



Plane Change Manoeuvres



Orbit Plane Change Requirements

There are times when it is **necessary** to change **plane** of an orbit, after the **satellite** establishes an **initial** orbit. It may also be needed for **inter-planetary** missions.

Plane change also is required if a **satellite**, launched into an **equatorial** orbit, is needed above a **different** latitude.



Orbit Plane Change Features

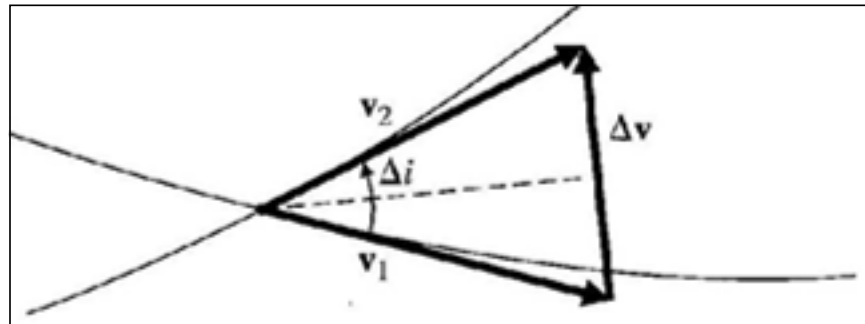
This is **particularly** true for sites in **higher** latitude (e.g. **Kiev** in Ukraine), for achieving **equatorial** orbits.

A change in **orbital** plane is an **expensive** manoeuvre and **every** effort is **made** to either avoid or **minimize** it.



Inclination Changing Concept

Plane change requires **non-coplanar** velocity impulse, as **shown** in the figure below.





Inclination Changing Formulation

In the **general** case when we want both the **orbit** and its **plane** to change, we can write the **following** relation.

$$\Delta V^2 = V_1^2 + V_2^2 - 2V_1V_2 \cos \Delta i$$

If both **orbits** are same except **inclination**, $V_1 = V_2 = V$.



Orbit Plane Changing Solution

The expression for ' ΔV ' can be simplified as follows.

$$\Delta V^2 = 2V^2(1 - \cos \Delta i) \rightarrow \Delta V = \sqrt{2} \cdot V \sqrt{1 - \cos \Delta i} = 2V \sin \frac{\Delta i}{2}$$

This ' ΔV ' **instantaneously** changes the orbit **inclination**.



Orbit Plane Change Solution Features

Small changes in 'i' are possible **anywhere** on the orbit.

However, for **large** inclination **changes**, impulse requirements are **large**, and hence large **changes** in 'i' are carried out where **local** velocity is **small**.



Large Inclination Changing Concept

In general, large **inclination** change is more **efficient** at **apogee**, in comparison to **perigee**, as shown below.

$$\frac{\Delta v_a}{\Delta v_p} = \frac{v_a}{v_p} = \frac{r_p}{r_a} = \frac{1-e}{1+e}$$



Large Inclination Changing Strategy

We see that ' ΔV ' required **reduces** with increase in ' e ' and becomes **zero** for $e = 1$.

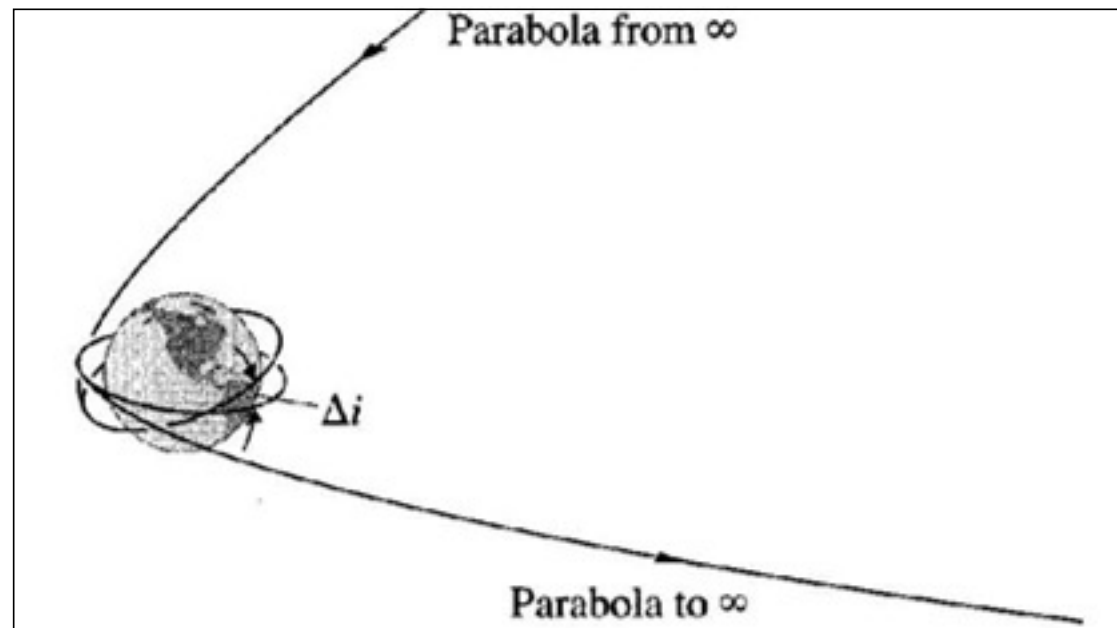
This has resulted in a novel way of **changing** ' i ', which involves **increase** in e to **1**, change of ' i ' & decrease in ' e ' **back** to original.

This manoeuvre requires **two** velocity impulses **equal** in magnitude **but** opposite in **direction**.



Orbit Plane Changing with $e \sim 1$

Consider an **inclination** change for two **circular** orbits, as shown **below**, through a nearly **parabolic** trajectory.





Orbit Plane Changing with Parabola

Initially, spacecraft is put on an **approximate** parabola and is allowed to **travel** until it reaches its **apogee**.

At this point, a **very** small normal **impulse** is sufficient to **rotate** the H vector through the **required** angle.



Orbit Plane Changing with Parabola

Once the **plane** is changed, spacecraft **returns** along the other **branch** to perigee, where next in-plane **impulse** brings it back to **circle** so that total ΔV for **e ~ 1** is,

$$\Delta V \approx 2 \left[\sqrt{\frac{2\mu}{r}} - \sqrt{\frac{\mu}{r}} \right] = 2(\sqrt{2} - 1)v_{cir} = 0.828v_{cir}; \quad v_{cir} = \sqrt{\frac{\mu}{r}}$$

Above solution is **independent** of inclination **change**.



Combined Orbit & Plane Changing

In **situations**, where there is a **need** to change both the **orbit** nature and its **plane**, there are many **possibilities**.

In **one** case, we can first **enter** the new orbit and then **later** give impulse for the **plane** change.



Combined Orbit & Plane Changing

In another case, we can **enter** the new orbit and **wait** for spacecraft to reach **apogee** and then make plane **change**.

Lastly, we can make both the **changes** simultaneously at **perigee**.



Summary

In **conclusion**, we see that plane change, though **feasible**, is an expensive manoeuvre and, **hence**, should be avoided, as far as **possible**.

In this **context** we also note that use of **parabola** for plane change is helpful when **large** plane changes are **needed**.