

CS 180 Homework 1  
Aaron Lu

#1 Solution:

An algorithm can be viewed as a systemic/accurate approach to accomplish a specific task or solve a specific problem. It is written in a form of design. A program is a sequence of lines (codes, for example) to run/execute in a machine through syntax and compiler. It is written in a form of implementation.

To speak in a general scheme, algorithm lies between mathematics and computing. Though, a program doesn't solve anything, it can serve as an implementation of algorithms.

#2 Solution:

False. Counter example:

(next page)

False

Counterexample:

Men's Preference Profile:

$$m \begin{array}{|c|c|} \hline w' & w \\ \hline y' & y \\ \hline \end{array}$$

$$m' \begin{array}{|c|c|} \hline w' & w \\ \hline y' & y \\ \hline \end{array}$$

Women's Preference Profile:

$$w \begin{array}{|c|c|} \hline m & m' \\ \hline y & y' \\ \hline \end{array}$$

$$w' \begin{array}{|c|c|} \hline m & m' \\ \hline y & y' \\ \hline \end{array}$$

Yupi's Preference Profile:

$$y \begin{array}{|c|c|} \hline m & m' \\ \hline w' & w \\ \hline \end{array}$$

$$y' \begin{array}{|c|c|} \hline m & m' \\ \hline w' & w \\ \hline \end{array}$$

All possible instances:

	$m \begin{array}{ c c } \hline w' & y' \\ \hline m' & w' \\ \hline \end{array}$ (unstable)	$m \begin{array}{ c c } \hline w & y' \\ \hline m' & w' & y' \\ \hline \end{array}$ (unstable)	$m \begin{array}{ c c } \hline w' & y' \\ \hline m' & w & y' \\ \hline \end{array}$ (unstable)	$m \begin{array}{ c c } \hline w & y' \\ \hline m' & w' & y' \\ \hline \end{array}$ (unstable)
Pair	$(w', y)$ unstable	$(m, w')$ unstable	$(m, y')$ unstable	$(m, w')$ unstable
	$w' \text{ prefers } y \text{ \& } y \text{ prefers } w'$	$m \text{ prefers } w' \text{ \& } w' \text{ prefers } m$	$m \text{ prefers } y' \text{ \& } y' \text{ prefers } m$	$m \text{ prefers } w' \text{ \& } w' \text{ prefers } m$

$\therefore$  All instances are unstable.