

17<sup>th</sup> October 2014

Total Marks = 20

Time 2 hours

**All parts of a question MUST be answered together.****Fragmented answers will not be corrected**

1. Justify or contradict the following:

- (a) Orbital approximation is given by  $\Psi(r, \theta, \phi) = R(r)\Theta(\theta)\Phi(\phi)$  where  $\Psi(r, \theta, \phi)$  is a one electron wavefunction.
- (b) The states given by  $n_x = 2, n_y = 3$  and  $n_x = 3, n_y = 2$  are always degenerate for a particle in a two dimensional box.
- (c) For any two wavefunctions  $\Psi_1$  and  $\Psi_2$ , which are eigenfunctions of an operator  $\hat{A}$ , the linear combination  $c_1\Psi_1 + c_2\Psi_2$  is always an eigenfunction of  $\hat{A}$ . **2 + 2 + 1**

2. (a) How many radial nodes and how many angular nodes does the following wavefunction possess? Where are these nodes situated?

$$\psi = (6 - r).r.e^{-r/3}.\sin\phi \sin\theta$$

(b) Find the most probable distance of an electron from the nucleus, when it resides in

i) 2s and ii) 2p orbital.

$$\psi_{2s} = N_1(2 - \sigma)e^{-\sigma/2} \text{ and } \psi_{2p} = N_2\sigma e^{-\sigma/2}\cos\theta \text{ where } \sigma = r/a_0 \text{ and } N_1, N_2 \text{ are constants.}$$

Hence, sketch the radial distribution functions for the two orbitals.

**2+3**

3. Suppose that the wavefunction for a system can be written as

$$\psi(x) = \frac{1}{2}\varphi_1(x) + \frac{1}{4}\varphi_2(x) + \frac{3 + \sqrt{2}i}{2}\varphi_3(x)$$

where,  $\varphi_1(x), \varphi_2(x), \varphi_3(x)$  are orthogonal to each other and are normalized eigenfunctions of the kinetic energy operator, with eigenvalues  $E_1, 3E_1$  and  $7E_1$  respectively.

- (a) Is  $\psi(x)$  normalized?
- (b) What are the possible values that you could obtain in measuring the kinetic energy on the system described by  $\psi(x)$ ?
- (c) What is the average value of kinetic energy that will be obtained for a large number of measurements? **1+2+2**

4. (a) Write the total Hamiltonian for a carbon atom.

(b) What is a spin orbital?

(c) Write the Slater determinant for the first singlet excited state of  $\text{Li}^+$ .

**2+1+2**