of  $x - \cos(x) = 0$ , same thing as  $\cos(x) = x$

1. Find  $s(x_0) = x$ ,
2. If  $|x_1 - x_0| < \epsilon$ , return  $x$ ,
3. Else: repeat with  $x_0 = x_1$ .

## FUNCTION POINTERS

Declaration of function pointed to: normal

Declaration of function using pointer:

return-type func-name ( - . . . , return-type (\* name) (param-type . . . ) )

Calling: give function name.

Using in function: use name as given in param-list.

## POLYNOMIALS

Represent as array of coefficients.

Computation:

1. Traditional:  $x \rightarrow x^n \rightarrow ax^n \rightarrow \text{add} \Rightarrow \# \text{ of } x: 2n-1, \# \text{ of } +: n$
2. Horner:  $2 + 9x + 4x^2 + 3x^3 = 2 + x(9 + x(4 + 3x)) \Rightarrow n \text{ multi} + \text{add}$   
for ( $i = n-2$ ;  $i \geq 0$ ;  $i--$ ) {  
     $y = y * x + p[i]$ ;  $\Leftarrow x$  is evaluating,  $p[i]$  is coefficient.  
     $\hookrightarrow \text{initial} = p[n-1];$   
    return  $y$

## PART 4

### STRUCTURES

```
struct struct-name {
    int var1;
    int var2;
};
```

```
struct struct-name instance-name = { __, __ };
= { .var1 = __ };
```

instance-name.var2  $\leftarrow$  Access

struct  $\rightarrow$  function (pass by value!)

- Simplify:

```
typedef struct { . . . } name;
```

```
name instance-name = { . . . };
```

- Pointers:  $*p = \&struct$

$p \rightarrow \text{var1} \Rightarrow$  Access to element in structure pointer (no dereference)  
 $\hookrightarrow$  Equivalent to  $(*p).\text{var1}$

### PAGE RANK

$$R(P) = \sum_{i=1}^M \frac{r(Q_i)}{|Q_i|} \Rightarrow \begin{array}{l} M: \text{number of linking pages} \\ Q_i: \text{a linking page} \end{array}$$

$\vdash$  Normalized to 1  $\vdash$

$|Q_i|: \# \text{ of outbound links of } Q_i$

- Ex: //



Find  $\text{rank}(A)$ ,  $\text{R}(B)$ ,  $\text{R}(C)$ :

①: Write down equations:

$$\text{①: } R(A) = \frac{R(C)}{1} \quad \text{③: } R(C) = R(B) + \frac{R(A)}{2}$$

$$\text{②: } R(B) = \frac{R(A)}{2} \quad \text{④: } R(A) + R(B) + R(C) = 1$$

②: Make all ranks in terms of 1:

$$\text{②: } R(B) = \frac{R(C)}{2}$$

$$\therefore \text{④: } R(C) + \frac{R(C)}{2} + R(C) = 1 \Rightarrow \begin{array}{l} R(C) = \frac{2}{3} \\ R(A) = \frac{2}{3} \\ R(B) = \frac{1}{3} \end{array}$$

- Random surfer model:

$$P(R) = \frac{1-\delta}{N} + \delta \sum_{i=1}^M \frac{r(Q_i)}{|Q_i|} \Rightarrow \delta: \text{P(exiting page)}$$

$\hookrightarrow$  Can be initialized

$N$ : # of pages in net

◦ Jacobi's Method:

1. Set all ranks of pages equal

2. Use random surfer model to converge to ranks faster

- Sinks:



◦ Fix:

$$P(R) = \frac{1-\delta}{N} + \delta \sum_{i=1}^M \frac{r(Q_i)}{|Q_i|} + \delta \sum_{i=1}^M \frac{r(S_i)}{N} \quad \begin{matrix} \text{# of sinks} \\ \hookrightarrow \# of pages \end{matrix}$$

$\hookrightarrow$  sink addition  $\rightarrow$

## PART 5

### POINTERS

type-var-pointers       $*\text{point-var} = \text{Var-pointing-to};$

$\swarrow$

point-var: address

$\searrow$  Dereference:

$*\text{point-var}: \text{value}$

$\hookrightarrow$  Memory address of

$\hookrightarrow$  Gets value of things

variable I'm pointing to you

it is pointing to.

- Arithmetic:  $a + m \quad (m \in \mathbb{Z})$

◦ Starting from  $a$  and moving  $m$  bytes (# of bytes depends on type of

$$a[8] = \{ \overset{①}{2}, \overset{②}{3}, \overset{③}{4}, \overset{④}{5}, \overset{⑤}{6}, \overset{⑥}{7}, \overset{⑦}{8}, \overset{⑧}{9} \}$$

int  $*p, *q;$

$\overset{③, ④}{}$

①:  $p = \&a[27]$

$\star$  However:

$$a = \&a[0] = 100$$

②:  $q = p + 4$

$$a + 1 = 104 \quad (4 \text{ bytes/int})$$

③:  $p += 4$

$$\&a + 1 = 136 \quad (\text{whole array} + 1)$$

④:  $*p = 10$

- Array pointers:

$$a[8] = \{ \overset{a[0]}{1}, \overset{a[1]}{2}, \overset{a[2]}{3}, \overset{a[3]}{4}, \overset{a[4]}{5}, \overset{a[5]}{6}, \overset{a[6]}{7}, \overset{a[7]}{8} \}$$

*Hilary*

$a + 5$

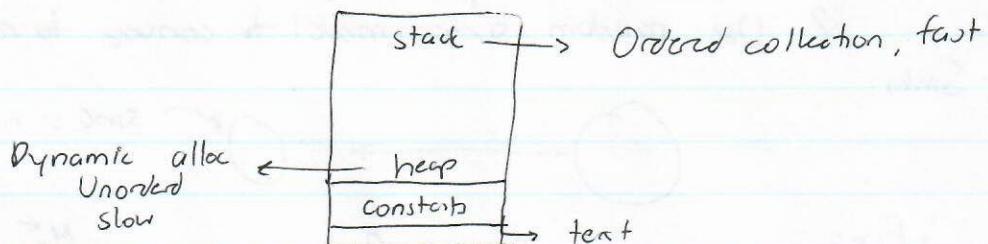
Combining `++` and `*`:

`* ++ p`  $\Rightarrow$  `* (++p)` (Increment `p` then use `*p`)

`* p++`  $\Rightarrow$  `* (p++)` (Use `*p` then increment `p`)

`(*p)++`  $\Rightarrow$  (Use `*p` then increment `*p`)

Know 2D array pointers:  $\star\star a \Rightarrow a[i][j] = \star(\star(a + i) + j)$   
MEMORY MANAGEMENT  $= \star(a + (i \times \text{no\_cols} + j))$



`#include <stdlib.h>`

→ `void * malloc (size_t size):` allocates 'size' number of bytes from `heap`  $\rightarrow$  pointer.

`malloc`  
↓  
pointer

`useful` ← null  $\Rightarrow$  Null pointer should be checked.

→ `void free (void *):` free memory allocated to pointer.

↳ Memory leak: Computer runs out of memory  
bcuz no memory was freed.

→ `void * calloc (nmemb, size):` allocates `nmemb` elements of 'size' bytes to 0

→ `void * realloc (void * p, size):` reallocate old block to new block.

## DYNAMIC ARRAYS

Structure malloc:  
↳ Access fields: `struct struct-name * var = malloc (sizeof (struct struct-name))`  
`(* var). field` OR `var-> field`

Struct hack:

1. `struct name {`

`field1 = ...`

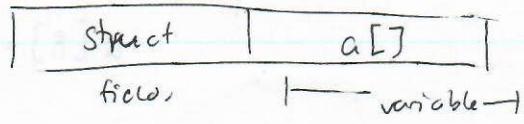
`field2 = ...`

`};`

`int a[7]`  
↑  
end must be  
array

2. Malloc:

`malloc (sizeof (struct) + array-size * sizeof (int))`



- ## - Vector implementation:

```
1. struct vector {  
    int *arr;  
    int size, len  
};
```

- ## 2. Creation:

```
struct vector * v = malloc (sizeof (struct vector))
```

$V \rightarrow \text{size} =$

v → arr = malloc (sizeof (int) \* 4)

- ### 3. Deletion:

free ( $v \rightarrow ar$ );

free (v)

Must be in this order: will have  
leads.

- #### 4. Add:

if (length == size):

newSize = size \* 2

```
int *newarr = malloc (sizeof(int) * newSize)
```

```
for (int i = 0; i < max size; i++)
```

update newArr w/ old arr elements } copying

newArr [v → size] = new Value

free ( $v \rightarrow ar$ )

$\leftarrow \text{size} = \text{newSize}$

`v7 arr = newArr;`

} New array h/

) } 2x size

1

## Updatins

else:

$v \rightarrow \text{arr} [v \rightarrow \text{length}] = \text{value}$

++ v → length

## PART 6

## CHARACTERS

```
char firstChr = 'a';
```

- ## · ASCII:

48-S7: Number  $\Rightarrow$  Convert character # to real number via num - '0'

65 - 90 : <sup>upper</sup> ~~lower~~ case letters

97 - 122: lower case letters. } Corresponding character  
is 32 away.

- Convert 'a' to 'A'.
  $\forall a 'a' - 32 \Rightarrow 'A'$
- You can add numbers to letters in chars.
  - Numbers can also be represented by characters! $'a' - ' ' \Rightarrow 'A'$

## STRINGS

- char s[] = "Hello"; really important
- char s[] = {'H', 'e', 'l', 'l', 'o', 'W', 'o', 'r', 'l', 'd'};
- Checking if string is truncated:  
 $s[i] = 'O'$
- char \*s = "Hello"
  - String literal: cannot change (undef. behavior)
  - char \*s = "Hello" "world!"  $\Rightarrow$  combines into 1
  - sizeof(s) is not always = sizeof("...")

## CONSTANTS

const ...  $\Rightarrow$  immutable

const int i = 10

Only way to change:

const int i = 10  
 int \*a = &i  
 $*a = 3$

} Undefined

Know the differences between constants + macros

const int \*p  
 OR int const \*p  
 P is a pointer to a constant  
 int  

- Can change address, but cannot change number.

 Let r: int \*r;  
 $r = p \Rightarrow$  error  

$r = (\text{int}^*)p \Rightarrow \text{Fine}$   
 $*r = 3 \Rightarrow \text{Fine}$

int \*const q:  
 Cannot change address  

- Pointer constant.

## STRING LIBRARIES

#strings.h

size\_t strlen(const char \*): returns length of string (w/out null)

- ↳ Compare to sizeof(char[7])  $\Rightarrow$  size including null.
- sizeof(char\*)  $\Rightarrow$  size of address.

char \* strcpy(char \*s0, const char \*s1):

- ↳ Copies s1  $\rightarrow$  s0. s0 might not == sizeof(s1)  $\Rightarrow$  undefined behavior.
- ↳ Includes '\0'

char \* strncpy(char \*s0, const char \*s1, size\_t n):

- ↳ Copies first n characters from s1  $\rightarrow$  s0
- ↳ If strlen(s1) < n - null padded.
- ↳ No null character added!

char \* strcat(char \*s0, const char \*s1):

- ↳ Concatenates s1  $\rightarrow$  s0
- ↳ Make sure s0 has enough space.

char \* strncat(char \*s0, const char \*s1, size\_t n):

- ↳ Concatenates first n characters from s1  $\rightarrow$  s0.
- ↳ Adds '\0' after.

char int strcmp(const char \*s0, const char \*s1):

- ↳ <0: s0[i] < s1[i] || all equal except s1 is bigger.
- 0: s0[i] > s1[i] || all equal except s0 is bigger.
- =0: completely equal.

char c[] = "hello"

char d[] = "~~hello~~ hello"

if(c == d) { "!" }  $\Leftarrow$  compares address! Need strcmp!

else { "not equal" }

Printing strings: printf("%s", char[7])

Get strings: scanf("%s", &var)  $\Rightarrow$  stops at whitespace

gets("%s", &var)  $\Rightarrow$  stops at \n

Hilroy

## OTHER STRING FUNCTIONS

`Void * mem copy (void * restrict s1, const void * restrict s2, size_t n)`

Copying n bytes from s2 to s1

- "restrict"  $\Rightarrow$  no other pointer can access array/memory.  
↳ Overlap not allowed
- Always remember to copy '\0' at end of string.

`Void * memmove (void * s1, void * s2, size_t n)`

Same thing as memcpy, s1 + s2 bytes can overlap

`int memcmp (void * s1, const void * s2, size_t n)`

Compares bytes of memory (similar to strcmp)

↳ Only looks at first n bytes.

$< 0$	$= 0$	$> 0$
$\downarrow$	$\downarrow$	$\downarrow$
1st byte that does not match is smaller in s1	equal	1st byte that does not match is greater than s1.

`Void * memset (void * s, int c, size_t n)`

Fills n bytes of s with byte C (converts to char)

## UNICODE

1 Character = 21 bits!

Divided into 21 planes (Plane 0 is Basic Multilingual Plane / BMP)

## PART 7.

### BIG O

$$g(x) \in O(f(x)) \Rightarrow g(x) \leq c f(x) \quad (c \in \mathbb{R}) \text{ where } x \geq x_0$$

$g(x)$  has same <sup>or lower</sup> growth rate as  $f(x)$  and I can multiply  $f(x)$  by some number s.t. the function will be bigger than  $g(x)$  at after ~~ever~~ a certain point.

↳  $g(x) \in O(f(x))$  if  $g(x)$  grows at equal/slower rate.

Asymptotic growth: look at values  $\rightarrow \infty$  (highest power term matters)

$$\text{↳ } \lim_{x \rightarrow \infty} \frac{g(x)}{f(x)} < \infty \Rightarrow g(x) \in O(f(x))$$

$$\lim_{x \rightarrow \infty} \frac{f(x)}{g(x)} = \infty \Rightarrow f(x) \in O(g(x))$$

Logs: bases don't matter:

$$\log_a x = \frac{\log_b x}{\log_b a} = \underbrace{\frac{1}{\log_b a}}_{\substack{\leftarrow \text{constant: no effect} \\ \text{for } x \rightarrow \infty}} \log_b x$$

Properties: let  $g_0(x) \in O(f_0(x))$  and  $g_1(x) \in O(f_1(x))$

1.  $g_0(x) + g_1(x) \in O(f_0(x) + f_1(x))$
2.  $g_0(x) \cdot g_1(x) \in O(f_0(x) \cdot f_1(x))$
3.  $O(f_0(x) + f_1(x)) \in O(\max\{f_0(x), f_1(x)\})$

Transitivity:  $h(x) \in O(g(x)) \wedge g(x) \in O(f(x)) \Rightarrow h(x) \in O(f(x))$

Growth rates:

$$1 \ll \log n \ll n^2 \ll c^n \ll n! \ll n^n$$

Others:

- Little - O:  $O(f(x))$ : <
- Big Omega:  $\Omega(f(x))$ : ≥
- Little Omega:  $\omega(f(x))$ : >
- Big Theta:  $\Theta(f(x))$ : =

Tips: look @ how many times code is run

Hilary

## SEARCHING

Linear search:

```
int lin-search (int a[], int n, int value) {  
    for (int i = 0; i < n; i++) {  
        if (a[i] == value) {  
            return i;  
        }  
    }  
    return -1;  
}
```

Analysis:

Best case: value at beginning  $\Rightarrow O(1)$

Worst case: value at end  $\Rightarrow$  # of ops =  $1 + (1+2+3+\dots+n) + 1 \in O(n)$

Average case:  $O(n)$

Binary search:

```
int bin-search (int a[], int n, int value) {  
    int beg = 0, end = n-1;  
    while ((a[(end - beg) / 2]) != value)
```

```
int bin-search (int a[], int n, int value) {  
    int left = 0, int right = n-1;  
    while (left <= right) {  
        int middle = left + (right - 1) / 2  
        if (a[middle] == value)  
            return middle;  
        if (a[middle] < value)  
            left = middle + 1;  
        else  
            right = middle - 1;  
    }  
    return -1.
```

$\Rightarrow$  Worst case:

$O(\log n)$

Requires sorted list

## SORTING

- ### - Selection sort:

1. Finds the smallest element
  2. Swap to front
  3. Repeat w/ array

```

Void selection - sort ( int a[], int n ) {
    for ( int i = 0 ; i < n ; ++i ) {
        int min = i
        for ( int j = i + 1 ; j < n ; ++j ) {
            if ( a[j] < a[min] ) min = j;
        }
        int temp = a[i];
        a[i] = a[min];
        a[min] = temp;
    }
}

```

- Time complexity:  $O(n^2)$  in worst case, best case + average case.
  - Problem: checking constantly if array is sorted, in a sense. (inner loop)

- Insertion Sort:

1. For all  $x$ , find where  $x$  should go
  2. Shift elements less than  $x$
  3. Insert  $x$  + repeat

} 1 pass of whole array!

```
void insertion-sort (int *a, int n) {
```

```
for (i=0; i< n; i++) {
```

$x = a[i];$

for (j = i; j > 0 && x < a[j-1]; j--) {

$a[j] = a[j-1]; \leftarrow$  Duplicating value to current position

$$a[j] = x;$$

✓ We can just simply drop in  $x$ .

- Time complexity:  $O(n^2)$  in worst case.  $O(n)$  in best case.  
    ↳ inner loop never executed if sorted.

-Merge sort:

1. Keep dividing array in half
  2. Sort recursively
  3. Combine
- $O(n \log n)$  for all cases.  
 $\hookrightarrow n$  for comparison,  $\log_2 n$  merge.

o Functions:

```
void main-merge (int a[], int n) {  
    int *t = malloc (n * sizeof (int));  $\hookrightarrow$  Creating temp. array  
    merge-sort (a, t, n);  $\hookrightarrow$  to store values.  
    free (t);
```

}

```
void merge-sort (int a[], int t[], int n) {
```

if ( $n \leq 1$ ) return;

int middle =  $n/2$

int \*lower = a

int \*upper = a + middle

// Take subarrays + sort

```
merge-sort (lower, t, middle);
```

```
merge-sort (upper, t, n - middle);
```

// Combine:

int i = 0;

int j = middle;

int k = 0;  $\Rightarrow$  temp index.

// Going through both subarrays + placing in temp.

```
while (i < middle && j < n) {
```

if ( $a[i] < a[j]$ )  $t[k++] = a[i++]$ ;

else  $t[k++] = a[j++]$ ;

}

// Putting in any remaining elements.

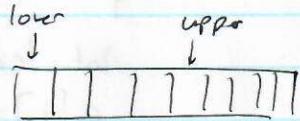
```
while (i < middle) {  $t[k++] = a[i++]$ ; }
```

```
while (j < n) {  $t[k++] = a[j++]$ ; }
```

// Copy into actual array.

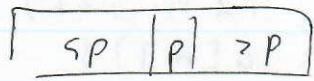
```
for (int i = 0; i < n; i++) a[i] = t[i];
```

}



- Quick sort:

1. Pick a pivot in array
2. Split array into partitions:



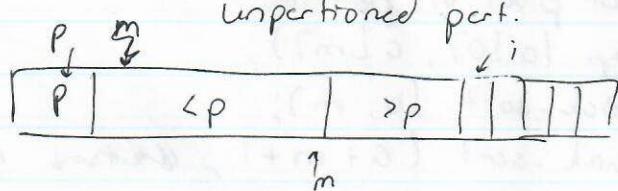
Space is conserved! No new arrays are created.

3. Sort 2 partitions.

- o Lomuto Partition:

- o Pivot is 1<sup>st</sup> element.

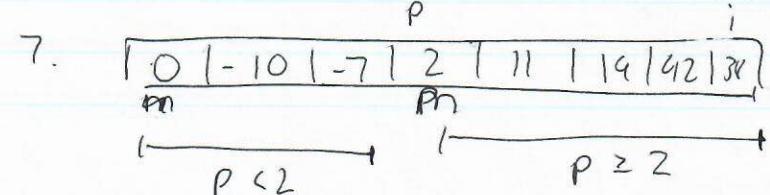
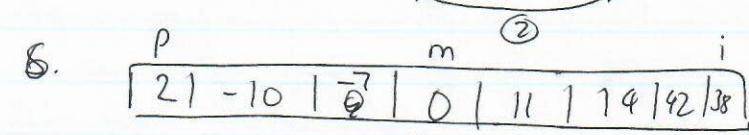
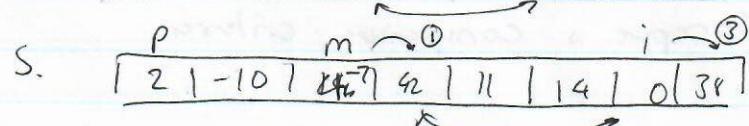
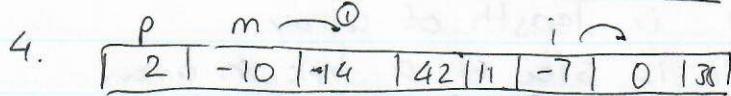
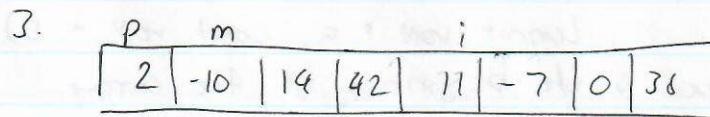
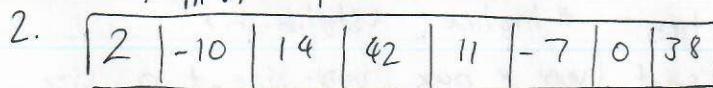
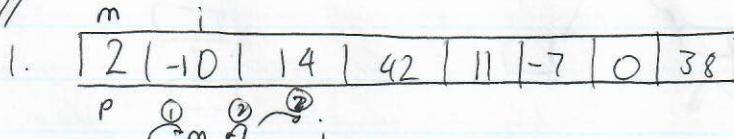
- o Index variables:  $m$  (last index of partition  $< p$ ),  $i$  is 1<sup>st</sup> index of unpartitioned part.



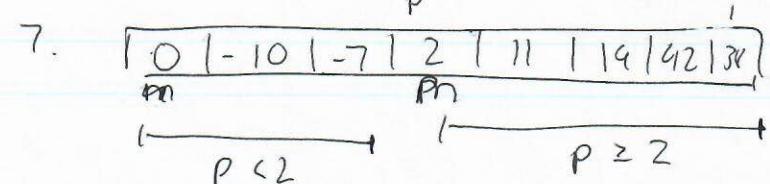
- o Steps:

1. If  $a[i] \leq p$ : put into ' $< p$ ' partition. Increment  $m$ , swap  $a[m] \leftrightarrow a[i]$ , increment  $i$ .
2. If  $a[i] \geq p$ : put into ' $> p$ ' partition. Increment  $i$ .
3. End: if  $i == n$ , then  $a[m] \leftrightarrow a[0]$ . Partition in middle.

- o Ex://



= Recur. Hilary



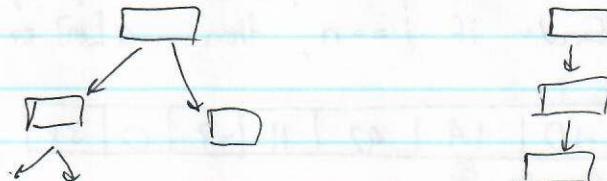
```

void quick-sort (int a[], int n) {
    if (n <= 1) return;
    int m = 0;
    for (int i = 1; i < n; i++) {
        if (a[i] < a[m]) {
            m++;
            swap (a[i], a[m]);
        }
    }
    // Put pivot in partition.
    swap (a[0], a[m]);
    quick-sort (a, m);
    quick-sort (a + m + 1, n - m - 1);
}

```

- Time complexity: average + best case:  $O(n \log n)$ . Worst  $O(n^2)$
- Space: long list of calls on stack.

- Tail recursion: have 1 recursive call @ end of function



- Built in sorting: `#include <stlib.h>`

```

void qsort (void * box, void size_t n, size_t size, int (*compare)
            (const void * a, const void * b));

```

- Box is the beginning of the array
- n is length of array
- Size is size of a byte in array
- Compare  $\Rightarrow$  comparison criteria.

## TAIL RECURSION

- Fibonacci:

$$f(n) = f(n-1) + f(n-2)$$

Iteratively  $\rightarrow$  tail recursion.

↳ Pass a counter!

```
int fib (int n) {  
    if (n == 0) return 0;  
    return helper (0, 1, n);  
}
```

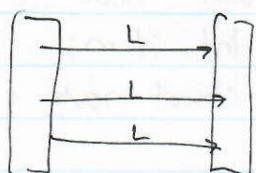
```
int helper (int a, int b, int n);  
    if (n == 0) return a;  
    return helper (a+b, a, n-1);  
}
```

↑  
state    state    count

## HIGHER-ORDER FUNCTIONS

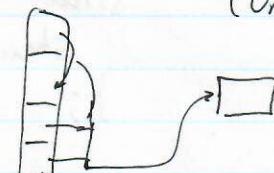
void — ( —, —, function )

Map



\* Linear transformation \*

Reduce.



Mapping function:

# of elements    size of 1 byte (linear)  
void map (void \*src, size\_t n, size\_t srcb, void \*dest, size\_t  
\*destb, void (\*f)(void \*, void \*)) {

for (size\_t i = 0; i < n; i++) {

f (src, dest);

src += srcb  
dest += destb

} Increment b up to next array element

}

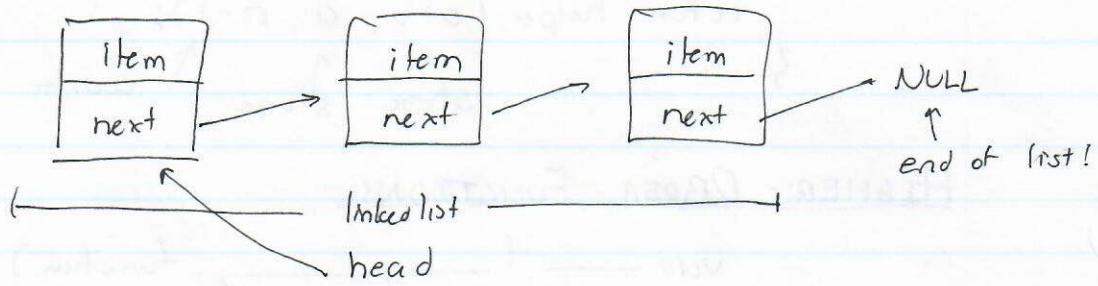
3

Hibroy

Reducing function.

```
void reduce (void *src, size_t n, size_t srcb, void *dest, void (*f)(void *, void))
{
    if (n == 1) {
        f(src, dest);
        return;
    }
    reduce (src + srcb, n - 1, dest, f);
    f(src, dest);
}
```

## LINKED LIST



Implementation:

1. Linked list structure:

```
struct linkedlist {
    struct node *head;
};
```

2. Node structure.

```
struct node {
    int item;
    struct node *next;
};
```

\* Do not lose pointer references! Be careful of order of operations!  
Important technique: have pointer to previous + current data nodes.

Re

- Polynomial linked list

```
struct llnode {  
    void * data;  
    void struct llnode * next; };  
struct ll {  
    void struct llnode * head; };
```

1. Create:

```
struct ll * llcreate () {  
    struct ll * new = malloc (sizeof (struct ll));  
    new -> head = NULL; return new;  
}
```

2. Adding elements.

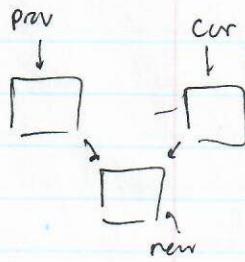
```
void addToFront (struct ll * l, void * element) {  
    struct llnode * new = malloc (sizeof (struct llnode));  
    llnode new -> next = l -> head;  
    new -> data = element;  
    ll -> head = new;  
    return;  
}
```

```
void addInOrder (struct ll * l, void * element, int void (*cmp) (void*, void)) {
```

```
    struct llnode * cur = l -> head; // Next point  
    struct llnode * prev = NULL; // Previous point  
    for (; cur && cmp (cur -> data, element) < 0; prev = cur,  
        cur = cur -> next) // Finds spot where cur > elem.
```

Is it front?  $\Rightarrow$  if (!prev) addToFront (l, element);

Addin elem. {  
 struct llnode \* new = malloc (sizeof (struct llnode));  
 new -> next = cur;  
 new -> data = element;  
 prev -> next = new;



### 3. Copying.

Creates  
new  
structure

Recursive  
definition!  
useful!

```
struct ll * copy (struct ll* src) {  
    void struct ll * new = malloc (sizeof (struct ll));  
    new -> head = copy-helper (src -> head);  
    return new;  
}  
  
struct llnode * copy-helper (struct llnode * src) {  
    if (!src) return NULL;  
    struct llnode * new = malloc (sizeof (llnode));  
    * new -> next = copy-helper (src -> next);  
    new -> data = copy-int (src -> data);  
    return new;  
}  
  
void * copy-int (void * data);  
int * src = malloc (sizeof (int));  
* src = * (int * ) data;  
return src;
```

### 4. Deletion.

```
*  
void delete_ll (struct ll) {  
    delete_ll_node (ll -> head);  
    free (ll);  
}  
  
void delete_ll_node (struct llnode * node) {  
    if (!node) free (node); return;  
    delete (node -> next);  
    free (node);  
    return;  
}
```