

Evaluating infectious disease forecasts with allocation scoring rules

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August 31, 2023

Abstract

The COVID-19 pandemic has led to rapid innovation in methods for eliciting and evaluating forecasts of infectious disease burdens, with a primary goal being to help public health workers make informed decisions about how to manage these burdens. However, explicit descriptions or quantifications of the value forecasts add to society through the decisions they support are elusive. Moreover, there has only been limited discussion of how predominant forecast evaluation metrics might indicate the success of policies based in part on those forecasts.

Here we pursue one possible tether between multivariate forecasts and policy: the allocation of limited medical resources in response to COVID-19 hospitalizations in various regions so as to minimize expected unmet need. Given probabilistic forecasts of hospitalizations in each region, we formulate an allocation algorithm following techniques developed in operations research. We then score forecasts according to how much unmet need their associated allocations would have allowed. We illustrate this scheme with quantile forecasts of COVID-19 hospitalizations in the US at the state level that are recorded in the COVID-19 Forecast Hub, with the goal of determining the allocation of a hypothetical limited resource across the states. The forecast skill ranking given by this allocation scoring rule can vary substantially from the ranking given by the weighted interval score now used by the CDC, especially during surges in hospitalizations such as in late 2021 as the Omicron wave began. We see this as strong evidence that the allocation scoring rule detects forecast value that is missed by traditional accuracy measures and that the general strategy of designing scoring rules that are directly linked to policy performance is a promising research direction for epidemic forecast evaluation.

1 Introduction

Infectious disease forecasting models have emerged as important tools in public health. Predictions of disease dynamics have been used to inform decision making about a wide variety of measures to reduce disease spread and/or mitigate the severity of disease outcomes. For example, estimates of expected onset of flu season have been used to aid national vaccination strategies [Igboh et al., 2023], and forecasts of Ebola dynamics have been used to allocate surveillance resources [Meltzer et al., 2014, Rainisch et al., 2015]. Bertsimas et al. [2021] developed tools to inform decision making from infectious disease forecasts, which have been used to inform allocation of limited medical supplies such as ventilators, ICU capacity planning, and vaccine distribution strategy. Models developed by Fox et al. [2022] have been used to inform resource and care site planning, as well as community guidelines for masking, traveling, dining and shopping (University of Texas, 2022). In April of 2022, the Centers for Disease Control and Prevention (CDC) announced the launch of the Center for Forecasting and

Outbreak Analytics (CFA) to translate disease forecasts into decision making (CDC, 2022), indicating that this has been identified as an important direction at the highest levels of government public health response. The value of infectious disease forecasts has typically been measured by how closely they predict disease outcomes such as cases, hospitalizations or deaths using, for example, root mean square error (RMSE) [Papastefanopoulos et al., 2020] or weighted interval score (WIS) [Bracher et al., 2021], however, recently authors have been calling for evaluating forecasts through their impact on policy [Marshall et al., 2023].

In decision making settings where it is possible to quantify the utility or loss associated with a particular action, standard tools of decision theory provide a procedure for developing forecast scoring rules that measure the value of forecasts through the quality of the decisions that they lead to. We give an overview of these procedures in Section ???. There is a large history of literature applying these ideas to obtain measures of the value of forecasts that are tied to a decision making context, primarily in fields such as economics and finance, supply chain management, and meteorology. We review this work only briefly here, and we refer the reader to Yardley and Petropoulos [2021] for a general overview, and to Pesaran and Skouras [2002] and [ELR:\[TODO: identify relevant review or book style summary for meteorology\]](#) for discussions focused on applications to economics and meteorology, respectively. In finance, the value of forecasts can often be measured by the profits generated by trading decisions informed by the forecasts, perhaps adjusted for risk levels [e.g., Leitch and Tanner, 1991, Cenesizoglu and Timmermann, 2012]. In applications to supply chain management and meteorology, the value of forecasts has typically been operationalized by considering the costs associated with decisions regarding the amount of inventory to hold or the level of protection against the impacts of extreme weather events to enact Peter Catt (2007), Fotios Petropoulos and colleagues (2019), Nada Sanders and Gregory Graman (2009), T.N. Palmer (2002), Florian Pappenberger and colleagues (2015). For example, in supply chain management these decisions may incur costs related to holding inventory, labor, or providing poor service, while in meteorology we may need to balance the costs of implementing protective measures with the costs of potentially preventable weather damages. In this framework, a forecast has value if it leads to decisions with low total costs. In all of these fields, analyses have consistently found that common measures of statistical forecast accuracy do not necessarily correspond directly to measures of the value of forecasts as an input to decision making [e.g., Leitch and Tanner, 1991, Cenesizoglu and Timmermann, 2012].

However, we are aware of only a limited body of work that explicitly attempts to measure the value of infectious disease forecasts through their impact on policy, and much of this discussion has proceeded informally. For example, Ioannidis et al. [2022] discuss the possible negative consequences of inaccurate forecasts of infectious disease, but do not attempt to quantify the utility or loss incurred as a result of those forecasts. Separately, there is a thread of literature that does quantify the link between infectious disease modeling and policy making, but this work has been done outside of a forecasting context. As an example, Probert et al. [2016] develop measures of the cost of actions designed to control a hypothetical outbreak of foot-and-mouth disease and use this framework to explore policy recommendations from a variety of simulation-based projection models.

In practice, probabilistic infectious disease forecasts have most often been made for observations that emerge from public health surveillance systems and have typically been evaluated with standard, “off-the-shelf” scoring rules. For example, seasonal influenza forecasts in the US and dengue forecasts for Peru and Puerto Rico targeted public health surveillance measures of incidence over time and space, and used log-score and mean absolute errors to evaluate forecast skill [McGowan et al., 2019, Reich et al., 2019, Johansson et al., 2019]. Pandemic COVID-19 forecasts of observed cases, hospitalizations

and/or deaths in the US and Europe, as reported by municipal, state, or federal surveillance systems, were evaluated using the weighted interval score (WIS, which is an approximation of the continuous ranked probability score, or CRPS), and prediction interval coverage [Cramer et al., 2022, Fox et al., 2022, Sherratt et al., 2023]. Similarly, CRPS was also used to assess probabilistic forecasts of dengue incidence at the district level in Vietnam [Colón-González et al., 2021]. While some of these scores can be interpreted through the lens of decision theory, and all of the application-specific papers cited above had authors from public health agencies, none of them make explicit connections between forecast evaluation and how a forecast was used in practice.

In this work, we begin to fill this gap between the ways that infectious disease forecasts have traditionally been evaluated and the ways that they have been used to support public health policy. We consider a setting in which forecasts are used to help determine the allocation of a limited quantity of medical supplies across multiple regions. We define a new forecast scoring rule — the *allocation score* — that evaluates forecasts based on how beneficial resource allocations derived from them would turn out to be.

Briefly, the allocation score of a forecast is the avoidable unmet need that results from using that forecast to set resource allocations by minimizing expected unmet need. For example, suppose that a decision maker is provided with forecasts of the level of need for medical resources in each of several states or hospital systems. If there is a limited amount of the medical resource that is available to distribute, a decision maker could choose an allocation of that resource across locations that minimizes the expected unmet need according to that forecast. As measured by the allocation score, one forecast is better than another if it would lead decision makers to an allocation that results in less unmet need. If the amount of resources that is available to distribute is less than the actual need, some amount of unmet need is unavoidable. The allocation score for a forecast does not include the unmet need that was unavoidable given the resource constraint, and so it measures only the amount of unmet need that could have been prevented by using a different allocation of available resources than that suggested by the forecast. We elaborate on these ideas in Section 2.

We present an illustrative analysis using the allocation score to evaluate forecasts of hospital admissions in the US leading up to the Omicron wave in winter 2022. This analysis is “synthetic” in that it does not correspond to an actual analysis that supported decision making in real-time. However, the framework described in this paper corresponds to real-world decisions that must be made by public health administrators around the globe, and could be adapted in the future for such real-time situations. For example, forecasts for districts in Sierra Leone of bed demand to care for patients with Ebola was the subject of a real-time modeling study in late 2014 and early 2015 [Camacho et al., 2015]. And, in 2020, a model developed by an academic research group turned predictions of COVID-19 hospitalizations into estimates of ventilator usage and shortages. This framework was used by the Hartford HealthCare system in Connecticut “to align ventilator supply with projected demand at a time where the [COVID-19] pandemic was on the rise” [Bertsimas et al., 2021]. These examples illustrate the potential for forecasts to inform decisions about how to allocate limited supplies such as temporary hospital beds, ventilators, personal protective equipment, or other supplies that are known to be effective at reducing transmission or severity of disease. However, we emphasize again that these studies did not take the step of evaluating forecasts based on the quality of the allocation decisions that they supported or could have been used to support.

The remainder of this article is organized as follows. We describe the allocation score in Section 2, and in Section 3 we illustrate the use of the score in an application to evaluate short-term forecasts of COVID-19 hospital admissions in the US. Section 4 summarizes our contributions and discusses

opportunities for further extensions in future work.

2 Methods

We begin with an informal description of the allocation score and some examples illustrating its key characteristics in section 2.1. In section 2.2 we develop the allocation score more carefully, building on decision theoretic procedures for deriving proper scoring rules. We then comment on some connections between the allocation score that we propose and other common scores that can be derived from decision theoretic foundations, such as the quantile score, WIS, and CRPS, in section 2.3.

2.1 Overview of Allocation Scoring

Suppose that a decision maker is tasked with determining how to allocate K available units of a resource across N locations. If the decision maker is provided with a multivariate forecast F where each marginal forecast distribution F_i predicts resource need in a particular location, one option is to choose the resource allocation that minimizes the expected total unmet need according to the forecast. We will give a more precise mathematical statement in section 2.2, but informally, the total expected unmet need according to the forecast is

$$\sum_{i=1}^N E_{F_i}[\text{unmet need in location } i], \quad (1)$$

where the unmet need in a particular location is the difference between resource need in that location and the number of resources that were allocated there. This allocation problem has an intuitively appealing solution: allocate so that the probabilities of need exceeding allocation in various locations are as close to each other as possible. This will lead to the allocations provided by F being quantiles of the marginal distributions F_i for some *single* probability level τ that is shared in common for all locations.

After time passes and the actual level of resource need has been observed, the quality of a selected allocation can be measured by comparing the actual need in each location to the amount of resources that were sent there. Specifically, we compute the total unmet need that resulted from the selected allocation:

$$\sum_{i=1}^N \text{unmet need in location } i. \quad (2)$$

We emphasize that in Equation (2) the calculation of unmet need is based on the actual resource need that was realized in each location, while in Equation (1) the calculation of unmet need was based on a hypothetical potential future level of resource need. Once the actual levels of resource need have been observed, we can obtain a quantitative measure of the quality of alternative allocation decisions: one allocation is better than another if it results in lower total unmet need.

The **allocation score** of the forecast F is the avoidable unmet need that results from using the allocation that minimizes the expected unmet need according to that forecast. By “avoidable unmet need”, we mean that the allocation score does not include the amount of unmet need that was inevitable simply because the amount of available resources K was less than the need for resources. Rather, the allocation score measures the unmet need that could have been avoided by an oracle that knows exactly how much need will occur in each location and divides the amount K so that nothing is wasted in one

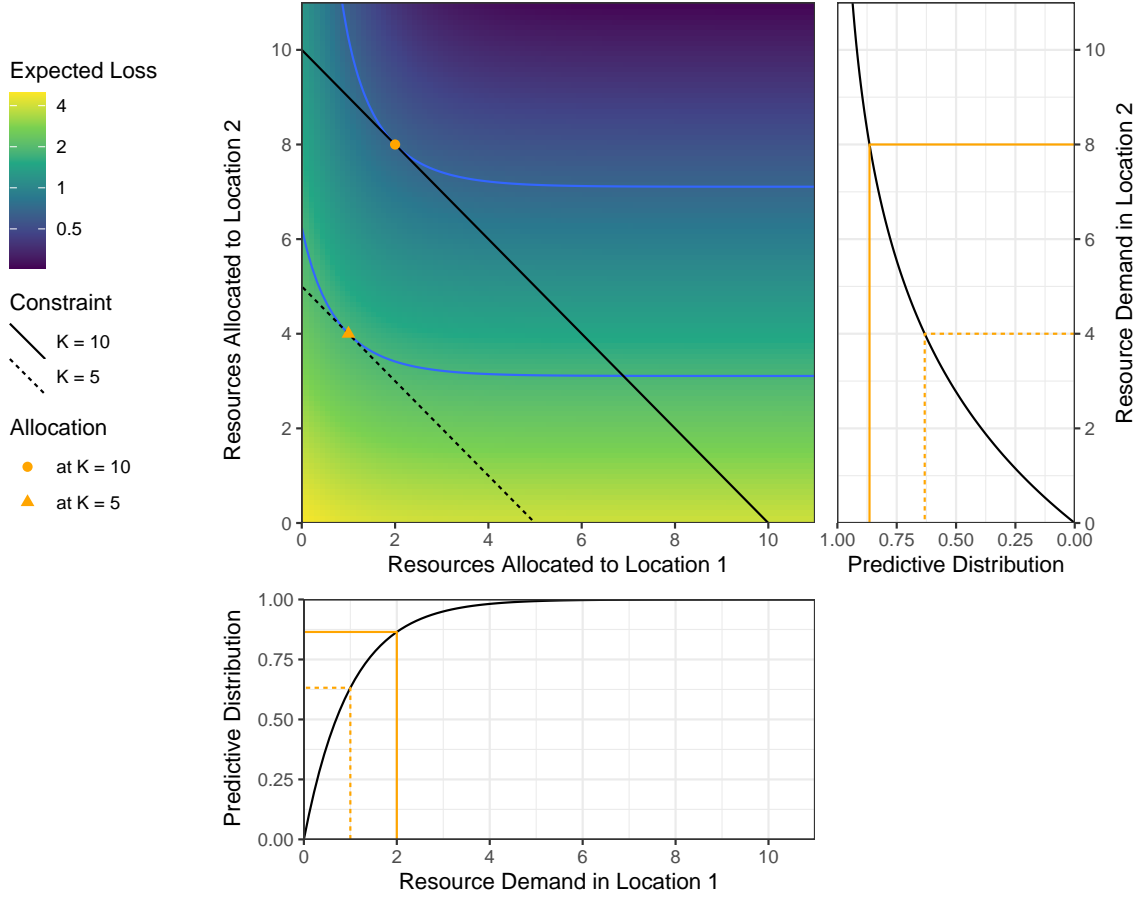


Figure 1: An illustration of the resource allocation problem in Example 1. There are $N = 2$ locations, with predictive distributions $F_1 = \text{Exp}(1)$ and $F_2 = \text{Exp}(1/4)$. The cdfs of these distributions are illustrated in the panels at bottom and right. In the center panel, the background shading corresponds to the expected loss according to these forecasts. Diagonal black lines indicate resource constraints at $K = 5$ and $K = 10$ units; any point along those lines corresponds to an allocation that meets the resource constraint. For these forecasts, the optimal allocations are $(1, 4)$ for $K = 5$ and $(2, 8)$ for $K = 10$. These allocations are at the point on the constraint line where the expected loss is smallest, which also corresponds to the point where a level set of the expected loss surface (blue curve) is tangent to the constraint.

location while it could be put to use in another. An allocation score of 0 is optimal, and indicates that no other allocation of resources could have met need better than the allocation suggested by F . A larger allocation score indicates that it would have been possible to improve upon the allocation suggested by F .

Example 1 Suppose we have a forecast F for need in two locations with $F_1 = \text{Exp}(1/\sigma_1)$ and $F_2 = \text{Exp}(1/\sigma_2)$, where $\sigma_1 = 1$ and $\sigma_2 = 4$. When the marginal forecasts are exponential distributions, it can be shown that the optimal allocation divides the available resources among the locations proportionally to the scale parameters σ_i (see section *** of the supplemental materials). If we have $K = 5$ units of our resource available, the optimal allocation according to F would be 1 unit of resources in location 1 and 4 units of resources in location 2. If, on the other hand, we have $K = 10$ units available, we will allocate 2 units of resources to location 1 and 8 units to location 2. Figure 1 illustrates the situation.

Next suppose that we observe needs of 1 and 10 in locations 1 and 2, respectively. Based on these

observed needs, we can measure the quality of the allocation suggested by the forecast by calculating the amount of unmet need that resulted from that allocation over and above what was unavoidable given the resource constraint. With $K = 5$ units of the resource, the allocation based on the forecast exactly meets the observed need in location 1, but it leaves 6 units of need unmet in location 2. However, working within the resource constraint, no other allocation could have done better: for example, allocating 0 units of resources to location 1 and 5 to location 2 still results in a total unmet need of 6 across both locations. Therefore, the forecast’s allocation score is 0 with $K = 5$. On the other hand, when $K = 10$, the forecast F ’s allocation results in $10 - 8 = 2$ units of unmet need in location 2 despite leaving no need unmet in location 1. In this case, the oracle would be able to prevent all but 1 of the total 11 units of need from going unmet, for example by allocating 1 unit of resources to location 1 and the remaining 9 units of resources to location 2. The allocation score for the forecast when $K = 10$ would therefore be 1 ($= 2$ realized $- 1$ unavoidable) in units of avoidable unmet need.

These scores illustrate a general result: allocation scores for a forecast will tend to be larger when the resource constraint is close to the observed need, because this is when it matters most which locations are allocated more or less resources. If the resource constraint is very small, any allocation of those limited resources will result in a large amount of unmet need. If the resource constraint is very large, it becomes less important which locations receive relatively more or less resources because all locations will receive enough resources to meet their need.

Example 2 Now consider a different forecast that also has exponential distributions for resource need in each location, but that has the scale parameters $\sigma_1 = 2$ and $\sigma_2 = 8$, twice as large as the scale parameters of the forecast in Example 1. Because the optimal allocation is proportional to the scale parameters, this forecast would lead to the same optimal allocations as the forecast in Example 1, and would therefore be assigned the same allocation score.

Note the way in which these forecasts incurred a positive (i.e., non-optimal) allocation score of 1 when $K = 10$. It was not directly due to individual misalignments of the marginal forecasts F_i with the observed needs, but rather because the allocations and observed needs were not proportional as vectors. Restating: as far as allocation decisions are concerned, with a fixed constraint $K = 10$ the fundamental problem with the forecast F in Example 1 is not that it predicts a mean total resource need of 5 units; it is that the realized need was 10 times as large in location 2 as in location 1, but the forecast only indicated that the resource allocation for location 2 should be 4 times the allocation for location 1.

This illustrates a fundamental property of the allocation score: at its core, it measures whether the forecast accurately captures the relative magnitudes of resource need across different locations, which is precisely the information that is needed to allocate resources to those locations subject to a fixed resource constraint. On the other hand, the allocation score is not directly sensitive to whether the forecasts in each location correctly capture the magnitude of resource need in each individual location. This stands in marked contrast to other common scoring methods for multivariate forecasts that aggregate univariate scores such as CRPS or WIS for the marginal forecasts where a misalignment in one coordinate is penalized regardless of alignments in other coordinates. Note that we do not claim that the allocation score is generically preferable to these other scores —rather, it provides a view of forecast performance that is specifically tuned to the context of decision making about resource allocations.

2.2 A decision theoretic development of the allocation score

We give a high-level review of a general procedure for developing proper scoring rules that are tailored to specific decision making tasks in section 2.2.1, and then in section 2.2.2 we apply that procedure to develop the allocation score based on the task of deciding on how to allocate a fixed supply of resources across multiple locations. In 2.2.3 we consider a small extension where the resource constraint is not known, or it is desired to consider the value of forecasts across a range of decision making scenarios. This gives rise to the *integrated allocation score*.

2.2.1 The decision theoretic setup for forecast evaluation

In the framework of decision theory, a decision corresponds to the selection of an action x from some set of possible actions \mathcal{X} . For example, x may correspond to the level of investment in a measure designed to mitigate severe disease outcomes such as hospital beds, ventilators, medication, or medical staff, with \mathcal{X} being the set of all possible levels of investment that we might select. The quality of a decision to take a particular action x is measured in relation to an outcome y that is unknown at the time the decision is made. For example, y may correspond to the number of individuals who eventually become sick and would benefit from the mitigation measure, and informally, an action x is successful to the extent that it meets the realized need. In the face of uncertainty, a decision maker may use a forecast F of the random variable Y to help inform the selection of the action to take. We measure the value of a forecast as an input to this decision making process by the quality of the decisions that it leads to.

We can formalize the preceding discussion with the following three-step procedure for developing scoring rules for probabilistic forecasts:

1. Specify a *loss function* $s(x, y)$ that measures the loss associated with taking action x when outcome y eventually occurs.
2. Given a probabilistic forecast F , determine the *Bayes act* x^F that minimizes the expected loss under the distribution F .
3. The *scoring rule* for F calculates the score as the loss incurred when the Bayes act was used: $S(F, y) = s(x^F, y)$.

This is a general procedure that may be applied in settings where it is possible to specify a quantitative loss function. Subject to certain technical conditions, scoring rules obtained from this procedure are proper. We refer the reader to discussion in (cite paper 2 on arxiv) for a more technically precise discussion.

2.2.2 The allocation score for a fixed resource constraint

In the decision making setting that we consider, an action $x = (x_1, \dots, x_N)$ is a vector specifying the amount that is allocated to each of N locations. We require that $0 \leq x$, i.e., that each x_i is non-negative, and that the total allocation across all locations equals the amount of available resources, K : $\sum_{i=1}^N x_i = K$. The set \mathcal{X} consists of all possible allocations that satisfy these constraints. The eventually realized resource need in each location is denoted by $y = (y_1, \dots, y_N)$. These levels of need are not known at the time of decision making, so we define the random vector $Y = (Y_1, \dots, Y_N)$ where Y_i represents the as-yet-unknown level of resource need in location i . Forecasts of need in each location are collected in $F = (F_1, \dots, F_N)$. We assume that resource need is non-negative and the forecasts

reflect that, i.e. the support of each F_i is a subset of \mathbb{R}^+ . Finally, we assume that each unit of unmet need incurs a loss denoted by L , so that if the selected resource level x_i in location i is less than the realized need y_i , a loss of $L(y_i - x_i)$ results.

We note that the problem formulation here assumes that the resource in question does not impact the amount of demand y_i that will materialize, but rather it is a resource that satisfies that demand. In the context of infectious disease, this means that we do not consider resources that are intended to reduce the number of people who will become sick at some point in the future, such as a preventative influenza or COVID-19 vaccine. Our set up addresses resources like hospital beds, oxygen supply, ventilators, or rabies vaccines which are intended to meet the medical needs of patients who are already sick.

With this notation in place, we can develop a proper scoring rule following the outline in section 2.2.1.

Step 1: specify a loss function. The loss associated with a particular allocation is calculated by summing contributions from unmet need in each location:

$$s_A(x, y) = \sum_{i=1}^N L(y_i - x_i)_+. \quad (3)$$

Here, $(y_i - x_i)_+$ is the unmet need in location i , which is given by $y_i - x_i$ if the realized need y_i in location i is greater than the amount x_i allocated to that location, or 0 if the amount x_i allocated to unit i is greater than or equal to the realized need.

Step 2: Given a probabilistic forecast F , identify the Bayes act. The Bayes act associated with the forecast, x^F , is the allocation that minimizes the expected loss:

$$x^F = \underset{0 \leq x}{\operatorname{argmin}} \mathbb{E}_F[s_A(x, Y)] \text{ subject to } \sum_{i=1}^N x_i = K, \quad (4)$$

where $\mathbb{E}_F[s_A(x, Y)] = \sum_{i=1}^N L \mathbb{E}_{F_i}[(Y_i - x_i)_+]$ sums the expected loss due to unmet need across all locations. It can be shown that the Bayes act has $x_i^F = F_i^{-1}(1 - \lambda^*/L)$, where λ^* depends on the problem parameters K and L as well as the forecast distributions and is chosen so as to satisfy the equation

$$\sum_{i=1}^N F_i^{-1}(1 - \lambda^*/L) = K. \quad (5)$$

This partial solution to the allocation problem seems to have first appeared in Hadley and Whitin [1963]; see the supplemental materials for a derivation.

One interpretation of this result is that the Bayes act sets the allocation in each location i to a quantile of the forecast distribution F_i for that location. The quantile is at a probability level $\alpha = 1 - \lambda^*/L$ that is the same for all locations, and is chosen such that the constraint is satisfied. According to this interpretation, we divide the available resources among the locations in such a way that the forecasted probability that need will exceed the available resources is the same in all locations. An alternative interpretation comes from noting that for each location i , $\frac{\partial}{\partial x_i} \mathbb{E}_F[s_A(x, Y)]|_{x=x^F} = -\lambda^*$ (see the supplement for a proof). In words, at the allocation given by the Bayes act, the rate of change of the expected score as a function of the amount allocated to location i is given by $-\lambda^*$. This

derivative is the same for all locations, so the optimal allocation divides the available resources across all locations in such a way that according to F , the expected benefit of 1 additional unit of resources is the same in all locations.

Step 3: Define the scoring rule. We can now define a proper scoring rule for the probabilistic forecast F as

$$S_A(F, y; K) = s_A(x^F, y) = \sum_{i=1}^n L(y_i - F_i^{-1}(1 - \lambda^*/L))_+ \quad (6)$$

This score measures the total unmet need across all locations that results from using the Bayes allocation associated with the forecast F when the actual level of need in each location is observed to be y_i .

2.2.3 Integrating the allocation score across resource constraint levels

The allocation score S_A that we developed in the previous section measures the skill of the forecast distributions F based on a single probability level $\alpha = 1 - \lambda^*/L$. This is appropriate if the resource constraint K is a known constant. However, if K is not precisely known at the time of decision making or there is interest in measuring the value of forecasts across a range of decision making scenarios with different resource constraints, we can use an *integrated allocation score* (IAS) that integrates the allocation score across values of K , weighting by a distribution p :

$$S_{IAS}(F, y) = \int S_A(F, y; K)p(K) dK$$

2.3 Generalizations and Connections to Other Scores

We have described how the allocation score arises from a standard procedure for developing proper scoring rules when the decision relates to how a fixed quantity of resources should be allocated to multiple locations. In fields such as meteorology and supply chain management, a great deal of attention has been given to a different problem where a decision must be made about the quantity of a resource to purchase for a single location in the face of a fixed cost C for each unit of the resource and a loss L that will be incurred for each unit of unmet need. This decision making problem leads to the pinball loss that is often used in quantile regression, and the optimal quantity of resources to purchase is the predictive quantile at the probability level $1 - \frac{C}{L}$.

This result bears a strong resemblance to the results for the allocation problem, where the optimal solution also sets the resource level in each location to a quantile of the respective forecast distributions. These decision making problems differ according to the challenge faced by the decision maker: a fixed constraint on the available resources for the allocation problem, or a cost per unit of resources in the resource purchasing problem. In fact, it is possible to combine these into a more general problem where the decision maker must decide on both the total level of resources to purchase and an allocation of those resources across multiple locations, subject to a cost per unit of resources and a constraint on the total quantity of resources that can be purchased. The quantile loss and the allocation score presented in this work are both special cases of the score that emerges from that more general decision making problem. We pursue this direction further in other work (cite arxiv version of paper 2).

Similarly, it is possible to see both the integrated allocation score and common scores such as the continuous ranked probability score (CRPS) and weighted interval score (WIS) as special cases of a more general score that integrates across resource cost and constraint parameters together. It is well known in the literature that WIS is equivalent to a weighted average of quantile scores across multiple

quantile levels (cite Bracher et al.) and CRPS integrates quantile scores across multiple quantile levels (cite cite). By integrating the combined resource acquisition and allocation score that we described in the previous paragraph across the parameters for both resource costs and constraints, we obtain a score that combines features of both IAS and CRPS and contains those scores as special cases. Again, we defer a more detailed discussion of these results to (cite arxiv version of paper 2).

3 Application

We illustrate with an application to hospital admissions in the U.S., considering the problem of allocation of a limited supply of medical resources to the states.

Case study heading into the Omicron wave. Some more detailed discussion of implications of bad forecasts for specific decision making purposes – take a ”deep dive” into one or two example states like FL.

Look at results over a broader range of time.

4 Discussion

We often conceive of infectious disease forecasts as being useful for decision making purposes, but it is rare for forecast evaluation to be tied directly to the value of the forecasts for informing those decisions. This work seeks to address that gap.

We have demonstrated that evaluation methods that are tied to decision making context can yield model rankings that are substantively different from generic measures of forecast skill like WIS.

In practice, there are many users of forecasts with many different decision making problems. Not all can be easily quantified. Those that can be easily quantified may differ enough that no single score is appropriate for all users. We suggest reporting multiple scores. This may be tricky to operationalize in the setting of a general forecast hub. It matters how you elicit and represent probabilistic forecasts (quantiles? samples? cdfs?).

The allocation score we developed here does not directly account for important considerations such as fairness/equity of allocations.

The allocation score we developed also does not attempt to capture the broader context of decision making. For example, in practice it may be possible to increase the resource constraint K by shifting funding from other disease mitigation measures.

Forecaster’s dilemma: a successful forecast may lead to decisions that change the distribution of the outcome Y . Our framework cannot be used in those settings.

There is much more to do in this general area.

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