# AMERICAN SOCIETY OF PENSION PROFESSIONALS & ACTUARIES JOINT BOARD FOR THE ENROLLMENT OF ACTUARIES SOCIETY OF ACTUARIES

#### **Enrolled Actuaries Basic Examination**

# EA-1

Date: Tuesday, May 12, 2009 Time: 8:30 a.m. – 11:00 a.m.

#### INSTRUCTIONS TO CANDIDATES

- Write your candidate number here \_\_\_\_\_. Your name must not appear.
- Do not break the seal of this book until the supervisor tells you to do so.
- 3. Special conditions generally applicable to all questions on this examination are found at the front of this book.
- 4. On this examination the symbol "a" will be used to represent an annuity. On this examination the symbol " $\ell_x$ " will be used to represent the number of lives at age x.
- 5. This examination consists of 35 multiple-choice questions worth a total of 100 points. The point value for each question is shown in parentheses at the beginning of the question.
- 6. Your score will be based on the point values of questions that you answer correctly. No credit will be given for omitted answers and no credit will be lost for wrong answers; hence, you should answer all questions even those for which you have to guess.
- 7. A separate answer sheet is inside the front cover of this book. During the time allotted for this examination, record all your answers on side 2 of the answer sheet. NO ADDITIONAL TIME WILL BE ALLOWED FOR THIS PURPOSE. No credit will be given for anything indicated in the examination book but not transferred to the answer sheet. Failure to stop writing or coding your answer sheet after time is called will result in the disqualification of your answer sheet or further disciplinary action.
- 8. Five answer choices are given with each question, each answer choice being identified by a key letter (A to E). For each question, blacken the oval on the answer sheet that corresponds to the key letter of the answer choice that you select
- 9. Use a soft-lead pencil to mark the answer sheet. To facilitate correct mechanical scoring, be sure that, for each question, your pencil mark is dark and completely fills only the intended oval. Make no stray marks on the answer sheet. If you have to erase, do so completely.
- Do not spend too much time on any one question. If a question seems too difficult, leave it and go on.
- 11. While every attempt is made to avoid defective questions, sometimes they do occur. If you believe a question is defective, the supervisor or proctor cannot give you any guidance beyond the instructions on the exam booklet.

- Clearly indicated answer choices in the test book can be an aid in grading examinations in the unlikely event of a lost answer sheet.
- Use the blank portions of each page for your scratch work. Extra blank pages are provided at the back of the examination book.
- 14. When the supervisor tells you to do so, break the seal on the book and remove the answer sheet.

On side 1 of the answer sheet, space is provided to write and to code candidate information. Complete Blocks A through G as follows:

- (a) in Block A, print your name and the name of this test center;
- (b) in Block B, print your last name, first name and middle initial and code your name by blackening the ovals (one in each column) corresponding to the letters of your name; for each empty box, blacken the small rectangle immediately above the "A" oval;
- (c) write your candidate number in Block C (as it appears on your ticket of admission for this examination) and write the number of this test center in Block D (the supervisor will supply the number);
- (d) code your candidate number and center number by blackening the five ovals (one in each column) corresponding to the five digits of your candidate number and the three ovals (one in each column) corresponding to the three digits of the test center number, respectively. Please be sure that your candidate number and the test center number are coded correctly;
- (e) in Block E, code the examination that you are taking by blackening the oval to the left of "Course EA-1."
- (f) in Block F, blacken the appropriate oval to indicate whether you are using a calculator; and
- (g) in Block G, sign your name and write today's date. If the answer sheet is not signed, it will not be graded.

On side 2 of your answer sheet, space is provided at the top for the number of this examination book. Enter the examination book number, from the upper right-hand corner of this examination book, in the four boxes at the top of side 2 marked "BOOKLET NUMBER."

15. After the examination, the supervisor will collect this book and the answer sheet separately. DO NOT ENCLOSE THE ANSWER SHEET IN THE BOOK. All books and answer sheets must be returned. THE QUESTIONS ARE CONFIDENTIAL AND MAY NOT BE TAKEN FROM THE EXAMINATION ROOM.

EA-1 Spring 2009 Answer Key

Question	Solution
1	С
2	D
3	Α
4	E
3 4 5 6 7 8	D
6	С
7	С
8	D
9	E
10	С
11	Е
12	Α
13	С
10 11 12 13 14 15 16	A E D C C C D E C C B C C
15	С
16	В
17 18 19	B D
18	D
19	E
20	С
21	D
22	В
23	D
24	В
25	С
21 22 23 24 25 26 27 28	B D C C C D
27	D
28	В
29	С
30	В
31	В
32	B B B
33	В
34	D
35	Α

#### \*\*BEGINNING OF EXAMINATION\*\*

#### <u>Data for Question 1</u> (2 points)

Terms of a 5-year annuity-certain:

Payment amount \$100

Payment frequency Monthly, with payments at the beginning of each

month

Interest rate 5% per year, compounded quarterly

#### Question 1

In what range is the present value of the annuity?

- (A) Less than \$5,190
- (B) \$5,190 but less than \$5,260
- (C) \$5,260 but less than \$5,330
- (D) \$5,330 but less than \$5,400
- (E) \$5,400 or more

# Data for Question 2 (3 points)

$$d_{45} = 502$$

$$\ell_{47} = 89,472$$

$$_{1|}q_{45} = 0.006141$$

# Question 2

In what range is  $d_{46}$ ?

- (A) Less than 512
- (B) 512 but less than 532
- (C) 532 but less than 552
- (D) 552 but less than 572
- (E) 572 or more

#### Data for Question 3 (3 points)

Terms of a 10-year annuity-certain:

Payments \$100 per year payable annually with the first

payment on January 1, 2012

Interest The interest rates used to value the annuity as of

January 1, 2009 are given by the following annual

spot rates:

<u>Years</u>	Spot rate
2009-2013	5%
2014-2018	6%
2019-2023	7%

X = the present value of the annuity as of January 1, 2009.

#### Question 3

- (A) Less than \$650
- (B) \$650 but less than \$685
- (C) \$685 but less than \$720
- (D) \$720 but less than \$755
- (E) \$755 or more

#### Data for Question 4 (3 points)

Selected values from a basic mortality table:

$\underline{x}$	$q_x$
84	0.0762
85	0.0852
86	0.0953
87	0.1075
88	0.1204
89	0.1341
90	0.1493

The basic mortality table is adjusted using a 1-year set forward for male lives and using a 2-year set back for female lives.

x = male life age 85

y = female life age 86

# Question 4

In what range is  $_3p_{\overline{xy}}$ ?

- (A) Less than 0.9075
- (B) 0.9075 but less than 0.9150
- (C) 0.9150 but less than 0.9225
- (D) 0.9225 but less than 0.9300
- (E) 0.9300 or more

# Data for Question 5 (4 points)

$$q_{20} = 0.10$$

$$q_x = 0.05 \text{ for all } x > 20$$

i = 4.0%, compounded annually

# Question 5

In what range is  $\ddot{a}_{20}$ ?

- (A) Less than 9.7
- (B) 9.7 but less than 10.2
- (C) 10.2 but less than 10.7
- (D) 10.7 but less than 11.2
- (E) 11.2 or more

Data for Question 6 (3 points)

$$\mu(x) = \frac{1}{100 - x}, \quad 0 \le x \le 100$$

$$i = 0.0\%$$

# Question 6

In what range is  $\ddot{a}_{40}$ ?

- (A) Less than 29.9
- (B) 29.9 but less than 30.4
- (C) 30.4 but less than 30.9
- (D) 30.9 but less than 31.4
- (E) 31.4 or more

#### <u>Data for Question 7</u> (3 points)

Employee Smith earns an annual salary in 2009 of \$50,000.

Assumed salary increases: 3% each year, beginning 1/1/2010.

At the end of each year, beginning 12/31/2009, 5% of Smith's annual salary is deposited into a fund earning an annual rate of interest of 6%.

X = the amount in Smith's fund on 1/1/2030.

#### Question 7

- (A) Less than \$122,000
- (B) \$122,000 but less than \$126,000
- (C) \$126,000 but less than \$130,000
- (D) \$130,000 but less than \$134,000
- (E) \$134,000 or more

# Data for Question 8 (2 points)

$$\ddot{a}_{\scriptscriptstyle |\!\!|\!\!|}=6.091836$$

$$\ddot{a}_{\overline{n+1}} = 6.381005$$

# Question 8

In what range is  $\ddot{s}_{\overline{n}}$ ?

- (A) Less than 20.10
- (B) 20.10 but less than 20.50
- (C) 20.50 but less than 20.90
- (D) 20.90 but less than 21.30
- (E) 21.30 or more

# Data for Question 9 (3 points)

Terms of a five-year bond issued on 1/1/2009:

Face amount \$1,000 Redemption amount \$1,000

Coupon rate 5.0% per year, payable annually

Yield rate 5.0% per year, compounded annually

X = the duration of this bond in years.

#### Question 9

- (A) Less than 3.75
- (B) 3.75 but less than 4.00
- (C) 4.00 but less than 4.25
- (D) 4.25 but less than 4.50
- (E) 4.50 or more

# Data for Question 10 (4 points)

A service table has two sources of decrement.

$$q_x^{(1)} = 4q_x^{(2)}$$

$$q_x^{(T)} = 0.24$$

#### Question 10

In what range is  $q_x^{\prime(1)}$ ?

- (A) Less than 0.195
- (B) 0.195 but less than 0.198
- (C) 0.198 but less than 0.201
- (D) 0.201 but less than 0.204
- (E) 0.204 or more

#### Data for Question 11 (4 points)

Selected net annual premiums for whole life insurance policy:

$$P_{50} = 0.03550$$

$$P_{51} = 0.03712$$

I = 4.0%

N = Out of the 100,000 alive at age 50, the number expected to die after age 51.

# Question 11

- (A) Less than 93,800
- (B) 93,800 but less than 95,300
- (C) 95,300 but less than 96,800
- (D) 96,800 but less than 98,300
- (E) 98,300 or more

# Data for Question 12 (3 points)

The following is an extract from a table with a 3-year select period:

<u>x</u>	$q_{[x]}$	$q_{[x]+1}$	$q_{[x]+2}$	$q_{x+3}$	<i>x</i> +3
50	0.074	0.094	0.114	0.126	53
51	0.076	0.096	0.116	0.128	54
52	0.078	0.098	0.118	0.130	55
53	0.080	0.100	0.120	0.132	56
54	0.083	0.103	0.123	0.135	57

 $\ell_{55} = 13,200$ 

# Question 12

In what range is  $d_{[53]+1}$ ?

- (A) Less than 1,460
- (B) 1,460 but less than 1,480
- (C) 1,480 but less than 1,500
- (D) 1,500 but less than 1,520
- (E) 1,520 or more

#### Data for Question 13 (3 points)

You have the following information about a group of participants in a pension plan:

Number of active participants at exact age 50	1,000
Number of deaths between exact ages 50 and 51	10
Number of decrements other than death between exact ages 50 and 51	57

All decrements other than death occur one-third of the way during the period between consecutive ages.

X = the rate of mortality at age 50 in the associated single decrement mortality table.

# Question 13

- (A) Less than 0.01025
- (B) 0.01025 but less than 0.01035
- (C) 0.01035 but less than 0.01045
- (D) 0.01045 but less than 0.01055
- (E) 0.01055 or more

#### Data for Question 14 (3 points)

Interest = 6% per year, compounded annually.

X =Present value of a perpetuity that pays \$1 at the end of the 2<sup>nd</sup> year, \$2 at the end of the 4<sup>th</sup> year, \$3 at the end of the 6<sup>th</sup> year, continuing to pay \$k\$ at the end of the 2k<sup>th</sup> year.

#### Question 14

- (A) Less than \$73.00
- (B) \$73.00 but less than \$76.00
- (C) \$76.00 but less than \$79.00
- (D) \$79.00 but less than \$82.00
- (E) \$82.00 or more

#### Data for Question 15 (5 points)

Terms of a serial bond:

Face amount of bond \$20,000

20 equal annual installments at par payable at the end of the  $11^{th}$  through the  $30^{th}$  years Terms of redemption

8%, payable semi-annually Coupons

Yield rate 9%, compounded semi-annually

X =the purchase price of the serial bond.

#### Question 15

- (A) Less than \$18,100
- \$18,100 but less than \$18,150 (B)
- \$18,150 but less than \$18,200 (C)
- \$18,200 but less than \$18,250 (D)
- \$18,250 or more (E)

#### Data for Question 16 (2 points)

An annuity provides level annual payments of \$1,000 at the end of each year for four years.

Term structure of interest rates as of 1/1/2009:

Length of	Spot
investment	<u>rate</u>
1 year	4.00%
2 years	5.00%
3 years	5.75%
4 years	6.25%

X = the present value of the payments as of 1/1/2009.

# Question 16

- (A) Less than \$3,460
- (B) \$3,460 but less than \$3,510
- (C) \$3,510 but less than \$3,560
- (D) \$3,560 but less than \$3,610
- (E) \$3,610 or more

#### Data for Question 17 (2 points)

The following assumed rates of retirement are used in the actuarial valuation of a defined benefit pension plan:

<u>Age</u>	Retirement rate at exact age
62	40%
63	25%
64	25%
65	100%

No other decrements apply from ages 62 through 65.

All active participants are currently under age 62.

X = the weighted average assumed retirement age for the pension plan.

#### Question 17

- (A) Less than 63.25
- (B) 63.25 but less than 63.45
- (C) 63.45 but less than 63.65
- (D) 63.65 but less than 63.85
- (E) 63.85 or more

#### Data for Question 18 (3 points)

Smith (age 45) purchases a single premium annuity with the following characteristics:

Single premium \$100,000

Monthly payment **Z** at the beginning of each month

Payment period For Smith's lifetime, with payments guaranteed for

the first 120 months

Interest rate 3% per year, compounded annually

Selected commutation functions:

$$\frac{x}{45}$$
 $\frac{D_x}{2,392,905}$ 
...
...
...
...
...
55 1,639,330 24,032,177

#### **Question 18**

- (A) Less than \$440.00
- (B) \$440.00 but less than \$445.00
- (C) \$445.00 but less than \$450.00
- (D) \$450.00 but less than \$455.00
- (E) \$455.00 or more

#### Data for Question 19 (2 points)

Values for a double decrement service table:

$$q_x^{(1)} = 0.015, \quad 50 \le x \le 70$$
  
 $q_x^{(2)} = 0.050, \quad 50 \le x \le 70$ 

No other decrements exist.

X = the probability that a 53-year old will still be employed by age 62.

#### Question 19

- (A) Less than 0.5465
- (B) 0.5465 but less than 0.5475
- (C) 0.5475 but less than 0.5485
- (D) 0.5485 but less than 0.5495
- (E) 0.5495 or more

# Data for Question 20 (2 points)

Terms of a 9-year annuity due:

Payments \$100 per year payable annually

Interest Applicable annual spot rates:

<u>Years</u>	Applicable spot rate
1 - 5	5.00%
6 - 9	6.00%

X = the present value of the annuity.

#### Question 20

- (A) Less than \$693
- (B) \$693 but less than \$713
- (C) \$713 but less than \$733
- (D) \$733 but less than \$753
- (E) \$753 or more

#### Data for Question 21 (4 points)

#### Terms of a loan:

Date of loan 1/1/2009
Amount of loan \$100,000
Frequency of payments Annual
First payment 12/31/2009
Term of loan 5 years

- X = the sum of payments under a level annual payment schedule, with interest rate of 6.0% per year compounded annually.
- Y = the sum of payments under the sinking fund method, where the lender receives interest annually at 6.0% per year, and a sinking fund accumulates annually at 5.0% per year.

#### Question 21

In what range is |X - Y|?

- (A) Less than \$500
- (B) \$500 but less than \$1,000
- (C) \$1,000 but less than \$1,500
- (D) \$1,500 but less than \$2,000
- (E) \$2,000 or more

#### Data for Question 22 (3 points)

Terms of an immediate annuity payable for life to a life age x on 1/1/2009:

Payment \$100,000 per year payable annually

Interest 5% per year, compounded annually

Mortality rates before improvement:

$$q_{x} = 0.051$$

$$q_{x+1} = 0.057$$

$$q_{x+2} = 0.063$$

Mortality rates are projected to improve by 1% per year, compounded annually, beginning 1/1/2010.

Z = the present value as of 1/1/2009 of the third payment.

#### Question 22

- (A) Less than \$72,570
- (B) \$72,570 but less than \$72,600
- (C) \$72,600 but less than \$72,630
- (D) \$72,630 but less than \$72,660
- (E) \$72,660 or more

#### Data for Question 23 (3 points)

Smith (age 60) and Jones (age 61) are joint annuitants entitled to a joint and 100% survivor annuity paying \$1,000 at the beginning of each year commencing 1/1/2009.

Selected commutation functions:

$\boldsymbol{\mathcal{X}}$	$D_{_{\scriptscriptstyle X}}$
60	285
61	267
• • •	•••
64	219
65	205

i = 6%, compounded annually.

X = the present value of 5<sup>th</sup> payment as of 1/1/2009.

#### Question 23

- (A) Less than \$720
- (B) \$720 but less than \$750
- (C) \$750 but less than \$780
- (D) \$780 but less than \$810
- (E) \$810 or more

#### Data for Question 24 (3 points)

The following actuarially equivalent annuities are available to Smith:

Annuity 1: Monthly payments of \$100 for life

Annuity 2: Monthly payments of \$94 for life, with monthly payments of \$47

continuing for the life of Smith's surviving spouse

Annuity 3: Monthly payments of *X* for life, with monthly payments of

75% of X continuing for the life of Smith's surviving spouse

#### Question 24

- (A) Less than \$90.52
- (B) \$90.52 but less than \$91.52
- (C) \$91.52 but less than \$92.52
- (D) \$92.52 but less than \$93.52
- (E) \$93.52 or more

#### Data for Question 25 (2 points)

Given the following values from a single decrement table:

$\mathcal{X}$	$q_x$
<del>46</del>	$0.0\overline{70}00$
47	0.06500
48	0.06000
49	0.05000

A 2-year select mortality table based on this single decrement table has the following characteristics:

$$q_{[x]} = 1.5q_x$$
  
 $q_{[x]+1} = 1.3q_{x+1}$ 

# Question 25

In what range is  $_{1|}q_{[46]+1}$ ?

- (A) Less than 0.05400
- (B) 0.05400 but less than 0.05450
- (C) 0.05450 but less than 0.05500
- (D) 0.05500 but less than 0.05550
- (E) 0.05550 or more

# Data for Question 26 (3 points)

$$\ddot{a}_{60:\overline{5}|} = 4.3393$$

$$\ddot{a}_{65:\overline{5}|} = 4.2985$$

$$\ddot{a}_{60} = 11.7952$$

$$\ddot{a}_{65} = 10.8207$$

$$\ddot{a}_{70} = 9.7262$$

# Question 26

In what range is  $_{10}E_{60}$ ?

- (A) Less than 0.4000
- (B) 0.4000 but less than 0.4500
- (C) 0.4500 but less than 0.5000
- (D) 0.5000 but less than 0.5500
- (E) 0.5500 or more

#### Data for Question 27 (2 points)

On 1/1/2009, Smith purchases a 5-year Certificate of Deposit that yields:

6% interest per year, compounded monthly for years 1 and 2

7% interest per year, compounded quarterly for year 3

8% interest per year, compounded semiannually for years 4 and 5

X = the equivalent annual rate of interest compounded annually.

#### Question 27

- (A) Less than 6.700%
- (B) 6.700% but less than 6.900%
- (C) 6.900% but less than 7.100%
- (D) 7.100% but less than 7.300%
- (E) 7.300% or more

# Data for Question 28 (2 points)

$$v^{11} = \frac{1}{2}$$

$$X = 100|i^{(4)}-d^{(4)}|$$

# Question 28

- (A) Less than 0.07
- (B) 0.07 but less than 0.14
- (C) 0.14 but less than 0.21
- (D) 0.21 but less than 0.28
- (E) 0.28 or more

#### Data for Question 29 (3 points)

Terms of a loan:

Initial amount of loan \$100,000 Term of loan 40 years

Level payments Every other year with first payment in two years

Interest rate 6% per year compounded annually

Immediately after the 10<sup>th</sup> payment, the loan is renegotiated to make level payments every 4 years, with the first such payment four years after the renegotiation. The original term of the loan remains unchanged.

I = the total interest paid over the entire term of the loan.

#### Question 29

- (A) Less than \$150,000
- (B) \$150,000 but less than \$170,000
- (C) \$170,000 but less than \$190,000
- (D) \$190,000 but less than \$210,000
- (E) \$210,000 or more

#### Data for Question 30 (3 points)

Smith is 55, Jones is 45, and Brown is 40.

The underlying mortality is the same for all three individuals.

There is a 40% probability that both Smith and Brown will be alive in 15 years.

There is a 44% probability that Jones will die before age 70.

X = the probability that Brown will die before age 45.

#### Question 30

- (A) Less than 0.250
- (B) 0.250 but less than 0.300
- (C) 0.300 but less than 0.350
- (D) 0.350 but less than 0.400
- (E) 0.400 or more

# Data for Question 31 (4 points)

$$_{t}p_{0}^{\text{(Male)}} = 1 - 0.01t, \qquad t \le 100$$
 $_{t}p_{0}^{\text{(Female)}} = (1 - 0.01t)^{2}, \quad t \le 100$ 

X = the complete joint expectation of life for a male and a female, both age 80.

# Question 31

- (A) Less than 4.5
- (B) 4.5 but less than 7.0
- (C) 7.0 but less than 9.5
- (D) 9.5 but less than 12.0
- (E) 12.0 or more

#### Data for Question 32 (2 points)

Data for members of a professional association:

Members as of $1/1/2008$	1,000
Retirements during 2008	10
Deaths during 2008	8
Suspensions during 2008	12
Non-renewals during 2008	42

Retirements occur at the beginning of each calendar year.

Deaths and suspensions occur uniformly throughout each calendar year.

Non-renewals occur at the end of each calendar year.

There are no other exits from the population.

X = the rate of suspension for 2008, given the data presented.

#### Question 32

- (A) Less than 0.012200
- (B) 0.012200 but less than 0.012400
- (C) 0.012400 but less than 0.012600
- (D) 0.012600 but less than 0.012800
- (E) 0.012800 or more

#### Data for Question 33 (2 points)

A company provides for a lump sum severance benefit equal to 6 months salary for employees under age 45 who terminate during the next year. Assume that the benefits are paid mid-year.

#### <u>Data for all employees</u>:

<u>x</u>	$q_x^{(\text{Termination})}$	Total salary
30	0.15	\$5,000,000
35	0.10	\$9,000,000
40	0.05	\$6,000,000

i = 8%, compounded annually.

X = the one-year term cost of the severance benefit as of 1/1/2009.

#### Question 33

- (A) Less than \$925,000
- (B) \$925,000 but less than \$945,000
- (C) \$945,000 but less than \$965,000
- (D) \$965,000 but less than \$985,000
- (E) \$985,000 or more

# Data for Question 34 (3 points)

Pension fund information for 2009:

<u>Date</u>	Fund Balance	<b>Contribution</b>	<b>Distribution</b>
12/31/2008	\$10,000,000	-	-
01/01/2009	-	\$500,000	-
03/31/2009	\$10,250,000	-	-
04/01/2009	-	-	\$200,000
06/30/2009	\$10,500,000	-	-
07/01/2009	-	-	\$350,000
09/30/2009	\$10,400,000	-	-
10/01/2009	-	\$800,000	-
12/31/2009	\$11,400,000	_	-

X= the dollar-weighted rate of return in 2009.

# Question 34

- (A) Less than 6.00%
- (B) 6.00% but less than 6.10%
- (C) 6.10% but less than 6.20%
- (D) 6.20% but less than 6.30%
- (E) 6.30% or more

#### Data for Question 35 (2 points)

A pension trust statement reported the following information:

Book value of assets Market value of assets	12/31/2008 \$5,000,000 X	12/31/2009 <i>Y</i> \$5,335,000
Activity during 2009:	\$<00,000	

\$600,000
\$315,000
\$250,000
\$60,000
\$465,000
(\$535,000)

# Question 35

In what range is (X - Y)?

- (A) Less than (\$900,000)
- (B) (\$900,000) but less than (\$300,000)
- (C) (\$300,000) but less than \$300,000
- (D) \$300,000 but less than \$900,000
- (E) \$900,000 or more

#### \*\*END OF EXAMINATION\*\*