

AE-705: Introduction to Flight

Bernoulli, Coandă & Mach

Three Giants of Fluid Mechanics

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WHO WAS BERNOULLI ?

"...there is no philosophy which is not founded upon knowledge of phenomena, but to get any profit from this knowledge it is absolutely necessary to be a mathematician."

DANIEL BERNOULLI

Early Life



Academics

Return to
Basel

Life in
Saint Petersburg

Source: <http://bernoulliprinciple.weebly.com/uploads/6/6/7/8/6678503/1009873.jpeg>



Daniel Bernoulli[1700-1782]

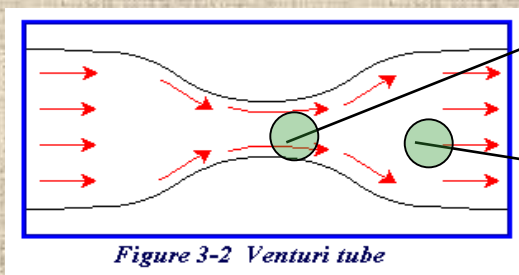
Exercitationes quaedam
Mathematicae

Hydrodynamica

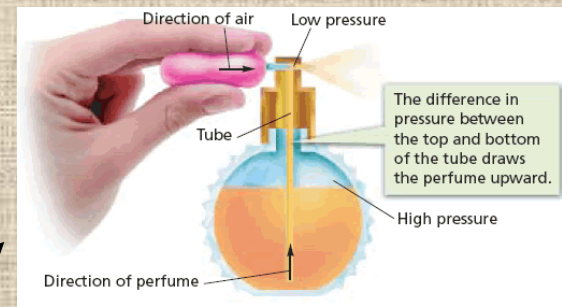


BERNOULLI
EQUATION

Source:https://static1.squarespace.com/static/530bb0b9e4b0f4676186966d/531fd317e4b0db5158a50c15/531fd317e4b0db5158a50c14/1394405054069/260px-Daniel_Bernoulli_001.jpg

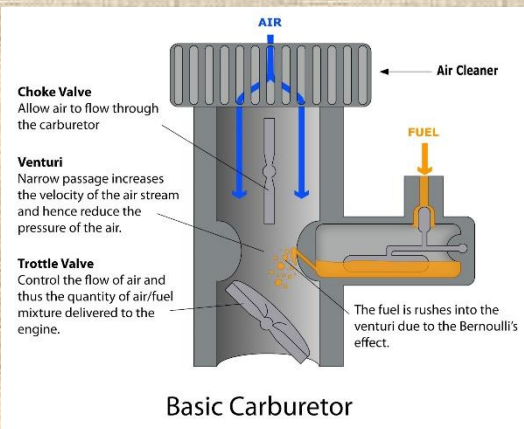


Source: <http://www.allstar.fiu.edu/aerojava/images/pic3-2.gif>

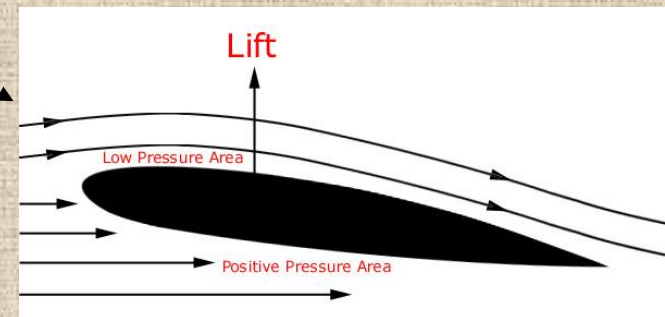


Source: <http://mycampus.nationalhighschool.com/doc/sc/physical%20science/ebook/products/0-13-190327-6/sx7097a3.gif>

Bernoulli Equation Applications

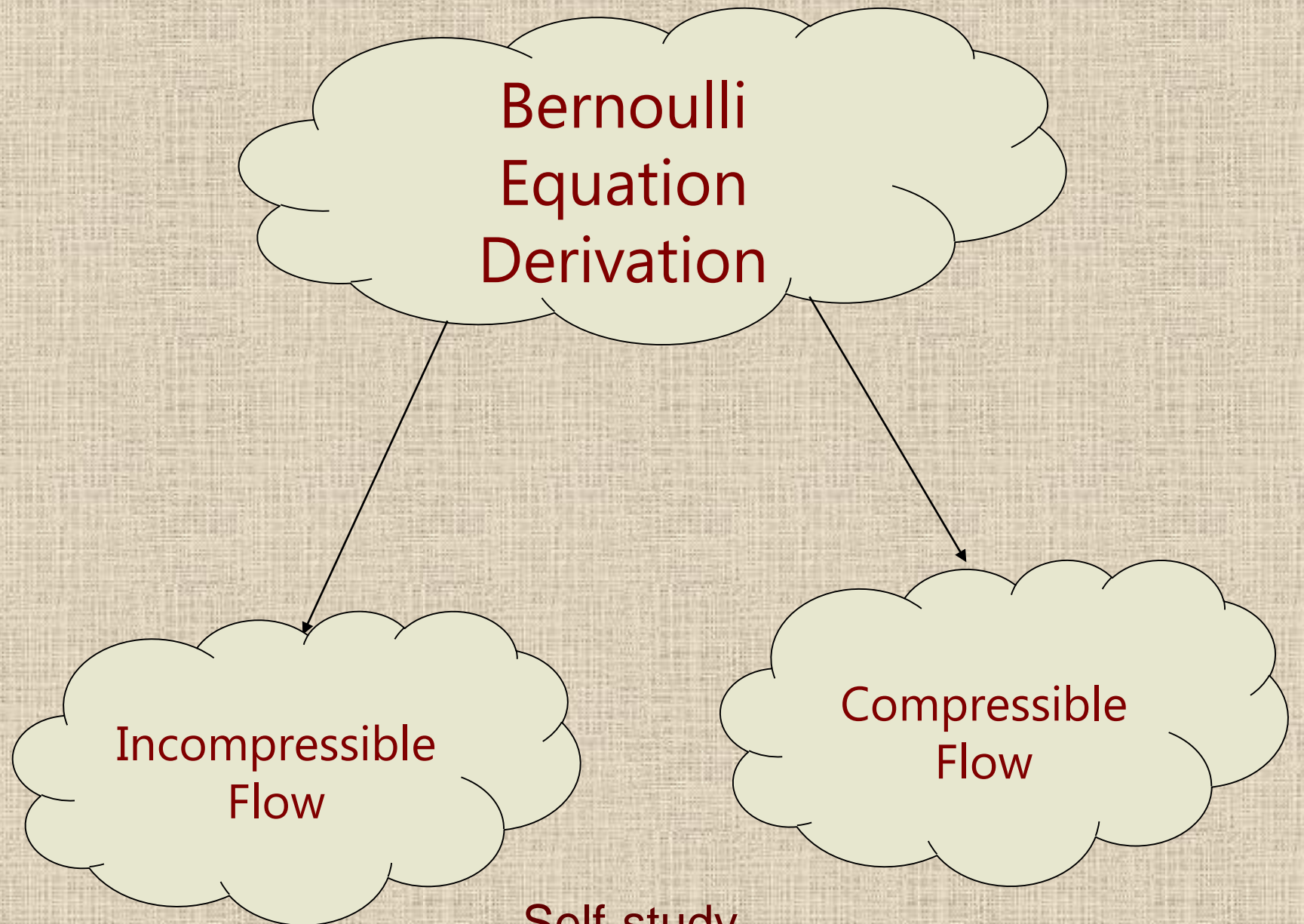


Source: <http://3.bp.blogspot.com/-puEhlmJyfgw/UcGHZFFy9vI/AAAAAAAAABuk/vAwPtYc6m8/s1600/Carburetor-01.png>



Source: <http://www.aviation-history.com/theory/airfoil-6a.jpg>

Bernoulli Equation Derivation



```
graph TD; A[Bernoulli Equation Derivation] --> B[Incompressible Flow]; A --> C[Compressible Flow];
```

Incompressible
Flow

Compressible
Flow

Self-study

THE MAGNUS EFFECT

FASTER AIR



SLOWER AIR

Fastball - Pitchers's Perspective

MAGNUS EFFECT

Spinning object moving through a fluid creates a pressure difference between its sides

Difference in pressure curves the object and changes its trajectory

Source: <https://static1.squarespace.com/static/55123e4ce4b0b2a9ab9020ca/55162b42e4b00ad45a1d2842/55162b42e4b00ad45a1d2a1a/1427516393546/magnus-effect.gif>

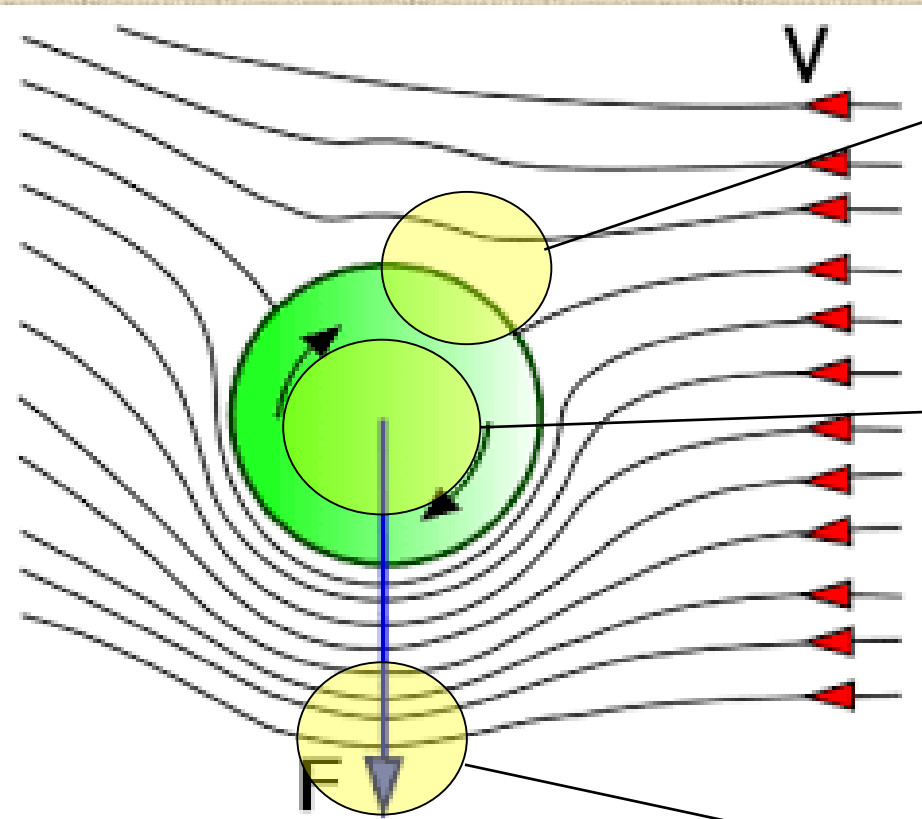


Lets look at
an
experiment

Source: <https://previews.123rf.com/images/chudtsankov/chudtsankov1308/chudtsankov130800439/21699409-Smiling-Mad-Scientist-Or-Professor-Holding-A-Frog-Stock-Vector-doctor-mad-cartoon.jpg>

Source: <https://www.youtube.com/watch?v=2OSrvzNW9FE>

MAGNUS EFFECT



relative motion between the spinning body and the fluid

spinning cylindrical or spherical solid immersed in a fluid

generation of a sidewise force

Source: http://schema-root.org/science/physics/effects/magnus/magnus_effect.png



Source: <https://www.youtube.com/watch?v=YIPO3W081Hw>

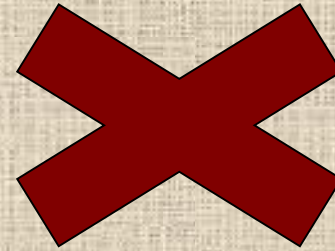


Source: https://static.vecteezy.com/system/resources/previews/000/077/164/non_2x/cartoon-scientist-vector.jpg

Question

Why does this happen?

Bernoulli Principle



Or

Coandă Effect



History and Applications

COANDĂ EFFECT



Henri Coandă [1886-1972]

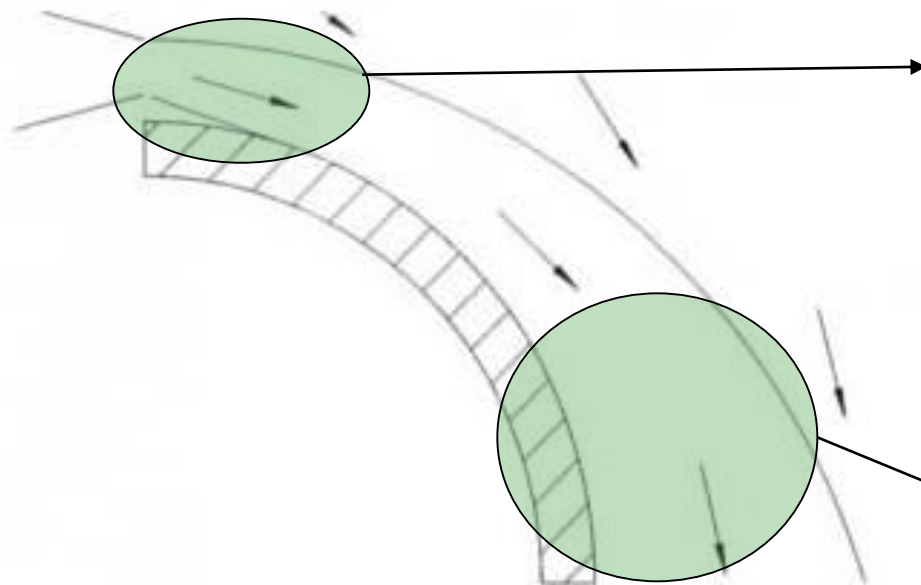
- born in Bucharest, Romania
- interested in the technical problems of flight
- designed and piloted the first jet plane known as the **Coandă-1910**



Source: https://upload.wikimedia.org/wikipedia/commons/thumb/f/f8/Coanda_1910.png/300px-Coanda_1910.png

- In 1930, he discovered the Coandă effect

Coandă Effect



jet flow attaches itself to a nearby surface

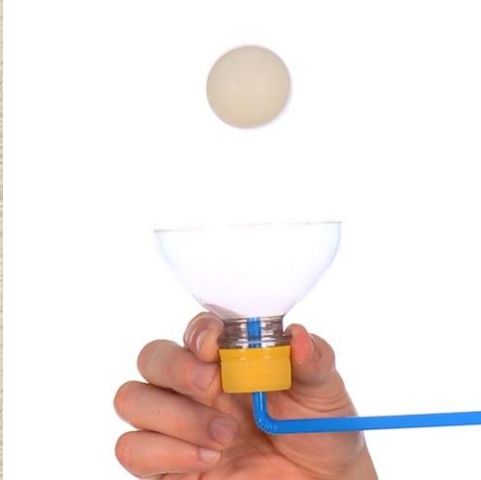
Jet remains attached even when the surface curves away

Source: <http://www.thermofluids.co.uk/images/coandaeffect2.jpg>

Let's understand
Coandă Effect with
an
experiment



Source: <https://thumbs.dreamstime.com/z/cartoon-boy-idea-28030171.jpg>

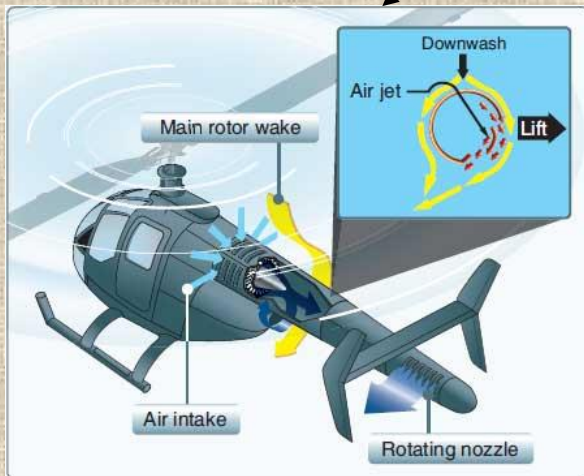


Source: <https://s-media-cache-ak0.pinimg.com/originals/38/2e/b7/382eb7839f80b65202c32fa3c4f642c8.jpg>



Source: <http://www.discoverhover.org/infoinstructors/images/cans.jpg>

Coandă Effect Applications



Source: <http://www.danubewings.com/wp-content/uploads/2015/11/4-14.jpg>

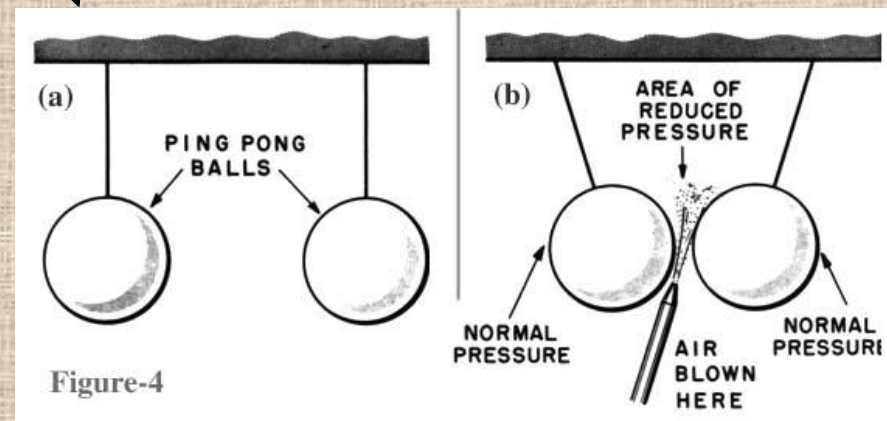


Figure-4

Source: <http://www.aethro-kinematics.com/Ping-pong.jpg>

Coandă Effect Saucer





The presentations and conceptions of the average man of the world are formed and dominated, not by the full and pure desire for knowledge as an end in itself, but by the struggle to adapt himself favourably to the conditions of life.

(Ernst Mach)

izquotes.com

History, Regimes, Applications and Shock Waves

MACH NUMBER

Mach Number

$$M = \frac{v}{a}$$

Local Flow Velocity

Speed of Sound in the medium

Lets take
a look...
shall we?



- Dimensionless number
- Determines the behaviour of fluid at $v > a$



Source: <http://www.kbvp.com/sites/default/files/images/F18F%20pushing%20the%20mach.preview.jpg>

Significance of Mach Number



- At high speeds →
Aircraft compresses air around it
- Local density of the air varies
- Varying Density →
Alters the net force on the aircraft

Source:<http://i178.photobucket.com/albums/w276/scd718/Aircraft/f14d2cm.jpg>

As per Conservation of Momentum

$$\rho V dV = -dP$$

Assuming Isentropic flow

$$\frac{dP}{P} = \gamma \frac{d\rho}{\rho} \quad dP = \gamma \frac{P}{\rho} d\rho$$
$$= \gamma RT d\rho$$

$$dP = \gamma \frac{P}{\rho} d\rho = \gamma RT d\rho$$

$$dP = a^2 d\rho$$

Combining with momentum equation

$$\rho V dV = -a^2 d\rho$$

$$-M^2 \frac{dV}{V} = \frac{d\rho}{\rho}$$

If

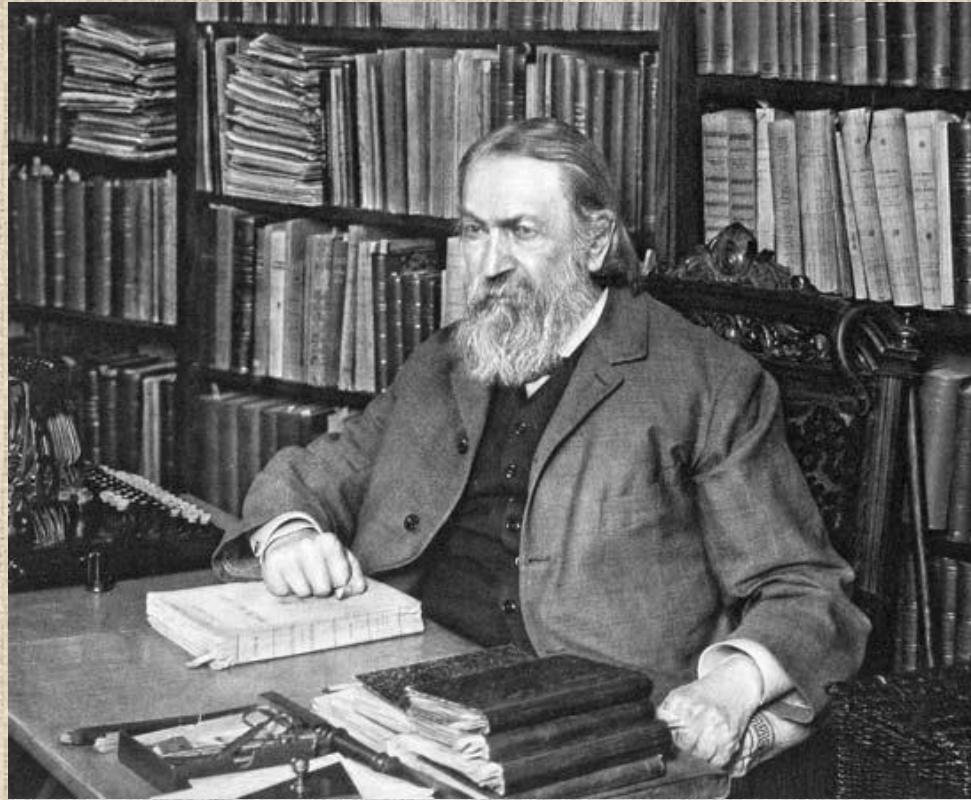
$$M < 1 \rightarrow \rho \sim \text{constant}$$

$$M \sim 1 \rightarrow d\rho \sim dV$$

$$M > 1 \rightarrow d\rho > dV \text{ by a factor of } M^2$$

Source: <https://www.grc.nasa.gov/www/k-12/airplane/machrole.html>

HISTORY OF MACH NUMBER



Source:<https://media1.britannica.com/eb-media/69/68569-004-0B1898D2.jpg>

Ernst Mach , February 18, 1838 to February 19, 1916

He was an Austrian physicist and philosopher, noted for his contributions to physics such as the Mach number and the study of shock waves. As a philosopher of science, he was a major influence on logical positivism and through his criticism of Newton, a forerunner of Einstein's relativity.

"...Science always has its origin in the adaptation of thought to some definite field of experience"

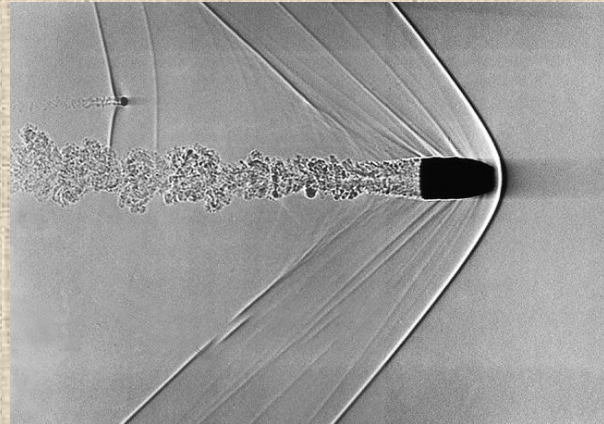
ERNST MACH

Ernst Mach [1838-1916]

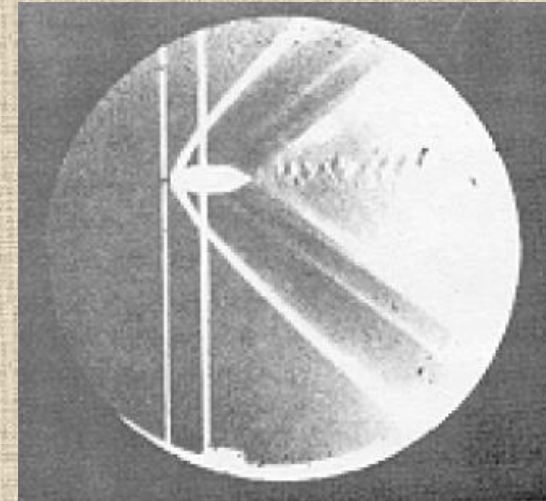


Source: https://upload.wikimedia.org/wikipedia/commons/thumb/b/be/Ernst_Mach_01.jpg/648px-Ernst_Mach_01.jpg

- First to understand the fundamental principles of supersonic flow



Source: https://www.wired.com/wp-content/uploads/images_blogs/wiredscience/2011/06/supersonic-bullet_660.jpg

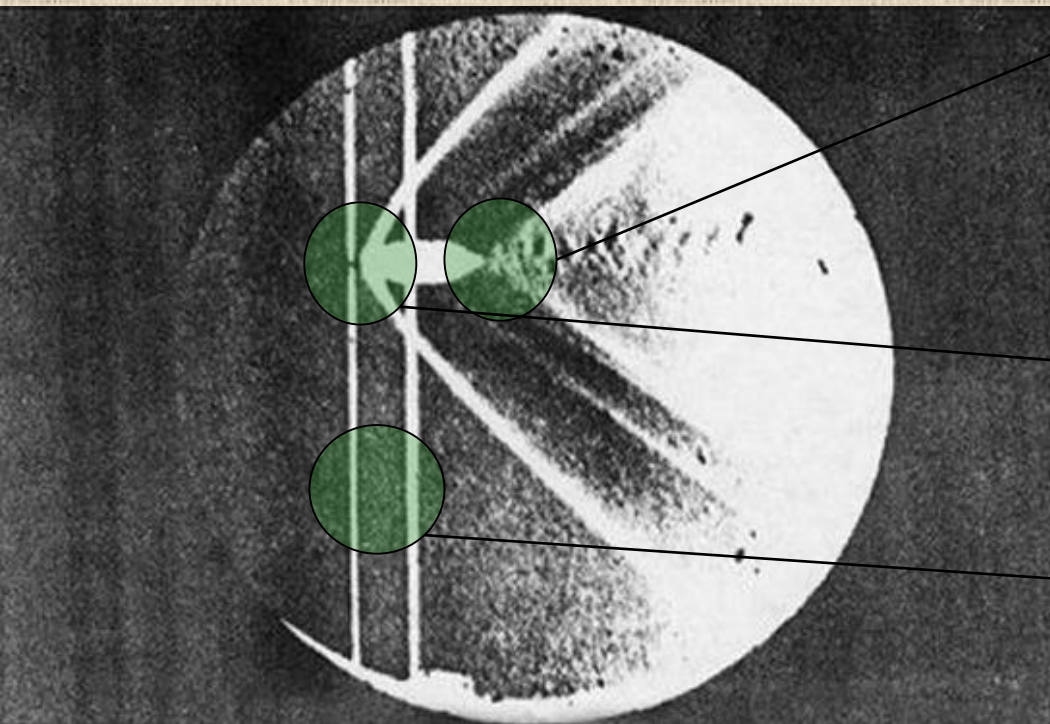


Source: Anderson, J. D., Jr. *History of High Speed Flight and its Technical Development*, AIAA Paper 2000-02, 30th ASM&E, Reno, NV, 2000

- Revolutionary paper *Photographische Fixierung der durch Projektile in der Luft eingeleiten Vorgange*, presented before the Academy of Sciences in Vienna in 1887

SUPERSONIC BULLET EXPERIMENT

- Demonstrated the existence of the shock waves
- Mach photographed shock waves formed by a bullet traveling faster than the speed of sound



weaker shock wave created at the aft end of the bullet

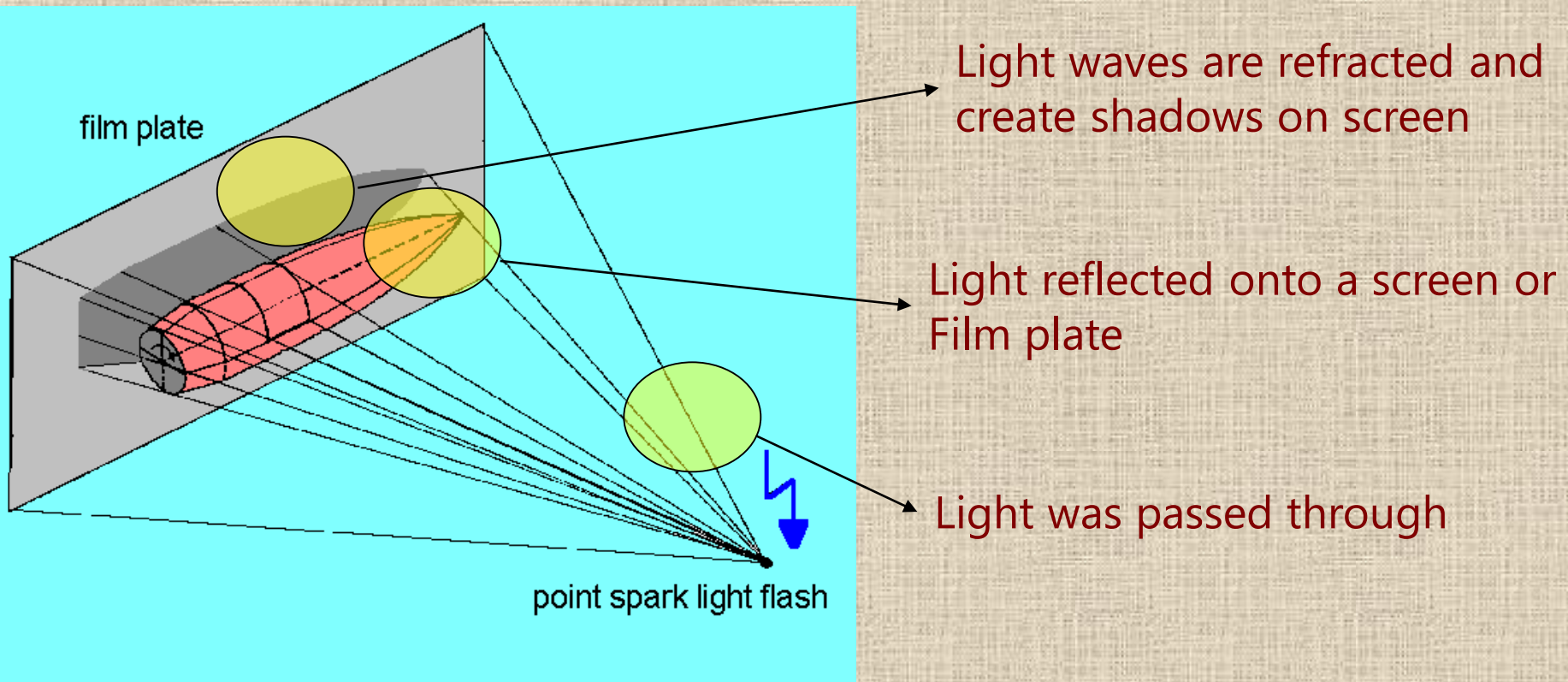
strong shock wave formed by the nose of the bullet

lines made by the trip wires that triggered the camera

Source: <http://www.aerospaceweb.org/question/history/mach/bullet.jpg>

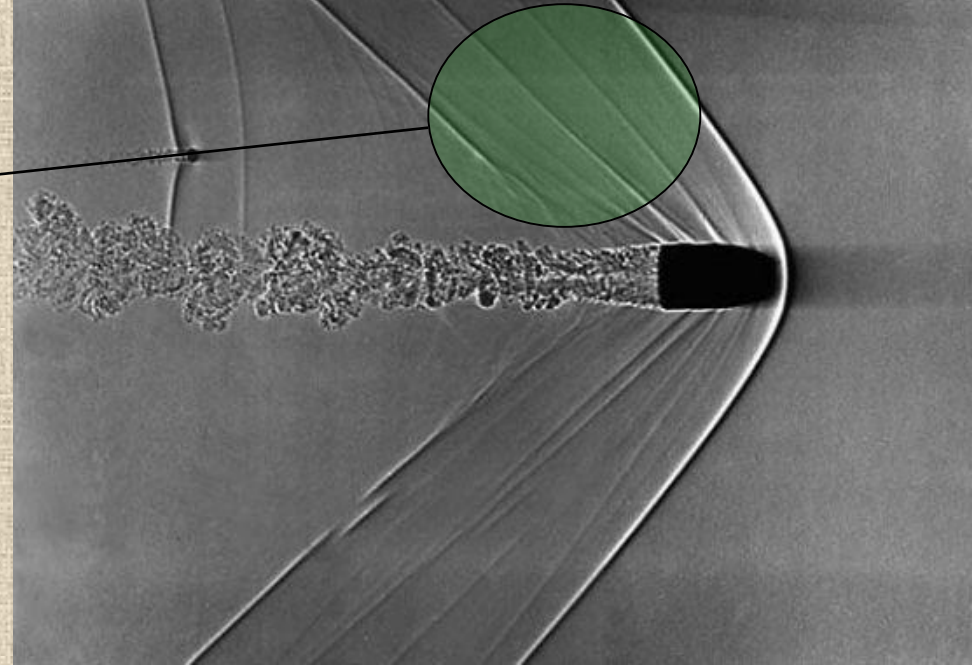
SUPERSONIC BULLET EXPERIMENT

A shadowgraph was used to obtain the photo

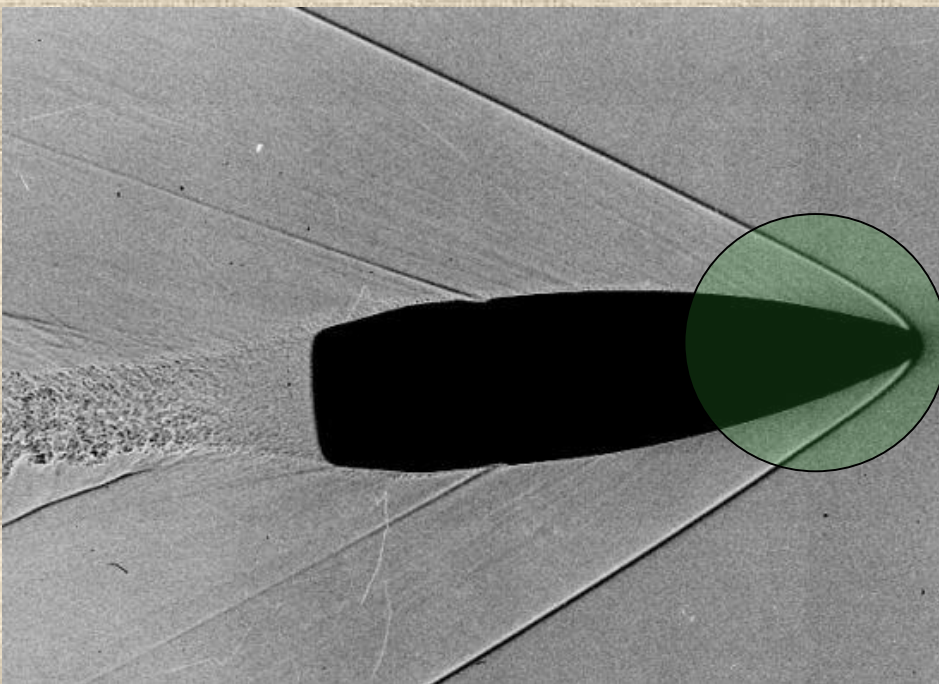


Source: <http://www.aerospaceweb.org/question/history/mach/shadowgraph.gif>

Shock waves create
changes in
temperature and air
flow



Source:<http://www.aerospaceweb.org/question/history/mach/shadowgraph.gif>



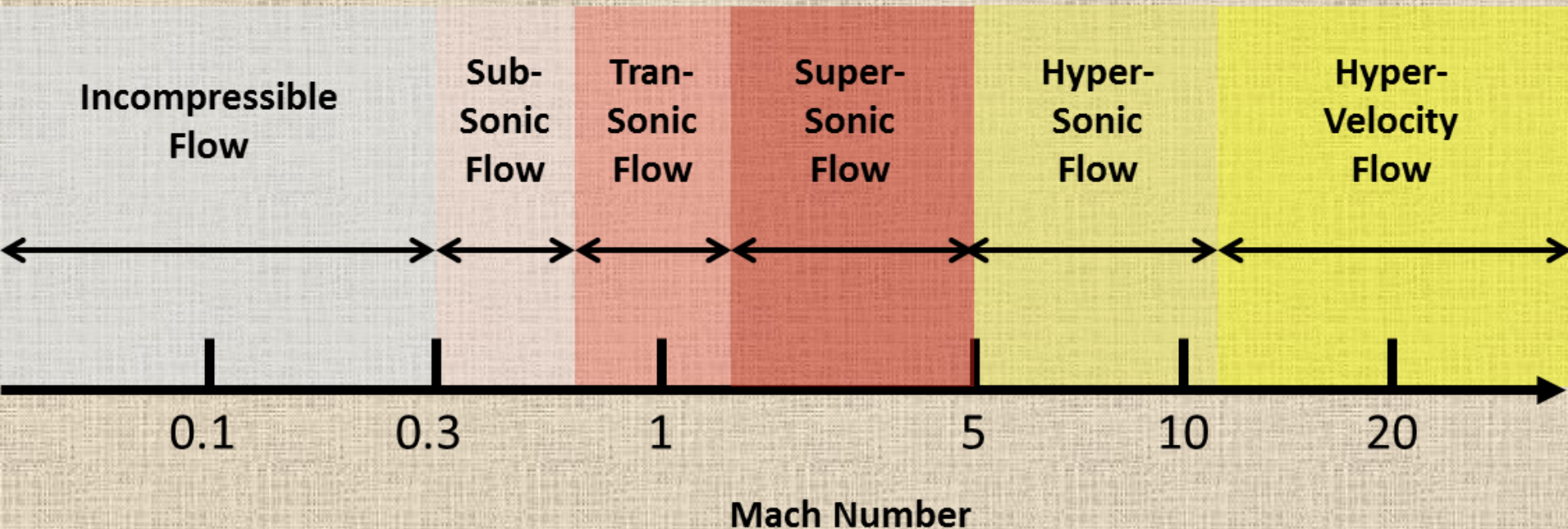
Shadows created on the
screen

Source:<http://www.aerospaceweb.org/question/aerodynamics/bullet/bullet2.jpg>

MACH REGIMES

Division of flight regimes based on Mach number

Mach Number Flow Regimes



Source: https://upload.wikimedia.org/wikipedia/commons/9/95/Mach_Number_Flow_Regimes.png

SUBSONIC FLOW

- Aircraft with high aspect ratio wings and rounded features



Source: <http://1j5jsm2mvi7w2f7x4m23n116.wpengine.netdna-cdn.com/wp-content/uploads/2015/07/ALH-jetbuyfeatured.jpg>

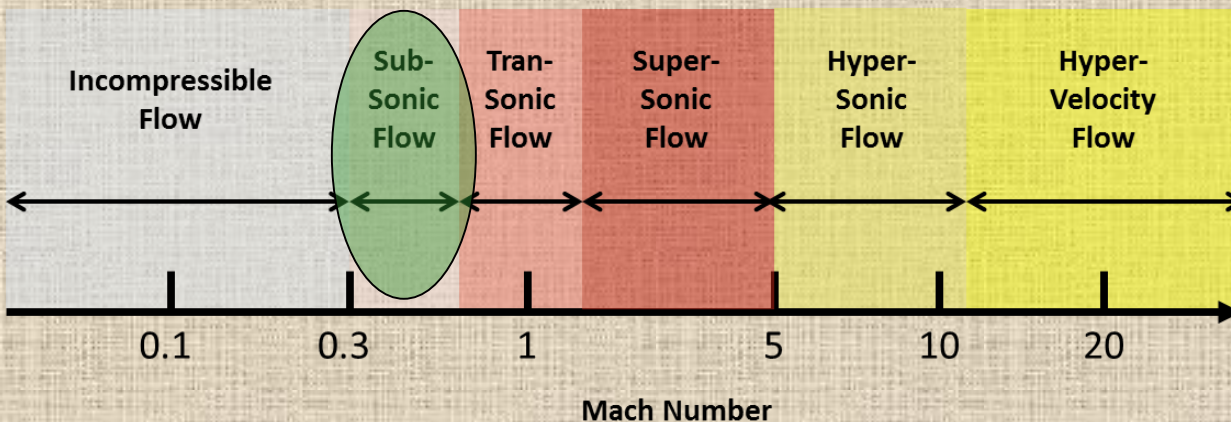
Grumman OV-1 Mohawk



Source: http://i.dailymail.co.uk/i/pix/2016/10/15/01/0A34186C000005DC-3839195-image-a-2_1476489689898.jpg

Focke-Wulf Fw 190

Mach Number Flow Regimes



Source: https://upload.wikimedia.org/wikipedia/commons/9/95/Mach_Number_Flow_Regimes.png

TRANSONIC FLOW

- Region which divides the subsonic and supersonic flows



Source: <http://www.airbusgroup.com/int/en/group-vision/what-we-do.html>

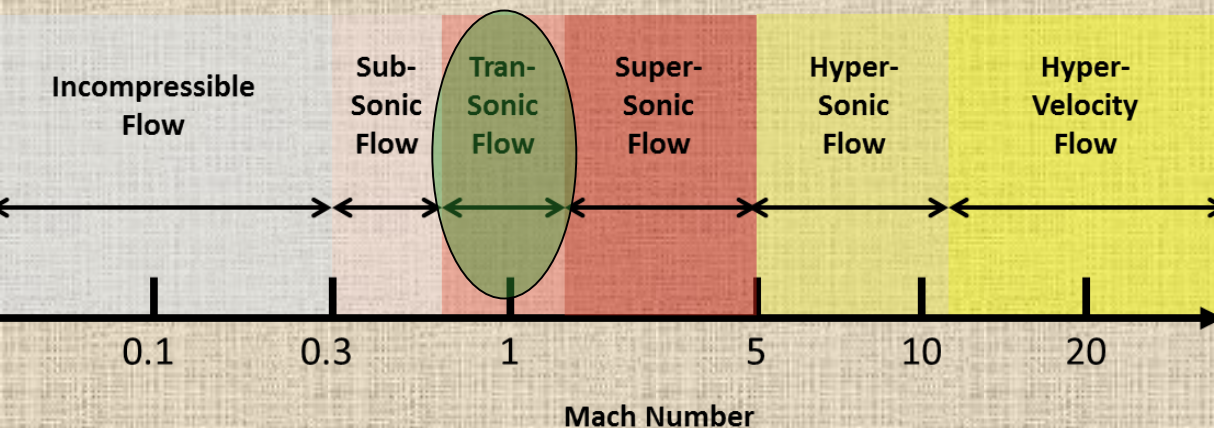
Airbus A350-1000



Source: <http://www.boeing.com/resources/boeingdotcom/commercial/747/assets/images/marquee-747.jpg>

Boeing 747-8

Mach Number Flow Regimes



Source: https://upload.wikimedia.org/wikipedia/commons/9/95/Mach_Number_Flow_Regimes.png

SUPERSONIC FLOW



Source: http://i.dailymail.co.uk/i/pix/2015/01/05/246C29D000000578-0-image-a-5_1420466801321.jpg

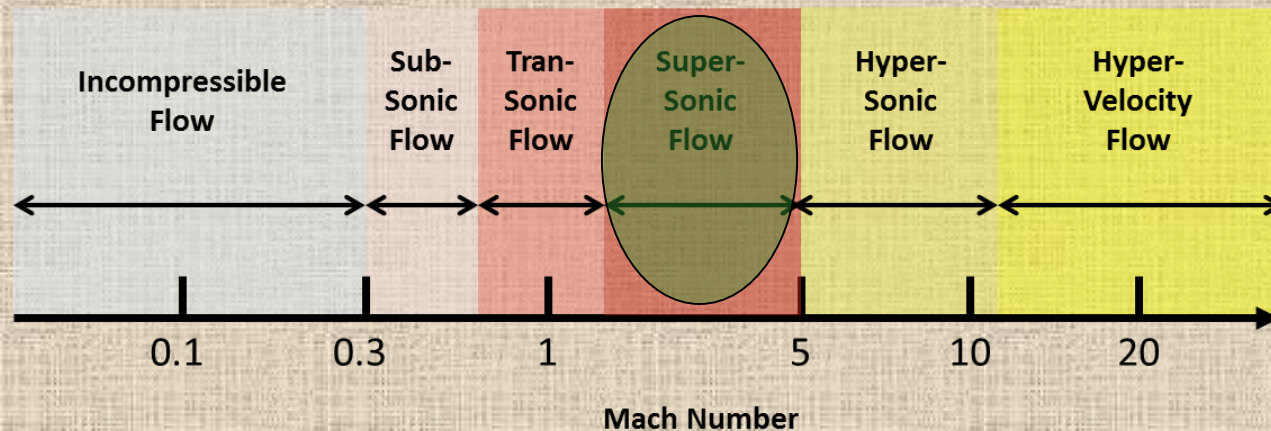


Source: <http://images.indianexpress.com/2016/07/tejas-oped-2-759.jpg>

Boeing F/A-18E/F Super Hornet

HAL Tejas

Mach Number Flow Regimes



Source: https://upload.wikimedia.org/wikipedia/commons/9/95/Mach_Number_Flow_Regimes.png

HYPERSONIC FLOW



Source: https://encrypted-tbn0.gstatic.com/images?q=tbn:ANd9GcT9tDN-en0h0yQjy0sQncQ_gYL7ai8RO7ySmh8Q_p5mqjeQrNsl

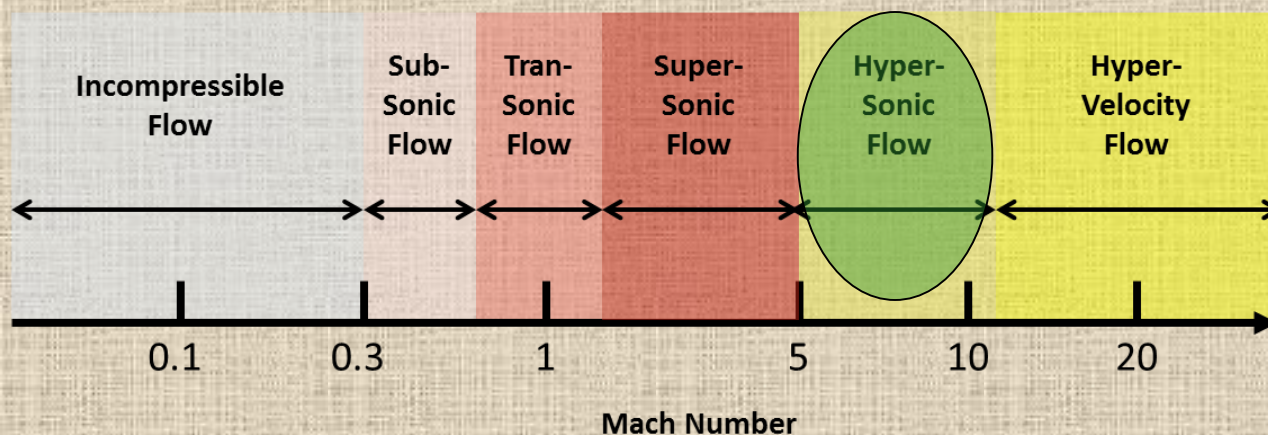
X-43 A Scramjet



Source: https://static.turbosquid.com/Preview/2014/05/21__10_53_06/rend02.jpg1e5d7a4d-c39f-4237-bc41-b4073ce4880bOriginal.jpg

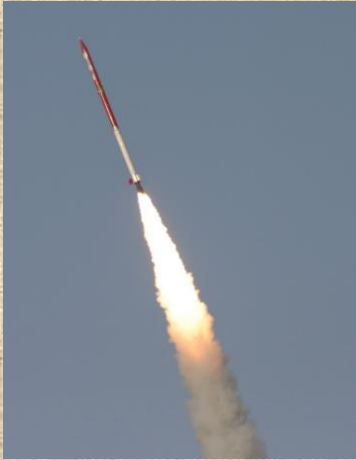
Boeing X-51A (WaveRider)

Mach Number Flow Regimes



Source: https://upload.wikimedia.org/wikipedia/commons/9/95/Mach_Number_Flow_Regimes.png

HYPER VELOCITY FLOW



Source: <http://www.space-rockets.com/photo/launch1.jpg>

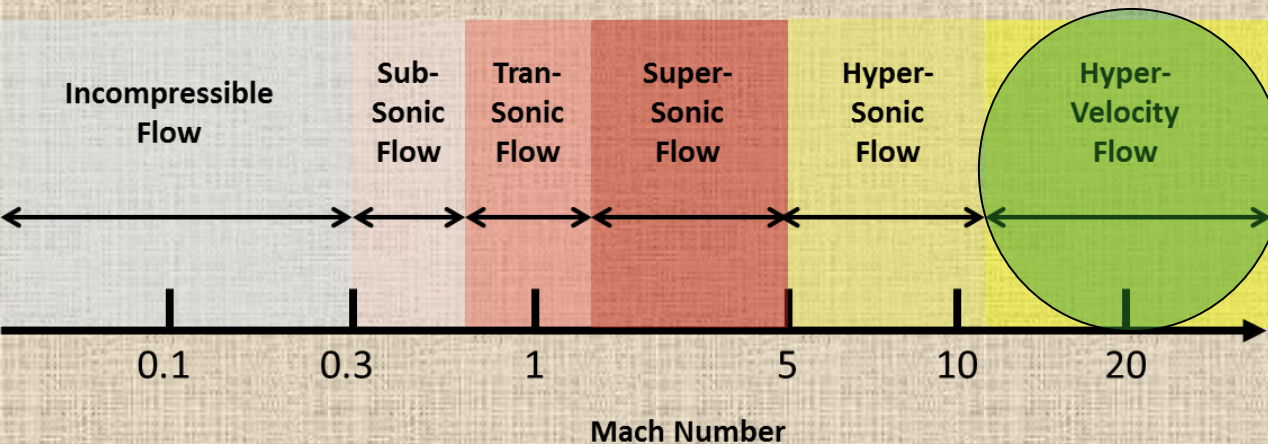
Pathfinder



Source: <https://www.nasa.gov/sites/default/files/orion-d4-liftoff-ingalls.jpg>

ULA Delta IV

Mach Number Flow Regimes



Source: https://upload.wikimedia.org/wikipedia/commons/9/95/Mach_Number_Flow_Regimes.png

Mach Number of aircrafts, spacecraft and missiles



Source: https://encrypted-tbn0.gstatic.com/images?q=tbn:ANd9GcT9tDN-en0h0yQjy0sQncQ_gYL7ai8RO7ySmh8Q_p5mqjeQrNsl

X-43 A Scramjet

- Mach 9.6
- Highest speed aircraft



Source: https://upload.wikimedia.org/wikipedia/commons/thumb/2/20/AGM-84_Harpoon_launched_from_USS_Leahy_%28CG-16%29.jpg/330px-AGM-84_Harpoon_launched_from_USS_Leahy_%28CG-16%29.jpg

Exocet missile

- Mach 3-5



Source: <https://upload.wikimedia.org/wikipedia/commons/thumb/3/34/Skylab-73-HC-440HR.jpg/220px-Skylab-73-HC-440HR.jpg>

Saturn V

- Mach 13

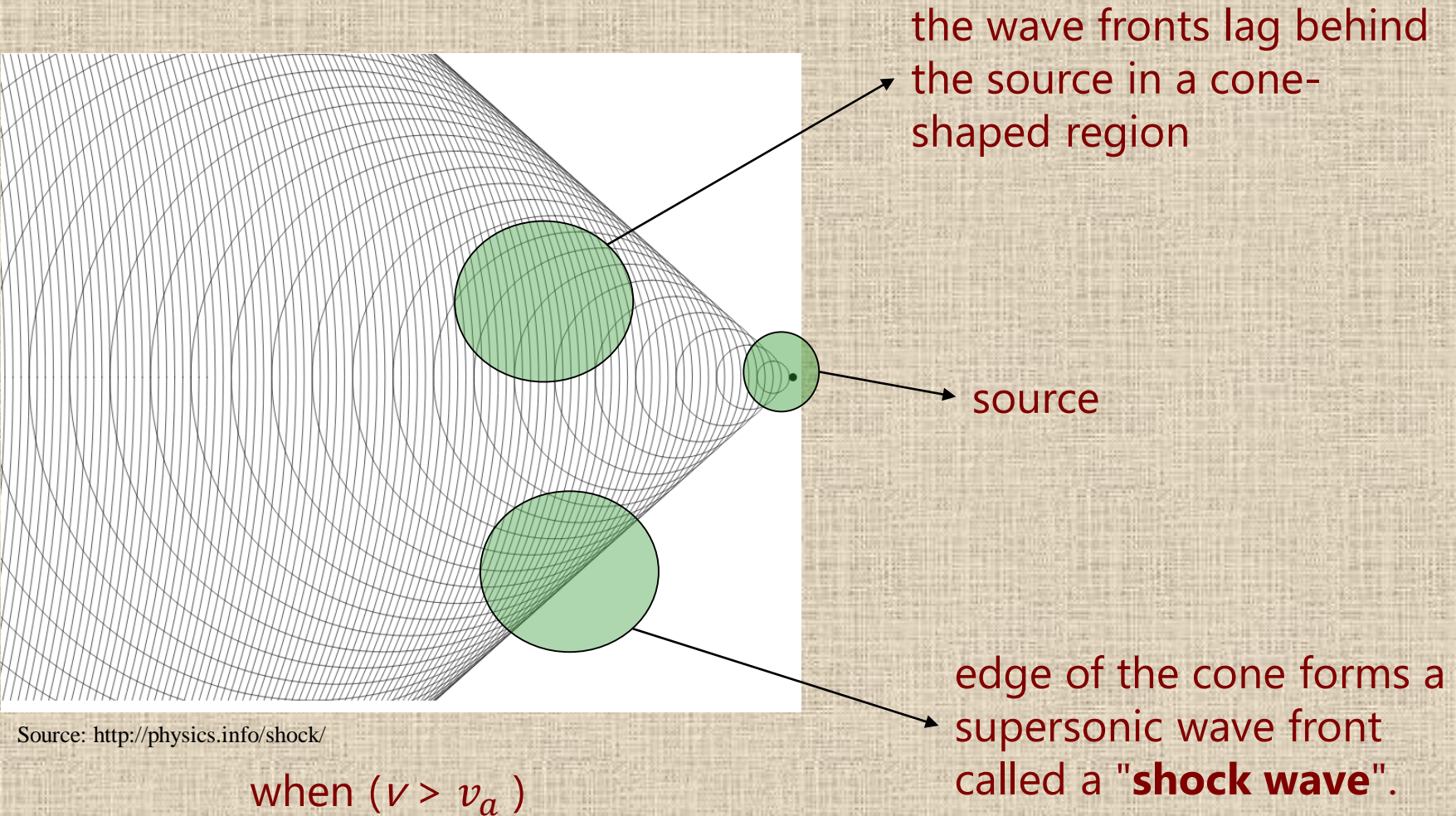
MACH WAVES

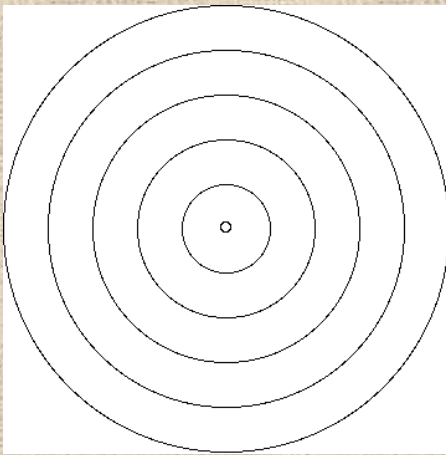
- $V_{mach\ waves} > V_{sound}$
- sudden change in stress, density and temperature

Source: <https://www.youtube.com/watch?v=-Zu5SGllmwc>

$$V_{shock\ wave} \uparrow \leftrightarrow Amplitude \uparrow$$

FORMATION OF SHOCK WAVES

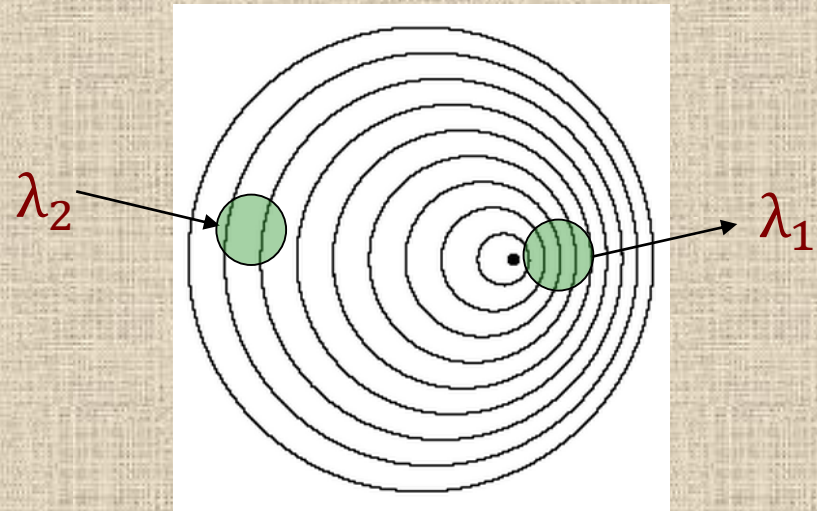




Source: <http://www.exo.net/~pauld/workshops/ligo/dopplercircles.gif>

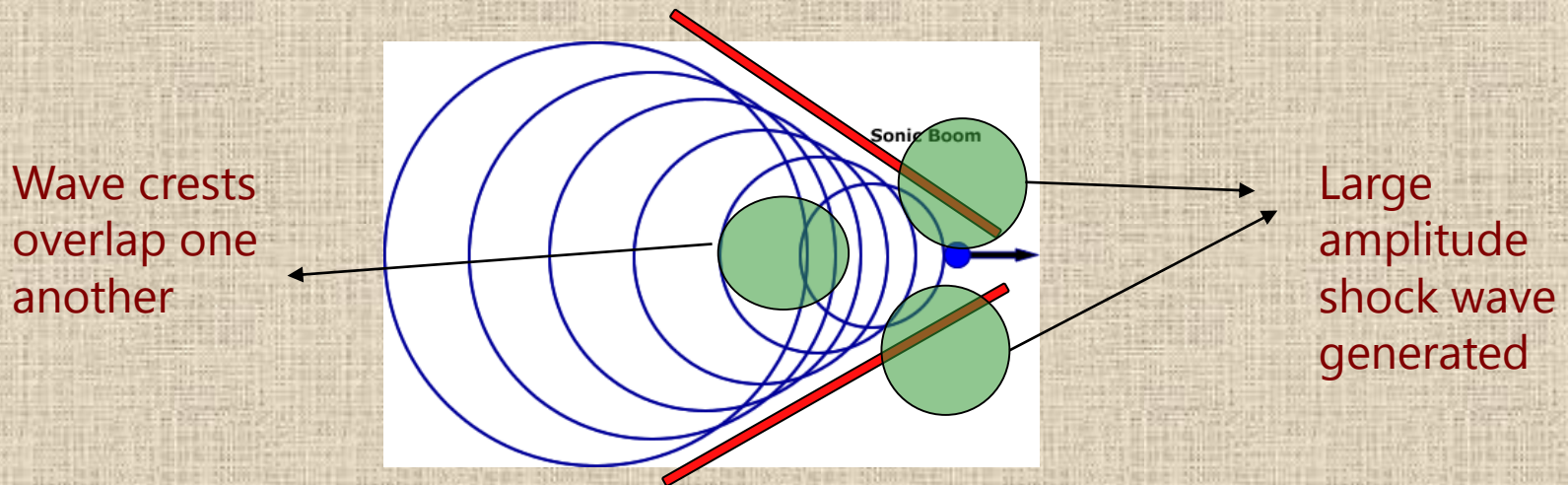
Stationary sound wave

Doppler effect takes place and $\lambda_1 < \lambda_2$



Source: <https://uprepcharlie.files.wordpress.com/2013/05/circles.png/>

Subsonic sound wave



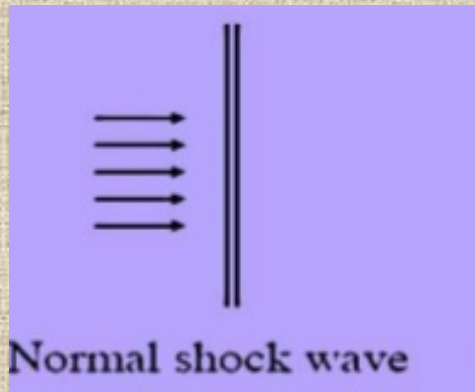
Source: http://www.school-for-champions.com/science/images/sound_traveling_faster_sonic_boom.gif

Supersonic sound wave

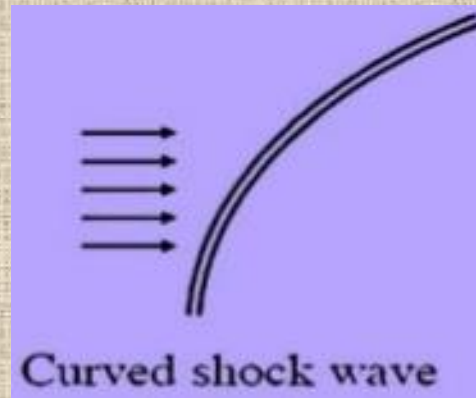
Types of shock waves

Normal Shock

Shock wave \perp flow direction

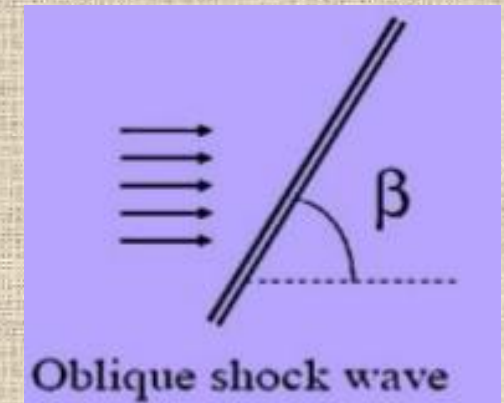


Curved Shock



Oblique Shock

- Shock wave not \perp flow direction
- Decreases with Mach number



SONIC BOOM



Source: <https://www.youtube.com/watch?v=x6DUbxCpszU>

MY
EARS!!



Source: https://img.buzzfeed.com/buzzfeed-static/static/2015-02/23/11/enhanced/webdr03/original-19818-1424710169-33.png?downsize=715:*&output-format=auto&output-quality=auto

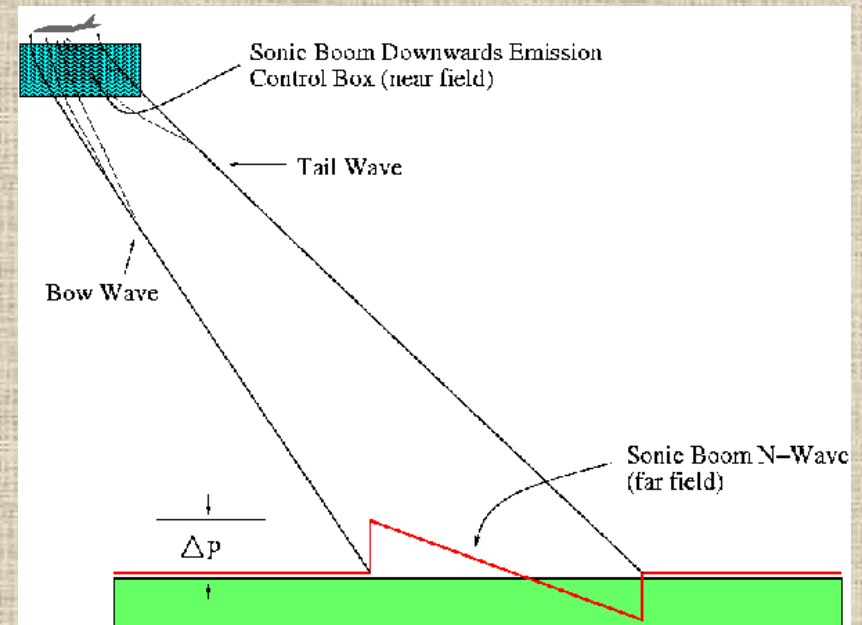


SONIC BOOM

- Loud noise created by shock wave
- Coherent addition of wave → creation of strong sum wave

Source: <https://www.scienceabc.com/wp-content/uploads/2017/04/Military-jet-plane-sonic-boom.jpg>

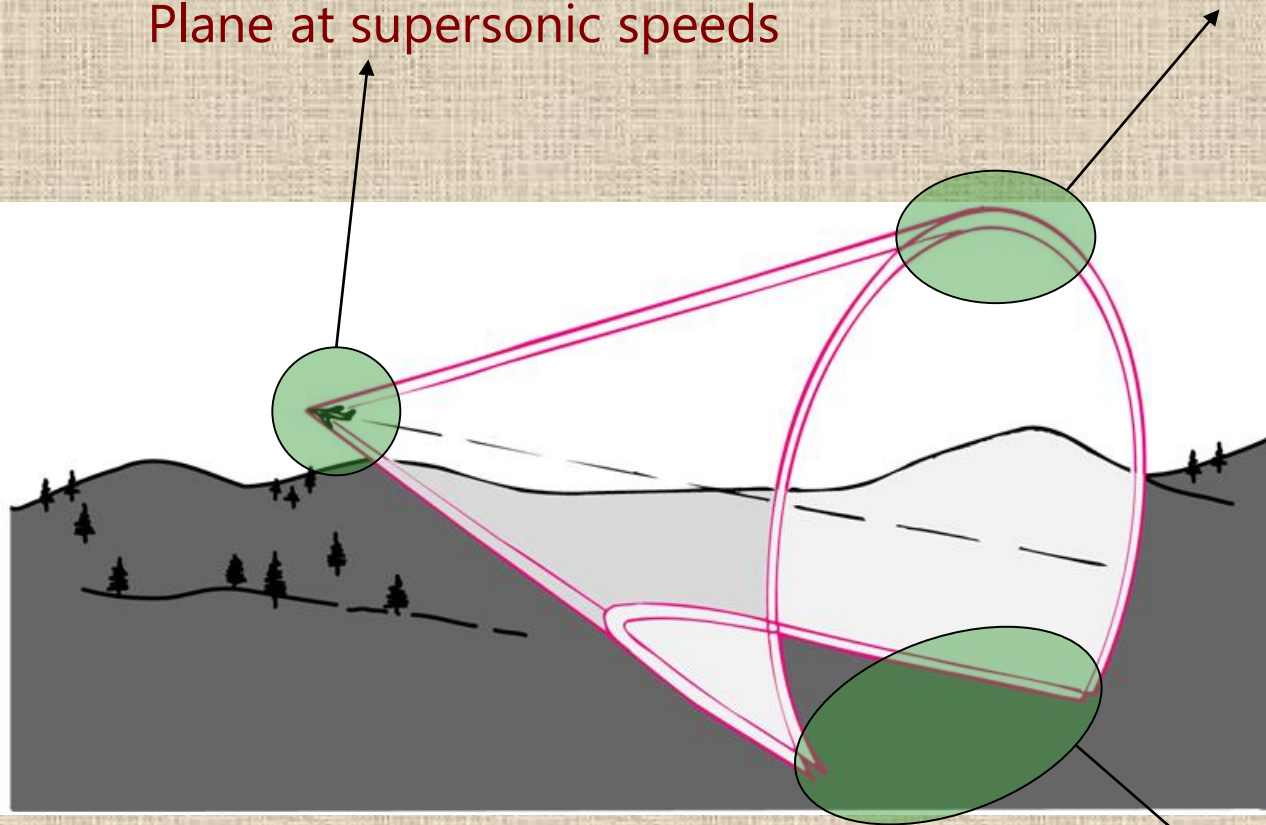
- Boom experienced when there is a sudden change in pressure
- Overall pressure profile known as *N-wave*



Source: <https://qph.ec.quoracdn.net/main-qimg-c921e1f0659b74c8de6eece7ff7eadc>

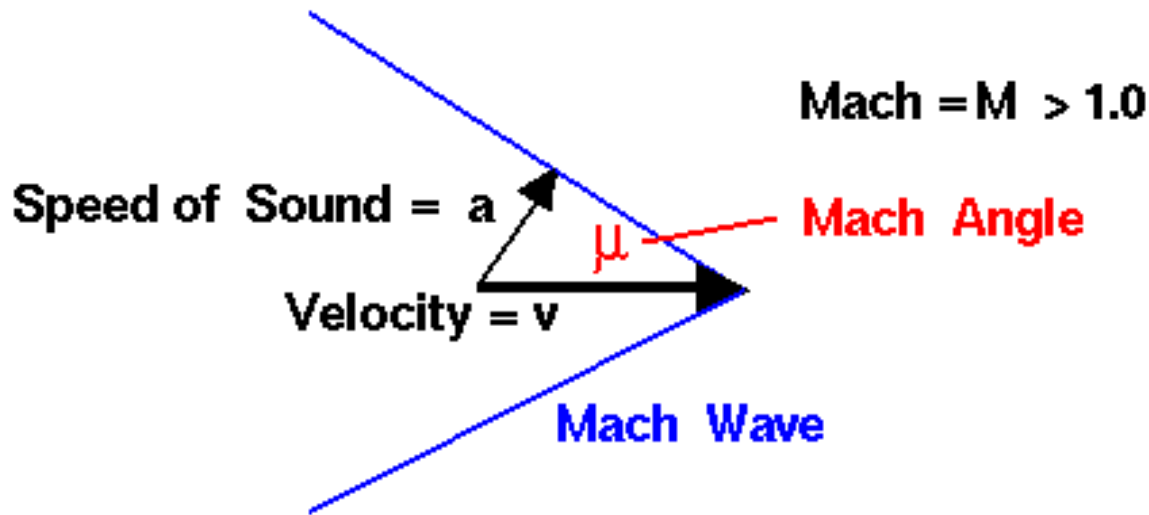
A conical pressure wave front is produced called **Mach Cone**

Plane at supersonic speeds



Mach cone meets the ground creating a hyperbolic area called **Boom Carpet**

Mach Angle



Source: <https://www.grc.nasa.gov/www/k-12/airplane/machang.html>

Mach angle is the angle a shock wave makes with the direction of motion

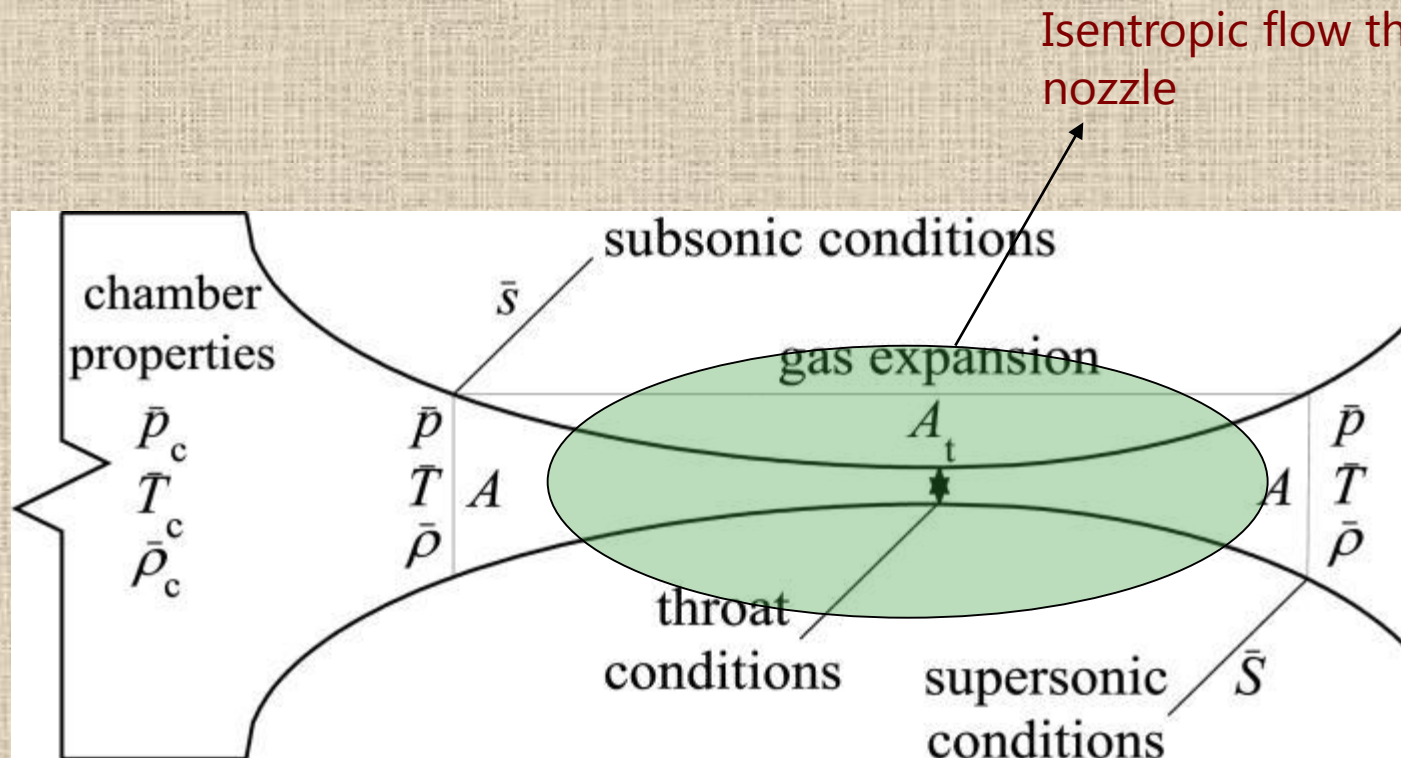
$$\sin \mu = \frac{a}{v}$$

$$\sin \mu = \frac{1}{M}$$

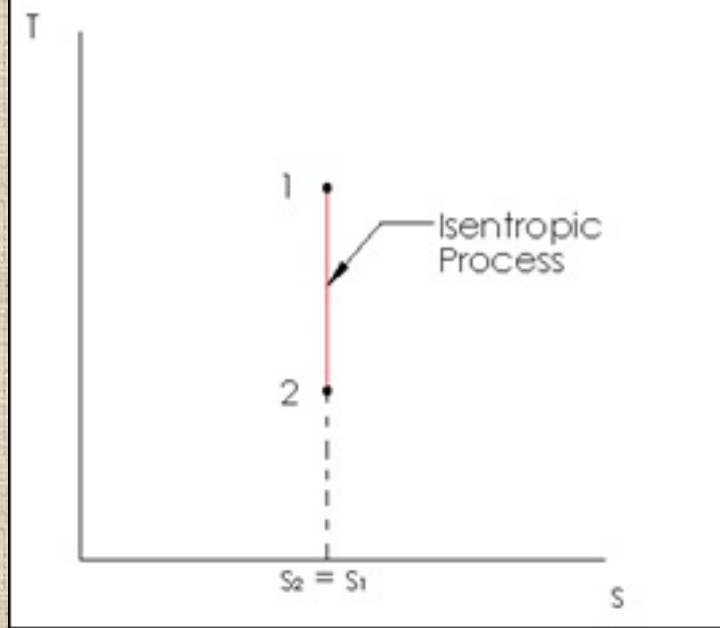
$$\mu = \sin^{-1} \frac{1}{M}$$

ISENTROPIC FLOW

- Reversible flow at constant value of entropy
- Sound waves creation → isentropic process
- change in flow variables → small and gradual



Source: http://gasturbinespower.asmedigitalcollection.asme.org/data/journals/jetpez/27186/031201_1_1_1.jpeg

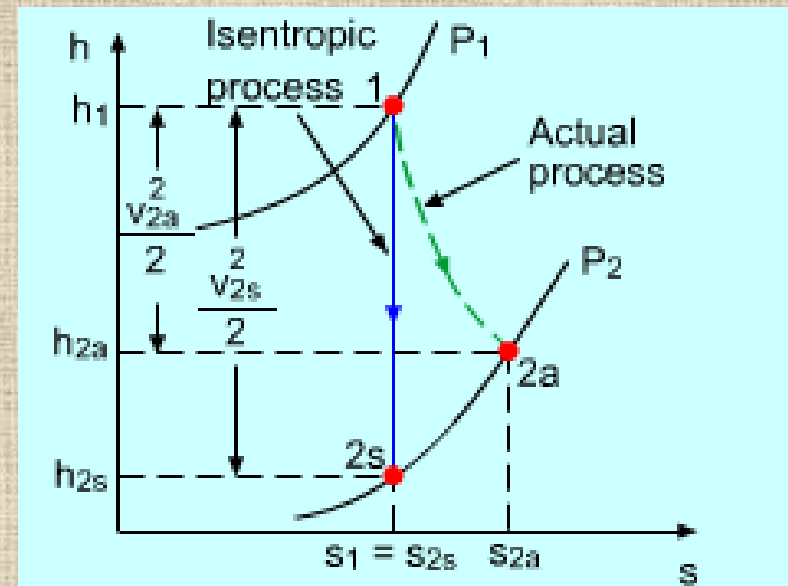


Source: <http://engineering-references.sbaivent.com/thermodynamics/pictures/isentropic-process.jpg>

T-S Diagram

- energy can be exchanged with the flow → as long as it doesn't happen as heat exchange.
- Example: an isentropic expansion or compression

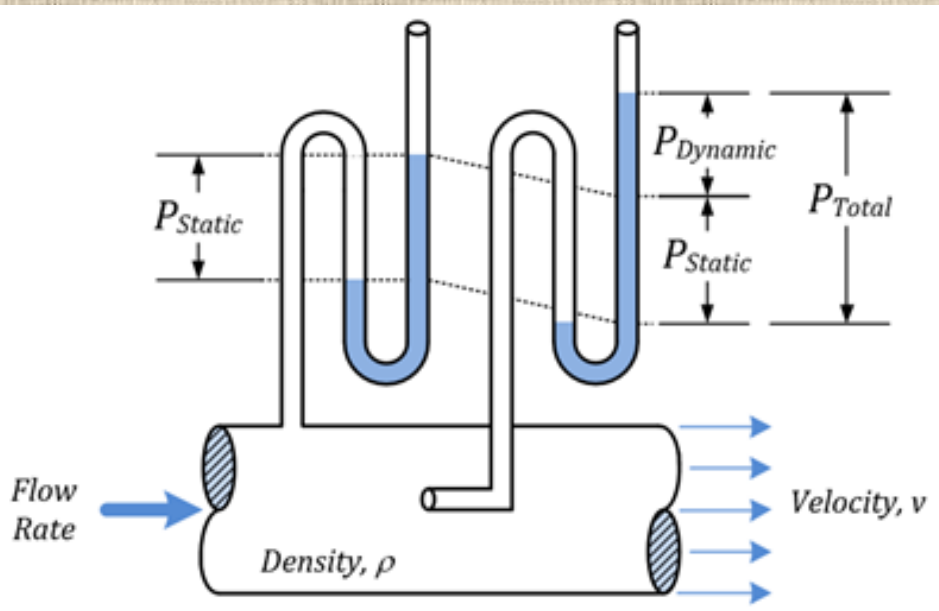
- No heat is added to the flow
- No energy transformations occur due to friction or dissipative effects



Source: <http://www.ecourses.ou.edu/ebook/thermodynamics/ch06/sec065/media/th060508p.gif>

h-s Diagram

TOTAL PRESSURE



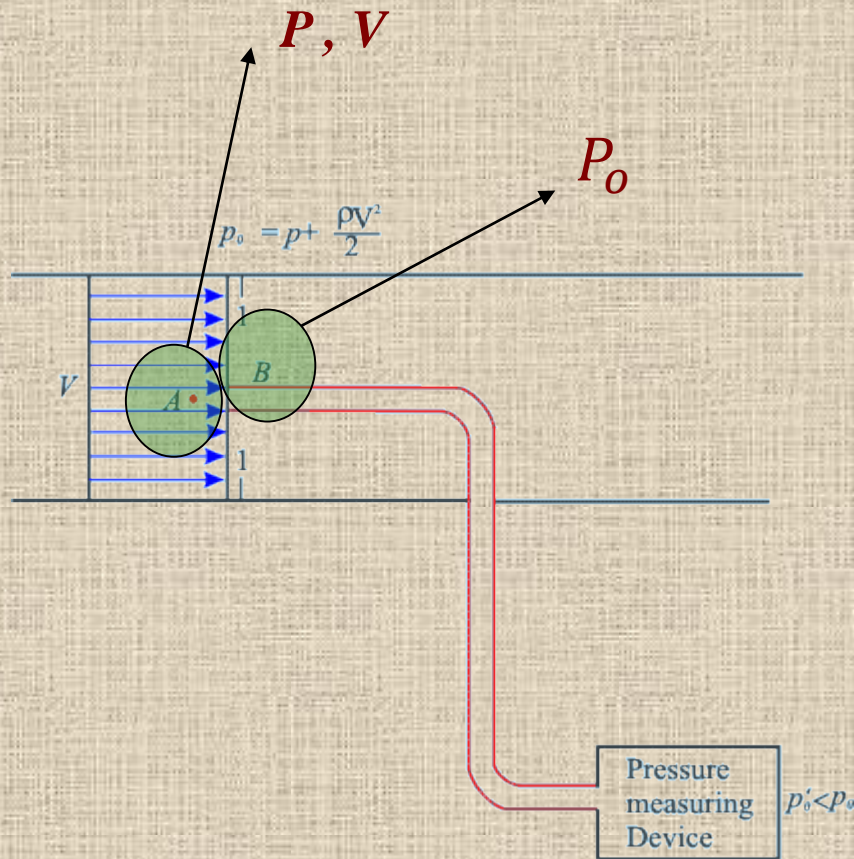
Source: <https://eng-software.com/media/1771/pressure2.png?width=400px&height=256px>

- Pressure developed if the fluid were brought to rest isentropically
- The entire kinetic energy of the fluid particle is utilized to increase its pressure only
- This is possible only in an isentropic process

$$P_{total} = P_{static} + P_{dynamic}$$

Assuming incompressible flow

Applying Bernoulli at A and B



$$P_o = \underbrace{P}_{\text{Static pressure}} + \underbrace{\frac{\rho V^2}{2}}_{\text{Dynamic Pressure}}$$

Source: http://www.nptel.ac.in/courses/112104118/lecture-16/images/fig_16.2.gif

$$V = \sqrt{2\left(\frac{P_o - P}{\rho}\right)}$$

TOTAL TEMPERATURE



Source: <https://wahlco.com/wp-content/uploads/2016/01/stagnation-thermocouple.jpg>

- Temperature developed when the moving flow is isentropically brought to a halt
- depends on the Mach number of the flow
- total temperature measured using thermocouples

$$T_{total} = T_{static} + T_{dynamic}$$

Assuming Isentropic flow, the relation between Total and Static temperature is

$$T_t = T \left(1 + \frac{\gamma - 1}{2} M^2 \right)$$

The diagram shows the equation $T_t = T \left(1 + \frac{\gamma - 1}{2} M^2 \right)$ with green circles around T_t , T , $\gamma - 1$, and M^2 . Arrows point from these circles to their respective labels: T_t to Total Temperature, T to Static Temperature, $\gamma - 1$ to Specific Heat Ratio, and M^2 to Mach Number.

Total Temperature

Static Temperature

Specific Heat Ratio

Mach Number

Also

$$\frac{P}{P_o} = \left(\frac{T}{T_t} \right)^{\frac{\gamma}{\gamma - 1}}$$

The diagram shows the equation $\frac{P}{P_o} = \left(\frac{T}{T_t} \right)^{\frac{\gamma}{\gamma - 1}}$ with a green circle around P_o . An arrow points from this circle to the label Total Pressure.

Total Pressure