Evaluating infectious disease forecasts with allocation scoring rules

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Abstract

Recent years have seen increasing efforts to forecast infectious disease burdens, with a primary goal being to help public health workers make informed policy decisions. However, there has only been limited discussion of how predominant forecast evaluation metrics might indicate the success of policies based in part on those forecasts. We explore one possible tether between forecasts and policy: the allocation of limited medical resources so as to minimize unmet need. We use probabilistic forecasts of disease burden in each of several regions to determine optimal resource allocations, and then we score forecasts according to how much unmet need their associated allocations would have allowed. We illustrate with forecasts of COVID-19 hospitalizations in the US, and we find that the forecast skill ranking given by this allocation scoring rule can vary substantially from the ranking given by the weighted interval score. We see this as evidence that the allocation scoring rule detects forecast value that is missed by traditional accuracy measures and that the general strategy of designing scoring rules that are directly linked to policy performance is a promising direction for epidemic forecast evaluation.

1 Introduction

Infectious disease forecasting models have emerged as important tools in public health outbreak response. Predictions of disease dynamics have been used to inform decision making about a wide variety of measures to reduce disease spread and/or mitigate the severity of disease outcomes. For example, estimates of expected onset of flu season have been used to aid national vaccination strategies (Igboh et al., 2023), and forecasts of Ebola and diptheria dynamics have been used to allocate resources (Meltzer et al., 2014; Rainisch et al., 2015; Camacho et al., 2015; Finger et al., 2019). Bertsimas et al. (2021) developed tools to guide decision making from infectious disease forecasts, which have been used to inform allocation of limited resources such as ventilators, ICU capacity, and vaccine supply. Models developed by Fox et al. (2022) have been used to inform resource and care site planning, as well as community guidelines for masking, traveling, dining and shopping (University of Texas, 2022).

In the wake of the COVID-19 pandemic, researchers have been calling for evaluating forecasts through their impact on policy (Marshall et al., 2023; Bilinski et al., 2023). The value of infectious disease forecasts has typically been measured by how closely they predict disease outcomes such as cases, hospitalizations or deaths using, for example, root mean square error (RMSE) (Papastefanopoulos et al., 2020), log-score (McGowan et al., 2019), or weighted interval score (WIS) (Bracher et al., 2021). However, as we show in this paper, these metrics only evaluate one specific dimension of accuracy, and often do not have a clear correspondence to features that would make a forecast valuable in the context

of a specific decision. While these ideas have received little attention in the context of infectious disease forecasting, the results are well known from other fields, such as economics and finance, supply chain management, and meteorology.

In decision making settings where it is possible to quantify the utility or loss associated with a particular action, standard tools of decision theory provide a procedure for developing forecast scoring rules that measure the value of forecasts through the quality of the decisions that they lead to (see details in Section 2.2.1). We refer the reader to Yardley and Petropoulos (2021) for a general overview, and to Pesaran and Skouras (2002) and Murphy (1993) for discussions focused on applications to economics and meteorology, respectively. In this framework, a forecast has value if it leads to decisions with low total costs. As one example, in meteorology, policy makers need to balance the costs of implementing protective measures with the costs of potentially preventable weather damages (Palmer, 2002; Pappenberger et al., 2015). Across many fields, analyses have consistently found that common measures of forecast accuracy do not necessarily correspond directly to measures of the value of forecasts as an input to decision making (e.g., Leitch and Tanner, 1991; Murphy, 1993; Cenesizoglu and Timmermann, 2012).

We are aware of only a limited body of work that explicitly attempts to measure the value of infectious disease forecasts through their impact on policy. For example, Ioannidis et al. (2022) discuss the possible negative consequences of inaccurate forecasts of infectious disease, but do not attempt to quantify the utility or loss incurred as a result of those forecasts. Bilinski et al. (2023) explore ways in which policymaker preferences could inform risk thresholds for predictive models using a framework for measuring the costs and losses associated with taking an action that is similar to methods that have been used in meteorology and elsewhere. Marshall et al. (2023) develop a forecast scoring rule that is informally motivated by utility considerations, but the score is not derived from a decision-theoretic set up. Separately, there is a thread of literature that quantifies the link between infectious disease modeling and policy making outside of a forecasting context. As an example, Probert et al. (2016) develop measures of the cost of actions designed to control a hypothetical outbreak of foot-and-mouth disease and use this framework to explore policy recommendations from a variety of simulation-based projection models.

In practice, probabilistic infectious disease forecasts have most often been made for observations that emerge from public health surveillance systems and have typically been evaluated with common scoring rules that have implementations available in existing software packages. For example, seasonal influenza forecasts in the US and dengue forecasts for Peru and Puerto Rico targeted public health surveillance measures of incidence over time and space, and used log-score and mean absolute errors to evaluate forecast skill (McGowan et al., 2019; Reich et al., 2019; Johansson et al., 2019). Pandemic COVID-19 forecasts of observed cases, hospitalizations and/or deaths in the US and Europe, as reported by municipal, state, or federal surveillance systems, were evaluated using the weighted interval score (WIS, which is an approximation of the continuous ranked probability score, or CRPS), and prediction interval coverage (Cramer et al., 2022a; Fox et al., 2022; Sherratt et al., 2023). Similarly, CRPS was also used to assess probabilistic forecasts of dengue incidence at the district level in Vietnam (Colón-González et al., 2021). While some of these scores can be interpreted through the lens of decision theory, and all of the application-specific papers cited above have benefited from direct collaboration with public health agencies, none of them make explicit connections between forecast evaluation and how a forecast was used in practice.

In this work, we begin to fill this gap between the ways that infectious disease forecasts have traditionally been evaluated and the ways that they have been used to support public health policy. We consider a setting in which forecasts are used to help determine the allocation of a limited quantity of medical supplies across multiple regions. In section 2 of the paper, we define a new forecast scoring rule — the allocation score — that evaluates forecasts based on how beneficial resource allocations derived from them would turn out to be.

In section 3, we present an illustrative analysis using the allocation score to evaluate forecasts of hospital admissions in the US leading up to the Omicron wave in winter 2022. This analysis is "synthetic" in that it does not correspond to an actual analysis that supported decision making in real time. However, the framework described in this paper corresponds to real-world decisions that must be made by public health administrators around the globe, and could be adapted in the future for such real-time situations such as informing bed demand, ventilator usage, or doses needed for specific medications. However, we emphasize again that these studies did not take the step of evaluating forecasts based on the quality of the allocation decisions that they supported or could have been used to support.

2 The Allocation Score

We begin with an informal description of the allocation score and some examples illustrating its key characteristics in section 2.1. In section 2.2 we develop the allocation score more carefully, using a decision theoretic procedure for deriving proper scoring rules. (See section 2 of the supplement for a definition of a proper scoring rule and a more technical discussion of the procedure). In section 2.3, we note that another group of common scores including the quantile score, WIS, and CRPS, can also be derived from decision theoretic foundations —starting from a different decision making context.

2.1 Overview of Allocation Scoring

Suppose that a decision maker is tasked with determining how to allocate K available units of a resource across N locations. If the decision maker is provided with a multivariate forecast F where each marginal forecast distribution F_i predicts resource need in a particular location, one option is to choose the resource allocation that minimizes the expected total unmet need according to the forecast. We will give a more precise mathematical statement in section 2.2, but informally, the total expected unmet need according to the forecast is

$$\sum_{i=1}^{N} \mathbb{E}_{F_i}[\text{unmet need in location } i], \tag{1}$$

where the unmet need in a particular location is the difference between resource need in that location and the number of resources that were allocated there. This allocation problem has an intuitively appealing solution: allocate so that the probabilities of need exceeding allocation in various locations are as close to each other as possible. This will lead to the allocations provided by F being quantiles of the marginal distributions F_i for some single probability level τ that is shared in common for all locations.

After time passes and the actual level of resource need has been observed, the quality of a selected allocation can be measured by comparing the actual need in each location to the amount of resources that were sent there. Specifically, we compute the total unmet need that resulted from the selected

allocation:

$$\sum_{i=1}^{N} \text{unmet need in location } i. \tag{2}$$

One allocation is better than another if it results in lower total unmet need, and one forecast is better than another if the allocation derived from it results in lower total unmet need.

The allocation score of the forecast F is the avoidable unmet need that results from using the allocation that minimizes the expected unmet need according to that forecast. By "avoidable unmet need", we mean that the allocation score does not include the amount of unmet need that was inevitable simply because the amount of available resources K was less than the need for resources. Rather, the allocation score measures the unmet need that could have been avoided by an oracle that knows exactly how much need will occur in each location and divides the amount K so that nothing is wasted in one location while it could be put to use in another. An allocation score of 0 is optimal, and indicates that no other allocation of resources could have met need better than the allocation suggested by F. A larger allocation score indicates that it would have been possible to improve upon the allocation suggested by F.

Example 1 Suppose we have a forecast F for need in two locations with $F_1 = \text{Exp}(1/\sigma_1)$ and $F_2 = \text{Exp}(1/\sigma_2)$, where $\sigma_1 = 1$ and $\sigma_2 = 4$. The means of these distributions are given by the scale parameters σ_i . When the marginal forecasts are exponential distributions, it can be shown that the optimal allocation divides the available resources among the locations proportionally to the scale parameters σ_i (see section 4 of the supplemental materials). If K = 5 units of the resource are available, the optimal allocation according to F would be 1 unit of resources in location 1 and 4 units of resources to location 2. If, on the other hand, K = 10 units are available, we will allocate 2 units of resources to location 1 and 8 units to location 2. Figure 1 illustrates the situation.

Next suppose that we observe resource needs of 1 and 10 in locations 1 and 2, respectively. Based on these observed needs, we can measure the quality of the allocation suggested by the forecast by calculating the amount of unmet need that resulted from that allocation over and above what was unavoidable given the resource constraint. With K=5 units of the resource, the allocation based on the forecast exactly meets the observed need in location 1, but it leaves 6 units of need unmet in location 2. However, working within the resource constraint, no other allocation could have done better: for example, allocating 0 units of resources to location 1 and 5 to location 2 still results in a total unmet need of 6 across both locations. Therefore, the forecast's allocation score is 0 with K=5. On the other hand, when K=10, the forecast's allocation results in 10-8=2 units of unmet need in location 2 despite leaving no need unmet in location 1. In this case, the oracle would be able to prevent all but 1 of the total 11 units of need from going unmet, for example by allocation 1 unit of resources to location 1 and the remaining 9 units of resources to location 2. The allocation score for the forecast when K=10 would therefore be 1 (= 2 realized - 1 unavoidable) in units of avoidable unmet need.

These scores illustrate a general result: allocation scores for a forecast will tend to be larger when the resource constraint is close to the observed need, because this is when it matters most which locations are allocated more or less resources. If the available resources are small compared to the observed need, any allocation of those limited resources will result in a large amount of unmet need. If the available resources are comparatively larger, it becomes less important which locations receive relatively more



Figure 1: An illustration of the resource allocation problem in Example 1. There are N=2 locations, with predictive distributions $F_1=\mathrm{Exp}(1)$ and $F_2=\mathrm{Exp}(1/4)$. The cumulative distribution functions of these distributions are illustrated in the panels at bottom and right. In the center panel, the background shading corresponds to the expected loss according to these forecasts. Diagonal black lines indicate resource constraints at K=5 and K=10 units; any point along those lines corresponds to an allocation that meets the resource constraint. For these forecasts, the optimal allocations are (1,4) for K=5 and (2,8) for K=10. These allocations are at the point on the constraint line where the expected loss is smallest, which also corresponds to the point where a level set of the expected loss surface (blue curve) is tangent to the constraint.

or fewer resources because all locations will receive enough resources to meet their need. In either of these extremes of resource availability, the avoidable unmet need that arises from the allocation suggested by a forecast (i.e., the forecast's allocation score) will tend to be small.

Example 2 Now consider a different forecast that also has exponential distributions for resource need in each location, but that has the scale parameters $\sigma_1 = 2$ and $\sigma_2 = 8$, twice as large as the scale parameters of the forecast in Example 1. Because the optimal allocation is proportional to the scale parameters, this forecast would lead to the same allocations as the forecast in Example 1, and would therefore be assigned the same allocation score.

Examination of these results leads to two observations. First, the reason that these forecasts had a positive (i.e., non-optimal) allocation score at K=10 is that they did not get the relative magnitude of resource need across the two locations right: the realized need was 10 times as large in location 2 as in location 1, but the forecasts only indicated that the resource allocation for location 2 should be 4 times the allocation for location 1. At its core, the allocation score measures whether the forecast accurately captures the relative magnitudes of resource need across different locations, which is precisely the information that is needed to allocate resources to those locations subject to a fixed resource constraint.

A second observation is that the forecasts in examples 1 and 2 predicted different mean levels of resource needs, but had the same allocation score. The allocation score does not directly measure whether the forecasts correctly capture the absolute magnitude of resource need in each individual location. This stands in contrast to other common scoring methods that aggregate scores such as log score, CRPS, or WIS for each location, where a poor forecast for one location is penalized regardless of alignments in other units.

2.2 A decision theoretic development of the allocation score

We give a high-level review of a general procedure for developing proper scoring rules that are tailored to specific decision making tasks in section 2.2.1, and then in section 2.2.2 we apply that procedure to develop the allocation score based on the task of deciding on how to allocate a fixed supply of resources across multiple locations. In 2.2.3 we consider a small extension where the resource constraint is not known, or it is desired to consider the value of forecasts across a range of decision making scenarios. This gives rise to the *integrated allocation score*.

2.2.1 The decision theoretic setup for forecast evaluation

In the framework of decision theory, a decision corresponds to the selection of an action x from some set of possible actions \mathcal{X} . For example, x may correspond to the level of investment in a measure designed to mitigate severe disease outcomes such as hospital beds, ventilators, medication, or medical staff, with \mathcal{X} being the set of all possible levels of investment that we might select. The quality of a decision to take a particular action x is measured in relation to an outcome y that is unknown at the time the decision is made. For example, y may correspond to the number of individuals who eventually become sick and would benefit from the mitigation measure, and informally, an action x is successful to the extent that it meets the realized need. In the face of uncertainty, a decision maker may use a forecast F of the random variable Y to help inform the selection of the action to take. We measure the value of a forecast as an input to this decision making process by the quality of the decisions that it leads to.

We can formalize the preceding discussion with the following three-step procedure for developing scoring rules for probabilistic forecasts:

- 1. Specify a loss function s(x,y) that measures the loss associated with taking action x when outcome y eventually occurs.
- 2. Given a probabilistic forecast F, determine the Bayes act x^F that minimizes the expected loss under the distribution F.
- 3. The scoring rule for F calculates the score as the loss incurred when the Bayes act was used: $S(F,y) = s(x^F,y)$.

This is a general procedure that may be applied in settings where it is possible to specify a quantitative loss function. We call a scoring rule obtained from this procedure a *Bayes scoring rule* and in section 2 of the supplement we demonstrate that Bayes scoring rules are proper by construction (a result also shown by Dawid (2007); Gneiting and Raftery (2007)).

2.2.2 The allocation score for a fixed resource constraint

In the decision making setting that we consider, an action $x = (x_1, \ldots, x_N)$ is a vector specifying the amount that is allocated to each of N locations. We require that $0 \le x$, i.e., that each x_i is nonnegative, and that the total allocation across all locations equals the amount of available resources, $K: \sum_{i=1}^N x_i = K$. The set \mathcal{X} consists of all possible allocations that satisfy these constraints. The eventually realized resource need in each location is denoted by $y = (y_1, \ldots, y_N)$. These levels of need are not known at the time of decision making, so we define the random vector $Y = (Y_1, \ldots, Y_N)$ where Y_i represents the as-yet-unknown level of resource need in location i. Forecasts of need in each location are collected in $F = (F_1, \ldots, F_N)$. We assume that resource need is non-negative and the forecasts reflect that, i.e. the support of each Y_i is a subset of \mathbb{R}^+ . Finally, we assume that each unit of unmet need incurs a loss denoted by Y_i , so that if the selected resource level Y_i in location Y_i is less than the realized need Y_i , a loss of Y_i results. A variety of extensions to this setup are possible; for example, we might account for storage costs for resources that go unused, allow for a different loss per unit of unmet need in each location, or account for resource transportation costs. In this work, we choose to keep the loss function relatively simple to focus on the core ideas.

It is helpful to clearly distinguish between the time t_d when a decision is made about a public health resource allocation and the time t_r when resource needs that might be addressed by that allocation occur. Our setup assumes that $t_d < t_r$. Additionally, the structure of our loss captures a setting where the resource in question does not impact the amount of demand that will materialize at time t_r , but rather it is a resource that satisfies that demand. In the context of infectious disease, this means that we do not consider resources that are intended to reduce the number of people who will become sick at some point in the future, such as a preventative influenza or COVID-19 vaccine. Instead, our setup addresses resources like hospital beds, oxygen supply, or ventilators which are intended to meet the medical needs of patients who are already sick. Additionally, our setup addresses decision-making that is related to resource needs only at the time t_r ; we do not explicitly consider sequences of multiple decisions that are made over time or account for the impact of decisions on resource needs at any time other than t_r . We outline some opportunities to extend our work to more complex decision making settings in the discussion.

With this problem formulation in place, we can develop a proper scoring rule following the outline in

section 2.2.1.

Step 1: specify a loss function. The loss associated with a particular allocation is calculated by summing contributions from unmet need in each location:

$$s_A(x,y) = \sum_{i=1}^{N} L \cdot \max(0, y_i - x_i).$$
 (3)

Here, $\max(0, y_i - x_i)$ is the unmet need in location i, which is given by $y_i - x_i$ if the realized need y_i in location i is greater than the amount x_i allocated to that location, or 0 if the amount x_i allocated to unit i is greater than or equal to the realized need. Also, L is a constant scalar value, the same across all locations, specifying the "cost" of one unit of unmet need.

Step 2: Given a probabilistic forecast F, identify the Bayes act. The Bayes act associated with the forecast, $x^{F,K}$, is the allocation that minimizes the expected loss, that is, the solution of the allocation problem associated with K:

$$\underset{0 \le x}{\text{minimize }} \mathbb{E}_F[s_A(x,Y)] \text{ subject to } \sum_{i=1}^N x_i = K, \tag{4}$$

where $\mathbb{E}_F[s_A(x,Y)] = \sum_{i=1}^N L \cdot \mathbb{E}_{F_i}[\max(0,Y_i-x_i)]$ sums the expected loss due to unmet need across all locations.

In the supplement we show that the components of the Bayes act are quantiles $x_i^{F,K} = F_i^{-1}(\tau^{F,K})$ at a probability level $\tau^{F,K}$ that depends on the forecast F and the resource constraint K, but is shared across all locations. This probability level is the level at which the resource constraint is satisfied: $\sum_{i=1}^{N} F_i^{-1}(\tau^{F,K}) = K.$ This tells us that in order to allocate optimally (according to F), we must divide resources among the locations so that there is an equal forecasted probability in every location that the allocation is sufficient to meet resource need. This solution to the allocation problem is well-known in inventory management and is often attributed to Hadley and Whitin (1963).

Step 3: Define the scoring rule. We can now use the Bayes act to define a proper scoring rule for the probabilistic forecast F. Consider first the "raw" score defined as

$$S_A^{\text{raw}}(F, y; K) = s_A(x^{F,K}, y) = \sum_{i=1}^N L \cdot \max(0, y_i - x_i^{F,K}).$$
 (5)

This measures the total unmet need across all locations that results from using the Bayes allocation associated with the forecast F when the actual level of need in each location is observed to be y_i .

To make this a more easily interpreted measure of forecast performance, we will adjust the raw score by subtracting the minimum loss achievable by an *oracle* allocator which has precise foreknowledge of the outcomes y_i . When the oracle has sufficient resources to meet the total need, i.e., when $\sum_{i=1}^{N} y_i \leq K$, the oracle's loss is zero and allocation score coincides with the raw score. On the other hand, when the oracle cannot cover all need and incurs a loss of $L \cdot \left(\sum_{i=1}^{N} y_i - K\right) > 0$, we adjust the raw score

by this loss. The oracle-adjusted score can therefore be written as

$$S_A(F, y; K) = S_A^{\text{raw}}(F, y; K) - L \cdot \max\left(0, \sum_{i=1}^N y_i - K\right)$$

$$\tag{6}$$

$$= L \left\{ \sum_{i=1}^{N} \max(0, y_i - x_i^{F,K}) - \max\left(0, \sum_{i=1}^{N} y_i - K\right) \right\}.$$
 (7)

The oracle adjustment aligns with a common theme in economic decision theory that *opportunity loss* (often known as *regret* or (negative) *relative utility*) is often a more important quantity than absolute loss (see e.g., Diecidue and Somasundaram (2017)).

2.2.3 Integrating the allocation score across resource constraint levels

The allocation score S_A that we developed in the previous section measures the skill of the forecast distributions F based on a single probability level $\tau^{F,K}$. This is appropriate if the resource constraint K is a known constant. However, if K is not precisely known at the time of decision making or there is interest in measuring the value of forecasts across a range of decision making scenarios with different resource constraints, we can use an *integrated allocation score* (IAS) that integrates the allocation score across values of K, weighting by a distribution p:

$$S_{IAS}(F, y) = \int S_A(F, y; K) p(K) dK$$

We note that the device of considering a range of hypothetical decision makers or decision making problems with different problem parameters has been employed in the past (e.g., Murphy, 1993).

2.3 Connections to Other Scores

The weighted interval score (WIS) was proposed in 2020 as a way to score forecasts that were being made in the early stages of the COVID-19 pandemic (Bracher et al., 2021); equivalent scores had also been used in previous forecast evaluation efforts (e.g., Hong et al., 2016). The WIS is a proper scoring rule for forecasts that use a set of quantiles to represent a probabilistic forecast distribution. While pointing a reader interested in more mathematical detail to Bracher et al. (2021), we note simply that the WIS is a weighted sum of interval scores at different probability levels (e.g., 50% prediction intervals, 80% PIs, 95% PIs, etc...). Larger interval scores indicate less skillful forecasts. An interval score consists of (a) the width of the interval, with larger intervals receiving higher scores (higher scores indicate less accuracy), and (b) a penalty if the interval does not cover the eventual observation, which increases the further away the interval is from the observed value. Equivalently, the WIS can also be characterized as a weighted sum of quantile scores for each individual predictive quantile. The quantile score for a particular quantile level assigns an asymmetric penalty to predictions that are too high or too low, with the relative sizes of the penalties set so that in expectation the score is minimized by the given quantile of the distribution. The most commonly used version of WIS is one that uses an equal weighting of all quantile levels, in which case WIS approximates the continuous ranked probability score (CRPS), a commonly used score for probabilistic forecasts. It is important to note that this weighting was proposed because the resulting score approximates the CRPS, and not because it aligned with any particular public health decision-making rationale.

That said, the quantile score and WIS can be derived using the same decision theoretic procedure that

we outlined in section 2.2. In fields such as meteorology and supply chain management, a great deal of attention has been given to the problem where a decision must be made about the quantity of a resource to purchase for a single location in the face of a fixed cost C for each unit of the resource and a loss L that will be incurred for each unit of unmet need. This leads to the quantile score for the probability level $\tau = 1 - C/L$. From this point, the WIS or CRPS can be obtained by averaging across a range of decision making settings with different cost and loss parameters, using a similar motivation that we used to obtain the IAS from the AS in section 2.2.3 (Gneiting and Ranjan, 2011).

3 Evaluating forecasts of COVID hospitalizations using the allocation score

We illustrate with an application to hospital admissions in the U.S., considering a hypothetical problem of allocating a limited supply of medical resources to states.

3.1 Data

The US COVID-19 Forecast Hub collected short-term forecasts of daily new hospital admissions for individuals with COVID-19 starting in December 2020 (Cramer et al., 2022b). The target data for these forecasts were hospital admissions as reported by the US Department of Health and Human Services through the HealthData.gov website. Forecasts were probabilistic predictions of the number of new hospital admissions on a particular day in the future, in a specific jurisdiction of the US (national level, state, or territory). Probability distributions were represented using a set of 23 quantiles for each individual prediction, including a median and the lower and upper limits of 11 central prediction intervals, from a 99% to a 10% prediction interval.

The analysis in this work focuses on forecasts made before and during the first wave of the Omicron SARS-CoV-2 variant in the US. As such, we analyzed forecasts for the 15 weeks starting with Monday November 22, 2021 through Monday February 28, 2022.

Submission to the Forecast Hub followed a weekly cycle, and each Monday the Hub collected the most recent forecasts submitted by all teams that met certain inclusion criteria and created ensemble forecasts using quantile averaging (Ray et al., 2023). Our analysis includes these ensembles (COVIDhubensemble and COVIDhub-trained ensemble) as well as one other ensemble of hub models created by another team (JHUAPL-SLPHospEns) and several other individual models. Models were eligible to be included in the analysis if they were designated as a "primary" model from a team. For a model to have a complete, eligible submission in a given week, it had to have a 14 day-ahead forecast for all 50 states plus Washington DC. Models had to have a complete forecast for at least 4 of the 15 weeks in the analysis to be eligible for inclusion.

The hospitalization data used for scoring forecasts were downloaded on February 01, 2024.

3.2 Evaluation metrics

We measured forecast skill using two forecast scores, the allocation score (AS) and the weighted interval score (WIS), both defined above. We computed these scores for the 14 day ahead forecasts made each week. For this analysis, we fixed the resource constraint used for the AS to be K = 15,000, based

roughly on a reported number of ventilators available for reallocation in the US (Ajao et al., 2015). We computed the mean WIS (MWIS) across all of the forecasted state-level locations.

For both scores, we also computed models standardized rank among all models that submitted forecasts each week. The standardized rank is between 0 and 1, where 0 corresponds to the worst rank and 1 to the best. In the case of a tie between one or more models, all models received the better rank.

As described above, predictions were submitted to the Forecast Hub in the form of a set of 23 quantiles of the predictive distribution. The WIS can be directly calculated from these quantiles. However, calculation of the AS requires that the full cumulative distribution functions of the forecast distributions for each location are available. For the purpose of this analysis, to calculate the allocation score we approximated the full cumulative distribution functions based on the provided quantiles. On the interior of the provided quantiles we used a monotonic cubic spline to interpolate the quantiles, and in the lower and upper tails we used normal distributions with parameters selected so as to match the two lowest and two highest quantiles (see the supplement for further details). In the supplement, we show that if this evaluation procedure had been specified prospectively, the resulting score would be proper —but a post hoc application of this procedure is improper. We use the procedure here to illustrate the properties of the score, and note that a forecaster or collaborative forecasting exercise interested in using the allocation score for evaluation could circumvent issues with propriety through thoughtful elicitation of representations of forecast distributions or by collecting the allocations at specified resource levels as part of forecast submissions.

3.3 Allocation benchmarks

To adequately compare allocations from individual models with existing standard practices, we used two benchmarks against which the performance of using forecasts to inform allocations could be evaluated. First, we evaluated forecasts from the COVIDhub-baseline model, which predicts a flat line from the most recent observation with uncertainty bounds based on a random walk, and the allocations that resulted from those forecasts (Cramer et al., 2022a). Second, we generated a proposed set of allocations on a per capita basis by state (using US Census data of vintage 2022 (United States Census Bureau, 2022)), referred to below as per-capita. These two approaches generally reflect common choices for "best practices" of allocation: either allocating resources based on the most recent observed data, or in proportion to the population of each location. As such, they serve as good comparisons for allocations based on forecast models.

3.4 Data and code availability

All forecast data used in this evaluation are available through the COVID-19 Forecast Hub (Cramer et al., 2022b). An R package implementing the allocation score is available at https://github.com/aaronger/alloscore. All code and data for the analyses presented in this manuscript are available at https://github.com/aaronger/utility-eval-papers. The analyses were generated using a reproducible workflow using R version 4.3.1 (2023-06-16) and the targets package (R Core Team, 2023; Landau, 2021).

3.5 Application results

3.5.1 Anatomy of forecast scores for one week

To illustrate the mechanics of allocation scoring, we start by focusing on how forecasts generated on or before December 20, 2021, with predictions for January 03, 2022, were scored by different metrics. This week was around the peak of the Omicon wave nationally, with individual states typically observing a peak at or after January 3, 2022.

Of the 10 models evaluated, the CU-select model had the most accurate forecasts according to the allocation score while the USC-SI_kJalpha model had the most accurate forecasts based on MWIS (Table 1). The JHUAPL-Bucky model had the second best MWIS but the third worst allocation score.

Model	AS	MWIS	IAS centered at 15k	IAS uniform
CU-select	669	133	774	326
per-capita	865		1029	366
COVIDhub-ensemble	873	159	1067	438
USC-SI_kJalpha	995	91	1216	1097
JHUAPL-Gecko	1034	164	1141	418
MUNI-ARIMA	1084	169	1248	440
$COVIDhub-trained_ensemble$	1089	169	1271	823
COVIDhub-baseline	1175	170	1317	535
JHUAPL-Bucky	1358	102	1566	1214
JHUAPL-SLPHospEns	1540	129	1604	1102
UVA-Ensemble	2469	213	2635	2494

Table 1: For one illustrative week, a comparison of allocation scores (AS), mean weighted interval scores (MWIS), and two varieties of Integrated Allocation Scores (IAS). All metrics are shown for 10 models that made forecasts of hospital admissions for 2022-01-03. Results are sorted by AS. For all metrics, lower scores indicate better accuracy.

A comparison of the forecasts from the JHUAPL-Bucky and CU-select models shows that while the JHUAPL-Bucky forecast distributions were closer to the eventual observations in many states, the allocations suggested by those forecasts often were more inefficient than those from the CU-select model (Figure 2). In the example of this one week, JHUAPL-Bucky had a worse allocation score than CU-select because its forecasts led to allocations that sent excess resources to several states, such as Ohio, Pennsylvania, and Michigan, that would have been more effectively allocated to states that did receive enough resources to meet their needs, such as Florida and California (Figure 3A). These allocation errors resulted because that model's forecasts did not consistently capture the relative resource needs across different states. (Figure 2 & 3A). The CU-select model made some similar errors—most prominently, over-allocating resources to Ohio—but overall, it did a better job of forecasting the relative resource demands across different locations.

On the other hand, CU-select had worse performance as measured by WIS. Its forecasts were biased downwards, and it consistently incurred a large penalty for underprediction (Figure 3B). Predictions from the JHUAPL-Bucky model were wider, and included the observed level of daily hospital admissions more often. Therefore, WIS did not as often assign that model severe penalties for forecasts that underpredicted or overpredicted the actual hospitalization count.

3.5.2 Forecast scores showed differences over time

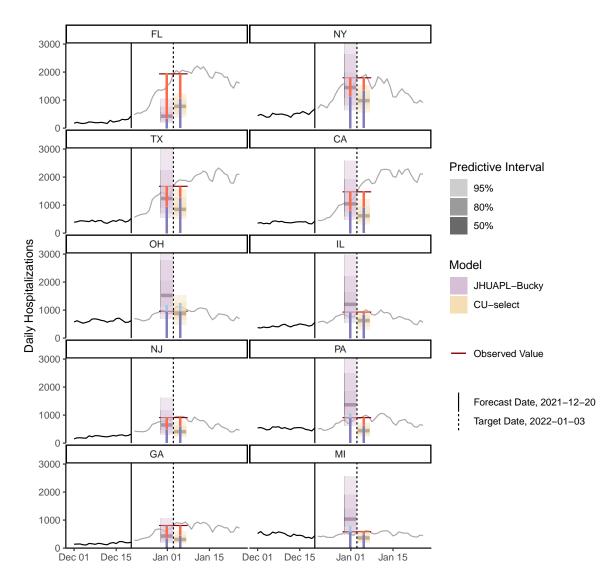


Figure 2: Probabilistic forecasts for new hospital admissions and the inferred resource allocations for COVID-19 on January 3, 2022 for the states with the ten highest hospitalization counts. For each state, the dark black line shows the data observed when the forecast was made and the grey line shows eventually observed counts. The side-by-side shaded regions show the median (solid red horizontal line) and 50%, 80% and 95% prediction intervals for the two selected models. The forecasts were made for new hospitalizations on January 3, 2022 (vertical dashed line, with number of hospitalizations indicated by red horizontal line segment at the intersection of the dashed line and the grey line of data). The vertical bars with purple, blue and red shading show the allocations. The purple bar goes from zero to the amount of need that was met by the allocation from that model to a specific location. A red bar indicates need that exceeded the resource allocation for a location, and a light blue bar shows suggested resource allocation suggested by that model that were above the need for that location.

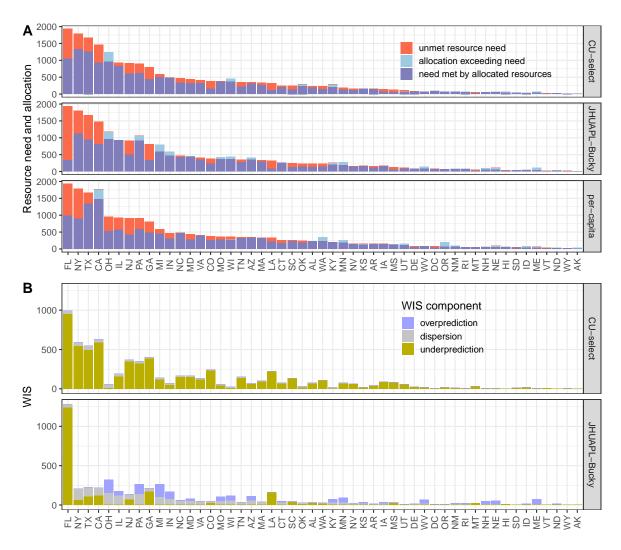


Figure 3: Component-wise breakdowns of the allocation score (Panel A) and weighted interval score (Panel B), by location for forecasts of hospitalization admissions on January 3, 2022, for two selected models (JHUAPL-Bucky and CU-select). Panel A shows the observed resource need, in this case the observed number of hospitalizations, for each state, along with the hypothetical number of resources allocated to the given location based on the forecasts from each model. The number of available resources was fixed at 15,000 and forecasts from each model were used to determine an optimal allocation strategy before the resource need was known. For most locations the resource need exceeded the resources allocated, indicated by the 'observed resource need' bar being larger than the 'allocation' bar. Panel B shows the breakdown of the weighted interval score (WIS) into components of underprediction, overprediction and dispersion. Larger values of WIS indicate more error, and the full WIS score for each location can be decomposed into the three components shown here.

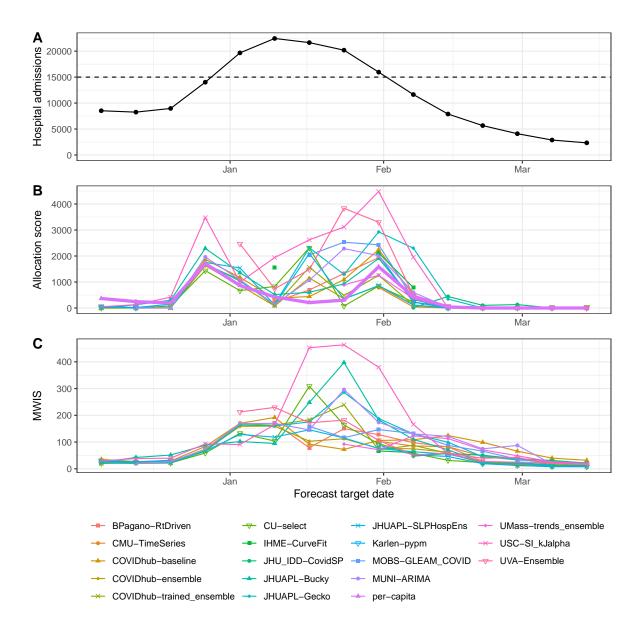


Figure 4: Hospital admissions and evaluation metrics over time. Panel A shows the number of hospital admissions in the US as a whole due to COVID-19 on a sequence of 15 Mondays from December 2021 through March 2022. These are the dates for which forecasts were made and evaluated. A horizontal dashed line at 15,000 shows the assumed resource constraint K. Panel B shows allocation scores (AS) for each model's 14 day-ahead forecast, across all US states. The x-axis corresponds to the date for which the prediction was made. AS typically are high when the observed value is near to the constraint, which occurs during the last Monday in December (on the way up) and the last Monday in January (on the way down). Panel C shows the MWIS metric across weeks, averaged across all states. MWIS values tend to scale with the observed and predicted values, and the peak MWIS values happen around and just after the peak of the Omicron wave.

Allocation scores varied substantially by date and by model (Figure 4). For predictions made for the first three Mondays in December 2021 and the last three Mondays in February 2022 all models had allocation scores under 500 (and the mean across all models was less than 100), indicating that unnecessary unmet need was fairly low on those days. The allocation scores were on the whole highest when the observed number of new hospital admissions was closest to the resource threshold of 15,000, as those are the times when any mistakes in allocation are costly in terms of wasting resources in one location that could have been used in another.

3.5.3 Metrics were not consistently correlated over time

Models showed differing levels of correlation between their allocation scores and MWIS values (Figure 5). Here are some examples of the different model-specific patterns observed:

- Several models showed a positive association between allocation score and MWIS ranks (e.g., Karlen-pypm and USC-SI_kJalpha).
- Several models had consistently strong MWIS ranks but also had highly variable allocation score ranks with no clear association between the two (e.g., JHUAPL-SLPHospEns and CU-select)
- One model performed consistently well for both metrics with no clear association (COVIDhub-ensemble)
- One model performed consistently well for allocation score but had only middlings ranks for MWIS (CMU-TimeSeries)

model	MWIS	MAS
COVIDhub-ensemble	70	389
per-capita	-	464
COVIDhub-trained_ensemble	87	483
CU-select	81	502
JHUAPL-SLPHospEns	67	526
COVIDhub-baseline	93	594
JHUAPL-Bucky	112	643
MUNI-ARIMA	116	707
JHUAPL-Gecko	110	929
USC - $SI_kJalpha$	155	1473

Table 2: Mean weighted interval scores (MWIS) and mean allocation scores (MAS) by model across 13 weeks. For the nine models that submitted forecasts for every week from 2021-11-29 through 2022-02-21, plus a per-capita allocation, these results show the average performance of each model across all weeks. Lower scores indicate better performance, and models are sorted with the most accurate allocations at the top.

3.5.4 Integrated allocation score across values of K

AS was computed for a range of K from 200 to 60,000 for forecasts made on December 20, 2020 predicting levels of hospitalizations on January 3, 2021 (Figure 6A). These calculations highlight that AS was highest at at values of K near the observed nationwide total hospital admissions of 19,581 that day. Rankings of AS from all models were fairly stable across a range of values for K, with some crossings, especially at K values further away from the observed value.

The integrated allocation score (IAS) summarizes allocation scores (AS) across a range of possible values of the constraint (K), possibly taking weights into account for different values of K that might be more or less likely (Section 2.2.3). IAS was computed for two distributions on K, one uniform across

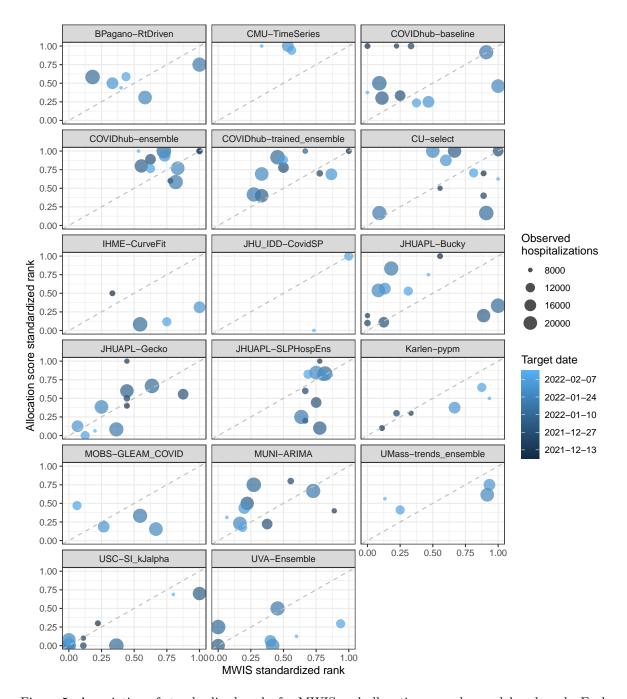


Figure 5: Association of standardized ranks for MWIS and allocation score by model and week. Each facet of the plot corresponds to one model. Within each facet, each point corresponds to a week. The x-and y-values correspond to the MWIS standardized rank and the allocation score standardized rank for that week. Points corresponding to earlier dates have darker shading. The size of the point corresponds to the observed value on the date for which the prediction was made. Models show different degrees of association between the two metrics.

the entire range and the other a symmetric distribution around 15,000 (Figure 6B). Both versions of the IAS were correlated with the original AS conducted at K = 15,000, with the higher correlation coming from the distribution that was centered at K = 15,000 (Figure 6C). Model rankings based on the AC and the centered IAS were roughly similar, with the top and bottom two models being the same for both scores (Table 1).

4 Discussion

In epidemiological forecasting, well-known proper scoring rules such as the log score or variations on the continuous ranked probability score (such as the weighted interval score, or WIS) have been frequently utilized to evaluate probabilistic forecasts. Often models are ranked with respect to accuracy according to a particular score, but without reference to any underlying decision-making process for which that score was designed or from which it might be derivable as a Bayes scoring rule. With careful thought and collaboration between modelers and public health officials, we argue that scores that are more aligned with public health decisions could be developed to inform specific problems. We have demonstrated that forecast evaluation methods that are tied to a specific decision making context can yield model rankings that differ substantively from those based on standard measures of forecast skill, a result that aligns with findings in other fields (Leitch and Tanner, 1991; Murphy, 1993; Cenesizoglu and Timmermann, 2012). In particular, the allocation score penalizes models that mischaracterize the relative magnitude of resource need across different locations, while WIS penalizes forecasts that do not capture the absolute magnitude of the target quantity in each location.

While our example used a hypothetical scenario to illustrate a potential application of the allocation score, resource allocation decisions are a realistic example of the kinds of decisions that could motivate more targeted forecasting exercises. We used ventilators as a notional example for a resource allocation problem because it (a) has been identified as a scarce resource during outbreaks(Huang et al., 2017), (b) could be allocated across different locations, with logistical considerations depending on the geographical scales, and (c) would likely be correlated (although not perfectly so) with hospitalization data. However, we acknowledge the limitations of this example in that not everyone who is hospitalized needs a ventilator, and new hospital admissions may not be the best stand in for a need that corresponds to a prevalence of severe cases. Other possible real-world examples include the allocation of a limited stockpile of vaccinations(Araz et al., 2012; Persad et al., 2023) or diagnostic tests(Du et al., 2022; Pasco et al., 2023). While there are limitations in the realism of the pairing of a specific resource and forecasted outcome, we emphasize that the important result from this work is how evaluating forecasts using a fundamentally different kind of score can illuminate previously hidden aspects of value in forecasts.

In practice, there are many potential users of forecasts with many different decision making problems. While outcomes of some decisions could potentially be specified by loss functions, other uses for forecasts may be less quantifiable, such as when forecasts are used to inform a general sense of situational awareness that may feed in unmeasurable ways into other decisions. And even those that are easily framed as expected loss minimization may differ enough that no single score would be appropriate for all users. Ideally, targeted forecasting tools could be developed through close collaboration between modelers and public health officials. However, this may only be possible in settings with sufficient staffing on both an analytics and a public health team. Increasingly, collaborative modeling hubs are being used to generate "one-size-fits-all" forecasts for many locations at once. In these settings, where

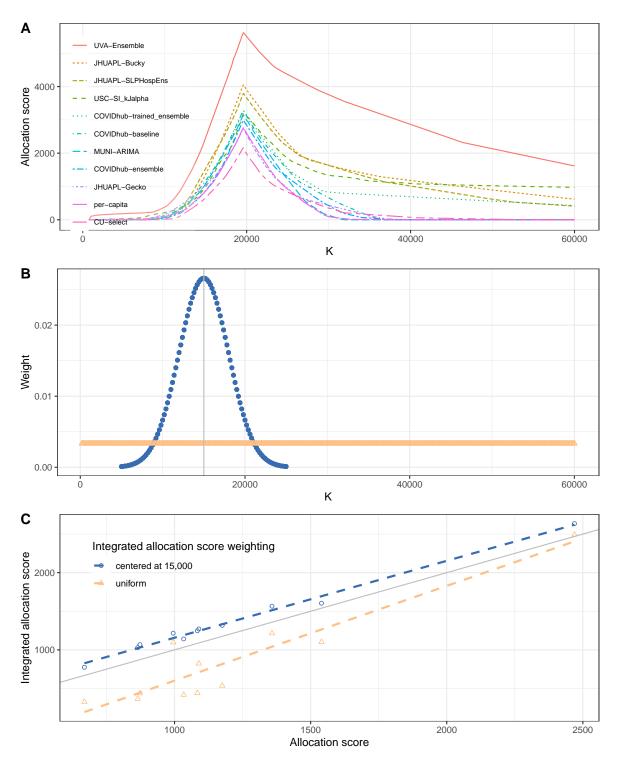


Figure 6: Allocation scores (AS) across different resource constraints (K) for 10 models that made forecasts on 2021-12-20. Panel A shows, for each model, the AS for values of K between 200 and 60,000 at increments of 200. The AS show a sharp peak just under 20,000, near the eventually observed number of hospitalizations. Panel B shows two possible weighting functions for the Integrated Allocation Score (IAS). The first (dark blue circles) computes weights proportional to a normal distribution centered at 15,000 (solid vertical gray line) with a standard deviation of 3,000, and truncated to be between 5,000 and 25,000. The second (light orange triangles) uses a uniform weight for all possible values of K. Note that the AS used in earlier sections of the application uses the single fixed value of K=15,000. Panel C shows how either method of computing the IAS (y-axis) is correlated with AS at K=15,000 (x-axis). Every point represents the AS and IAS for one model. The IAS centered at 15,000 are more closely correlated with the AS values.

tailored models are not available, it still could be possible to evaluate contributed models using a set of multiple scores to support public health end users in understanding the value of forecasts as an input to their particular decision making contexts.

There are several important limitations to the current work. The allocation score we developed here does not directly account for important considerations such as fairness or equity of allocations. Nor does the proposed framework attempt to capture the broader context of decision making. For example, in practice it may be possible to increase the resource constraint K by shifting funding from other disease mitigation measures. We also note that in some settings, a "successful" epidemiological forecast may lead to policy decisions that change the distribution of the predicted outcome Y. Our framework would need considerable enhancements before being applicable to forecast evaluation beyond horizons for which causal feedback can be neglected.

An opportunity for further investigation is to more carefully evaluate whether a forecast adds value to existing decision making processes. In the context of decisions about allocations, standard procedures might involve extrapolating need based on a current observed data (similar to the 'baseline' model presented above), with or without adjustments based on other political or real-world considerations. For example, in many settings public health stakeholders will make decisions after synthesizing information from a variety of quantitative and qualitative sources coupled with expert judgment. The allocation score presented in this work does not directly measure whether a given forecast adds useful information to such an existing decision-making process. While the scoring procedures as presented do not directly address this question, they could be modified (say, by comparison to a 'baseline' model or expert-elicited allocations in the absence of forecast data) to quantify the benefit of using a forecast to inform a specific decision.

In conclusion, we argue that the way modelers and policymakers view and evaluate forecasts should change depending on the specific decision-making context. Defaulting to standard forecast evaluation metrics can mask the utility (or disutility) of certain forecasts, or lead to forecasts being used in decision making contexts very different from those for which they might offer useful guidance. New collaborative work between public health officials and modeling teams is needed to assess the value and relevance of the initial findings presented here, including real-time pilot studies or simulation exercises that could be used to inform further development of new or alternative scoring metrics. We see this work as an initial overture for what we hope will grow to be a large, collaborative body of work more closely coupling applied epidemiological forecasting with public health decision making.

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