

Impact of Drag



Drag Loss Example - Slow Burn

 $\mathbf{m_0} = \mathbf{80} \ \mathbf{T}, \ \mathbf{m_p} = 60 \ \mathbf{T}, \ \mathbf{I_{sp}} = 240 \ \mathbf{s}, \ \mathbf{g_0} = 9.81 \mathrm{m/s^2}, \ \boldsymbol{\beta} = \mathbf{600}$ kg/s, $\mathbf{C_{D0}} = 1.0, \ \mathbf{S_r} = \pi \ \mathrm{m^2}. \ \mathbf{D}$ is maximum at $t = 50 \mathrm{s}.$

Determine the **impact** of drag on burnout **parameters**.

Non-drag Values: $V_b = 2.30 \text{ km/s}$, $h_b = 78.3 \text{ km}$,

 $\mathbf{h_{50s}} = 13.2 \text{ km}, \, \mathbf{\rho_{50s}} = 0.267 \text{ kg/m}^3, \, \mathbf{V_{50s}} = 616 \text{ m/s}$

 $D_{50s} = 159.1 \text{ kN}, m_{50s} = 50 \text{ Tons}, a_{D50s} = 3.18 \text{ m/s}^2$

 $a_D = 1.59 \text{ m/s}^2$, $V_{b-drag} = 2.14 \text{ km/s}$, $h_{b-drag} = 70.3 \text{ km}$



Drag Loss Example - Fast Burn

 $\mathbf{m_0} = \mathbf{80} \, \mathbf{T}, \, \mathbf{m_p} = 60 \, \mathbf{T}, \, \mathbf{I_{sp}} = 240 \, \mathbf{s}, \, \mathbf{g_0} = 9.81 \, \mathrm{m/s^2}, \, \boldsymbol{\beta} = \mathbf{3000} \, \mathrm{kg/s}, \, \mathbf{C_{D0}} = 1.0, \, \mathbf{S_r} = \boldsymbol{\pi} \, \mathrm{m^2}. \, \mathrm{D} \, \mathrm{is} \, \mathrm{maximum} \, \mathrm{at} \, \, \mathbf{t} = \mathbf{15s}.$

Determine the **impact** of drag on burnout **parameters**.

Non-drag values: $V_b = 3.07 \text{ km/s}, h_b = 23.4 \text{ km},$

 $\mathbf{h_{15s}} = 11.5 \text{ km}, \, \mathbf{\rho_{15s}} = 0.337 \text{ kg/m}^3, \, \mathbf{V_{15s}} = 1799.2 \text{ m/s}$

 $\mathbf{D_{15s}} = 1713.6 \text{ kN}, \mathbf{m_{15s}} = 35 \text{ Tons}, \mathbf{a_{D15s}} = 48.96 \text{ m/s}^2$

 $\mathbf{a_D} = 24.48 \text{ m/s}^2$, $\mathbf{V_{b-drag}} = 2.58 \text{ km/s}$, $\mathbf{h_{b-drag}} = 18.5 \text{ km}$



Impact of Burn Rate on Overall Performance

The **results** obtained for drag **bring** out the fact that **drag** loss increases rapidly as we **increase** the burn rate.

On the **other** hand, we have already **seen** that gravity loss reduces **significantly** with increase in burn **rate**.

Therefore, we **realize** that there is **possibility** of a burn rate for which the **both** these losses can be kept **minimum** so that combined loss may **also** be a minimum.



Combined Minimum Loss Example

 $\mathbf{m_0} = \mathbf{80} \, \mathbf{T}, \, \mathbf{m_p} = 60 \, \mathbf{T}, \, \mathbf{I_{sp}} = \mathbf{240} \, \mathbf{s}, \, \mathbf{g_0} = 9.81 \, \text{m/s}^2, \, \mathbf{C_{D0}} = 1.0, \, \mathbf{S_r} = \boldsymbol{\pi} \, \mathbf{m}^2.$

Obtain the variation of combined **energy** loss as a function of **burn** rate and locate the **minima** and determine the corresponding **optimal** burn rate.

Let us **assume** that drag profile **peak** is at 12 km altitude and **use** β in the range 400 to **1200**.

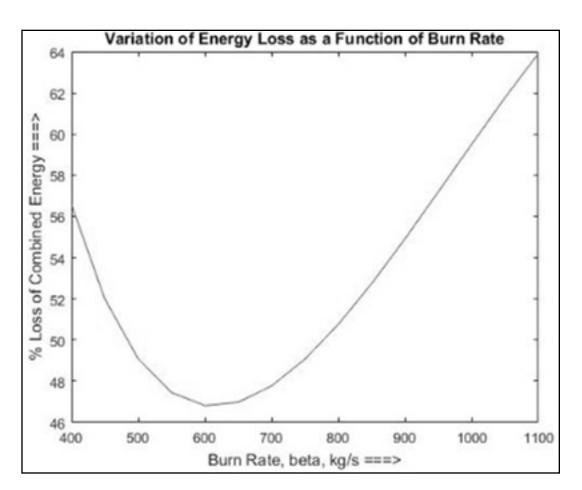


Combined Minimum Loss Example

An **approximate** solution for this case is **shown** alongside.

We note that the **minima** in this case is close to $\beta = 600$ kg/s.

However, this is only an **approximation** and we need a more rigorous **analysis** to arrive at the **optimal** burn rate.





A Generic Solution for Optimal \beta

While, a **rigorous** solution for ' β ' is generally carried out **towards** end of design, there is a need for a **gross** value at the start of the **design**, in order to assess **performance**.

Such a **value** can be typically obtained by using the **hypothesis** that an optimal ' β ' would lie close to the **trajectory** that has equal gravity and **drag** loss.

This is **based** on the fact that the **variation** of these two effects are **broadly** similar and also that when **gravity** is secondary effect, **drag** is tertiary effect and vice **versa**.



Summary

An **optimal** burn rate exists that **results** in the most efficient **mission** for a given vehicle from the **point** of view of minimizing the **combined** gravity and drag loss.