

WI23_CSBR-NY_1_NC_INT2 HW6 (Q5)

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TOTAL POINTS

16.5 / 20

QUESTION 1

1 Q5 16.5 / 20

✓ - 0.5 pts Did not properly define $\forall n \geq n_0$

✓ - 3 pts Did not show clear work identifying constants for (b)

1 ??

2 Typo. We need to prove $\Theta()$ instead of $O()$ only

Question #5:

a) $5n^3 + 2n^2 + 3n = O(n^3)$

Proof:

$$5n^3 \leq 5n^3 + 2n^2 + 3n \leq 5n^3 + 2n^3 = 15n^3$$

$$C_1 = 15$$

$$C_2 = 5$$

$$N_0 = 3$$

Therefore, $5n^3 + 2n^2 + 3n = O(n^3)$ 2

b) $\sqrt{7n^2 + 2n - 8} = O(n)$

Proof:

$$\sqrt{7n^2 + 2n - 8} = 7n + 2\sqrt{n} - \sqrt{8} \quad \text{1}$$

$$7n \leq 7n + 2\sqrt{n} - \sqrt{8} \leq 7n + 2n = 9n$$

$$C_1 = 9$$

$$C_2 = 7$$

$$N_0 = 4$$

Therefore, $\sqrt{7n^2 + 2n - 8} = O(n)$

1 Q5 16.5 / 20

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