DDU

Master's Thesis

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DDU

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Abstract

ABSTRACT

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Preface

This is where you thank people for helping you etc.

Aaron Ang
Delft, The Netherlands
January 20, 2018

Contents

List of Figures

Chapter 1

Introduction

Software systems are complex and error-prone, likely to expose failures to the end user. When a failure occurs, the developer has to debug the system to eliminate the failure. This debugging process can be described in three phases [10]. In the first phase, the developer has to pinpoint the fault, also known as the root cause, in code that causes the failure. In the second phase, the developer has to develop an understanding of the root cause and its context. Finally, in the third phase, the developer has to implement a patch that corrects the behavior of the system. This process is time-consuming and can account for 30% to 90% of the software development cycle [13, 3, 4].

Traditionally, developers use four different approaches to debug a software system, namely program logging, assertions, breakpoints and profiling [19]. Program logging is the act of inserting *print* statements in the code to observe program state information during execution. Assertions are constraints that can be added to a program that have to evaluate to true during execution time. Breakpoints allow the developer to pause the software system during execution, and observe and modify variable values. Profiling is used to perform runtime analysis and collect metrics on, for example, execution speed and memory usage. These techniques provide an intuitive approach to localize the root cause of a failure, but, as one might expect, are less effective in the massive size and scale of software systems today.

Therefore, in the last decades a lot of research has been performed on improving and developing *advanced* fault localization techniques [19] such that they are applicable to the software systems of today. Specifically, a prominent fault localization technique is spectrum-based fault localization (SBFL). SBFL techniques pinpoint faults in code based on execution information of a program, also known as a program spectrum [12]. The output of SBFL techniques is a list of components ranked by their fault probability, e.g. statements or methods. Intuitively, if a statement is executed primarily during failed executions, then this statement might be assigned a higher suspiciousness score. Similarly, if a statement is executed primarily during successful executions, then this statement might be assigned a lower suspiciousness score.

While SBFL techniques show promising results for debugging purposes, there are still aspects that prevent SBFL techniques from being used in practice. First, the diagnostic performance of SBFL techniques relies on the quality of the test suite. SBFL techniques cannot accurately pinpoint a fault with a single failing test that covers multiple components, e.g. methods. However, if the test suite consists of many tests with different coverage patterns, then SBFL might be able to pinpoint the fault more accurately because it can indict or exonerate components more precisely with more evidence, i.e. more execution traces. Second, in one of the pioneering user studies performed by Parnin and Orso [10], the authors show that several assumptions made by SBFL techniques do not hold in practice. For example, the authors find no evidence that the effectiveness of SBFL techniques is affected by the rank of the faulty statement.

The quality of test suites is commonly measured using an adequacy metric that focuses on error detection like statement coverage, branch coverage, method coverage. However, these metrics do not enforce a good test suite. For example, one could easily obtain a 100% test coverage with a set of tests that each covers a big part of the codebase. In this case, when a test fails due to a bug, it might be difficult for the developer to pinpoint the root cause.

To address the first problem — SBFL techniques rely on the quality of the test suite — Perez *et al.* [11] propose a new metric, called DDU, to quantify the diagnosability of a test suite. As opposed to optimizing a test suite with respect to adequacy measurements that focus on error detection, e.g. branch coverage, line coverage. However, Perez *et al.* [11] show evidence that optimizing a test suite with respect to DDU — a metric to quantify the test suite's diagnosability — improves the diagnostic performance of SBFL by 34% compared to a test suite optimized with respect to branch coverage. The goal of DDU is to capture diagnosability and to serve as a complementary metric to code coverage for developers to use to improve the test suite's diagnosability.

1.1 Problem Definition

Currently, when the DDU is computed for a given test suite, its value is in the domain $[0, 1]$, where 0 suggests that the test suite's diagnosability is low, and 1 suggests that the test suite's diagnosability is high. The problem with this value is that the developer does not know how to extend or update the test suite given a DDU value. For example, when the test suite's DDU is equal to 0.1, the developer does not know how to write tests that improve the DDU. In other words, time spent on software debugging cannot be reduced using DDU because its practical implications are unclear to the developer.

2

1.2 Goal

Although DDU is currently not usable in practice, Perez *et al.* [11] have shown that optimizing a test suite with respect to DDU can yield a 34% gain in diagnostic performance using SBFL. In addition, having a test suite with a high diagnosability could possibly reduce the time spent debugging because the fault is easier to find manually. Therefore, the goal of this thesis is to find ways to make DDU usable in practice. In other words, we explore possibilities to convey DDU to the developer such that the developer knows what kind of tests to write to improve the system's diagnosability. To be able to

1.3 Structure of Report

The structure of this report is as follows. TODO: Update once all chapters are done.

Chapter 2

Background

In this chapter, we discuss topics that are relevant to understanding this study. First, we discuss spectrum-based fault localization and spectrum-based reasoning, which is used in the experiments to perform fault diagnosis. Second, we discuss the metric used to evaluate the diagnostic performance of spectrum-based fault localization techniques. Then, we explain the definition of diagnosability and diagnosability assessment metrics.

2.1 Spectrum-Based Fault Localization (SBFL)

In spectrum-based fault localization, we define a finite set $C = \langle c_1, c_2, \ldots, c_M \rangle$ of M system components, and a finite set $T = \langle t_1, t_2, \ldots, t_N \rangle$ of N system transactions, i.e. test executions. The outcomes of all system tests are defined as an error vector $e = \langle e_1, e_2, \ldots, e_N \rangle$, where $e_i = 1$ indicates that test t_i has failed and $e_i = 0$ indicates that test t_i has passed. To keep track of which system components were executed during which test execution, we construct a $N \times M$ activity matrix $\mathcal{A}$, where $\mathcal{A}_{ij} = 1$ indicates that component c_j was exercised during test t_i. The pair $(\mathcal{A}, e)$ is also known as a program spectrum, which was first coined by Reps *et al.* citereps1997use.

Given the program spectrum, SBFL techniques compute the suspiciousness scores of system components, resulting in a diagnostic report, which is a list of components ranked by their fault probability. The fault probabiliy is often computed using a similarity coefficient [7, 1, 9, 16, 18, 21, 17]. Intuitively, the similarity coefficient indicates the similarity between the component's activity and the error vector. When a component is more frequently exercised by test executions that fail, then the component is more likely to be faulty. Conversely, when a component is more frequently exercised by test executions that pass, then the component is more likely to be healthy.

2.2 Spectrum-Based Reasoning (SBR)

Spectrum-based reasoning distinguishes itself from SBFL techniques by leveraging a reasoning framework. The diagnostic report is generated by reasoning about the program spectrum instead of using a so-called similarity coefficient. The two main phases of SBR are candidate generation and candidate ranking:

1. In the candidate generation phase, a set $\mathcal{D} = \langle d_1, d_2, \ldots, d_k \rangle$ is constructed using a minimal hitting set (MHS) algorithm to cover all failing transactions, where each candidate d_i is a subset of $\mathcal{C}$. An MHS algorithm is used to prevent generation of a possibly exponential number of diagnostic candidates [2].

2. In the candidate ranking phase, the fault probability for each candidate d_i is computed using the Naive Bayes rule [2]:

$$P(d_i | (\mathcal{A}, e)) = P(d_i) \cdot \prod_{j \in 1..N} \frac{P((\mathcal{A}_j, e_j) | d_i)}{P(\mathcal{A}_j)} \tag{2.1}$$

$P(d_i)$ is the prior probability, i.e. the probability that d_i is faulty without any evidence. $P(\mathcal{A}_j)$ is a normalizing term that is identical for all candidates. $P((\mathcal{A}_j, e_j) | d_i)$ changes the prior probability with every new observation from the program spectrum. This term can be computed using maximum likelihood estimation.

In the experiments of this study, we make use of *Barinel* [2], which implements the spectrum-based reasoning technique to perform software fault localization.

2.3 Evaluation of Diagnosis

Presently, cost of diagnosis C_d and wasted effort [2, 20, 5, 14, 11] are the most prevalent evaluation metrics for SFL techniques. In essence, C_d computes the number of components that have to be inspected before the actual fault is investigated in the diagnostic report. When $C_d = 0$, it indicates that the actual fault is ranked first in the diagnostic report and, therefore, no effort is wasted investigating diagnosed components that are non-faulty. Wasted effort (or effort) is the cost of diagnosis normalized by the number of components in the diagnostic report.

Both evaluation metrics assume *perfect bug understanding*, which has been pointed out by Parnin and Orso [10] as a non-realistic assumption. However, cost of diagnosis and effort serve as an objective evaluation metric that can be used for comparison and therefore will also be used in this study.

2.4 Diagnosability

Diagnosability is the property of faults to be easily and precisely locate [15]. In other words, given that a fault exists in a software system, if the test suite's diagnosability

is high and we would perform SFL using an automated debugging technique, then the faulty component would be ranked high in the diagnostic report, resulting in a low wasted effort. On the contrary, if the test suite's diagnosability is low and we would perform SFL using an automated debugging technique, then the faulty component would be ranked low in the diagnostic report, resulting in a high wasted effort.

2.5 Diagnosability Metric: Entropy

The optimal diagnosability is achieved by having an exhaustive test suite that would exercise any combination of software components. This way, any fault, whether it involves a single component or multiple components, can be diagnosed using an automated debugging technique with 100% accuracy. Perez *et al.* [11] find that Shannon's entropy accurately captures the test suite's exhaustiveness:

$$H(T) = -\sum_i P(t_i) \cdot \log_2(P(t_i)) \tag{2.2}$$

where T is the set of unique test activities, and $P(t_i)$ is the probability of test activity t_i occuring in the activity matrix. The optimal entropy for a system with M component is M shannons, and therefore we can compute the normalized entropy $\frac{H(T)}{M}$. SBFL techniques are able to diagnose faults with 100% accuracy when $\frac{H(T)}{M} = 1.0$.

However, an optimal normalized entropy would require $2^M - 1$ tests, which is difficult to achieve in practice. First, not all activity patterns can be generated from tests due to ambiguity groups and software topology. For example, a basic block consisting of several statements; these statements will always be activated together. Second, systems of today can consist of millions of lines of code and would therefore require a non-realistic amount of effort to write the tests.

2.6 Diagnosability Metric: DDU

To elevate the problem with entropy, Perez *et al.* [11] propose a new diagnosability metric: DDU. DDU combines three diagnosability metrics that capture characteristics of the activity matrix, namely normalized density, diversity, and uniqueness.

2.6.1 Normalized Density

Prior work [6] has used density to assess the diagnosability of the activity matrix:

$$\rho = \frac{\sum_{i,j} \mathcal{A}_{ij}}{N \cdot M} \tag{2.3}$$

Gonzàles-Sanchez *et al.* [6] show by induction that the optimal density is obtained when $\rho = 0.5$. For DDU, Perez *et al.* [11] propose a normalized density ρ' where its optimal value is 1.0 instead of 0.5:

$$\rho' = 1 - |1 - 2\rho| \tag{2.4}$$

7

	c_1	c_2	c_3	c_4
t_1	1	1	0	0
t_2	1	1	0	0
t_3	1	1	0	0
t_4	1	1	0	0

(a) No test diversity. $\rho' = 1.0$, $\mathcal{G} = 0.0$

	c_1	c_2	c_3	c_4
t_1	1	1	0	0
t_2	0	0	1	1
t_3	1	1	1	0
t_4	0	0	0	1

(b) Test diversity. $\rho' = 1.0$, $\mathcal{G} = 1.0$.

	c_1	c_2	c_3	c_4
t_1	1	1	0	0
t_2	0	0	1	1
t_3	1	1	1	0
t_4	0	0	0	1

(c) Component ambiguity. $\rho' = 1.0$, $\mathcal{G} = 1.0$, $\mathcal{U} = 0.75$

	c_1	c_2	c_3	c_4
t_1	1	1	0	0
t_2	0	1	1	0
t_3	1	0	1	1
t_4	0	0	0	1

(d) No component ambiguity. $\rho' = 1.0$, $\mathcal{G} = 1.0$, $\mathcal{U} = 1.0$

Figure 2.1: The effect of diversity and uniqueness on diagnosability.

Note that an optimal value for normalized density can be obtained without improving the diagnosability, see Figure 2.1(a). For this reason, Perez *et al.* [11] propose two enhancements: diversity and uniqueness.

2.6.2 Diversity

The first enhancement to normalized density is diversity, which ensures test diversity. Test diversity captures the diversity among test activity patterns. The test diversity is low when the test suite consists of many tests that have identical activity patterns. Conversely, the test diversity is high when the test suite consists of many tests that have distinct activity patterns.

Perez *et al.* use the Gini-Simpson index $\mathcal{G}$ [8] to capture test diversity:

$$\mathcal{G} = 1 - \frac{\sum_{i \in 1..|G|} |g_i| \cdot (|g_i| - 1)}{N \cdot (N - 1)} \tag{2.5}$$

where $G = \langle g_1, \ldots, g_k \rangle$ is the set of ambiguity groups, and N is the number of tests. As we can observe in Figure 2.1(b), when optimizing the activity matrix for test diversity, the shortcoming of normalized density, shown in Figure 2.1(a), is mitigated.

2.6.3 Uniqueness

The second enhancement to normalized density is uniqueness, which controls for the number of ambiguity groups. An ambiguity group is a set of components that have identical activation patterns across the test suite, i.e. identical columns in the activity matrix. Component ambiguity is undesirable because it prevents SBR from updating the fault probabilities of the individual components in the ambiguity group, resulting

in a less accurate diagnosis. If test suite's uniqueness is low, then many components in the activity matrix have identical activity patterns, i.e. components are involved in the same test cases. Conversely, if the test suite's uniqueness is high, then many components in the activity matrix have distinct activity patterns.

Given the set of component ambiguity groups $H = \langle h_1, \ldots, h_l \rangle$, then the test suite's uniqueness is computed as follows:

$$\mathcal{U} = \frac{|H|}{M} \tag{2.6}$$

We observe in Figure 2.1(c) that optimizing the test suite with respect to normalized density and diversity can still result in component ambiguity groups, namely $\langle c_1, c_2 \rangle$. When optimizing the test suite with respect to normalized density, diversity and uniqueness, we observe in Figure 2.1(d) that there are no identical test activity patterns and no ambiguity groups, which results in a better diagnosability.

2.6.4 Combined

The DDU combines normalized density, diversity, and uniqueness as follows:

$$DDU = normalized\ density \cdot diversity \cdot uniqueness \tag{2.7}$$

If $DDU = 1$, then the test suite's diagnosability is high. Vice versa, if $DDU = 0$, then the test suite's diagnosability is low. Perez *et al.* [11] have shown in an experiment that optimizing a test suite with respect to DDU yields a 34% diagnostic performance compared to a test suite optimized for branch coverage.

Chapter 3

Research Questions

Ideally, we would like to propose an intuitive approach that allows developers to use DDU in their software development cycle. However, to the best of our knowledge, there has been no study yet on DDU that investigates how it actually behaves in practice. For this reason, the goal of this study is to explore how DDU behaves in practice and to potentially improve DDU. To achieve this goal, we define four research questions.

> **RQ1:** How do normalized density, diversity, uniqueness, and DDU vary in practice?

To be able to propose an intuitive approach that allows developers to use DDU in practie, we first need to understand how the metrics vary in practice. By analyzing how these metrics perform in practice, we are able to propose improvements for DDU, and potentially propose an approach that enables DDU in practice.

> **RQ2:** What is the relation between normalized density, diversity, uniqueness, and DDU and diagnosability?

In Perez *et al.*'s work [11], the authors show that generating tests with respect to DDU yields a 34% diagnostic performance compared to a test suite optimized for branch coverage. However, this does necessarily imply that DDU is strongly correlated with diagnosability. Therefore, we would like to validate that DDU and diagnosability are strongly correlated, i.e. the higher DDU, the better the diagnosability, and vice versa. This question is important to answer because DDU was proposed as a metric to quantify the diagnosability.

> **RQ3:** What is the relation between density, diversity, uniqueness, and DDU and test coverage?

The intention of test coverage is to optimize for error detection. Perez *et al.* [11] propose DDU as a complementary metric to test coverage because DDU is meant to capture the diagnosability and not error detection. However, if there is a strong correlation between DDU and test coverage, then DDU could possibly replace test coverage as a test adequacy metric, which is a use case that the authors have not thought of. Furthermore, assuming that DDU is strongly correlated with diagnosability and test coverage is representative for error detection, answering this research question will give us a better understanding on the relation between diagnosability and error detection, and could give us insight in how DDU and test coverage can be used together in practice.

> **RQ4:** How can we improve the correlation between DDU and diagnosability?

Ultimately, we would like to decrease time spent on debugging, if not fully automate it, during the development cycle. We believe that writing a test suite with a high diagnosability can improve the debugging process because faults are easier to diagnose whether diagnosis is performed manually or automatically. Therefore, it is important to improve DDU's performance such that it strongly correlates with diagnosability.

Chapter 4

DDU in Practice

> **RQ1:** How do normalized density, diversity, uniqueness, and DDU vary in practice?

In this chapter, the goal is to obtain a better intuition on what common values are for density, diversity, uniquness, and DDU by analyzing open source projects hosted on GitHub. First, we take a look at the distributions of normalized density, diversity, uniqueness, and DDU. Second, we give examples of classes that have a low or high value for any of the diagnosability metrics and analyze why these components have either a low or high value by investigating the class' test suite. Finally, we conclude this chapter with a list of observations.

4.1 Approach

To get a better understanding of how the values vary for normalized density, diversity, uniqueness, and DDU, we use `ddu-maven-plugin`[1], developed by Perez, to instrument Java code and construct the activity matrix. Once we obtain the activity matrices, we analyze the data using multiple Python scripts[2]. With these two tools we collect data such as density, normalized density, diversity, uniqueness, DDU, and the activity matrix.

Then, we analyze the collected data and show examples to illustrate how DDU and its individual terms vary as a consequence to particular kinds of tests or testing strategies. We are interested in what kinds of testing approaches result in a high or low value.

Note that `ddu-maven-plugin` is able to instrument the code for three different granularity levels, namely statements, branches, and methods. By default `ddu-maven-plugin` uses the method level granularity. In this study, we make use of the same

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[1] https://github.com/aperez/ddu-maven-plugin
[2] https://github.com/aaronang/ddu

granularity used in the study performed by Perez *et al.* [11], namely branch granularity.

4.2 Selection

The selection of open source projects is done according to the following criteria.

- *The project must have an executable test suite.* To compute the DDU for a software project, we must construct an activity matrix. The program spectra is constructed by running the test suite and instrumenting the code such that we can keep track of what components are executed during a program execution.

- *The project must use Apache Maven, a software project management and comprehension tool.* The current tool that instruments the code to construct the activity matrix is implemented as a Maven plugin. Note that the current Maven plugin does not work for all Maven projects, and therefore only projects, that can be analyzed with this plugin, are used.

Based on these requirements, we choose the following open source projects. Note that some of the projects are also used in Perez *et al.*'s study [11].

- Commons Codec[3]: a package that contains simple encoders and decoders for various formats such as Base64 and Hexadecimal.
- Commons Compress[4]: an API for working with compression and archive formats.
- Commons Math[5]: a library of lightweight, self-contained mathematics and statistics components addressing the most common practical problems.
- Guice[6]: a lightweight dependency injection framework for Java 6 and above.
- Jsoup[7]: an API for extracting and manipulating data, using the best of DOM, CSS, and jquery-like methods.

4.3 Normalized Density

In Figure 4.1, we show the distribution of normalized densities for all classes of the five open source projects mentioned before. The average equals to 0.5145. The peak for the interval [0, 0.1] is primarily caused by classes that are exercised by tests that involve all components. In the interval [0, 0.1], 43 classes consist of only one branch. A class with one branch will always have a density of 1.0 and therefore a normalized density of 0.

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[3]https://github.com/apache/commons-codec
[4]https://github.com/apache/commons-compress
[5]https://github.com/apache/commons-math
[6]https://github.com/google/guice
[7]https://github.com/jhy/jsoup
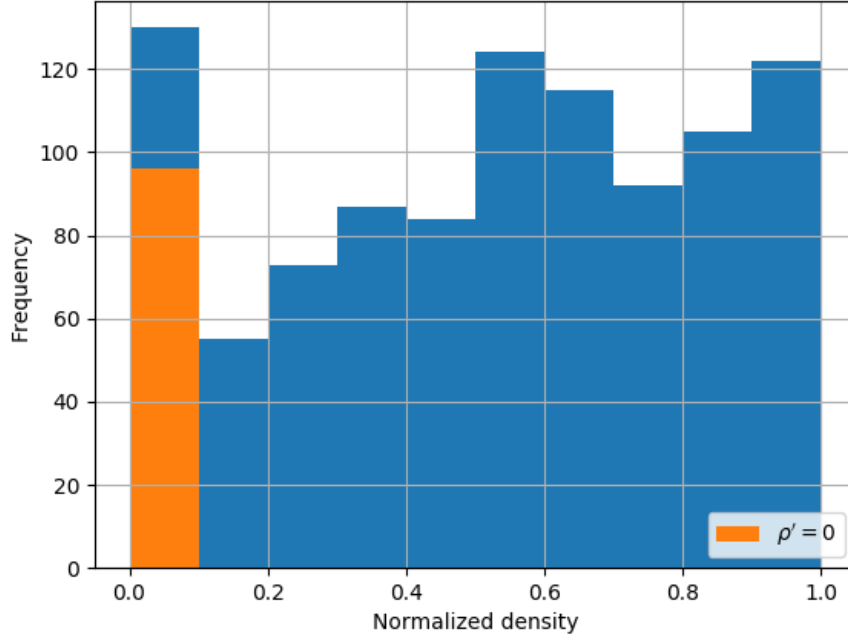
Figure 4.1: Normalized density distribution.

Table 4.1: Partial activity matrix of the
`com.google.inject.internal.ProvidesMethodScanner` class.

transaction	c_1	...	c_{22}	c_{23}	c_{24}	...	c_{35}
`BinderTest#testUntargettedBinding`	0	...	0	1	0	...	0
`BinderTest#testMissingDependency`	0	...	0	1	0	...	0
`BinderTest#testProviderFromBinder`	0	...	0	1	0	...	0
`BinderTest#testToStringOnBinderApi`	0	...	0	1	0	...	0
`BinderTest#testUserReportedError`	0	...	0	1	0	...	0
⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮

The normalized density value is low when a class is tested by many tests that only cover a couple of branches, or covered by tests that involve all components. For example, `com.google.inject.internal.ProvidesMethodScanner` has 35 branches and its partial activity matrix is shown in Table 4.1. All the transactions that cover `ProvidesMethodScanner` are sparse, i.e. a row consisting of many zeroes.

In the partial activity matrix of `ProvidesMethodScanner`, see Table 4.1, the columns represent branches of `ProvidesMethodScanner`. For example, in the first row, we observe that the transaction `testUntargettedBinding` only hits one branch c_{23}, indicated by a 1. Since every transaction is only hitting a few components, the normalized density is low. In fact, `ProvidesMethodScanner` has 35 components and if a transaction only hits a few components, it results in the activity matrix to

Table 4.2: Activity matrix of the
`org.apache.commons.math4.fitting.leastsquares.CircleProblem` class.
Every transaction hits every component.

transaction	c_1	c_2	...	c_{26}
LevenbergMarquardtOptimizerTest#testParameterValidator	1	1	...	1
LevenbergMarquardtOptimizerTest#testCircleFitting2	1	1	...	1

Table 4.3: Activity matrix of
`org.apache.commons.math4.genetics.ElitisticListPopulation`.

transaction	c_1	c_2	c_3	c_4	c_5	c_6	c_7	c_8
ElitisticListPopulationTest#testChromosomeListConstructorTooLow	1	0	0	1	0	0	0	0
ElitisticListPopulationTest#testSetElitismRateTooLow	1	0	0	1	0	0	1	0
ElitisticListPopulationTest#testConstructorTooHigh	1	0	0	1	0	0	0	0
ElitisticListPopulationTest#testConstructorTooLow	1	0	0	1	0	0	0	0
ElitisticListPopulationTest#testSetElitismRateTooHigh	1	0	0	1	0	0	1	0
ElitisticListPopulationTest#testChromosomeListConstructorTooHigh	1	0	0	1	0	0	0	0
ElitisticListPopulationTest#testSetElitismRate	1	0	0	0	0	1	1	0
ElitisticListPopulationTest#testNextGeneration	1	1	1	0	1	1	1	1
FitnessCachingTest#testFitnessCaching	1	1	1	0	1	1	1	1
GeneticAlgorithmTestBinary#test	1	1	1	0	1	1	1	1
GeneticAlgorithmTestPermutations#test	1	1	1	0	1	1	1	1
TournamentSelectionTest#testSelect	1	0	0	0	0	0	1	0

become sparse.

In the activity matrix of `CircleProblem`, shown in Table 4.2, we observe a high density; all branches of `CircleProblem` are hit in every single test. The normalized density is low: 0.0, because the density is high: 1.0.

Thus, ideally, to obtain a high value for the normalized density, we need a good balance between tests that cover many components and tests that cover a few. In Commons Math, the `ElitisticListPopulation` class has a normalized density of 0.979. In its activity matrix, see Table 4.3, we observe that there is a good balance between tests that cover a few components and tests that cover many components. This results in a density close to 0.5 and a nearly optimal normalized density of 1.0.

4.4 Diversity

In Figure 4.2, the distribution of diversity of classes is shown. The average is 0.588. The peak for the interval [0, 0.1] occurs for various reasons. The first reason is that there are classes with only one method and therefore every row is identical, resulting in a diversity of 0. The second reason is that for some classes there exist only one test, and in the current Python script the diversity defaults to 0 when there is only one test. The third reason is that there are test suites where all the test cases have identical activity patterns.

Intuitively, the diversity has a low value when the number of identical transactions is high, i.e. identical rows in the activity matrix. Conversely, the diversity is high when the number of identical transactions is low.
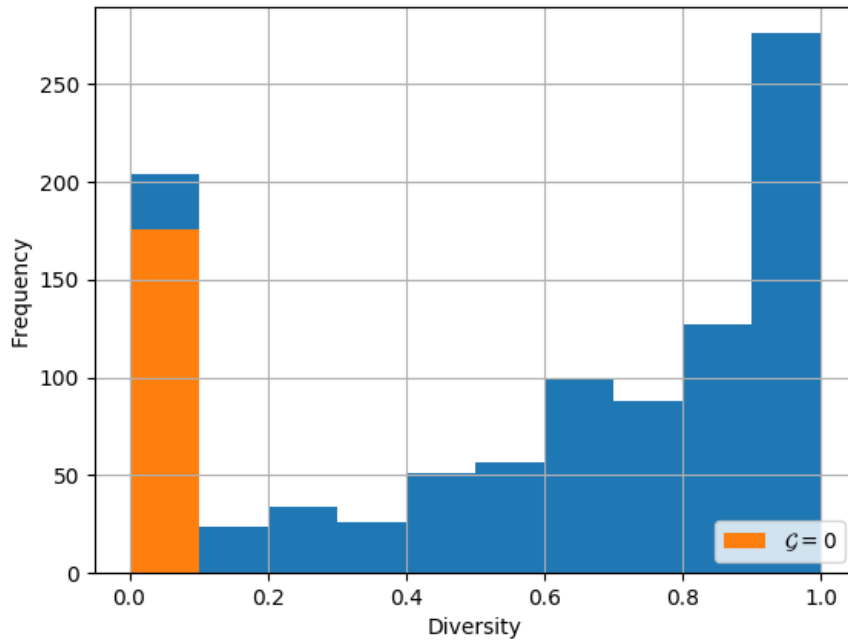
Figure 4.2: Diversity distribution.

Table 4.4: Partial activity matrix of
`org.apache.commons.math4.analysis.function.Power`.

transaction	c_1	c_2	c_3
`FunctionUtilsTest#testFixingArguments`	1	1	0
`FunctionUtilsTest#testMultiplyDifferentiable`	1	0	1
`FunctionUtilsTest#testComposeDifferentiable`	1	1	1
`FunctionUtilsTest#testCompose`	1	1	0
`FunctionUtilsTest#testMultiply`	1	1	0
`ArrayRealVectorTest#testMap`	1	1	0
`ArrayRealVectorTest#testMapToSelf`	1	1	0
`RealVectorTest#testMap`	1	1	0
$\vdots$	$\vdots$	$\vdots$	$\vdots$

Table 4.5: Activity matrix of
`org.apache.commons.math4.ode.AbstractParameterizable`.

	c_1	c_2	c_3	c_4	c_5	c_6	c_7	c_8
JacobianMatricesTest#testHighAccuracyExternalDifferentiation	1	0	1	0	1	0	1	0
JacobianMatricesTest#testAnalyticalDifferentiation	1	0	1	0	1	0	1	0
JacobianMatricesTest#testInternalDifferentiation	0	0	0	0	1	0	1	0
JacobianMatricesTest#testParameterizable	1	0	0	0	1	0	1	1
JacobianMatricesTest#testWrongParameterName	0	0	1	1	1	1	0	1
JacobianMatricesTest#testFinalResult	1	0	1	0	1	0	1	1

In the partial activity matrix of `Power`, shown in Table 4.4, we observe that almost every transaction has an identical activity and therefore the diversity is low: 0.077. Another reason for the low diversity of `Power` is that it is covered by 102 test cases, while there are only $2^3 - 1 = 7$ possible different tests for two components. After 7 unique tests every additional test will have a negative effect on the diversity because it will share an identical activity with an existing test.

In the activity matrix of `AbstractParameterizable`, shown in Table 4.5, we observe that almost every transaction has a unique activity and therefore its diversity is high: 0.933. Note that the diversity suffers when there are too many test cases, but does not suffer from a low number of test cases.

An interesting case for diversity is parameterized testing. Although parameterized testing is a common practice to test different inputs for a unit, it has a negative effect on the diversity due to identical activity patterns.

4.5 Uniqueness

The distribution of uniqueness of classes is shown in Figure 4.3. The average is 0.477. The peak for the interval [0.9, 1.0] is partially caused by classes that only have one component; activity matrices that consist of one component always have a uniqueness of 1.0. There are 130 classes that have a uniqueness of 1.0 and 43 out of the 130 classes only have one branch.

The uniqueness of a class is high when there is a high number of unique columns in the activity matrix. Conversely, the uniqueness is low when there is a low number of unique columns in the activity matrix.

An example of a class with a high uniqueness is the `Crypt` class of Commons Codec, see Table 4.6. The `Crypt` class has a uniqueness of 0.916 because it only has one ambiguity group $\langle c_8, c_{10} \rangle$.

In the activity matrix of `UnitSphereRandomVectorGenerator`, see Table 4.7, we observe that all components have identical activity patterns and, therefore, the uniqueness is low: 0.142. Note that the uniqueness does not equal zero although there is no component with a unique activity.

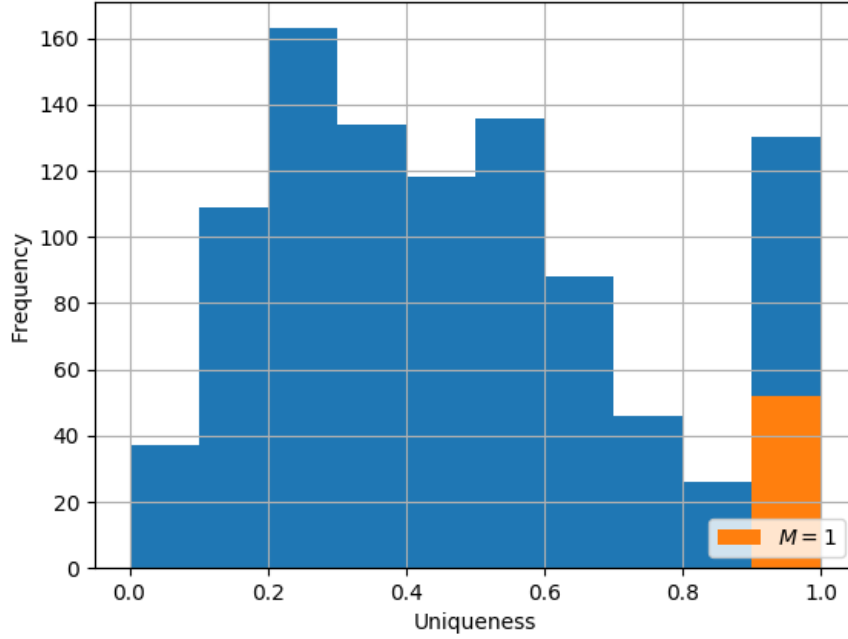Figure 4.3: Distribution of uniqueness.

Table 4.6: Activity matrix of `org.apache.commons.codec.digest.Crypt`.

	c_1	c_2	c_3	c_4	c_5	c_6	c_7	c_8	c_9	c_{10}	c_{11}	c_{12}
CryptTest#testDefaultCryptVariant	0	0	0	1	1	0	0	1	0	1	0	0
CryptTest#testCryptWithEmptySalt	1	1	0	0	0	0	1	1	0	1	1	0
CryptTest#testCryptWithBytes	0	1	1	1	0	1	0	1	0	1	0	0
Md5CryptTest#testMd5CryptBytes	0	1	0	0	0	0	1	1	1	1	1	0
Md5CryptTest#testMd5CryptLongInput	0	1	0	0	0	0	1	1	1	1	1	0
Md5CryptTest#testMd5CryptStrings	0	1	0	0	0	0	1	1	1	1	1	0
Sha256CryptTest#testSha256CryptBytes	0	1	0	0	0	0	0	1	0	1	1	1
Sha256CryptTest#testSha256CryptStrings	0	1	0	0	0	0	0	1	0	1	1	1
Sha512CryptTest#testSha512CryptBytes	0	1	1	0	0	0	0	1	0	1	0	0
Sha512CryptTest#testSha512CryptStrings	0	1	1	0	0	0	0	1	0	1	0	0
UnixCryptTest#testUnixCryptStrings	1	1	0	0	0	0	1	1	0	1	1	0
UnixCryptTest#testUnixCryptBytes	1	1	0	0	0	0	1	1	0	1	1	0

Table 4.7: Partial activity matrix of
`org.apache.commons.math4.random.UnitSphereRandomVectorGenerator`.

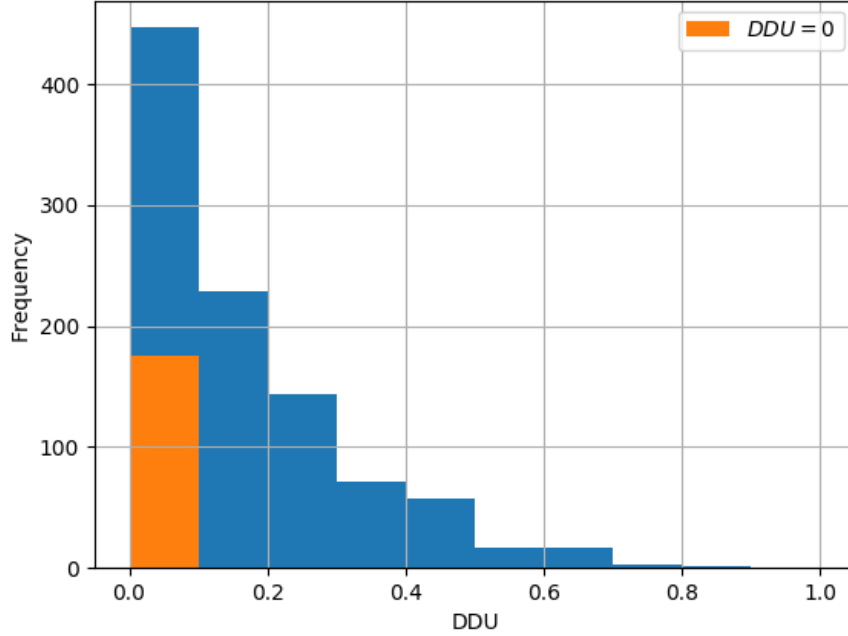|	c_1	c_2	c_3	c_4	c_5	c_6	c_7
MicrosphereProjectionInterpolatorTest#testLinearFunction2D	1	1	1	1	1	1	1
FieldRotationDfpTest#testDoubleVectors	1	1	1	1	1	1	1
FieldRotationDfpTest#testDoubleRotations	1	1	1	1	1	1	1
FieldRotationDSTest#testDoubleVectors	1	1	1	1	1	1	1
FieldRotationDSTest#testDoubleRotations	1	1	1	1	1	1	1
SphereGeneratorTest#testRandom	1	1	1	1	1	1	1
⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮

Figure 4.4: DDU distribution.

Table 4.8: Activity matrix of
`org.apache.commons.math4.analysis.function.Min`, $\rho' = 1.0$, $\mathcal{G} = 0.809$,
and $\mathcal{U} = 1.0$.

transaction	c_1	c_2	c_3	c_4
UnivariateDifferentiableFunctionTest#testMinus	1	0	1	1
FunctionUtilsTest#testCollector	0	1	0	0
FunctionUtilsTest#testAdd	1	0	1	0
FunctionUtilsTest#testComposeDifferentiable	0	0	1	1
FunctionUtilsTest#testCombine	1	0	1	0
FunctionUtilsTest#testCompose	1	0	1	0
FunctionUtilsTest#testAddDifferentiable	0	0	1	1

4.6 DDU

The distribution of DDU of classes is shown in Figure 4.4. The average is 0.157. We observe that 176 classes have a DDU of zero due to either normalized density, diversity, or uniqueness being equal to zero.

In Table 4.8, we observe a class with a high DDU: 0.809. Its DDU is high because it has an optimal normalized density, uniqueness, and an almost optimal diversity.

In Table 4.9, we observe a class with a low DDU: 0.082. Eventhough the normalized density and uniqueness are above average, the DDU is low due to the low diversity.

Table 4.9: Partial activity matrix of `org.jsoup.parser.ParseSettings`, $\rho' = 0.727$, $\mathcal{G} = 0.204$, and $\mathcal{U} = 0.555$.

transaction	c_1	c_2	c_3	c_4	c_5	c_6	c_7	c_8	c_9
`ParseTest#testBaidu`	0	1	1	0	0	1	1	1	1
`AttributesTest#html`	0	0	1	0	0	0	1	1	0
`HtmlParserTest#canPreserveAttributeCase`	0	1	1	0	0	0	1	1	1
`HtmlParserTest#handlesBaseTags`	0	1	1	0	0	1	1	1	1
`SelectorTest#descendant`	0	1	1	0	0	1	1	1	1
$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$	$\vdots$

4.7 Observations

In this section, we summarize our findings with regards to normalized density, diversity, uniqueness, and DDU.

The optimal normalized density is 1.0 and the optimal density is 0.5 for a test suite. It is difficult to utilize normalized density to recommend the developer what kind of test to write — a test that covers a few components or a test that covers many components. For example, if $\rho' = 0.6$, then the density can either be $\rho = 0.3$ or $\rho = 0.7$. Therefore, the density can be used to guide the developer in writing tests. For example, when the test suite's density is less than 0.5, it is recommended to write tests that cover many components. Conversely, when the test suite's density is greater than 0.5, it is recommended to write tests that cover a few components.

In practice, we write tests to account for many corner cases. From the diagnostic perspective, adding tests, that do not improve the information gain, is useless. For example, the diversity can be negatively impacted when we write parameterized tests due to inputs causing the same activation patterns. Another example is property-based testing, where the outputs are checked against a so-called *property* that should hold true given arbitrary inputs that meet certain criteria. Therefore, we pose the question whether we need a metric that penalizes tests that have identical component coverage.

We observe in Figure 4.4, that the DDU distribution is right-tailed. This can be explained by the fact that the DDU is the product of normalized density, diversity, and uniqueness, which all operate in the domain [0, 1]. Even when a test suite has a high normalized density and diversity but a low uniqueness, then the value for DDU can only be as high as the uniqueness. In other words, the DDU can only be as high as the component with the lowest value.

Revisiting the first research question:

> **RQ1:** How do normalized density, diversity, uniqueness, and DDU vary in practice?

A: We observed that the average for normalized density, diversity, and uniqueness are 0.5145, 0.588, 0.477, respectively. However, the values for DDU have an average

of 0.157. In addition, the distribution of DDU is right-tailed which could be explained by the fact that DDU can only be as high as the lowest component — normalized density, diversity, or uniqueness.

Chapter 5

DDU vs. Diagnosability

> **RQ2:** What is the relation between density, diversity, uniqueness, and DDU and diagnosability?

In prior work Perez *et al.* [11] show that optimizing test suite generation with respect to DDU results in better fault diagnosis. Optimizing test suite generation with respect to DDU yields a 34% diagnostic performance compared to a test suite optimized for branch coverage. Therefore, in this chapter, we perform experiments to verify the correlation between DDU and diagnosability.

5.1 Experimental Setup

To verify the correlation between DDU and diagnosability, we generate 10 artificial multiple components faults of cardinality 2 for each class that has at least 8 components, i.e. branches. For each generated fault set, we construct an activity matrix. We determine for each test that exercises the faulty components whether it is failing according to an *oracle quality probability* of 0.75, which was also used in prior work [11]. Then, for each generated activity matrix, we use *STACCATO* to generate fault candidates and *BARINEL* to generate a diagnosis report. Based on the diagnosis report we compute the wasted effort which is a measurement for diagnosability. To account for randomness of generating fault sets, we repeat this process 10 times. Note that we do not generate single component faults because in this case the optimal matrix for diagnosability is a diagonal activity matrix, i.e. each component each tested individually by a unit test. Additionally, *STACCATO* can sometimes take hours or days to generate fault candidates. Hence, we discard classes when generating fault candidates takes longer than 10 seconds; this resulted in 16 classes being discarded.

In the construction of the activity matrix we use the branch granularity, that is, every component of the activity matrix represents a method branch; this granularity is also used by Perez *et al.* [11]. To construct the activity matrix of a class we
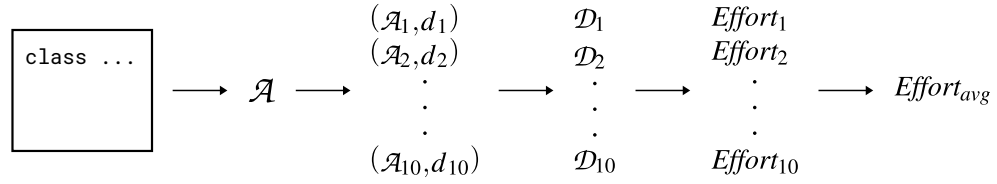
$$\boxed{\texttt{class ...}} \longrightarrow \mathcal{A} \longrightarrow \begin{matrix} (\mathcal{A}_1, d_1) \\ (\mathcal{A}_2, d_2) \\ \vdots \\ (\mathcal{A}_{10}, d_{10}) \end{matrix} \longrightarrow \begin{matrix} \mathcal{D}_1 \\ \mathcal{D}_2 \\ \vdots \\ \mathcal{D}_{10} \end{matrix} \longrightarrow \begin{matrix} \mathit{Effort}_1 \\ \mathit{Effort}_2 \\ \vdots \\ \mathit{Effort}_{10} \end{matrix} \longrightarrow \mathit{Effort}_{avg}$$

Figure 5.1: An activity matrix $\mathcal{A}$ is generated for a particular class. Then, 10 fault candidates of cardinality 2 are generated with a corresponding activity matrix $\mathcal{A}_k$. For each generated matrix, we perform fault diagnosis with *BARINEL* resulting in diagnostic report $\mathcal{D}_k$ and compute the wasted effort. Finally, we compute the average wasted effort. This process is repeated 10 times.

$$\begin{matrix} (\mathcal{A}_1, d_1) \\ (\mathcal{A}_2, d_2) \\ \vdots \\ (\mathcal{A}_{10}, d_{10}) \end{matrix} \quad \begin{matrix} \mathcal{D}_1 \\ \mathcal{D}_2 \\ \vdots \\ \mathcal{D}_{10} \end{matrix} \quad \begin{matrix} \mathit{Effort}_1 \\ \mathit{Effort}_2 \\ \vdots \\ \mathit{Effort}_{10} \end{matrix}$$
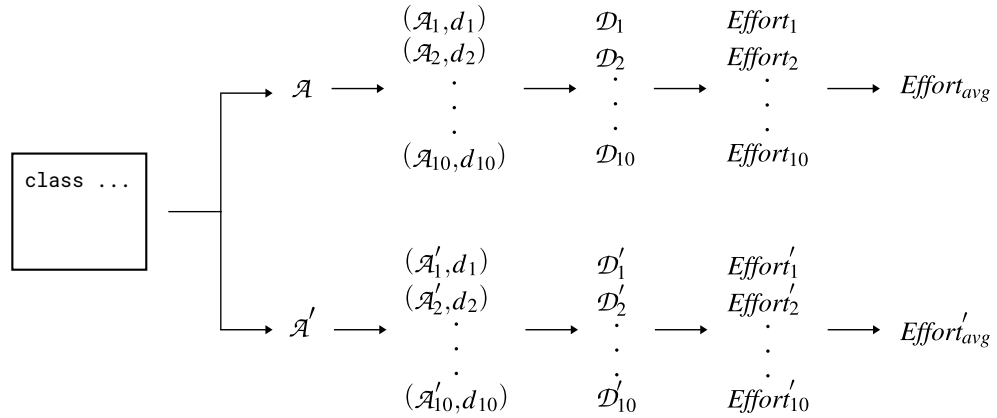
Figure 5.2: Two activity matrices $\mathcal{A}$ and $\mathcal{A}'$ are generated for a particular class based on two different test suites. We generate 10 fault candidates of cardinality 2 and accordingly generate 10 activity matrices. Then, we use *BARINEL* to perform fault diagnosis and compute the wasted effort.

use Perez' DDU Maven plugin[1] using the `basicblock` granularity, which represents branch granularity. The steps after the obtaining the activity matrix in Figure 5.1 are performed using Python scripts[2].

This experiment is different from Perez *et al.*'s work because we do not improve the DDU of a fixed system. Specifically, in Perez *et al.*'s study, the authors improved the DDU of a fixed system under test by generating new test cases using *EvoSuite*. However, in this experiment, we compute the DDU for each class and measure for each class its diagnosability using the aforementioned approach. Essentially, the difference is that we do not improve the DDU of a fixed system but we are simply measuring the DDU.

For this reason, we perform another experiment where we generate two test suites for each class with at least 8 components and at least 10 unit tests. In addition, we

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[1] https://github.com/aperez/ddu-maven-plugin
[2] https://github.com/aaronang/ddu

(a) Normalized density, $r = 0.183$, $p < 0.001$.

(b) Diversity, $r = -0.326$, $p < 0.001$.

(c) Uniqueness, $r = -0.120$, $p < 0.001$.

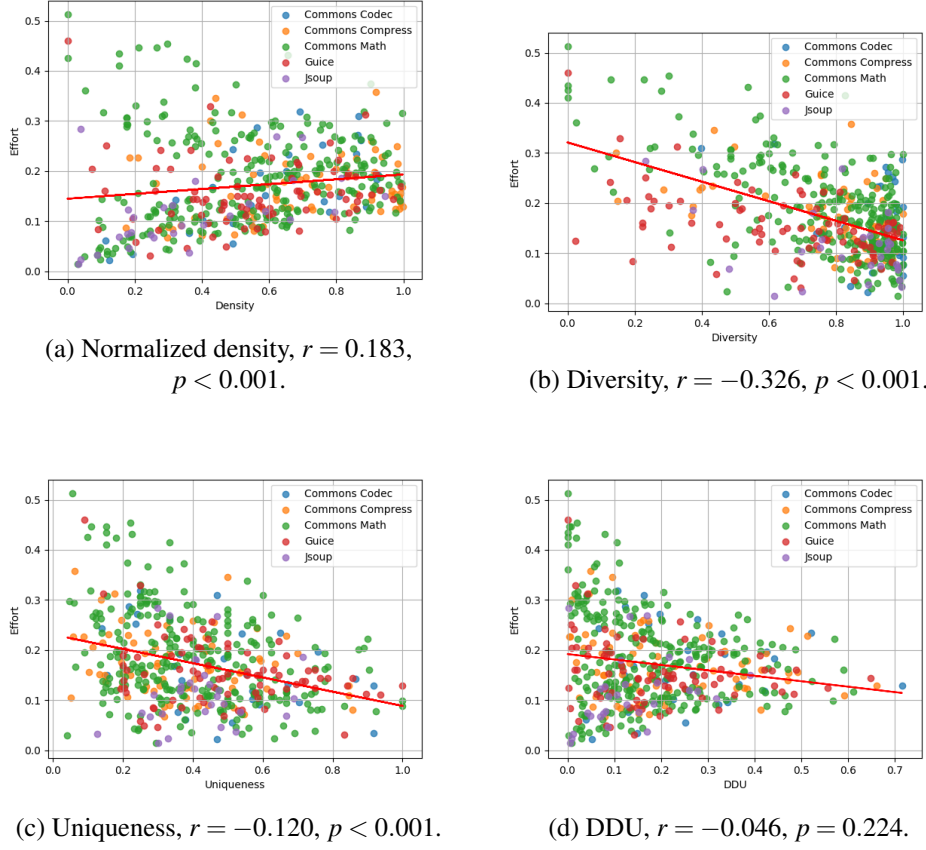(d) DDU, $r = -0.046$, $p = 0.224$.

Figure 5.3: Scatterplot of density, diversity, uniqueness, and DDU against effort.

perform the same experiment but for all classes with at least 8 components. We generate two test suites by using all test cases and 50% of the test cases. For both test suites we compute the DDU and randomly generate 10 multiple components faults of cardinality 2 to compute the wasted effort. Similar to previous experiment we perform this process 10 times to account for randomness of generating fault sets. The intuition behind this experiment is when we improve the DDU of a fixed system, its diagnosability should improve too. The setup of this experiment is illustrated in Figure 5.2.

5.2 Experimental Results

In the first experiment, we measure for each class the density, diversity, uniqueness, DDU, and diagnosability. The results of this experiment are shown in Figure 5.3. Note that in Figure 5.3 the population comprises all classes of all projects. Each datapoint in Figure 5.3 represents a class for which 100 fault candidates are generated

Table 5.1: Correlation between density, diversity, uniqueness, DDU, and effort.

Subject	Size	Pearson correlation / Correlation p-value			
		Density	Diversity	Uniqueness	DDU
Commons Codec	34	0.63 $\mathbf{5.880 \times 10^{-5}}$	-0.33 0.057	-0.65 $\mathbf{3.713 \times 10^{-5}}$	-0.23 0.197
Commons Compress	104	-0.22 $\mathbf{0.027}$	-0.45 $\mathbf{1.348 \times 10^{-6}}$	-0.40 $\mathbf{2.083 \times 10^{-5}}$	-0.37 $\mathbf{1.121 \times 10^{-4}}$
Commons Math	420	0.20 $\mathbf{4.982 \times 10^{-5}}$	-0.36 $\mathbf{1.782 \times 10^{-14}}$	-0.19 $\mathbf{7.553 \times 10^{-5}}$	-0.03 0.572
Guice	94	0.01 0.935	-0.31 $\mathbf{0.002}$	-0.29 $\mathbf{0.005}$	-0.22 $\mathbf{0.031}$
Jsoup	37	0.29 0.085	-0.37 $\mathbf{0.024}$	0.16 0.337	0.20 0.229

in (potentially overlapping) sets of 10 fault candidates as described in Figure 5.1. We observe the that there is a positive correlation between density and effort, a negative correlation between diversity and effort, a negative correlation between uniqueness and effort, and a statistically non-significant weak correlation between DDU and effort.

To investigate the relations between these metrics in more detail, we display the correlation values per project in Table 5.1. For three projects we can say with 95% confidence that density is correlated with effort. However, the Pearson correlation for Commons Compress is negative while the Pearson correlation values for Commons Math and Commons Codec are positive. Hence, the results show no strong evidence that density is correlated with effort. Regarding diversity and uniqueness, we observe in Table 5.1 and Figure 5.3 that both metrics have a weak negative correlation with effort, and that the correlation values in 4 out of 5 projects are statistically significant. Regarding DDU, for two projects the results show statistical significance that DDU is negatively correlated to effort. However, for three projects there is no evidence that DDU is correlated to effort. Therefore, there is no strong evidence that DDU is negatively correlated to effort.

In the second experiment, we generate two test suites for a given class: a test suite with 50% of the test cases enabled, and a test suite with 100% of the test cases enabled. This naturally results in two test suites with two different DDU values. For each class, we compare the effort of a test suite with a lower DDU value with a test suite with a higher DDU value. Identical approach is used for density, diversity, and uniqueness. Note that we exclude classes where the two test suites do not result in a metric difference. The results of this experiment are shown in Figure 5.4 and Table 5.2. In Figure 5.4, we observe that an increase in any metric — density, diversity, uniqueness, DDU — results in a lower required effort to diagnose mistakes. Although the results are statistically significant, see Figure 5.4, the correlations are weak.
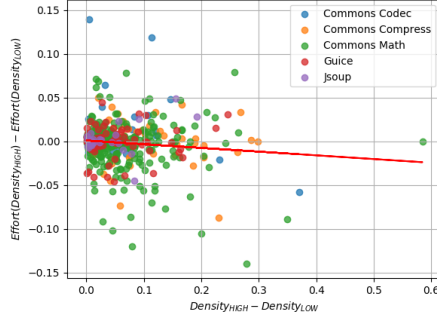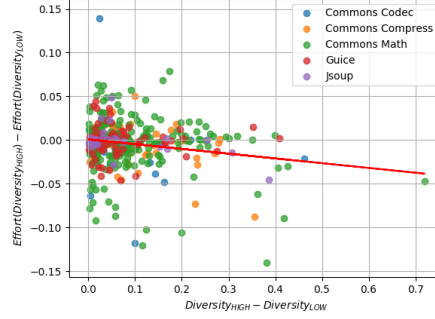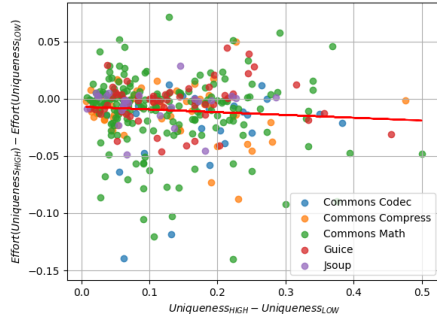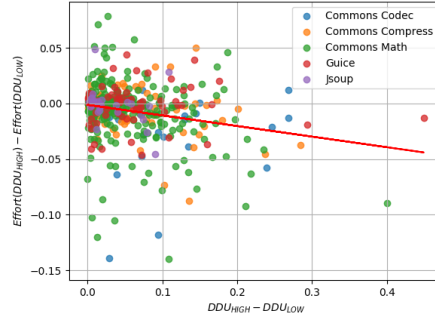
(a) Density, $r = -0.107$, $p < 0.01$.   (b) Diversity, $r = -0.189$, $p = 4.479 \times 10^{-5}$.

(c) Uniqueness, $r = -0.079$, $p = 0.137$.   (d) DDU, $r = -0.223$, $p = 9.044 \times 10^{-7}$.

Figure 5.4: Scatterplot of delta density, delta diversity, delta uniqueness, and delta DDU against delta effort.

Revisiting the second research question:

RQ2: What is the relation between density, diversity, uniqueness, and DDU and diagnosability?

A: In the first experiment, two out of the five projects show that DDU is negatively correlated with diagnosability. In the second experiment, two out of the five projects show that improving the DDU value of a class' test suite will improve the diagnosability. Therefore, based on these two experiments, there is no evidence that DDU is strongly correlated to diagnosability. However, in the second experiment, we observe that an increase in DDU is weakly correlated to an decrease in effort and, thus, weakly correlated to diagnosability. There is also no strong evidence that density, diversity, and uniqueness are correlated to diagnosability.

Table 5.2: Correlation between delta density, delta diversity, delta uniqueness, delta DDU, and delta effort.

| Subject | Size / Pearson correlation / Correlation p-value | | | |
	Density	Diversity	Uniqueness	DDU
Commons Codec	29 -0.277 0.145	24 -0.229 0.281	26 0.230 0.256	29 0.011 0.950
Commons Compress	74 -0.098 0.401	73 -0.372 **0.001**	55 -0.217 0.111	74 -0.297 **0.010**
Commons Math	251 -0.142 **0.023**	256 -0.162 **0.009**	186 -0.109 0.135	262 -0.280 $\mathbf{3.855 \times 10^{-6}}$
Guice	78 0.103 0.368	78 0.001 0.995	57 0.047 0.728	78 -0.006 0.952
Jsoup	29 0.452 **0.013**	29 -0.465 **0.011**	27 0.012 0.951	29 -0.273 0.150

Chapter 6

DDU vs. Test Coverage

RQ3: What is the relation between density, diversity, uniqueness, and DDU and test coverage?

In this chapter, we investigate the relation between DDU and test coverage. The reason for researching the relation between DDU and test coverage is to investigate whether DDU should be used as a complementary metric to test coverage as Perez *et al.* proposed. If there is a strong correlation between DDU and test coverage, then it means that DDU might function as an error detection metric too. Furthermore, investigating the relation between DDU and test coverage might give us insight in how DDU and test coverage could work together in practice.

To answer the research question we will perform several experiments. First, we would like to confirm that test coverage is strongly correlated with error detection since test coverage presumably optimizes the test suite for error detection. Second, we would like to investigate the relation between DDU and test coverage. Third, we would like to examine the relation between DDU and error detection.

6.1 Experimental Setup

We have to measure the test coverage and error detection to analyze the relation between test coverage and error detection. Test coverage can be determined by dividing the number of components hit in the activity matrix by the total number of components in the activity matrix. Given the acitity matrix in Table 6.1, we observe that 3 out of the 4 components are hit and therefore the test coverage is $\frac{3}{4} = 0.75$. The error detection is computed by generating 10 artificial faults — in the experiments we generate multiple components faults with a cardinality 2. For each fault, we compute the error vector using an *oracle probability* of 0.75, similar to Perez *et al.*'s study, and check whether the vector contains an error, i.e. $1 \in e_i$. Finally, the error detection is computed by dividing the sum of faults that were detected by 10, the number

Table 6.1: Example of activity matrix with a test coverage of 75%. Bolded components are hit by one of the tests.

transactions	c_1	c_2	c_3	c_4
t_1	0	0	0	1
t_2	1	0	0	1
t_3	1	1	0	0

of generated faults. To account for randomness of generating fault candidates, we repeat this process 10 times. We obtain the activity matrices by using Perez *et al.*'s `ddu-maven-plugin`, similar to the experiments in Chapter 5. The computation of error detection is illustrated in Figure 6.1.

For the second experiment, in which we investigate the relation between DDU and test coverage, we compute the normalized density, diversity, uniqueness, DDU, and test coverage for each activity matrix, and compute the correlation. Furthermore, we use a similar approach as the experiments in Chapter 5, see Figure 6.2, where we create two test suites: (1) a test suite that consists of 50% of the available tests and (2) a test suite that consists of 100% of the available tests. This will most likely result in a system with two test suites with different DDU values, allowing us to investigate whether improving the DDU for a fixed system results in a test coverage improvement.

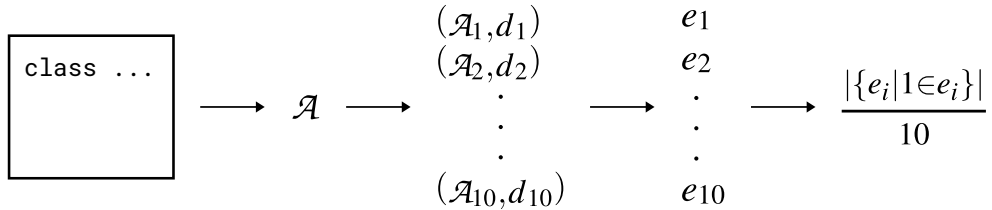For the third experiment, we generate two test suites with different DDU values

Figure 6.1: We compute the activity matrix for a given class and generate 10 artificial fault candidates d_1, d_2, d_{10} of cardinality 2. For each pair $(\mathcal{A}_i, d_i)$, the error vector e_i is computed. The error detection is computed by dividing the sum of faults that were detected $|\{e_i | 1 \in e_i\}|$ by 10, the number of generated faults.
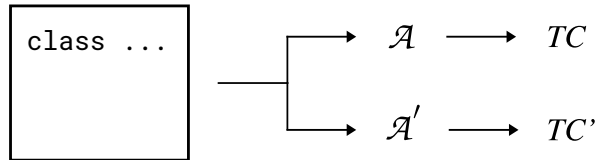

Figure 6.2: For each class, two test suites are generated, resulting in two activity matrices $\mathcal{A}$ and $\mathcal{A}'$. For each activity matrix, we compute test coverage TC, DDU, normalized density, diversity, uniqueness.
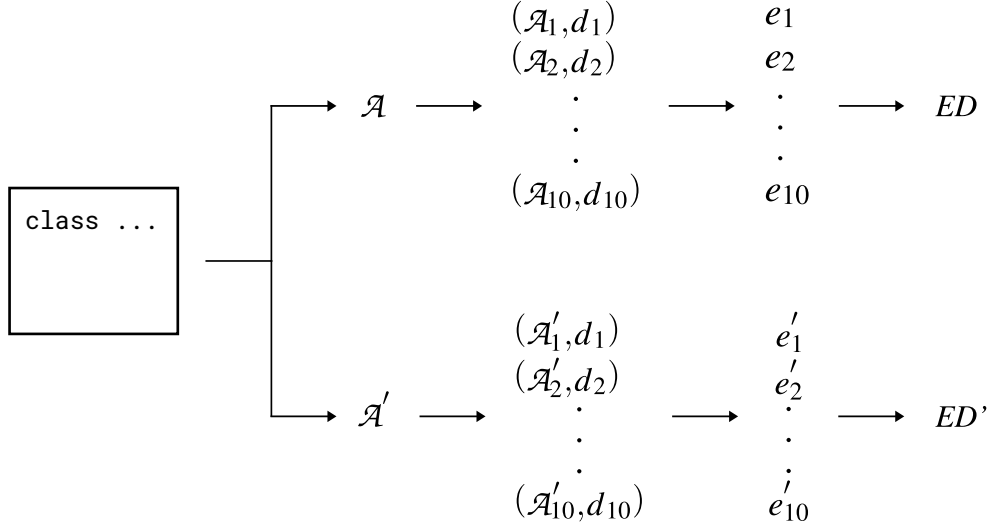
$$
\begin{array}{ccc}
(\mathcal{A}_1, d_1) & e_1 & \\
(\mathcal{A}_2, d_2) & e_2 & \\
\mathcal{A} \longrightarrow \quad \vdots & \longrightarrow \quad \vdots & \longrightarrow ED \\
(\mathcal{A}_{10}, d_{10}) & e_{10} &
\end{array}
$$

$$
\begin{array}{ccc}
(\mathcal{A}'_1, d_1) & e'_1 & \\
(\mathcal{A}'_2, d_2) & e'_2 & \\
\mathcal{A}' \longrightarrow \quad \vdots & \longrightarrow \quad \vdots & \longrightarrow ED' \\
(\mathcal{A}'_{10}, d_{10}) & e'_{10} &
\end{array}
$$

Figure 6.3: For each class, we generate two different test suites, resulting in a two activity matrices. For each matrix, we generate 10 fault candidates of cardinality 2 and compute the error vector. Finally, we compute the error detection and repeat this process 10 times.

and investigate whether the error detection improves when DDU improves, see Figure 6.3. Similar to the first experiment, we generate 10 fault candidates of cardinality 2 and compute the error vector with an *oracle probability* of 0.75 to determine the error detection. To account for randomness of generating fault candidates, we repeat this process 10 times.

Note that for the experiments we use the same projects used in previous experiments, namely Commons Codec, Commons Compress, Commons Math, Guice, Jsoup.

6.2 Experimental Results

In the first experiment, we confirm whether test coverage is representative for error detection. In Figure 6.4, we observe that there is a strong correlation between branch coverage and error detection. Furthermore, we observe that branch coverage puts an upper bound on error detection. The upper bound can be explained with the following example. Assuming that 60% of the components are tested, faults that involve untested components (in the remaining 40%) can never be detected. Therefore, the error detection can only be 100% if the test coverage is 100%.

In the second experiment, we examine the correlation between normalized density, diversity, uniqueness, and DDU and branch coverage. The results are shown in Figure 6.6 and Figure 6.7. We observe in Figure 6.6(a) and Figure 6.6(b) that normalized density is uncorrelated to branch coverage, and that diversity is weakly
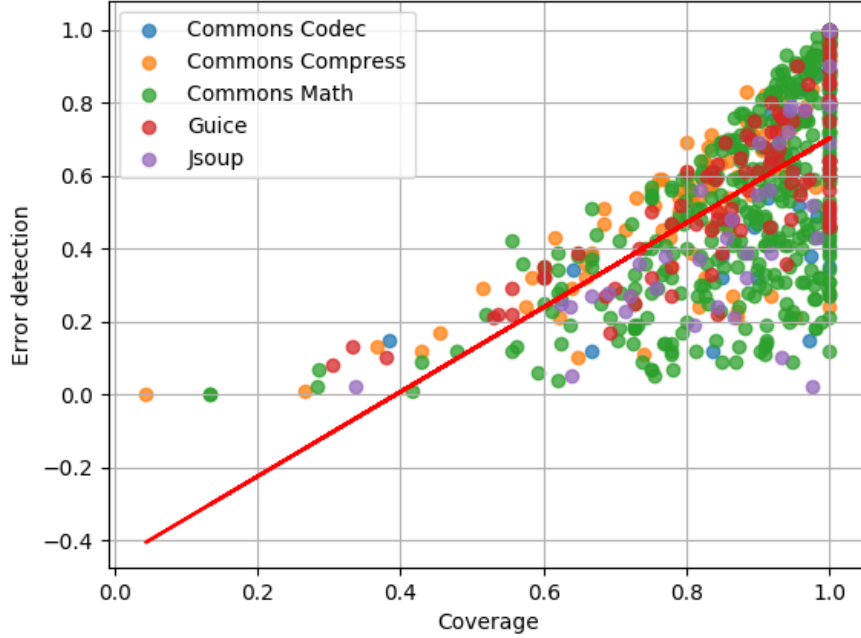
Figure 6.4: Scatterplot of coverage and error detection, $r = 0.628$, $p < 0.01$.

correlated to branch coverage. In Figure 6.6(c) and Figure 6.6(d), we observe that uniqueness and DDU are weakly correlated to branch coverage.

Nevertheless, we observe that uniqueness and DDU put a lower bound on branch coverage. The branch coverage is lower bounded by uniqueness since uniqueness enforces the number of unique columns in the activity matrix. This means that if the uniqueness is low, then the number of unique columns is low and therefore the branch coverage is potentially low. In Figure 6.5(a) and Figure 6.5(b), we observe that branch coverage can be high or low given an activity matrix with a low uniqueness. If the uniqueness is high, then the number of unique columns is high and therefore the branch coverage has to be high too. In Figure 6.5(c) and Figure 6.5(d), we observe two activity matrices with optimal uniqueness, resulting in a relative high or optimal coverage. The DDU lower bounds coverage since uniqueness is a component of DDU.

In the third experiment, we analyze the relation between DDU and error detection. In Figure 6.8, we observe that there is no strong correlation between normalized density, diversity, uniqueness, DDU, and error detection. In Figure 6.9, we observe similar results; no strong correlation between delta normalized density, delta diversity, delta uniqueness, delta DDU, and delta error detection, i.e. improving the components of DDU does not result in an improvement in the error detection. The results in Figure 6.8(c) and Figure 6.9(c) are unexpected because we have seen in
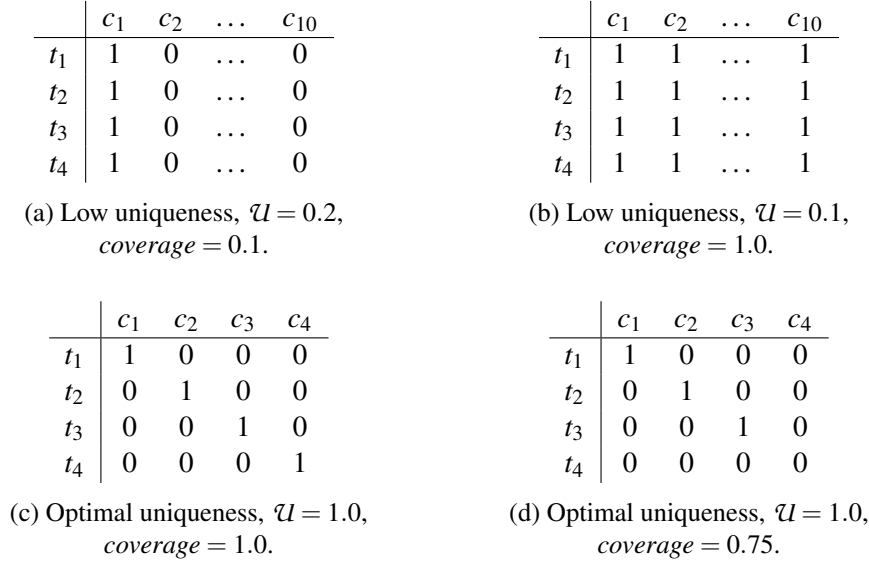
	c_1	c_2	...	c_{10}
t_1	1	0	...	0
t_2	1	0	...	0
t_3	1	0	...	0
t_4	1	0	...	0

(a) Low uniqueness, $\mathcal{U} = 0.2$,
coverage $= 0.1$.

	c_1	c_2	...	c_{10}
t_1	1	1	...	1
t_2	1	1	...	1
t_3	1	1	...	1
t_4	1	1	...	1

(b) Low uniqueness, $\mathcal{U} = 0.1$,
coverage $= 1.0$.

	c_1	c_2	c_3	c_4
t_1	1	0	0	0
t_2	0	1	0	0
t_3	0	0	1	0
t_4	0	0	0	1

(c) Optimal uniqueness, $\mathcal{U} = 1.0$,
coverage $= 1.0$.

	c_1	c_2	c_3	c_4
t_1	1	0	0	0
t_2	0	1	0	0
t_3	0	0	1	0
t_4	0	0	0	0

(d) Optimal uniqueness, $\mathcal{U} = 1.0$,
coverage $= 0.75$.

Figure 6.5: Examples of activity matrices with a low or high uniqueness.

previous experiments that branch coverage is strongly correlated to error detection, see Figure 6.4, and that an improvement in uniqueness is strongly correlated to an improvement in branch coverage, see Figure 6.7(c). However, we do not observe any correlation between uniqueness and error detection.

Revisiting the third research question:

> **RQ3:** What is the relation between density, diversity, uniqueness, and DDU and test coverage?

A: In the first experiment, we confirmed that branch coverage is strongly correlated to error detection. In the second experiment, in which we analyze the relation between the diagnosability metrics and branch coverage, we observed that only an improvement in uniqueness is strongly correlated to an improvement in branch coverage. The other metrics did not show any significant correlation. Further, we observed that uniqueness and DDU put a lower bound on branch coverage. In final experiment, we found no evidence that uniqueness and the other diagnosability metrics are correlated to error detection.
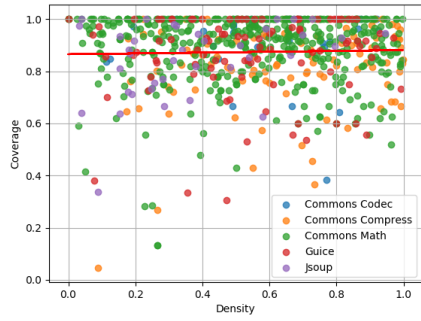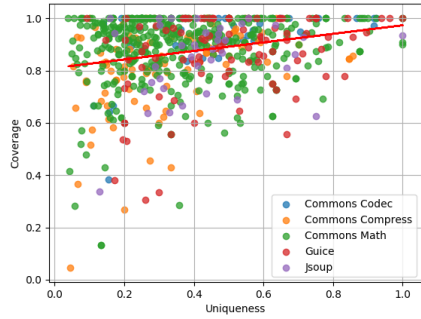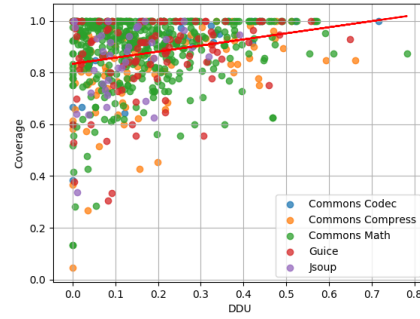
(a) Density, $r = 0.029$, $p = 0.44$.
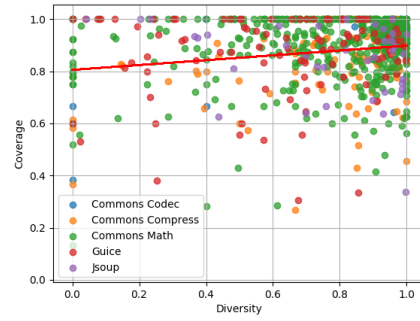
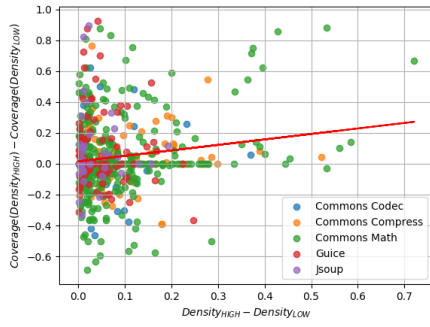(b) Diversity, $r = 0.173$, $p < 0.01$.

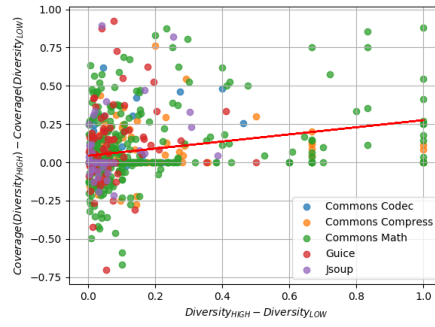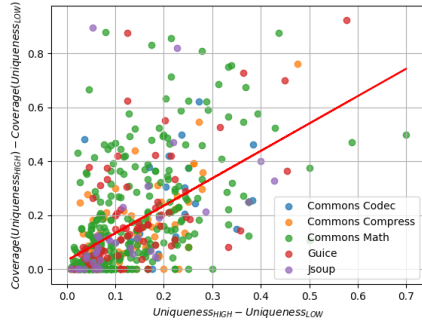(c) Uniqueness, $r = 0.237$, $p < 0.01$.

(d) DDU, $r = 0.228$, $p < 0.01$.

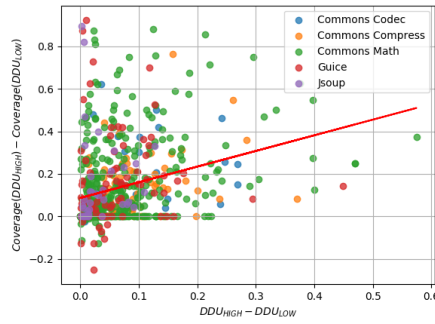Figure 6.6: Scatterplot of normalized density, diversity, uniqueness, and DDU against branch coverage.

(a) Density, $r = 0.143$, $p < 0.01$.

(b) Diversity, $r = 0.230$, $p < 0.01$.
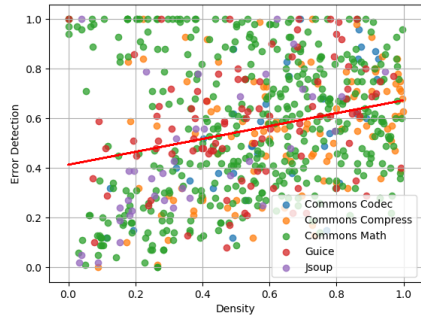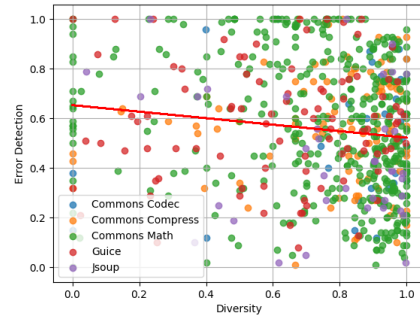
(c) Uniqueness, $r = 0.546$, $p < 0.01$.

(d) DDU, $r = 0.290$, $p < 0.01$.

Figure 6.7: Scatterplot of delta normalized density, delta diversity, delta uniqueness, and delta DDU against delta branch coverage.
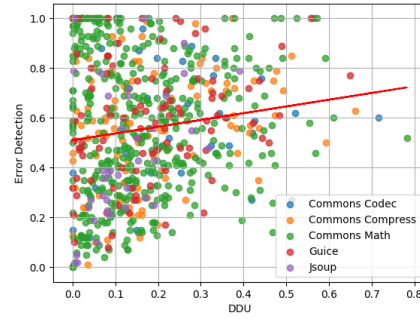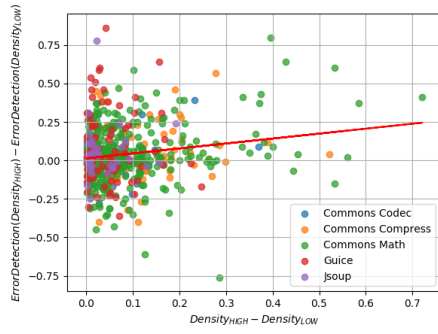
(a) Density, $r = 0.256$, $p < 0.01$.

(b) Diversity, $r = -0.132$, $p < 0.01$.
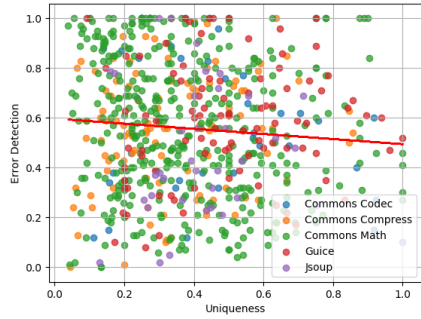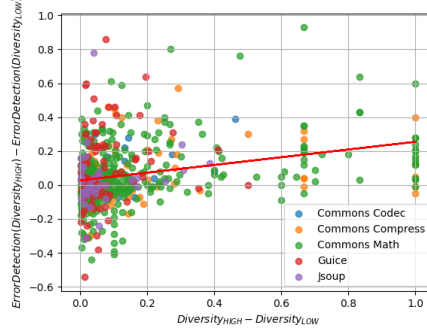
(c) Uniqueness, $r = -0.080$, $p < 0.05$.

(d) DDU, $r = 0.142$, $p < 0.01$.

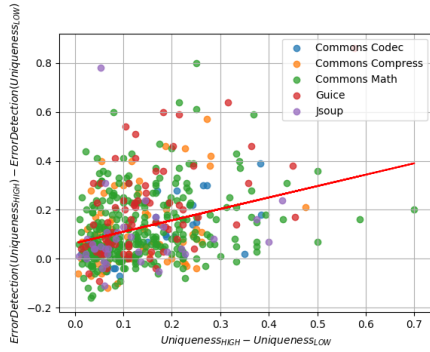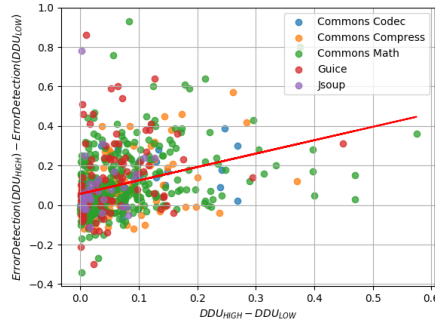Figure 6.8: Scatterplot of normalized density, diversity, uniqueness, and DDU against error detection.

(a) Density, $r = 0.165$, $p < 0.01$.

(b) Diversity, $r = 0.275$, $p < 0.01$.

(c) Uniqueness, $r = 0.323$, $p < 0.01$.

(d) DDU, $r = 0.324$, $p < 0.01$.

Figure 6.9: Scatterplot of delta normalized density, delta diversity, delta uniqueness, and delta DDU against delta error detection.

Chapter 7

Improving DDU

Chapter 8

Conclusion

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