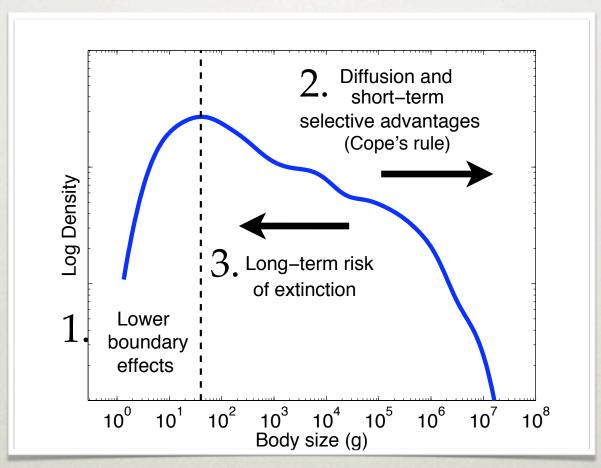
## CETACEAN MACROEVOLUTION

Lecture 14 21 October 2010 CSCI 7000-003 Inference, Models and Simulation for Complex Systems

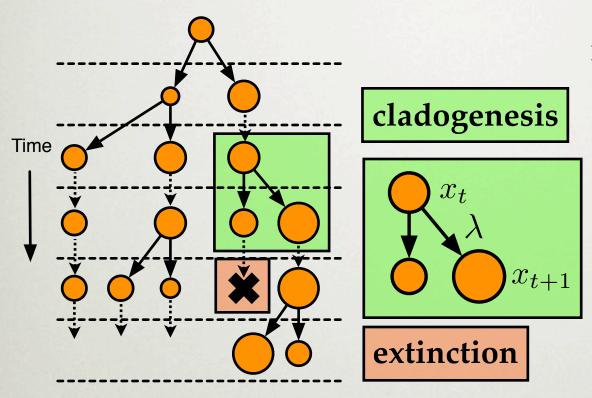
Prof. Aaron Clauset University of Colorado

#### MACROEVOLUTIONARY MODEL

#### three mechanisms



#### CLADOGENESIS



#### model features

- size-dependent fluctuations
- Cope's rule
- size-dependent extinction rate
- lower limit  $x_{\min}$

#### ANALYTIC VERSION

#### reaction-diffusion-convection equation:

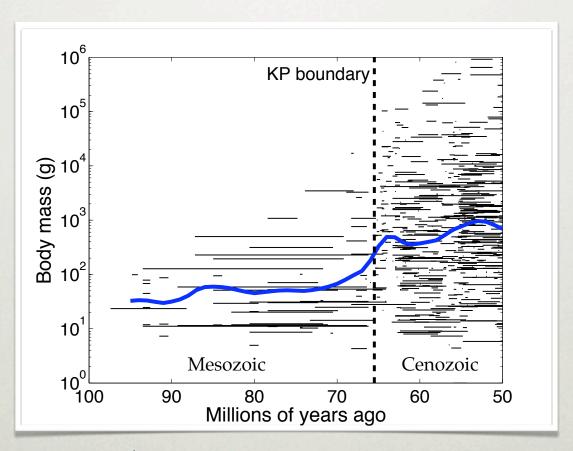
$$\frac{\partial c}{\partial t} + v \frac{\partial c}{\partial x} = D \frac{\partial^2 c}{\partial x^2} + (k - A - Bx)c$$

$$\uparrow \qquad \uparrow \qquad \uparrow$$
drift term diffusion speciation (Cope's rule) term and extinction

3 parameters: 
$$\beta=B/D$$
 
$$\mu=v/D$$
 estimated from fossil data

### SIZE DIVERSIFICATION

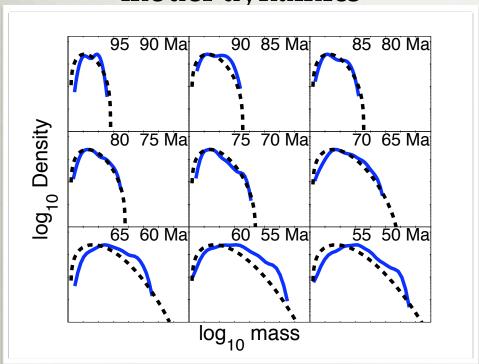
### SIZE DIVERSIFICATION



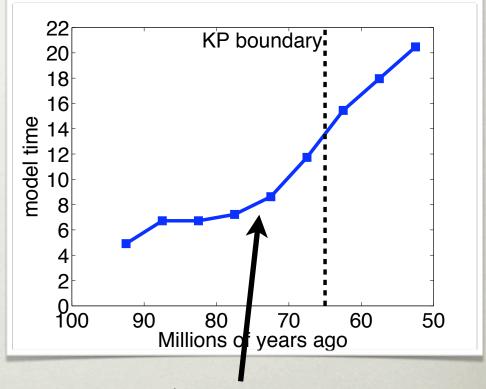
[North Am. terrestrial mammals]

#### SIZE DIVERSIFICATION

#### model dynamics



#### model time



agrees with molecular-clocks for genetic diversification

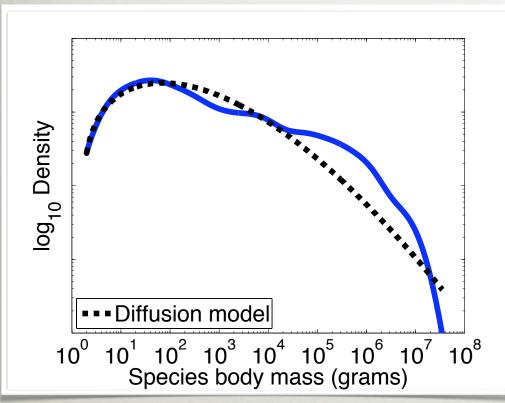
### CETACEAN MACROEVOLUTION



Southern Right whale (photo credit: Brian Skerry)

#### CETACEAN BODY SIZES

#### Terrestrial mammals

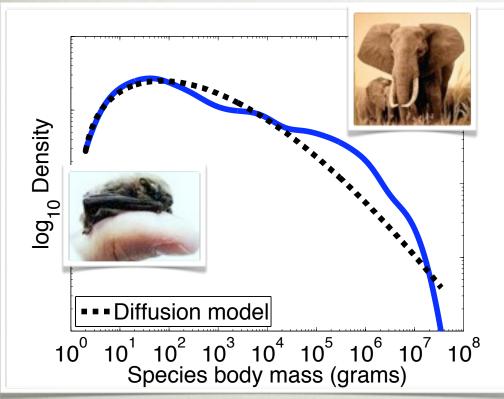


#### out-of-sample test

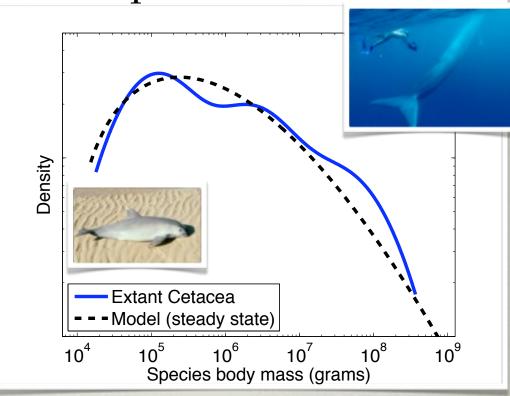
- estimate parameters for terrestrial mammals
- change  $x_{\min} \approx 20 \text{kg}$
- compare predicted pdf for aquatic mammals to empirical data

#### CETACEAN BODY SIZES

Terrestrial mammals



Aquatic mammals

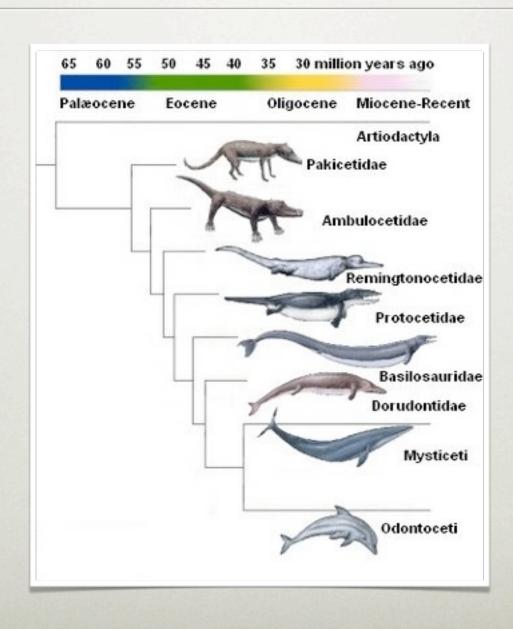


 $x_{\rm min} \approx 20 {\rm kg}$ 

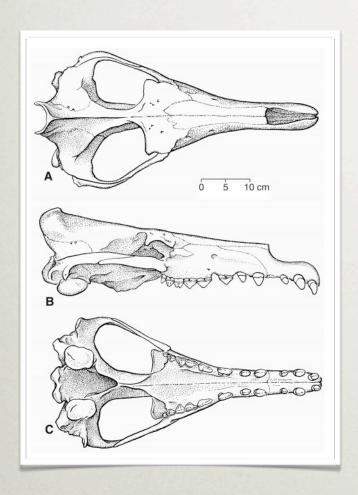
but, do the dynamics agree?

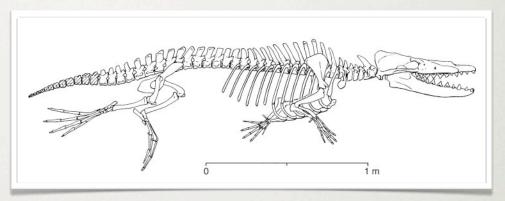
need fossil data to test

#### FOSSIL WHALES



#### FOSSIL WHALES





Rodhocetus kasrani (47 Ma)

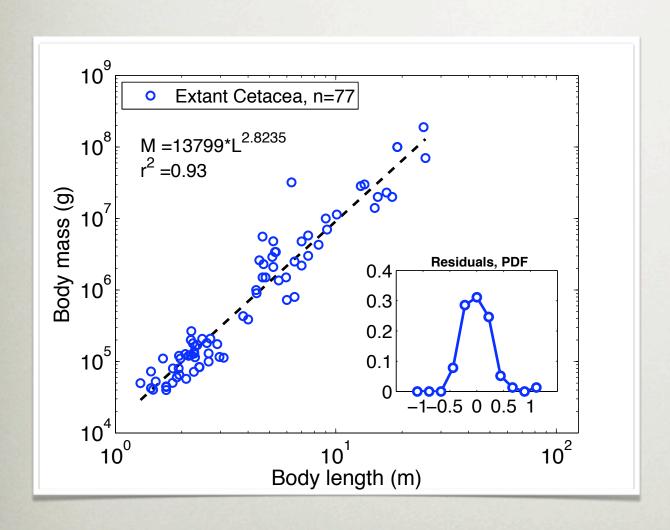
data we can get from fossils:

- length of skeleton L
- length of skull CbL
- width of skull OcW

data we want:

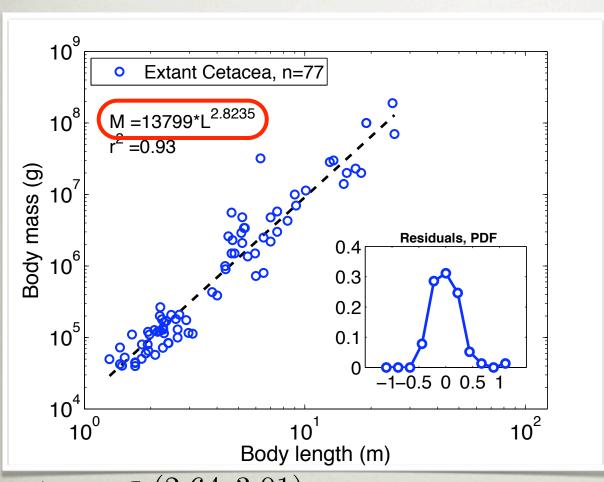
body mass M

#### A MODEL

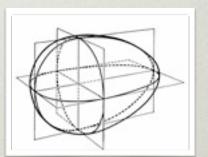


- measure L, CbL,
   OcW & M for
   extant Cetaceans
- build model
- estimate M for fossil species

#### A MODEL



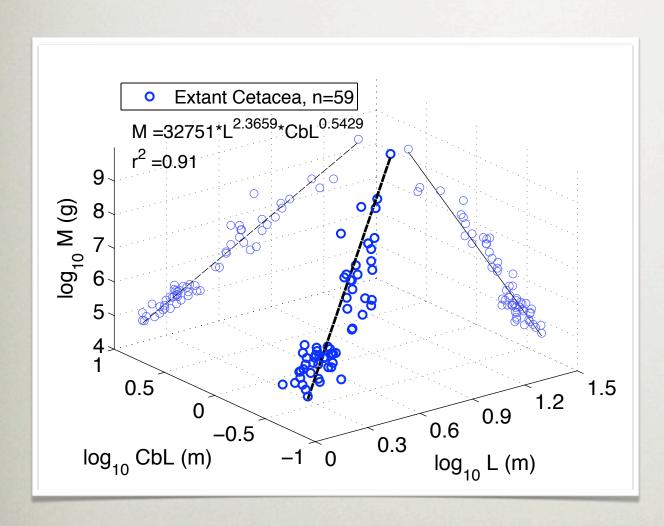
- measure L, CbL,
   OcW & M for
   extant Cetaceans
- build model
- estimate M for fossil species



95% CI: 
$$\alpha \in (2.64, 3.01)$$

$$M = \left(\frac{4}{3}\pi abc\right)\rho = \left(\frac{4\pi L^3}{24k_1k_2}\right)(10^6[g/m^3])$$

#### A MODEL



- measure L, CbL,
   OcW & M for
   extant Cetaceans
- build model
- estimate M for fossil species

### FOSSIL WHALE DATA

list of species:

## The Paleobiology Database

size measurements:

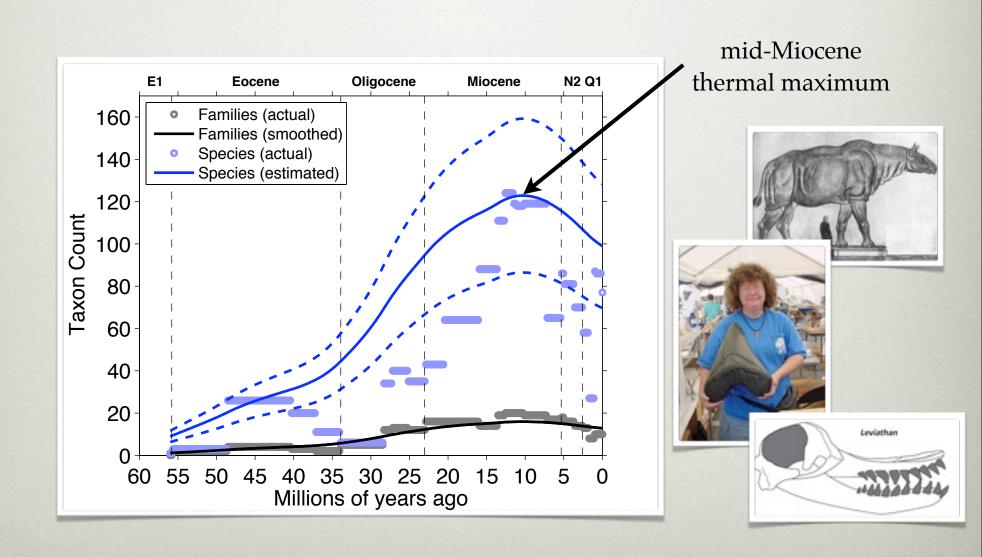
primary literature (200+ papers)

796 measurements

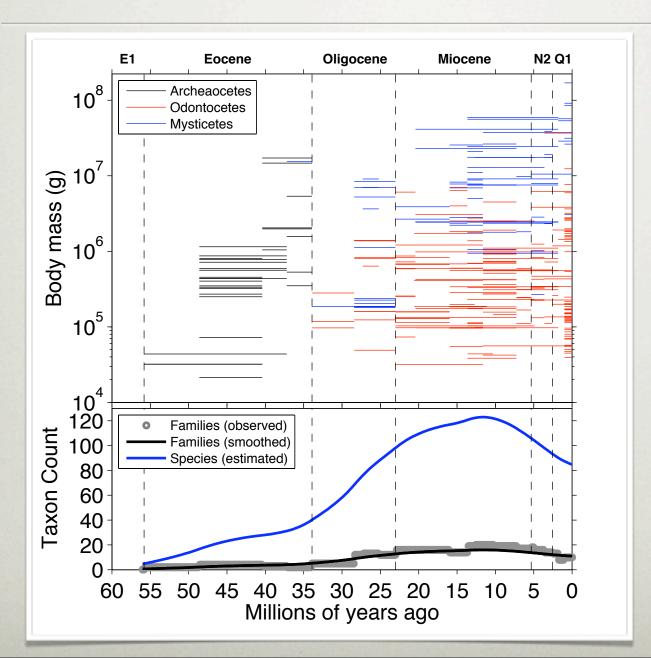
214 extinct species (of 403 known)

78 extant species

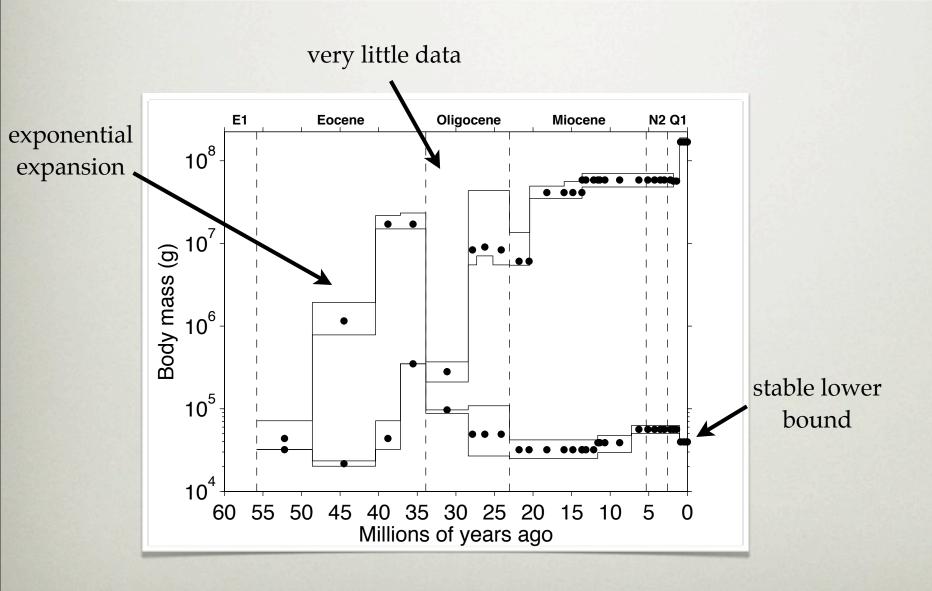
#### FOSSIL WHALE DIVERSITY



### FOSSIL WHALE SIZES



#### SIZE DISPARITY



### FITTING THE MODEL

fit disparity

disparity(t) = 
$$\frac{x_{\text{max}}(t)}{x_{\text{min}}}$$

where

$$\frac{1}{n(t)} = \int_{x_{\text{max}}(t)}^{\infty} \Pr(x, t) dx$$

parameters:  $\beta = B/D$   $\mu = v/D$  from terrestrial model

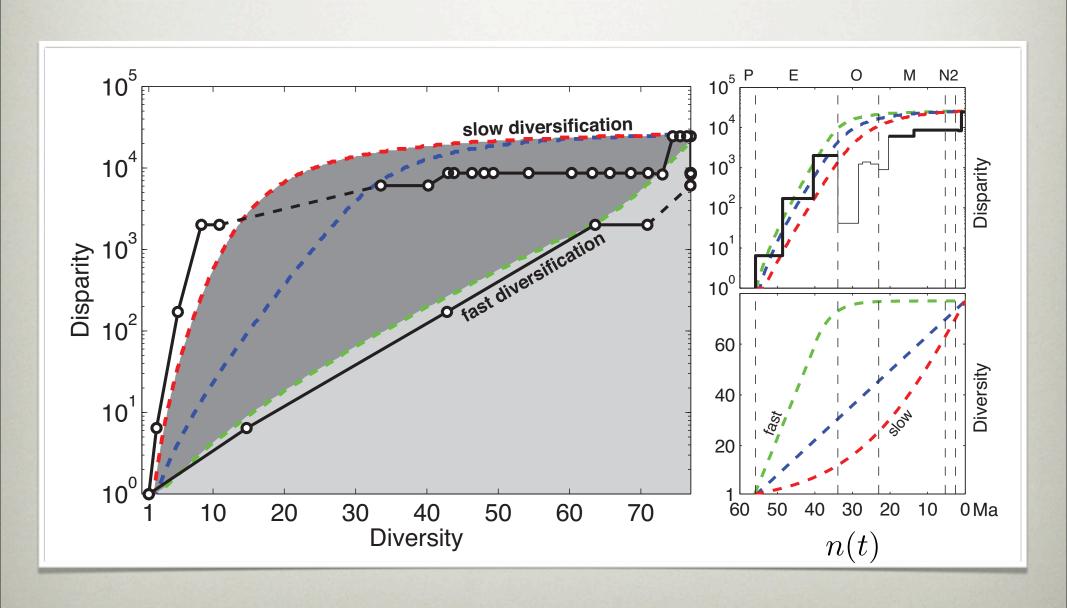
 $x_{\min}$ 

for aquatic mammals

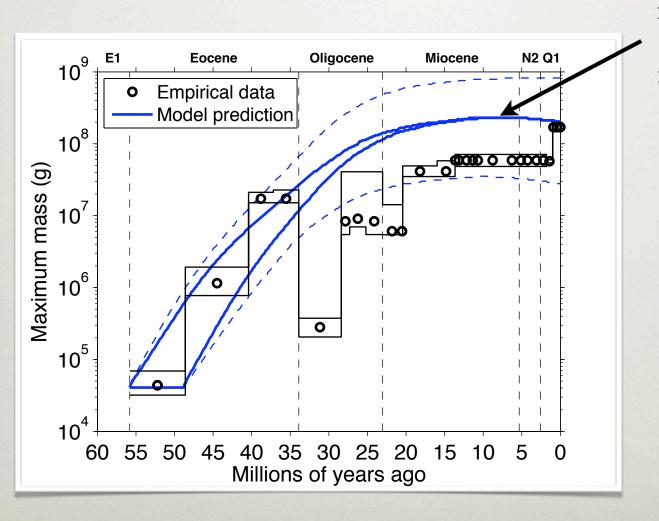
n(t)

simulated & empirical

# MORPHOLOGICAL DIVERSIFICATION DYNAMICS



# MORPHOLOGICAL DIVERSIFICATION DYNAMICS



maximum disparity coincides with maximum diversity

## SOME GENERAL INSIGHTS

# MORPHOLOGICAL DIVERSIFICATION DYNAMICS

