# FOUNDATIONS OF STATISTICAL DECISION MAKING

Measuring Uncertainty

May 29, 2018

Aaron R. Baggett, Ph.D.

Department of Physical Therapy University of Mary Hardin-Baylor PHTH 7147: Critical Inquiry I





**PREVIEW** 

#### **Preview**

- 1. May 29, 2018
  - Fundamentals of Statistical Inference: Measuring Uncertainty
- 2. June 5, 2018
  - Fundamentals of Statistical Decision Making: Comparing Multiple Groups
- 3. June 5, 2018
  - Fundamentals of Statistical Decision Making: Relationships and Prediction



#### **Outline**

- Descriptive vs. inferential statistics
- The normal distribution
- Comparing groups
- Statistical/practical significance

#### Resources

• Slides, data, and handouts available at:

bit.ly/umhb\_dpt



#### **Statistics**

- Experimentation and observation:
  - 1. Measurement of uncertainty
  - 2. Examination of the consequences of that uncertainty

#### **Statistics**

- Two fundamental branches
  - 1. Descriptive statistics
    - Summarize data
    - Condense larger themes
  - 2. Inferential statistics
    - Infer meaning
    - Test predictions



# **Low Birth Weight Study**

- Baystate Medical Center, Springfield, MA.
- Sample of 189 births in 1986
- Risk factors in low birth weight babies

# **Low Birth Weight Study**

Age	Weight	Race	Smoking Status	Birth Weight
19	182	Black	Non-Smoker	5.56
33	155	Other	Non-Smoker	5.62
20	105	White	Smoker	5.64
21	108	White	Smoker	5.72
18	107	White	Smoker	5.73
21	124	Other	Non-Smoker	5.78

# DESCRIPTIVE STATISTICS

- How many babies were born at low birth weight (< 5.5 lbs.)?</li>
- How many mothers smoked during pregnancy?
- How much did the average baby weigh?
  - Given mothers' smoking status
  - Given mothers' race

#### **Question:**

Do babies born to mothers who smoked during pregnancy weigh less than those born to mothers who did not?

#### **Question:**

Do babies born to mothers who smoked during pregnancy weigh less than those born to mothers who did not?

How should we answer this question?

#### **Question:**

[ON AVERAGE], do babies born to mothers who smoked during pregnancy weigh less than those born to mothers who did not?

<b>Smoking Status</b>	n	Min.	Max.	Μ	SD
Non-Smoker	115	2.25	11.00	6.74	1.66
Smoker	74	1.56	9.34	6.11	1.46

#### **Question:**

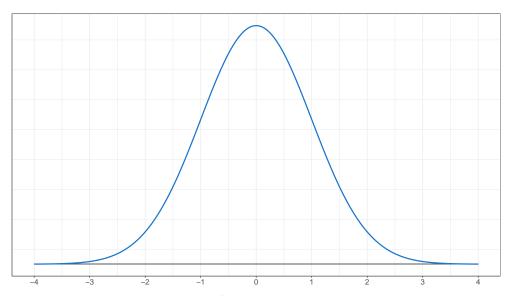
1. Based on our sample, what are we left to assume about the weights of babies *in the population* born to smoking and non-smoking mothers?

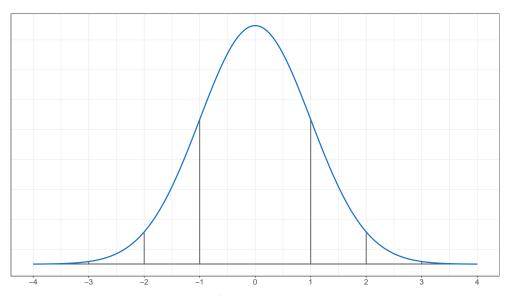
#### **Question:**

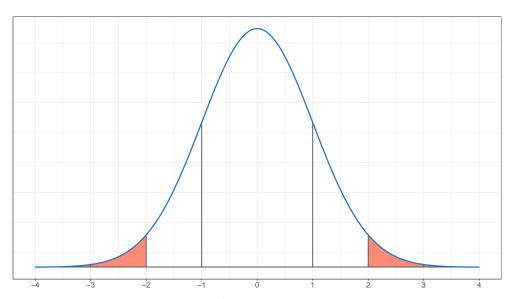
- 1. Based on our sample, what are we left to assume about the weights of babies *in the population* born to smoking and non-smoking mothers?
  - That the sample estimates represent the population parameters

Smoking Status	n	Min.	Max.	М	SD
Non-Smoker	115	2.25	11.00	6.74	1.66
Smoker	74	1.56	9.34	6.11	1.46

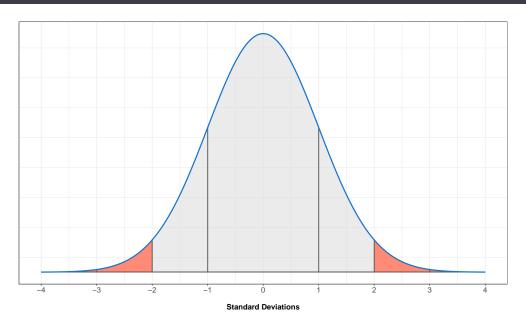
 In fact, we assume that the population distribution of baby weights is "normal"







Baggett (PHTH 7147)



# INFERENTIAL STATISTICS

#### **Inferential Statistics**

- More useful than descriptives
- Allow for making predictions or generalizations
- Key to hypothesis testing
- Two varieties:
  - 1. 95% confidence intervals (CIs)
  - 2. Null-hypothesis significance testing (NHST)

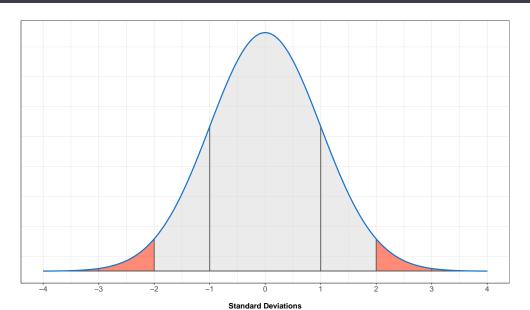
#### **Inferential Statistics**

#### **Question:**

Do babies born to mothers who smoked during pregnancy weigh less than those born to mothers who did not?

- Since we are interested in the mean difference in birth weights in the population, a first inferential step is to calculate a 95% confidence interval
- Confidence intervals are a plausible range of values for a population parameter
- Point estimates often may not represent the population parameter
- Cls are more likely to capture the population parameter than a point estimate alone

28 / 49



• 95% CI:

$$(M_1 - M_2) \pm 2 \times \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

• 95% CI:

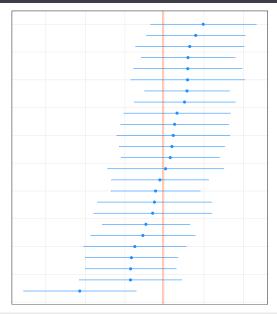
$$(6.11_{NS} - 6.74_S) \pm 2 \times \sqrt{\frac{2.12_{NS}}{74_{NS}} + \frac{2.75_S}{115_S}}$$

• 95% CI:

$$-0.63 \pm (2 \times 0.229) =$$
$$(-1.09, -0.17)$$

 Thus, we can be 95% confident that, in the population, the true difference in birth weight of babies born to smoking mothers compared to those born to non-smoking mothers is between -1.09 and -0.17 lbs. less, on average.

 In other words, if we replicated this study 25 times, 24 of the 25 replications would include the true population parameter



#### **Inferential Statistics**

#### **Question:**

Do babies born to mothers who smoked during pregnancy weigh [STATISTICALLY SIGNIFICANTLY] less than those born to mothers who did not?

How should we answer this question?

# Inferential Statistics::Hypothesis Testing

• What do we mean by statistical significance?

# Inferential Statistics::Hypothesis Testing

- What do we mean by statistical significance?
- Observed differences which exceed "normality."

# Inferential Statistics::Hypothesis Testing

- We usually consider differences beyond  $\pm$  2 SDs from M to be "statistically significant"
- NOTE: Statistical significance  $\neq$  practical significance

## **Low Birth Weight Study**

#### **Question:**

• Do babies born to mothers who smoked during pregnancy weigh less than those born to mothers who did not?

# Low Birth Weight Study

#### **Hypotheses:**

•  $H_0$ : There is no mean difference in the birth weight of babies born to mothers who did and did not smoke during pregnancy

$$(M_{non\text{-smoker}} - M_{smoker} = 0)$$

•  $H_1$ : There is some difference in the birth weight of babies born to mothers who did and did not smoke during pregnancy

$$\circ (M_{non\text{-smoker}} - M_{smoker} \neq 0)$$

# Low Birth Weight Study

- Let's test our hypothesis using an independent-samples t-test
  - IV: Mothers' smoking status (smoker, non-smoker)
  - DV: Baby birth weight

$$t = \frac{\overline{X}_{non-smokers} - \overline{X}_{smokers}}{\sqrt{\frac{s_{non-smokers}^2}{N_{non-smokers}} + \frac{s_{smokers}^2}{N_{smokers}}}}$$

41 / 49

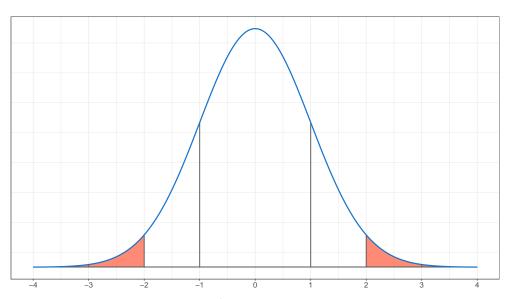
Table 1: Results of Independent-Samples t-Test

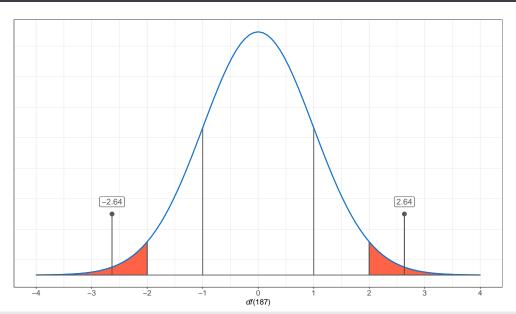
	Non-Smokers				Smokers				
	n	М	SD	n	М	SD	t(187)	р	$\omega^2$
Baby birth weight	115	6.74	1.66	47	6.11	1.46	2.63	0.009	0.008

Note: M = Mean; SD = Standard deviation

- Assuming the null hypothesis, in reality, is true, the probability of obtaining a mean difference in birth weight  $\geq$  0.62 lbs. is 0.009 (0.90%)
- Birth weights appear to differ statistically significantly

43 / 49





• But, is the difference of M = 0.62 lbs. meaningful?

- But, is the difference of M = 0.62 lbs. meaningful?
- A meaningful difference implies practicality or usefulness in the real world

- But, is the difference of M = 0.62 lbs. meaningful?
- A meaningful difference implies practicality or usefulness in the real world
- Effect size ( $\omega^2$ ): Proportion of variance explained in the model

- But, is the difference of M = 0.62 lbs. meaningful?
- A meaningful difference implies practicality or usefulness in the real world
- Effect size ( $\omega^2$ ): Proportion of variance explained in the model
- Smoking status explains 0.009 (0.90%) of the variance in baby birth weight

- But, is the difference of *M* = 0.62 lbs. meaningful?
- A meaningful difference implies practicality or usefulness in the real world
- Effect size ( $\omega^2$ ): Proportion of variance explained in the model
- Smoking status explains 0.009 (0.90%) of the variance in baby birth weight
- Thus, 100% 0.991% = 99.10% of the variance in baby birth weight is left unexplained



## Recap

- Descriptive statistics allow us to summarize data from a sample
- Inferential statistics allow us to predict and generalize about a population
- Hypothesis testing allows us to construct a sense of meaning about the world

48 / 49

#### **Next Time**

- Making decisions using hypothesis testing and prediction
  - Statistical variables
  - Multiple group comparisons (ANOVA)
  - Predicting outcomes (Regression)