



Lecture 9b: Exploration, testing , and prediction

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**"In God we trust. All others must bring data."
— W. Edwards Deming**

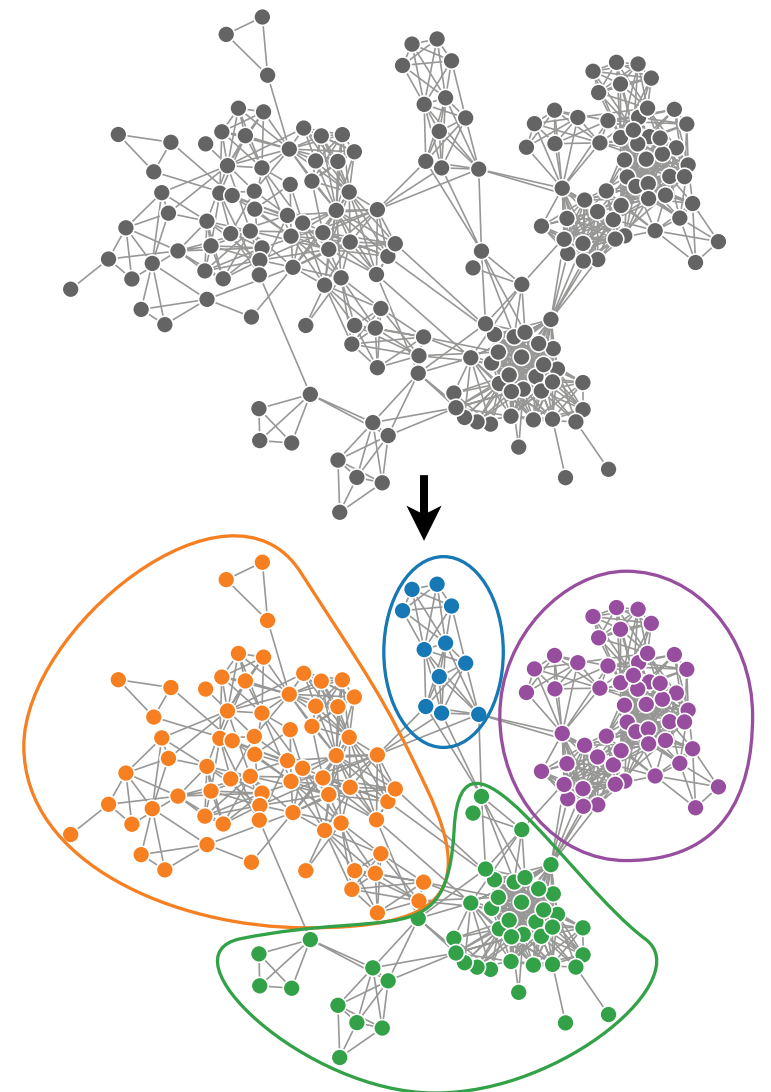
"God must bring data, too." — unknown

three roles of statistics

- data exploration
- model testing
- prediction

data exploration : community detection

- given a graph G
- divide its vertices into coherent groups $z(G)$
- consummate data exploration!
- a common task in network analysis
- helped yield insight into real social, biological, technological systems
- scores of methods, many extremely powerful, some with guarantees (stochastic block model, Belief Propagation, etc.)



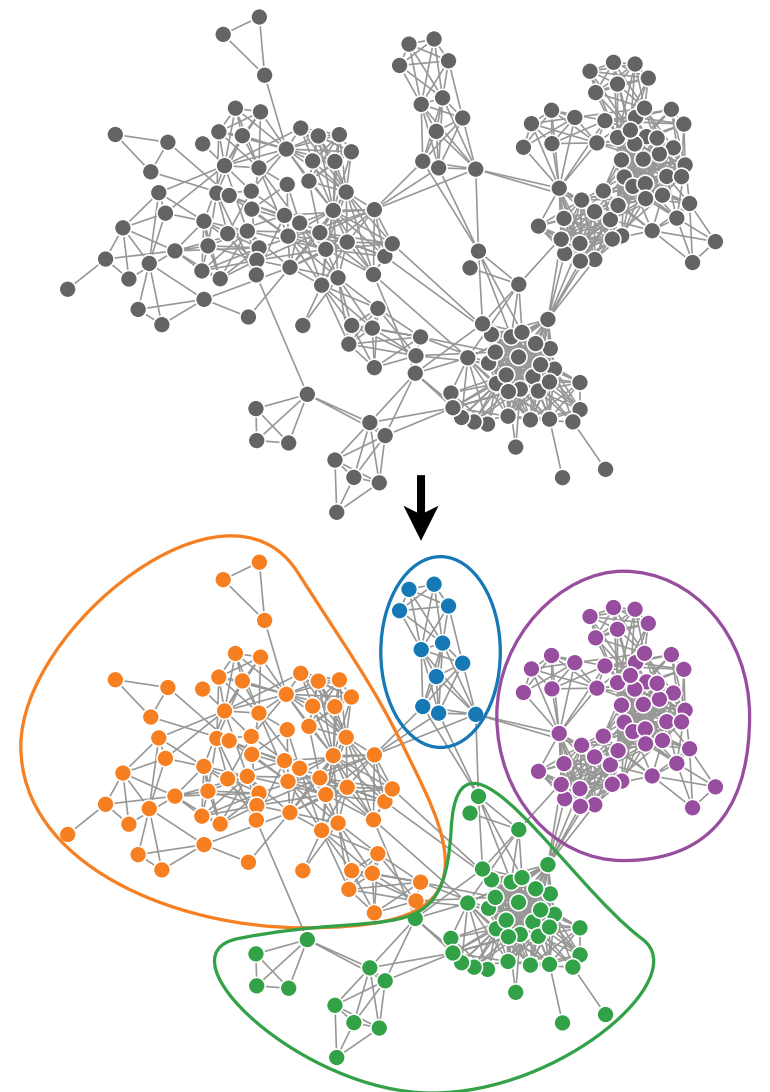
data exploration : community detection

- given a graph G
- divide its vertices into coherent groups $z(G)$

- nearly all methods:

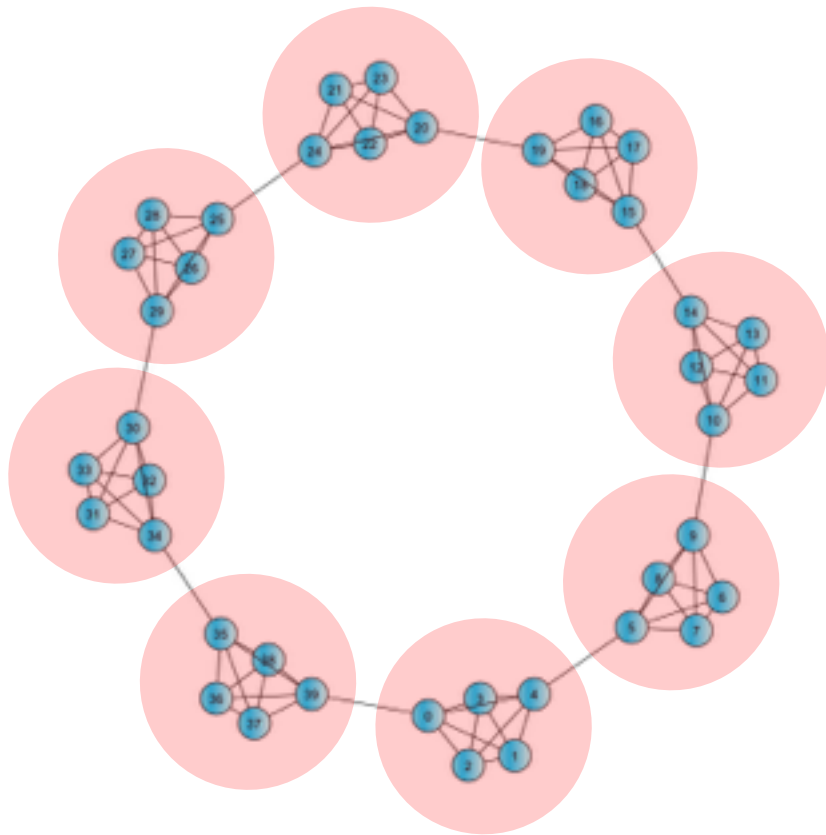
estimate $\max_z f(z(G))$

[WARNING: typically NP-hard]



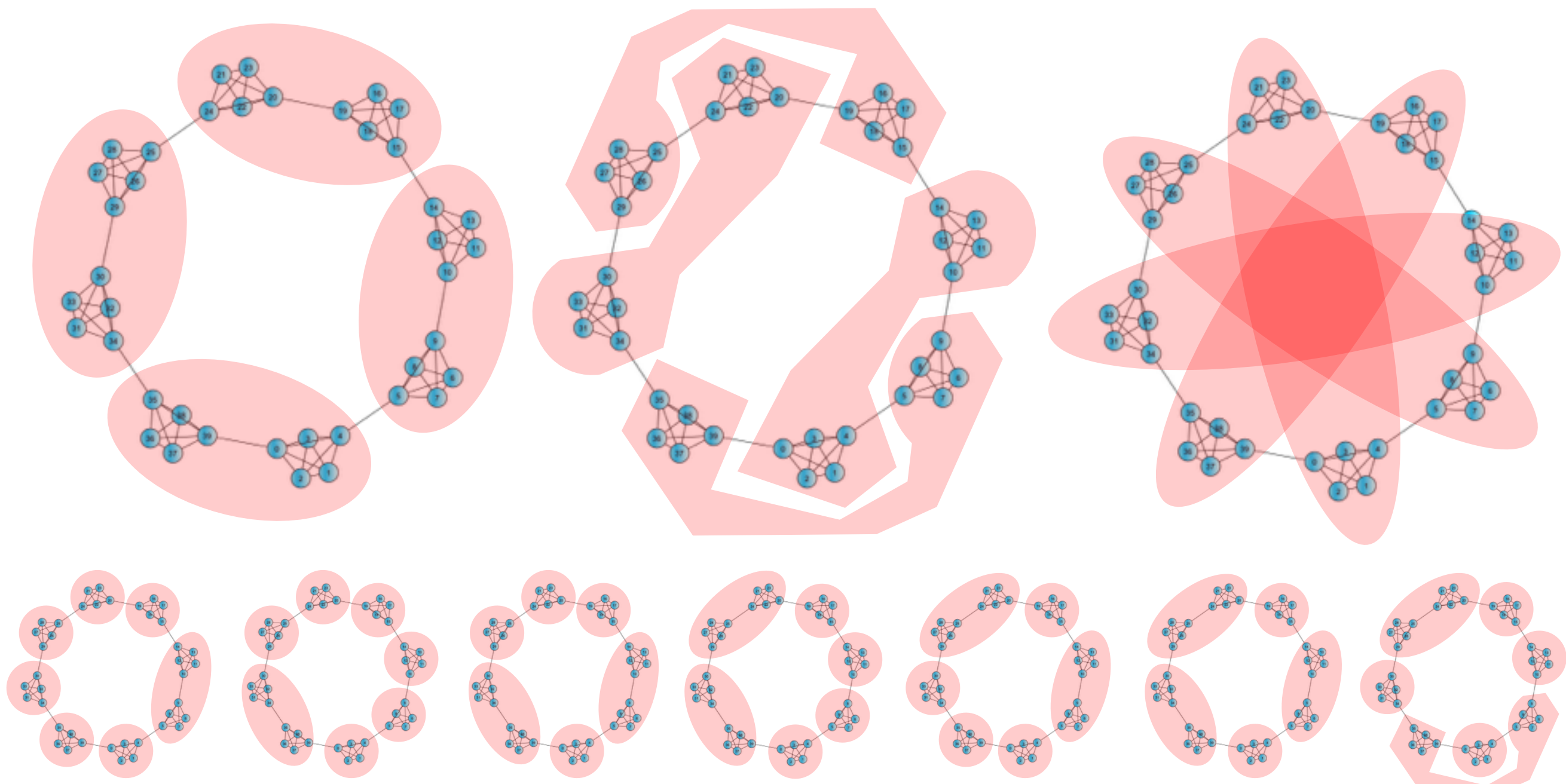
the trouble with community detection

this is a pretty good division (under nearly any f)



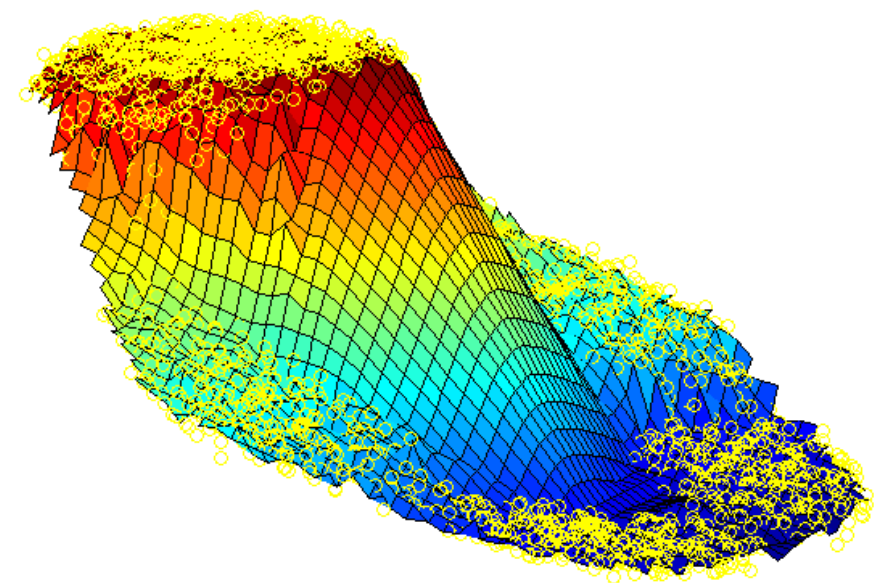
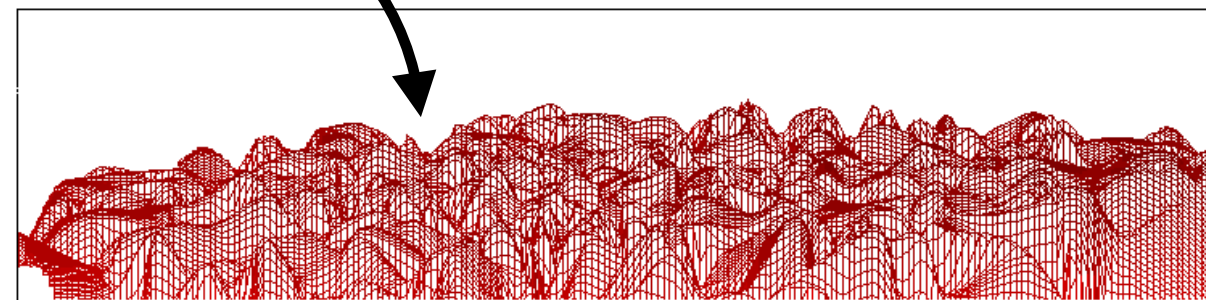
data exploration : community detection

so are all of these (and many more)



data exploration : community detection

- there are an exponential number of good-looking local maxima
each algorithm chooses one
- this is okay for data exploration!
- anything else requires caution
- **risks**: 'wrong' optima
- **opportunities**: community structure is genuinely interesting!
- **difficulties**: how do we select among all these good divisions?



model testing : scale-free networks

Inferring network mechanisms: The *Drosophila melanogaster* protein interaction network

Manuel Middendorf[†], Etay Ziv[‡], and Chris H. Wiggins^{§¶||}

- *observation*: many protein interaction networks have heavy-tailed (power-law?) degree distributions

model testing : scale-free networks

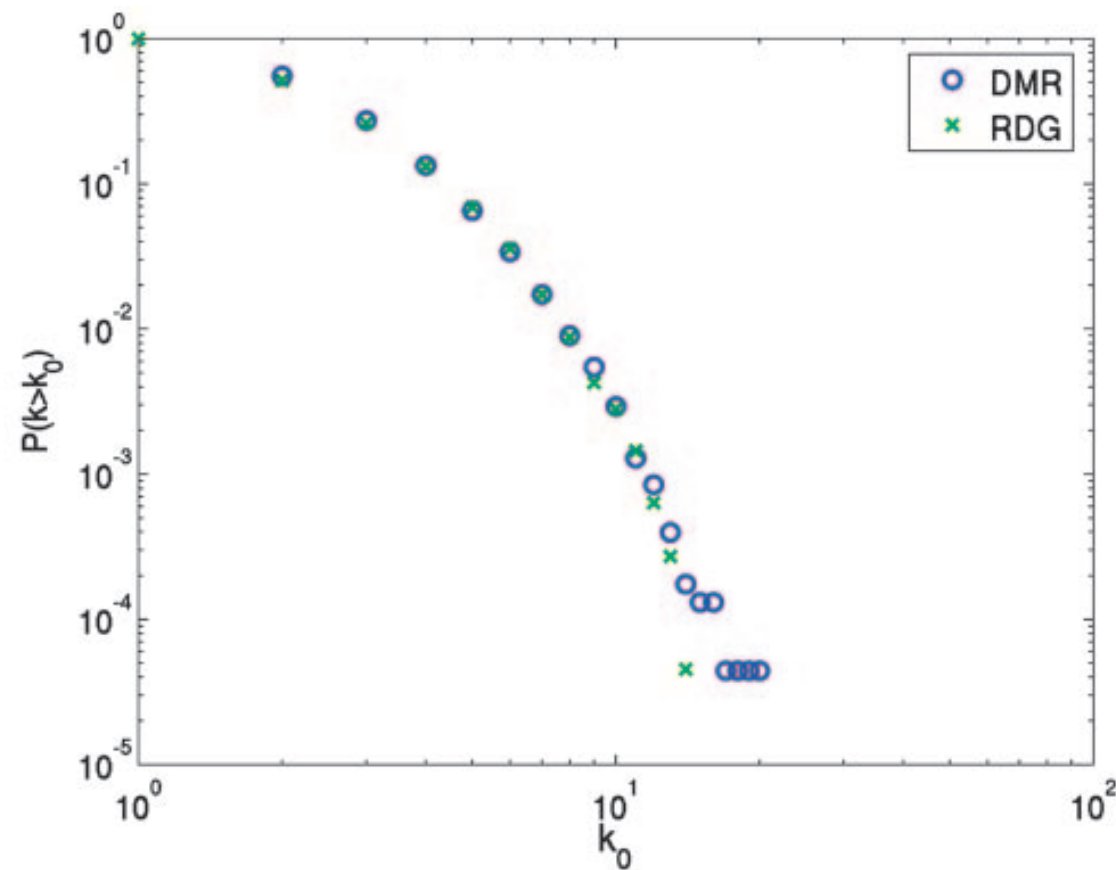
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- *observation*: many protein interaction networks have heavy-tailed (power-law?) degree distributions
- *claims*: as of 2005, FIVE different models proposed as generative mechanisms
- duplication mutation complementation (DMC), duplication mutation-random (DMR), linear preferential attachment (LPA), random growing networks (RDG), aging vertex networks (AGV)

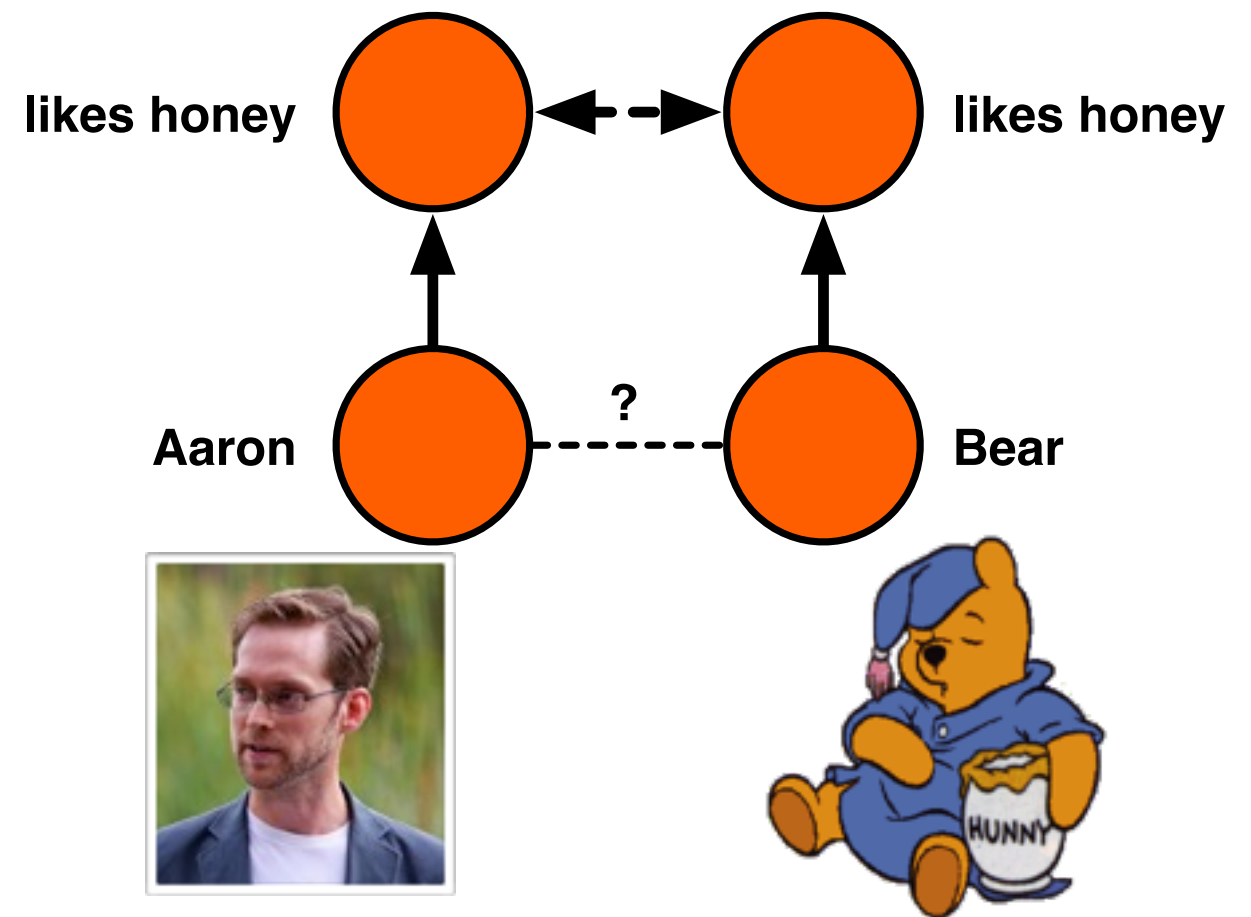
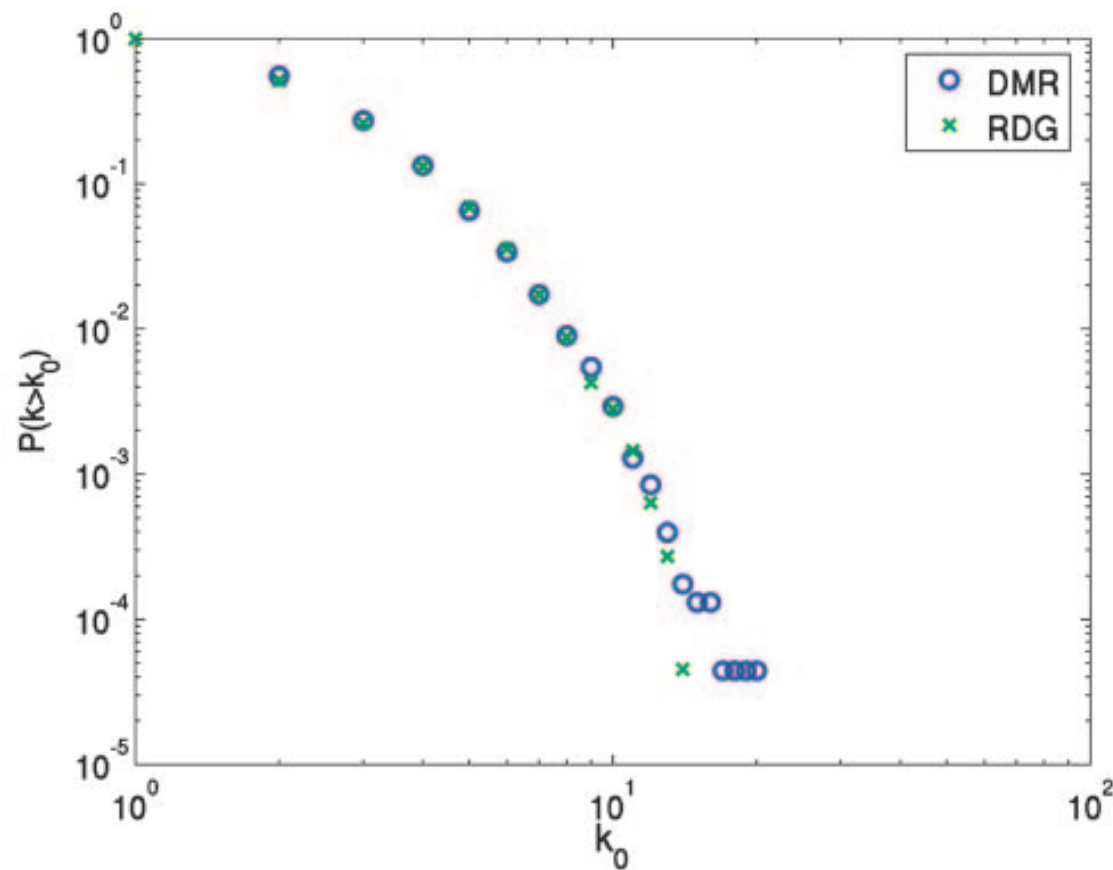
model testing : scale-free networks

- *the problem*: all models fit the observed degree distribution



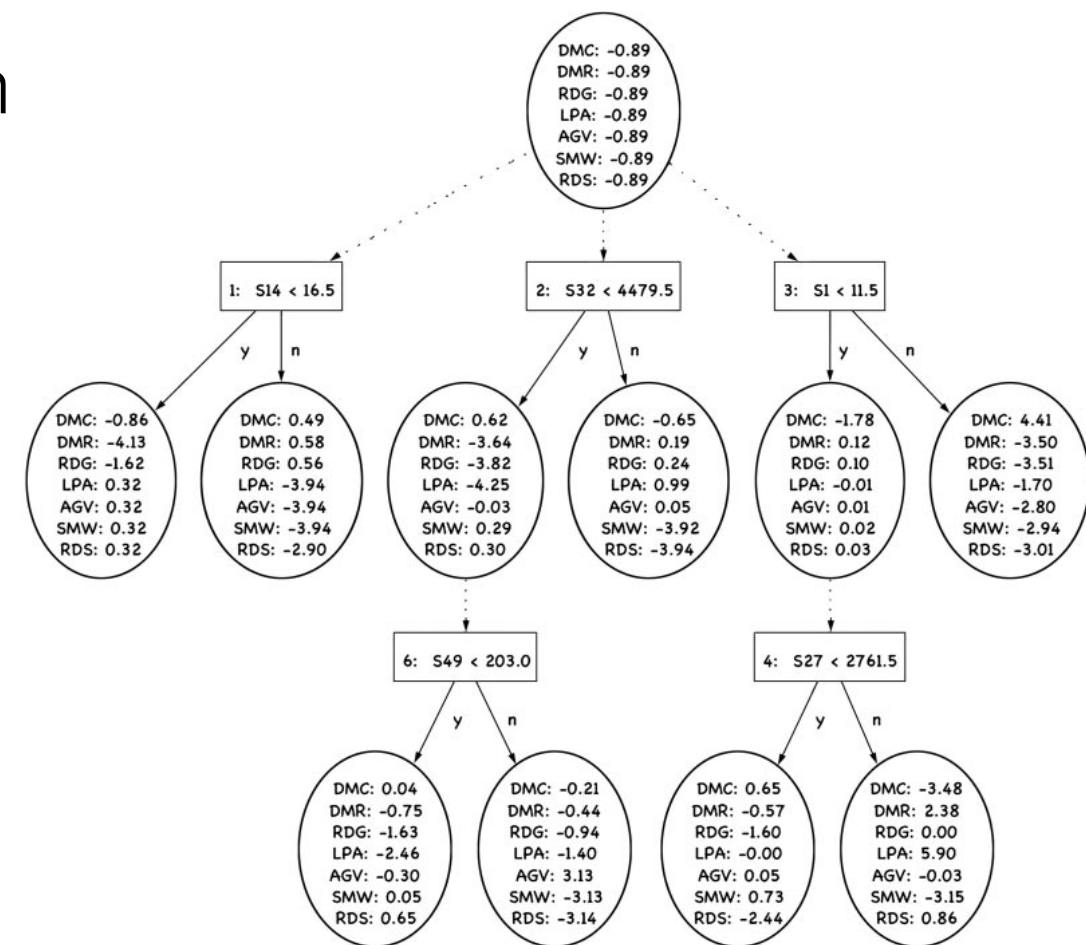
model testing : scale-free networks

- *the problem*: all models fit the observed degree distribution



model testing : scale-free networks

- *the solution*: build a **classifier** that can **distinguish** networks generated by the 5 models + 2 controls **based on their motif frequencies**
- use decision trees + Adaboost (very powerful) to **learn which motifs** distinguish the models
- *validated* on synthetic graphs with known structure:



Truth	Prediction						
	DMR	DMC	AGV	LPA	SMW	RDS	RDG
DMR	99.3	0.0	0.0	0.0	0.0	0.1	0.6
DMC	0.0	99.7	0.0	0.0	0.3	0.0	0.0
AGV	0.0	0.1	84.7	13.5	1.2	0.5	0.0
LPA	0.0	0.0	10.3	89.6	0.0	0.0	0.1
SMW	0.0	0.0	0.6	0.0	99.0	0.4	0.0
RDS	0.0	0.0	0.2	0.0	0.8	99.0	0.0
RDG	0.9	0.0	0.0	0.1	0.0	0.0	99.0

model testing : scale-free networks

- *then pass the classifier the real PPIN*

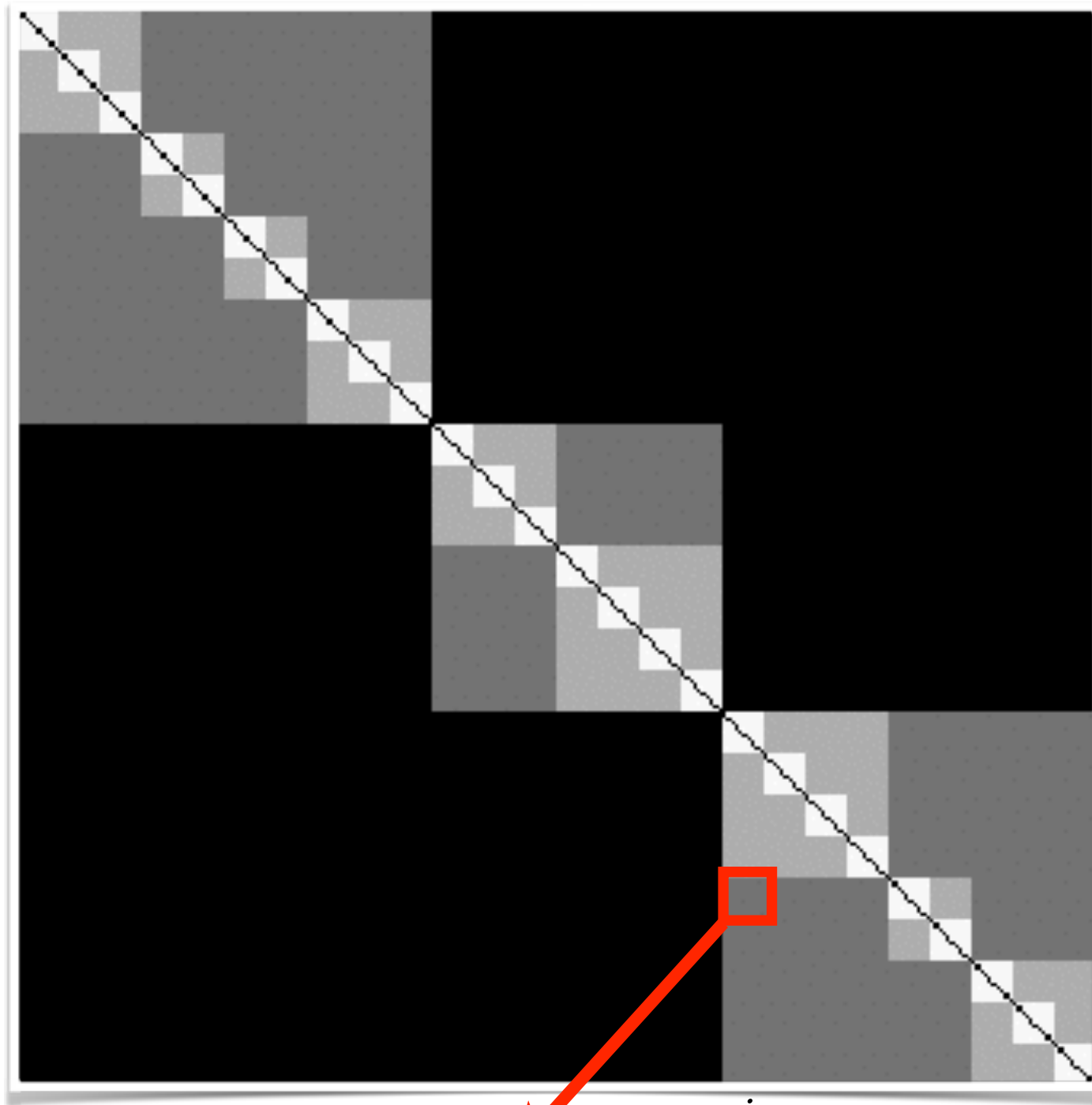
Rank	Eight-step subgraphs ($p^* = 0.65$)		Subgraphs with up to seven edges ($p^* = 0.65$)	
	Class	Score	Class	Score
1	DMC	8.2 ± 1.0	DMC	8.6 ± 1.1
2	DMR	-6.8 ± 0.9	DMR	-6.1 ± 1.7
3	RDG	-9.5 ± 2.3	RDG	-9.3 ± 1.6
4	AGV	-10.6 ± 4.2	AGV	-11.5 ± 4.1
5	LPA	-16.5 ± 3.4	LPA	-14.3 ± 3.2
6	SMW	-18.9 ± 0.7	SMW	-18.3 ± 1.9
7	RDS	-19.1 ± 2.3	RDS	-19.9 ± 1.5

- **risks**: we sometimes fall in love with our models
- **opportunities**: statistics offers powerful tools for model testing
- **difficulties**: requires learning new tools, and bravery

prediction : link prediction

- *how can we evaluate how good a model is?*
- **cross-validation**
 - hold out some data
 - fit the model to what remains
 - quantify model's ability to predict held-out data
- for networks, this usually means *link prediction*
- to do this well, we use **probabilistic generative models**

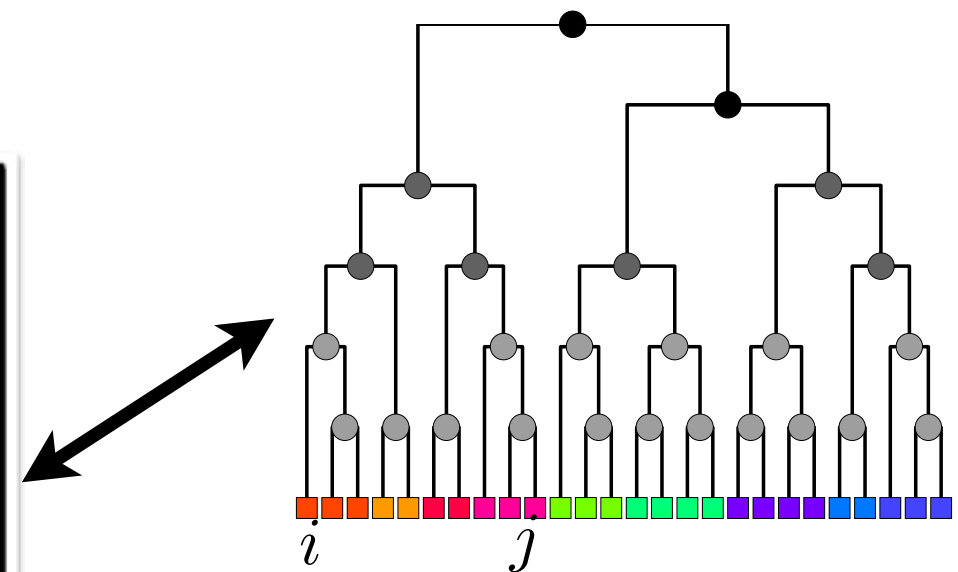
hierarchical random graph (HRG)



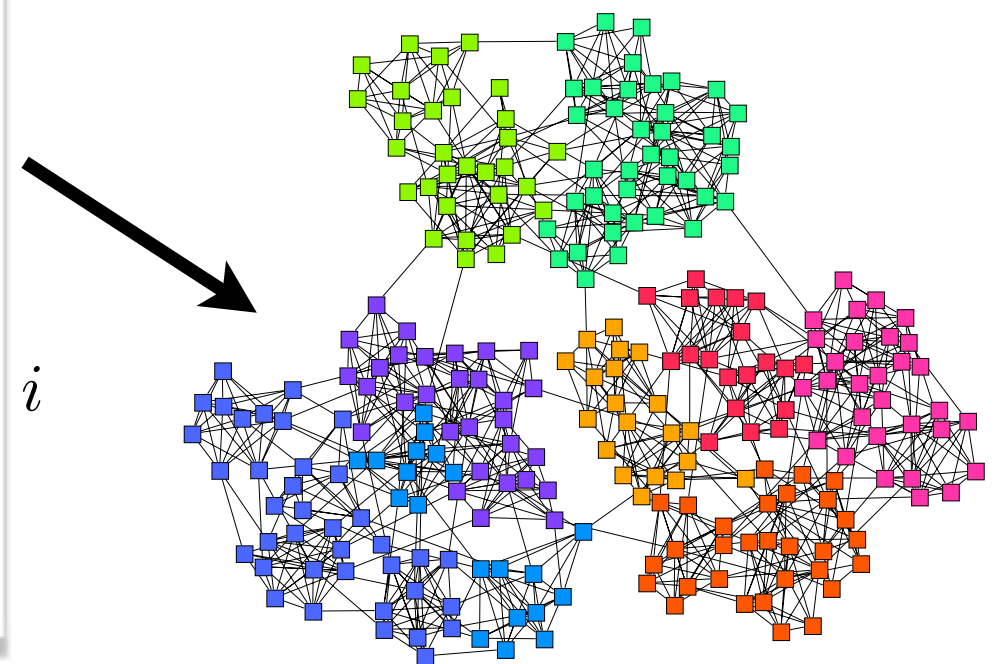
$$\Pr(i, j \text{ connected}) = p_r$$

$$= p_{(\text{lowest common ancestor of } i, j)}$$

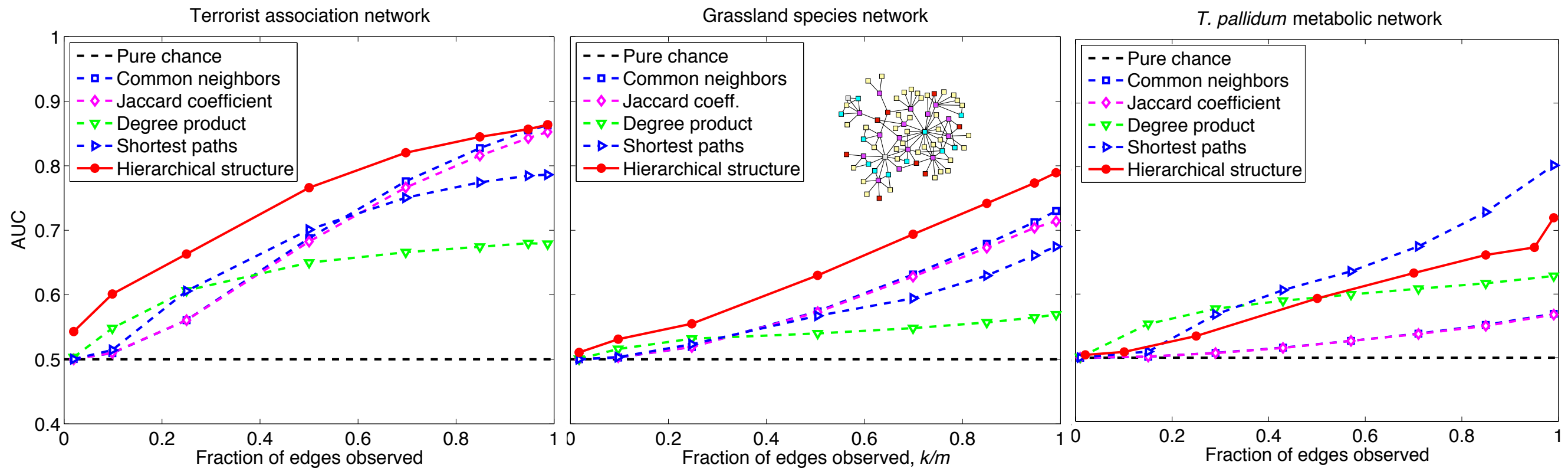
model



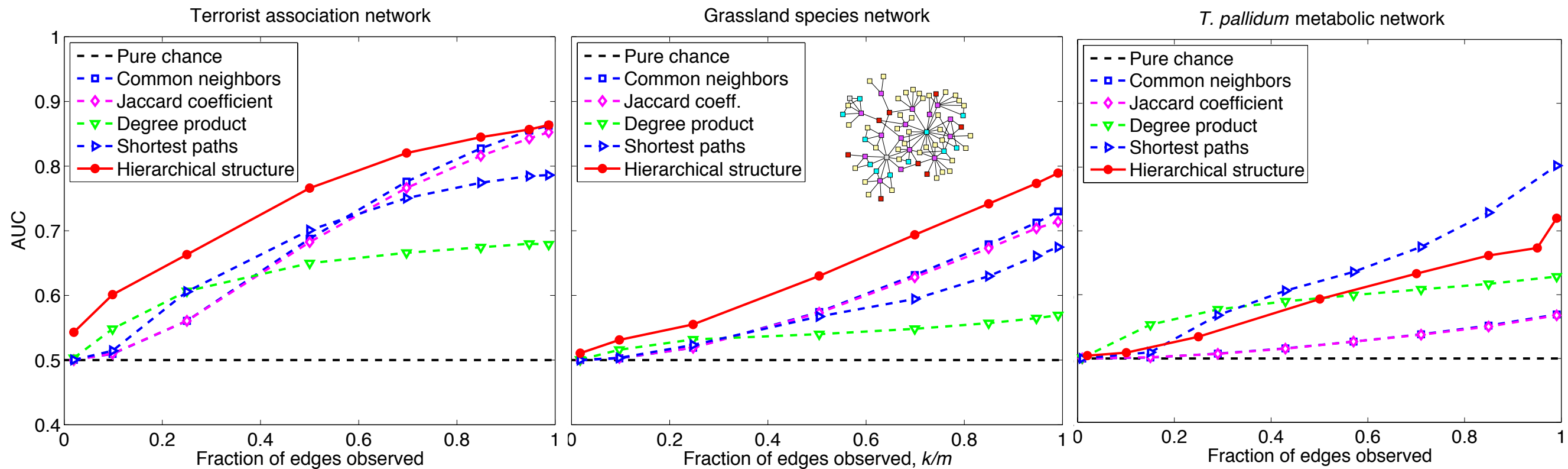
instance



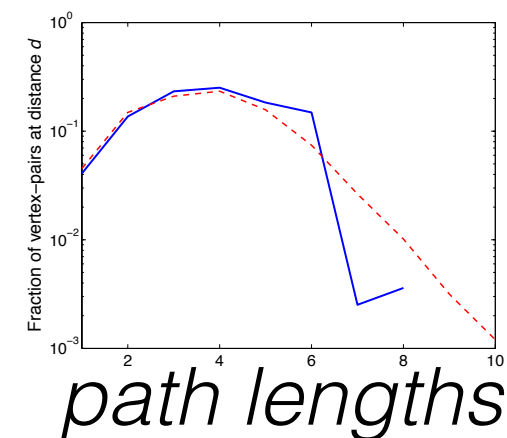
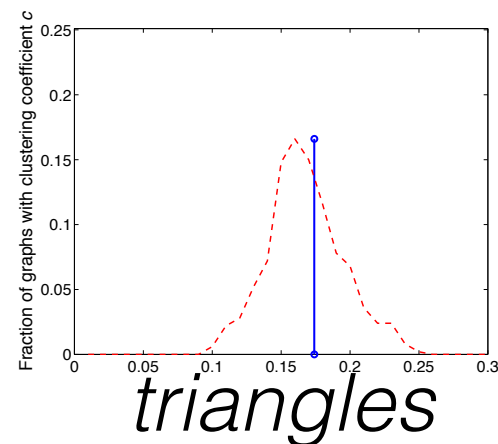
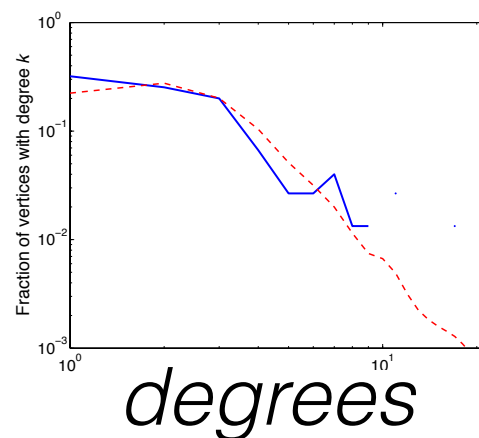
prediction : link prediction



prediction : link prediction



and reproduces motifs and other patterns



prediction : link prediction

- link prediction is a **hard** form of validation
- simple and clear evaluation measure
- **risks**: overfitting
cross-validation *not* well-defined for networks
we care about more than missing links
- **opportunities**: data driven with up-front assumptions
generative models quantify uncertainty, predict missing data
- **difficulties**: usually non-mechanistic (predictive but not explanatory)
how do we test more complicated predictions?

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- statistics are the foundation of a data-driven Network Science.
- **exploration** — what patterns need to be explained?
- **model testing** — how well can I capture those patterns?
- **prediction** — how well can I predict missing / future patterns?
- **the BIG risk:** we'll reinvent statistics, slowly, haltingly
- **the BIG opportunity:** we'll use modern Statistics to be better scientists, to find truth more quickly, accurately
- **the BIG difficulty:** Statistics is hard



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