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Unit 3: Foundations for inference

2. Confidence intervals

Sta 101 - Spring 2016

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Slides posted at http://bit.ly/sta101_s16

1. Statistical inference methods based on the CLT depend on the same conditions as the CLT

Always check these in context of the data and the research question!

- 1. Independence: Sampled observations must be independent.
 - * This is difficult to verify, but is more likely if
 - random sampling/assignment is used, and,
 - if sampling without replacement, n < 10% of the population.
- 2. Sample size/skew: Either the population distribution is normal or n>30 and the population distribution is not extremely skewed (the more skewed the distribution, the higher n necessary for the CLT to apply).
 - * This is also difficult to verify for the population, but we can check it using the sample data, and assume that the sample mirrors the population.

- ➤ Tips for project: be mindful of the two big deadlines, read over the assignment and start asking questions, don't save the work till the last night – this is not a project you can complete by pulling an all nighter
- ► Peer eval feedback:
 - Lateness / absence, mental presence, communication, commitment
 - Tips: Move seats around in class and lab, give your best, and don't assume the worst
 - Instructions: Give scores that reflect your verbal comments
- ▶ Discussion section tomorrow: CLT, Cls, HTs

2. Use confidence intervals to estimate population parameters

 $\mathit{CI}: point\ estimate\ \pm\ margin\ of\ error$

If the parameter of interest is the population mean, and the point estimate is the sample mean,

$$\bar{x} \pm Z^* \frac{s}{\sqrt{n}}$$

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Clicker question

What is the critical value (Z^*) for a confidence interval at the 91% confidence level?

- (a) $Z^* = 1.34$
- (b) $Z^* = 1.65$
- (c) $Z^* = 1.70$
- (d) $Z^* = 1.96$
- (e) $Z^* = 2.33$

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4. Calculate the sample size a priori to achieve desired margin of error

$$ME = z^* \frac{s}{\sqrt{n}}$$

So if we know the desired ME, and confidence level (and hence z^*), and the sample standard deviation, we can solve for n.

1. The confidence level of a confidence interval is the probability that the true population parameter is in the confidence interval you construct for a single sample.

The confidence level is equal to the proportion of random samples that result in confidence intervals that contain the true pop. parameter.

2. A narrower confidence interval is always better.

This is incorrect since the width is a function of both the confidence level and the standard error.

3. A wider interval means less confidence.

This is incorrect since it is possible to make very precise statements with very little confidence.

Application exercise: 3.1 Confidence interval for a single mean

See course website for details.

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Summary of main ideas

- 1. Statistical inference methods based on the CLT depend on the same conditions as the CLT
- 2. Use confidence intervals to estimate population parameters
- 3. Critical value depends on the confidence level
- 4. Calculate the sample size a priori to achieve desired margin of error