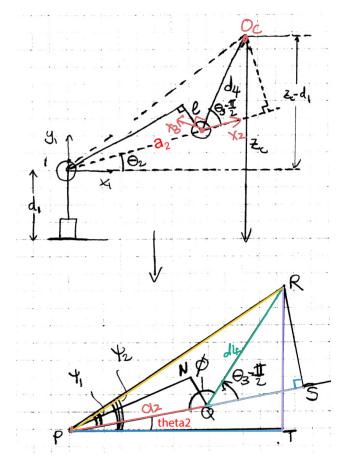


$$\theta_1 = \phi - \psi = a \tan 2(\gamma_c, x_c) - a \tan 2(-d_2, \sqrt{\chi_2^2 + {\gamma_1}^2 - d_2^2})$$

Side View: (graph copied from hints)



$$\overline{RT} = 2c - d_1$$

$$\overline{PT} = \sqrt{\chi_c^2 + \gamma_c^2 - d_2^2}$$

$$\overline{PR} = \sqrt{(2c - d_1)^2 + \chi_c^2 + \gamma_c^2 - d_2^2}$$

$$\overline{PQ} = \alpha_2$$

$$\overline{QR} = d_4$$

D low of cosine to
$$\triangle PQR$$

$$\overline{PR^2} = \overline{PQ^2} + \overline{QR^2} - 2\overline{PQ} \overline{QR} \cos(\phi)$$

$$(2c-d_1)^2 + \chi_c^2 + \gamma_c^2 - d_2^2 = \alpha_2^2 + d_4^2 - 2\alpha_2 d_4 \cos(\phi)$$

$$\cos(\phi) = \frac{\alpha_2^2 + d_4^2 - (2c - d_1)^2 - Xc^2 - Yc^2}{2 \alpha_2 d_4}$$

$$\phi = \cot(\alpha_1 - \alpha_2 + d_4)^2 + \cos(\phi)$$

$$\phi = \pi - (\theta_3 - \frac{\pi}{2}) = \frac{3\pi}{2} - \theta_3$$

$$\theta_3 = \frac{3\pi}{2} - \phi = \frac{3\pi}{2} - \cot(1 + \sqrt{1 - \cos(6)^2}, \cos(6))$$

With θ_3 known, we can calculate \overline{QS} $\overline{QS} = \overline{\overline{QS}} = \overline{\overline{QS}}$ $\overline{QS} = d_4 COS(\theta_3 - \frac{7}{2})$ $\overline{PS} = \overline{PQ} + \overline{QS} = a_2 + d_4 COS(\theta_3 - \frac{7}{2})$ $\overline{RS} = d_4 \sin(\theta_3 - \frac{7}{2})$ $\overline{Y_1} = atan_2(\overline{RS}, \overline{PS})$ $\overline{Y_1} = atan_2(\overline{d_4} \sin(\theta_3 - \frac{7}{2}), a_2 + d_4 COS(\theta_3 - \frac{7}{2}))$

$$Ψ_2 = Otan_2(RT, PT)$$
 $Ψ_2 = atan_2(Z_c - d_1, \sqrt{x_c^2 + x_c^2 - d_2^2})$
 $Ω_2 = Ψ_2 - Ψ_1$

$$\theta_2 = atan_2(z_c - d_1, \sqrt{x_c^2 + y_c^2 - d_2^2}) - atan_2(d_4 sin(\theta_3 - \Xi), a_2 + d_4 a_8(\theta_3 - \Xi))$$

Solve $\theta_4, \theta_5, \theta_6$ for the spherical whist:

We know from lecture that $\theta4$, $\theta5$, $\theta6$ are precisely the 272 Euler angles where $\theta4=\varphi$, $\theta5=\theta$, $\theta6=\psi$

We need to solve $R_3^3(\theta_1,\theta_3,\theta_3)$ $R_3^3(\theta_4,\theta_5,\theta_6) = R_3$ $R_3^3(\theta_4,\theta_5,\theta_6) = R_3^3(\theta_1,\theta_2,\theta_3)^T$ $R_d = M$

let Mij be the entires of M Using the formula for Euler angles, we can find:

 $\theta_{4} = \frac{\text{atan2}(m_{23}, m_{13})}{\theta_{5}} = \frac{\theta_{4} = \frac{\text{atan2}(-m_{23}, -m_{13})}{\theta_{5}}}{\theta_{5} = \frac{\text{atan2}(m_{23}, m_{33})}{\theta_{6} = \frac{\text{atan2}(m_{32}, -m_{31})}}$

where $m_{13}^{2} + M_{23}^{2} \neq 0$