

Supplementary Material

Aaron

06 July, 2020

4 Model description

5 Discrete time model equations

6 The age structured viral dynamics model, with all potential transitions is stated in the equations below,
 7 with parameters corresponding to table 1 in the main text, transitions between states occurs in discrete
 8 time ($t \rightarrow t + 1$), in each model discrete time setps (t) are set to 0.25 days.

$$S_N(t+1) = S_N(t) + b(t)(S_F(t) + I_F(t)) - (\omega_m + m_j \frac{N_j}{\kappa} + \beta(I_J(t) + I_N(t) + I_F(t) + I_M(t)))S_N(t) + \omega R_N(t)$$

$$_{11} \quad S_J(t+1) = S_J(t) + \omega_m(S_N(t) + Ma) - (\mu + m_j \frac{N}{\kappa} + \beta(I_J(t) + I_N(t) + I_F(t) + I_M(t)))S_J(t) + \omega R_J(t)$$

$$_{12} \quad S_M(t+1) = S_M + (t)\mu \frac{S_J}{2} - (m\frac{N}{\kappa} + \beta(I_J(t) + I_N(t) + I_F(t) + I_M(t)))S_M(t)I_M(t) + \omega R_M(t)$$

$$_{13} \quad S_F(t+1) = S_F(t) + \mu \frac{S_J}{2} - (m \frac{N}{\kappa} + \beta(I_J(t) + I_N(t) + I_F(t) + I_M(t)))S_F(t) + \omega R_F(t)$$

$$^{14} \quad L_N(t+1) = L_N(t) - (\omega_m + m_j \frac{N}{\kappa} + \epsilon) L_N + \rho I_N$$

$$L_J(t+1) = L_J(t) + \omega_m L_N(t) - (m_j \frac{N}{\kappa} + \epsilon) L_J(t) + \rho L_J(t)$$

$$L_M(t+1) = L_M(t) + \mu \frac{L_J}{2} - (m_j \frac{N}{\kappa} + \epsilon) L_M(t) + \rho L_M(t)$$

$$^{17} \quad L_F(t+1) = L_F(t) + \mu \frac{L_J}{2} - (m_j \frac{N}{\kappa} + \epsilon) L_F(t) + \rho L_F(t)$$

$$^{18} \quad I_N(t+1) = I_N(t) - (\omega_m + m_j \frac{N}{\kappa} + \gamma + \rho) I_N + \beta(I_J(t))$$

$$I_J(t+1) = I_J(t) + \omega_m I_N - (\mu \frac{S_J}{2} + m_j \frac{N}{\kappa} + \gamma + \rho) I_J + \beta(I_J(t) + I_N(t) + I_F(t) + I_M(t)) S_J$$

$$I_F(t+1) = I_F(t) + \mu \frac{I_J}{2} - (m \frac{N}{\kappa} \gamma + \rho) I_F(t) + \beta (I_F(t) + I_M(t)) S_F(t) + \epsilon L_F(t)$$

$$I_M(t+1) = I_M(t) + \mu \frac{I_J}{2} - (m \frac{N}{\kappa} + \gamma + \rho) I_M(t) + \beta(I_M(t) + I_F(t)) S_M(t) + \epsilon I$$

$$R_N(t+1) = R_N(t) - (\omega_m + m_j \frac{N}{\kappa} + \omega) R_N(t)$$

$$_{23} \quad R_J(t+1) = R_J(t) + \omega_m R_N(t) - (m_j \frac{N}{\kappa} + \omega) I$$

$$^{24} \quad R_M(t+1) = R_M(t) + \mu \frac{R_J(t)}{2} - (m \frac{N}{\pi} + \omega) R_M(t) +$$

$$B_E(t+1) \equiv B_E(t) + \mu \frac{R_J(t)}{\gamma} - (m \frac{N}{\gamma} + \omega) B_E(t) + \gamma J_E(t)$$

$$^{26} M_a(t+1) \equiv M_a(t) + b(R_E(t) + L_E(t)) - (\omega_m + m_i \frac{N}{M}) M_a(t)$$

29 Births occur in seasonal pulses, as previously described (Peel et al. 2014), with timing, amplitude and
30 seasonality derived from three parameters in a modified Gaussian function.

$$b(t) = c \exp^{s \cos^2(\pi t - \phi)} \quad (1)$$

β is derived from a rearrangement of equation (2) in the main text, here N is considered an upper limit to the population, thus N is equal to the carrying capacity κ :

$$\beta = R_0 \left(\frac{(\epsilon + m)(\gamma + m + \rho) - \epsilon \rho}{N(\epsilon + m)} \right) \quad (2)$$

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33 **Stochastic transitions between states**

34 Movement between states at each discrete time-step (set as 0.25 days) for individuals is a stochastic process,

35 using a combination of binomial, and multinomial distributions where multiple transition possibilities occur.

36 e.g. for bats exiting the variable state R , transitions will occur with the following steps:

37 • The total number of individuals transitioning between states is determined by first summing all of the
38 rates of exiting a current state, e.g. $(R \rightarrow \text{exit}) = \omega + \frac{N}{\kappa}$.

39 • We then convert the sum of rates to a probability for each possible transition occurring during a single
40 time-step, e.g. for a rate x , the equivalent probability of transition in one time-step is $p = 1 - e^{-x}$,
41 thus $Pr(R \rightarrow \text{exit}) = 1 - e^{-(R \rightarrow \text{exit})}$

42 • For each individual, a random draw from a binomial distribution is then performed at each time-step
43 to obtain the number of individuals exiting R e.g. $R_e = \text{bin}(R, Pr(R \rightarrow \text{exit}))$.

44 • The relative probabilities are then computed for transition to each of the potential states

$$Pr(R \rightarrow S) = \frac{\omega}{m \frac{N}{\kappa} + \omega} \quad (3)$$

and

$$Pr(R \rightarrow \text{death}) = \frac{m \frac{N}{\kappa}}{m \frac{N}{\kappa} + \omega} \quad (4)$$

44 • A multinomial distribution is used with each probability to determine the destination of each
45 individual $M(R_e, Pr(R \rightarrow S), Pr(R \rightarrow \text{death}))$

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47 **Model fitting**

48 As discussed in the main text, our models are considered state-space (hidden Markov) models, with ob-
49 servations k and hidden state variables Z at time t and we seek to identify an unbiased estimate of the
50 likelihood value, (also known as a marginal likelihood) $pr(k|\theta)$, by essentially “marginalising out” (Z). Here
51 we do this using a particle markov chain monte carlo (pMCMC) algorithm. Which combines a particle filter
52 as an unbiased estimator of the marginal likelihood value, and an MCMC acceptance/rejection algorithm
53 (Andrieu, Doucet, and Holenstein 2010).

54 pMCMC generic example

55 Particle filters act as an unbiased estimator of marginal likelihood by applying a form of importance re-
 56 sampling, to generate an approximate sample from, and make inferences about an unobserved Markov
 57 process (Smith 2013). They are becoming popular in disciplines where state-space models are common such
 58 as ecology and epidemiology (Kantas et al. 2015; Peters, Hosack, and Hayes 2010; Knape and De Valpine
 59 2012; Fasiolo et al. 2016; Sheinson, Niemi, and Meiring 2014).

60 In brief, the marginal likelihood $pr(k|\theta)$ for the observed data k , the hidden state Z and the parameter
 61 vector θ is considered the joint posterior probability $pr(k|Z, \theta) * p(Z|\theta)$. Using Monte-Carlo approximation
 62 for $p(k|\theta)$, a particle filter with J particles which have the possible trajectories/evolution of Z_j , the marginal
 63 likelihood can be considered as $pr(k|\theta) \approx \sum_J pr(k|Z_j, \theta) * pr(Z_j|\theta)$.

64 To run the particle filter algorithm requires the following steps:

1. Initialise the particles with equal weights.

$$Z_j \sim pr(Z_j|\theta) \\ w_j = \frac{1}{J} \quad (5)$$

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2. For each particle j at time t , simulate the initial conditions at the first observed data point.

$$Z_{jt} \sim pr(Z_{jt}|Z_j, \theta) \quad (6)$$

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3. Calculate a probability weighting for each particle based on the results of the simulation and the observed data.

$$w_{jt} = pr(k_t|Z_j, \theta) \quad (7)$$

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4. The marginal likelihood for this data point can be considered the average of each particle weighting.

$$p(k_t|\theta) = \frac{1}{J} \sum_J w_{jt} \quad (8)$$

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5. Normalise the weightings $\frac{w_{jt}}{\sum_J w_{jt}}$, resample with replacement each particle based on their weighting and simulate forward to the next observed data point.

$$Z_{jt+1} \sim pr(Z_{jt+1}|Z_t, \theta) \quad (9)$$

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Repeat steps 3 to 5 for all observed data, an estimate for the total marginal likelihood value can be considered the product of the average particle weights at each observed timepoint.

$$\mathcal{L}(\theta|k_{1:n}) = \prod_{t=1}^n \left(\frac{1}{J} \sum_{j=1}^J w_{jt} \right) \quad (10)$$

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77 This marginal likelihood value is then used in a traditional MCMC algorithm, in this instance Metropolis-
78 Hastings, where rejection or acceptance of a parameter proposal is based on the current and previous marginal
79 likelihood values.

80 **Model fitting with pMCMC to Boonah bat data**

81 To fit the model with pMCMC to our observed data, we developed a likelihood function which incorporated
82 the three unique longitudinal data-types; Individual serology for Hendra virus antibodies, individual PCR
83 of urine for Hendra virus RNA, and under roost PCR of urine for Hendra virus RNA.

- 84 • *Firstly, we consider the observed data:*

85 If the sampling time points are $i_1 \dots i_n$, the number of individual samples through time are $N_{i \dots n}$ of
86 which $k_{i \dots n}^p$ are PCR positive and $k_{i \dots n}^s$ are seropositive, the number of under-roost urine samples is
87 $N_{i \dots n}^u$ of which $k_{i \dots n}^u$ are PCR positive.

- 88 • *Secondly, the hidden state:*

89 If the system state of the model at each time point is $Z_{i \dots n}$, the transition probability density function
90 for Z from the stochastic model, conditioned on the parameters θ , is $pr(Z_i | Z_{i-1}, \theta)$.

91 Below we define how each data type contributes to the likelihood function in detail:

Table 1: Parameter and variable descriptions for supplementary materials

Parameter	Unit	Prior	Description
S	Individual bats	-	Number of susceptible bats
I	Individual bats	-	Number of infectious bats
R	Individual bats	-	Number of recovered bats
L	Individual bats	-	Number of latently infected bats
N	Individual bats	-	Total population of bats
θ	-	-	Parameter vector
Z	-	-	System state
z	-	-	Vector of simulated individual bat states
ζ_s	-	0-1	Individual serology coefficient
ζ_p	-	0-1	Individual PCR coefficient
ζ_u	-	0-1	Under roost PCR coefficient
k^s	Individual bats	-	Observed individual seropositive bats
k^p	Individual bats	-	Observed individual PCR positive bats
k^u	Individual bats	-	Predicted no. positive bats contributing to pooled under roost samples
k	-	-	Vector of observed individual bat states
N^u	-	-	Number of pooled under-roost samples (mean)
p	$\frac{I\zeta_u}{N}$	-	Probability of bat being positive (infection prevalence)
P_t	$1 - (1 - p)^d$	-	Probability of pooled sample being positive
O_u	-	>0	Overdispersion parameter for under roost data
d	-	1-25	Number of bats contributing to each pooled under roost sample
T_i	-	-	Pooled under roost sample test state

¹ Informative priors are based on normal distributions and are shown with 95% credible intervals in brackets, uninformative priors use a uniform distribution and are shown as a minimum and maximum value

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94 ***Individual serological and PCR of urine samples***

95 In the observed data, individual bats are found to be in all four empirical states of serological and PCR
 96 positivity:

- 97 • PCR positive and seropositive ($k^{P^+S^+}$)
 98 • PCR negative and seropositive ($k^{P^-S^+}$)
 99 • PCR positive and seronegative ($k^{P^+S^-}$)
 100 • PCR negative and seronegative ($k^{P^-S^-}$)

101 Logically, a relationship between the PCR and serology states is likely and so we consider a joint conditional
 102 probability function rather than treating the data as independent. Transitory states and test detection
 103 failure are also considered by fitting the coefficients ζ_s and ζ_p , which are bounded between 0 and 1. Thus,
 104 the simulated implementation of each observed empirical state are as follows:

- 105 • $k^{P^+S^+}$: Bats are assumed to be in the I state of the model and are equivalent to the number of I state
 106 bats proportionate to the value of the coefficients; $z^{P^+S^+} = I\zeta_p\zeta_s$
 107 • $k^{P^-S^+}$: Bats are assumed to be in either the L or R states of the models, or in the I state of the model;
 108 $z^{P^-S^+} = (I + L + R)\zeta_s(1 - \zeta_p)$
 109 • $k^{P^+S^-}$: Bats are considered to be in the I state of the model; $z^{P^+S^-} = I(1 - \zeta_s)\zeta_p$
 110 • $k^{P^-S^-}$: Bats are assumed to be in the S state of the models or in the I state; $z^{P^-S^-} = I(1 - \zeta_s)(1 - \zeta_p) + S$

111 If k is a vector of the observed counts of bats in each empirical state, $k = (k^{P^+S^+}, k^{P^-S^+}, k^{P^+S^-}, k^{P^-S^-})$,
 112 z is a vector of the simulated prevalences of each state $z = (z^{P^+S^+}, z^{P^-S^+}, z^{P^+S^-}, z^{P^-S^-})$ and N is the
 113 total observed bats, we can then propose a joint probability function based on a multinomial distribution,
 114 $pr(k^p, k^s | Z, N)$.

$$pr(k^p, k^s | Z) = \frac{N!}{\prod_{j=1}^4 k_j!} \prod_{j=1}^4 z_j^{k_j} \quad (11)$$

115 ***Pooled under roost samples***

If the probability of at least one bat within a pooled urine sample of d individuals being PCR positive for virus RNA can be considered $P_t = 1 - (1 - p)^d$, where p is the probability of each individual bat contributing to a pool being positive (Chiang and Reeves 1962). The result of PCR testing on a pooled sample (T_i) will be one of two states, with the following probabilities:

$$T_i = \begin{cases} \text{positive} = 1 - (1 - p)^d \\ \text{negative} = (1 - p)^d \end{cases} \quad (12)$$

116 Therefore, assuming that any one under-roost sample comes from d bats with a prevalence of p , considering
 117 the model state $Z(t)$, we aim to identify the likelihood of the contribution of positive under-roost samples at
 118 time (t) given (from the predicted GAM values) the number of samples $N^u(t)$, of which $k^u(t)$ were positive,
 119 $pr(k^u | N^u, Z)$. As the predicted values from the GAM are for prevalence, the total number of bats ($N^u(t)$)
 120 was considered the mean number of samples collected on each sampling occasion.

121 Due to the nature and challenges of field-sampling, under-roost data is likely to contain a degree of overdisper-
 122 sion, as it is highly exposed to external factors which are difficult to account for in study design. Therefore,
 123 the probability is unlikely to follow a standard binomial distribution, where the variance is defined by the
 124 mean. To account for this, we used a probability function based around a beta-binomial distribution, which

125 allows for an additional variance parameter to be fitted to account for any overdispersion in the observations.
 126 A beta-binomial distribution, is a binomial distribution such $pr(k^u|N^u, Z)$ would be:

$$pr(k^u|N^u, Z) = \binom{N^u}{k^u} p_t^{k^u} (1 - p_t)^{N^u - k^u} \quad (13)$$

127 However, p_t is not constant and is generated from a beta distribution, which takes two shape parameters α
 128 and β , $beta(\alpha, \beta)$ thus;

$$pr(k^u|N^u, Z) = \frac{\binom{N^u}{k^u} beta(k^u + O_u p, N^u - k^u + O_u(1 - p_t))}{beta(O_u p, O_u(1 - p_t))} \quad (14)$$

129 Here, O_u accounts for overdispersion in the data, and the prevalence of infectious bats p in p_t is derived from
 130 the model state $Z(t)$ as $\frac{I(t)\zeta_u}{N(t)}$, where ζ_u is a fitted coefficient accounting for detection failure.

131 As there is no precise measure of exact bat numbers contributing to a pooled sample, d is a fitted parameter
 132 with a prior based on expert knowledge and estimates from the field. For simplicity, only one value of d is
 133 derived for all pools on a single sampling occasion, assuming that each pooled sample on average has the
 134 same number of bats contributing. We also assume that there is no effect of pooling on the diagnostic tests,
 135 and any that does occur should be primarily accounted for by the ζ_u coefficient.

136 **full likelihood function**

137 Considering the above, and the sampling time points (i), we can define the full likelihood function as:

$$\mathcal{L}(\theta|N, N^u, k^{(s,p,u)}) = pr(\theta) * \prod_{i=1}^{16} pr(k_i^s, k_i^p|N_i, Z_i) * pr(k_t^u|N_i^u, Z_i) \quad (15)$$

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¹⁴⁰ **Initial conditions**

¹⁴¹ Starting parameters are estimated by running a Metropolis-Hastings MCMC algorithm with a deterministic
¹⁴² version of the model for 50,000 iterations with a 10,000 iteration burn-in. The median parameter set from
¹⁴³ each posterior distribution was then used in the pMCMC.

¹⁴⁴ Initial conditions for the bat population are derived from the carrying capacity parameter (κ). A population
¹⁴⁵ equal to the carrying capacity is first assumed and this is then split into demographic compartments as
¹⁴⁶ follows:

$$N = \kappa \quad (16)$$

$$b = (\omega_m + m_j) \frac{m_j + \mu}{\omega_m} \quad (17)$$

$$S_F = 0.5 \left(\frac{N}{\frac{1+m}{\mu} + \frac{b}{\omega_m + m_j}} \right) \quad (18)$$

$$S_M = 0.5 \left(\frac{N}{\frac{1+m}{\mu} + \frac{b}{\omega_m + m_j}} \right) \quad (19)$$

$$S_J = (S_F + S_M) \frac{m}{mu} \quad (20)$$

$$S_N = N - S_M - S_F - S_J \quad (21)$$

¹⁴⁷ Infectious and exposed individuals are added as 5% of the population and the model is run for 50 years to
¹⁴⁸ reach an equilibrium before fitting to the first data point.

¹⁴⁹ **Further results**

Table 2: Model 1

Parameter	Prior	Posterior
γ	1 day - 10 years	0 (0-0) year $^{-1}$
ρ	1 day - 10 years	0.2 (0.2-2.729) year $^{-1}$
ϵ	1 day - 10 years	0.298 (0.2-114.288) year $^{-1}$
m	0.186 (0.146-0.225) year $^{-1}$	0.173 (0.134-0.214) year $^{-1}$
m_j	0.500 (0.480-0.520) year $^{-1}$	0.498 (0.478-0.516) year $^{-1}$
c	-	14.682 (11.104-18.281)
s	130 (111-150)	128.936 (110.326-148.48)
ϕ	7.180 (6.787-7.571)	7.182 (7.161-7.202)
ω	1 day - 10 years	0 (0-0) year $^{-1}$
ω_m	0.800 (0.741-0.859) year $^{-1}$	0.801 (0.742-0.857) year $^{-1}$
R_0	> 1	2.96 (1.342-4.369)
d	0-25	5.237 (0.019-17.406)
ζ_s	0-1	0.92 (0.823-0.985)
ζ_p	0-1	0.071 (0.032-0.264)
ζ_u	0-1	0.062 (0.006-0.368)
κ	4000 (2570-6300)	4001.637 (2518-6295)
c_ν	1	1
s_ν	-	0 (0-0)
ϕ_ν	-	0 (0-0)

¹ Table for model 1, SILI with no maternal immunity and no seasonal force, posterior estimates, 95% credible intervals are shown in brackets, model corresponds to model 1 in table SM1

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Table 3: Model 2

Parameter	Prior	Posterior
γ	1 day - 10 years	0 (0-0) year ⁻¹
ρ	1 day - 10 years	13.756 (3.451-40.926) year ⁻¹
ϵ	1 day - 10 years	0.2 (0.2-0.652) year ⁻¹
m	0.186 (0.146-0.225) year ⁻¹	0.191 (0.148-0.226) year ⁻¹
m_j	0.500 (0.480-0.520) year ⁻¹	0.501 (0.48-0.519) year ⁻¹
c	-	16.303 (12.596-20.006)
s	130 (111-150)	129.454 (109.418-148.865)
ϕ	7.180 (6.787-7.571)	7.18 (7.159-7.199)
ω	1 day - 10 years	0 (0-0) year ⁻¹
ω_m	0.800 (0.741-0.859) year ⁻¹	0.802 (0.745-0.861) year ⁻¹
R_0	> 1	4.19 (1.674-8.526)
d	0-25	11.365 (3.541-19.997)
ζ_s	0-1	0.919 (0.811-0.99)
ζ_p	0-1	0.673 (0.437-0.856)
ζ_u	0-1	0.604 (0.24-0.989)
κ	4000 (2570-6300)	3835.93 (2415-5970)
c_ν	1	1
s_ν	-	0 (0-0)
ϕ_ν	-	0 (0-0)

¹ Table for model 2, SILI with maternal immunity and no seasonal force, posterior estimates, 95% credible intervals are shown in brackets, model corresponds to model 2 in table SM1

Table 4: Model 3

Parameter	Prior	Posterior
γ	1 day - 10 years	0 (0-0) year ⁻¹
ρ	1 day - 10 years	4.96 (1.791-222.331) year ⁻¹
ϵ	1 day - 10 years	27.268 (2.999-273.527) year ⁻¹
m	0.186 (0.146-0.225) year ⁻¹	0.174 (0.136-0.212) year ⁻¹
m_j	0.500 (0.480-0.520) year ⁻¹	0.499 (0.481-0.519) year ⁻¹
c	-	14.843 (11.328-18.438)
s	130 (111-150)	129.524 (110.026-149.121)
ϕ	7.180 (6.787-7.571)	7.182 (7.161-7.201)
ω	1 day - 10 years	0 (0-0) year ⁻¹
ω_m	0.800 (0.741-0.859) year ⁻¹	0.801 (0.744-0.859) year ⁻¹
R_0	> 1	2.515 (1.009-4.724)
d	0-25	3.8 (0.005-16.522)
ζ_s	0-1	0.905 (0.785-0.988)
ζ_p	0-1	0.156 (0.054-0.334)
ζ_u	0-1	0.169 (0.018-0.787)
κ	4000 (2570-6300)	3971.778 (2600-6237)
c_ν	1	1
s_ν	-	11.118 (1.162-147.314)
ϕ_ν	-	46.448 (0-46.728)

¹ Table for model 3, SILI with maternal immunity and no seasonal force, posterior estimates, 95% credible intervals are shown in brackets, model corresponds to model 3 in table SM1

Table 5: Model 4

Parameter	Prior	Posterior
γ	1 day - 10 years	0 (0-0) year ⁻¹
ρ	1 day - 10 years	59.22 (19.409-306.196) year ⁻¹
ϵ	1 day - 10 years	3.799 (0.2-25.351) year ⁻¹
m	0.186 (0.146-0.225) year ⁻¹	0.187 (0.148-0.224) year ⁻¹
m_j	0.500 (0.480-0.520) year ⁻¹	0.5 (0.48-0.52) year ⁻¹
c	-	16.068 (12.405-19.664)
s	130 (111-150)	129.744 (110.155-148.909)
ϕ	7.180 (6.787-7.571)	7.18 (7.16-7.2)
ω	1 day - 10 years	0 (0-0) year ⁻¹
ω_m	0.800 (0.741-0.859) year ⁻¹	0.799 (0.742-0.856) year ⁻¹
R_0	> 1	7.659 (3.393-18.199)
d	0-25	12.091 (2.598-19.975)
ζ_s	0-1	0.922 (0.829-0.99)
ζ_p	0-1	0.689 (0.392-0.876)
ζ_u	0-1	0.661 (0.278-0.999)
κ	4000 (2570-6300)	4204.429 (2716-6486)
c_ν	1	1
s_ν	-	1.861 (0.906-2.655)
ϕ_ν	-	0.034 (0-0.136)

¹ Table for model 4, SILI with maternal immunity and seasonal force, posterior estimates, 95% credible intervals are shown in brackets, model corresponds to model 4 in table SM1

Table 6: Model 5

Parameter	Prior	Posterior
γ	1 day - 10 years	3.135 (2.094-4.036) year ⁻¹
ρ	1 day - 10 years	0 (0-0) year ⁻¹
ϵ	1 day - 10 years	0 (0-0) year ⁻¹
m	0.186 (0.146-0.225) year ⁻¹	0.232 (0.167-0.232) year ⁻¹
m_j	0.500 (0.480-0.520) year ⁻¹	0.502 (0.485-0.514) year ⁻¹
c	-	18.658 (13.68-21.359)
s	130 (111-150)	130.022 (112.701-151.075)
ϕ	7.180 (6.787-7.571)	7.191 (7.17-7.2)
ω	1 day - 10 years	0 (0-0) year ⁻¹
ω_m	0.800 (0.741-0.859) year ⁻¹	0.8 (0.749-0.859) year ⁻¹
R_0	> 1	42.152 (35.431-49.914)
d	0-25	10.372 (3.7-19.165)
ζ_s	0-1	0.94 (0.864-0.986)
ζ_p	0-1	0.531 (0.481-0.69)
ζ_u	0-1	0.317 (0.261-0.819)
κ	4000 (2570-6300)	2351.889 (2350-6353)
c_ν	1	1
s_ν	-	0 (0-0)
ϕ_ν	-	0 (0-0)

¹ Table for model 5, SIR with no seasonal force, posterior estimates, 95% credible intervals are shown in brackets, model corresponds to model 5 in table SM1

Table 7: Model 6

Parameter	Prior	Posterior
γ	1 day - 10 years	22.449 (11.455-48.417) year ⁻¹
ρ	1 day - 10 years	0 (0-0) year ⁻¹
ϵ	1 day - 10 years	0 (0-0) year ⁻¹
m	0.186 (0.146-0.225) year ⁻¹	0.187 (0.151-0.231) year ⁻¹
m_j	0.500 (0.480-0.520) year ⁻¹	0.499 (0.481-0.519) year ⁻¹
c	-	15.973 (12.262-19.695)
s	130 (111-150)	129.841 (110.473-149.831)
ϕ	7.180 (6.787-7.571)	7.181 (7.163-7.199)
ω	1 day - 10 years	0 (0-0) year ⁻¹
ω_m	0.800 (0.741-0.859) year ⁻¹	0.801 (0.741-0.859) year ⁻¹
R_0	> 1	13.395 (7.087-22.842)
d	0-25	8.246 (1.751-18.817)
ζ_s	0-1	0.918 (0.81-0.992)
ζ_p	0-1	0.512 (0.376-0.637)
ζ_u	0-1	0.433 (0.133-0.925)
κ	4000 (2570-6300)	4216.503 (2582-6166)
c_ν	1	1
s_ν	-	26.581 (5.96-149.089)
ϕ_ν	-	0.573 (0.389-0.904)

¹ Table for model 6, SIR with seasonal force posterior estimates, 95% credible intervals are shown in brackets, model corresponds to model 6 in table SM1

Table 8: Model 7

Parameter	Prior	Posterior
γ	1 day - 10 years	5.194 (2.897-7.907) year ⁻¹
ρ	1 day - 10 years	0 (0-0) year ⁻¹
ϵ	1 day - 10 years	0 (0-0) year ⁻¹
m	0.186 (0.146-0.225) year ⁻¹	0.192 (0.153-0.234) year ⁻¹
m_j	0.500 (0.480-0.520) year ⁻¹	0.499 (0.485-0.523) year ⁻¹
c	-	16.402 (12.731-20.153)
s	130 (111-150)	130.552 (110.826-149.526)
ϕ	7.180 (6.787-7.571)	7.182 (7.162-7.199)
ω	1 day - 10 years	0.218 (0.002-0.57) year ⁻¹
ω_m	0.800 (0.741-0.859) year ⁻¹	0.801 (0.74-0.858) year ⁻¹
R_0	> 1	42.316 (29.747-49.987)
d	0-25	7.866 (0.364-17.982)
ζ_s	0-1	0.918 (0.833-0.99)
ζ_p	0-1	0.478 (0.311-0.627)
ζ_u	0-1	0.407 (0.167-0.994)
κ	4000 (2570-6300)	3960.368 (2576-5888)
c_ν	1	1
s_ν	-	0 (0-0)
ϕ_ν	-	0 (0-0)

¹ Table for model 7, SIRS with no seasonal force posterior estimates, 95% credible intervals are shown in brackets, model corresponds to model 7 in table SM1

Table 9: Model 8

Parameter	Prior	Posterior
γ	1 day - 10 years	4.653 (0.968-6.653) year ⁻¹
ρ	1 day - 10 years	0 (0-0) year ⁻¹
ϵ	1 day - 10 years	0 (0-0) year ⁻¹
m	0.186 (0.146-0.225) year ⁻¹	0.191 (0.152-0.228) year ⁻¹
m_j	0.500 (0.480-0.520) year ⁻¹	0.501 (0.481-0.52) year ⁻¹
c	-	16.301 (12.586-19.817)
s	130 (111-150)	129.979 (109.237-148.619)
ϕ	7.180 (6.787-7.571)	7.179 (7.16-7.199)
ω	1 day - 10 years	5.701 (1.345-18.309) year ⁻¹
ω_m	0.800 (0.741-0.859) year ⁻¹	0.801 (0.742-0.857) year ⁻¹
R_0	> 1	35.426 (22.46-49.849)
d	0-25	5.221 (0.01-17.558)
ζ_s	0-1	0.924 (0.823-0.987)
ζ_p	0-1	0.401 (0.083-0.558)
ζ_u	0-1	0.356 (0.046-0.903)
κ	4000 (2570-6300)	4153.78 (2618-6383)
c_ν	1	1
s_ν	-	125.843 (37.69-199.776)
ϕ_ν	-	1.75 (1.473-2.111)

¹ Table for model 8, SIRS with seasonal force posterior estimates, 95% credible intervals are shown in brackets, model corresponds to model 8 in table SM1

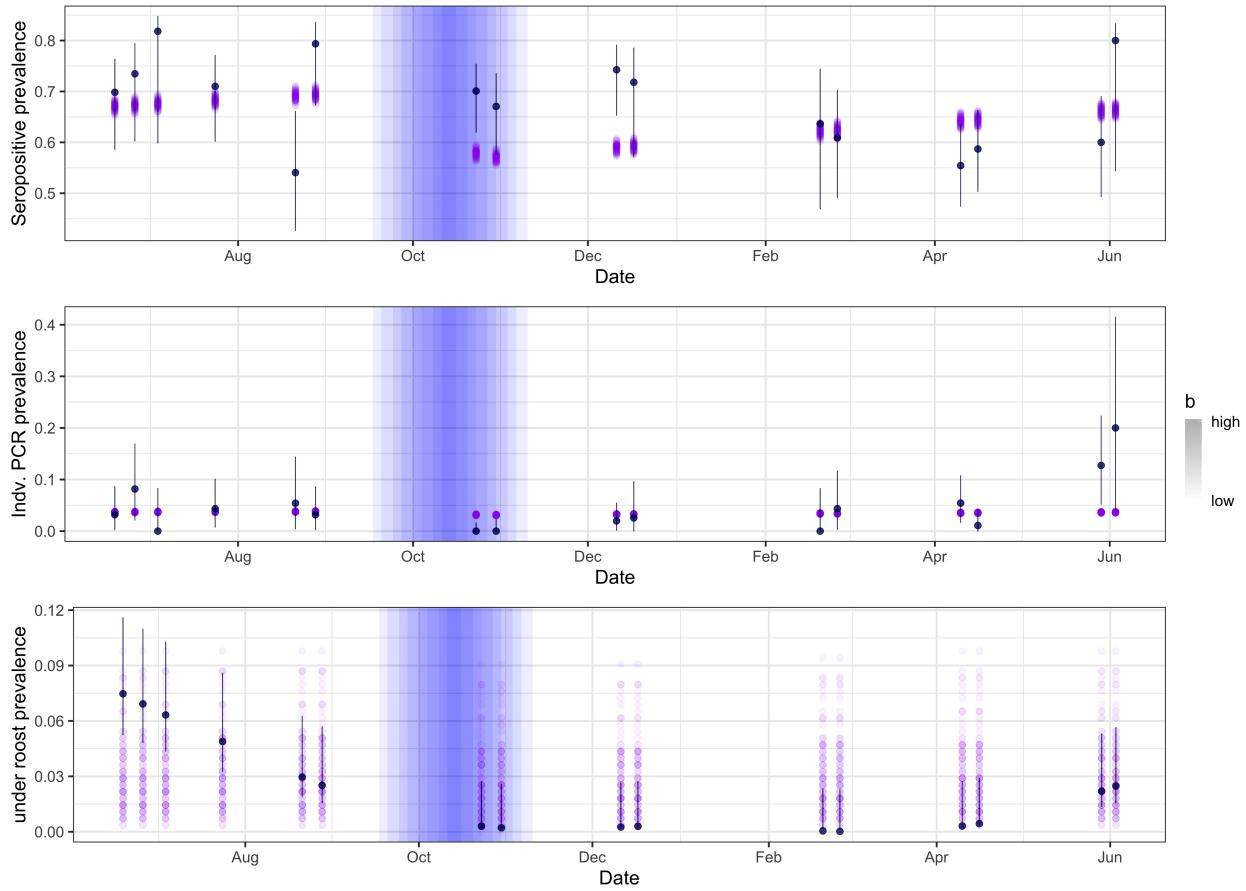


Figure 1: 100 repeat runs of the SILI model without seasonal forcing and without maternal immunity (model 1 in table 1), parameterised using the median values from the posterior estimates of each parameter. Dark blue points show the observed data, purple points show the model outputs for each run of the model at the corresponding observed time period. The top figure shows the simulated and observed serological prevalence, the middle figure shows the simulated and observed virus RNA prevalence from individual urine samples, and the bottom figure shows the simulated and predicted (using observed data and contributing bats parameter d) virus RNA prevalence from the under-roost samples. Confidence intervals on observed data are calculated as binomial confidence intervals, with a beta prior on the binomial distribution; the shape of the beta prior for individual samples is uninformative and for under-roost data is derived from the corresponding fitted overdispersion parameters for each data-type.

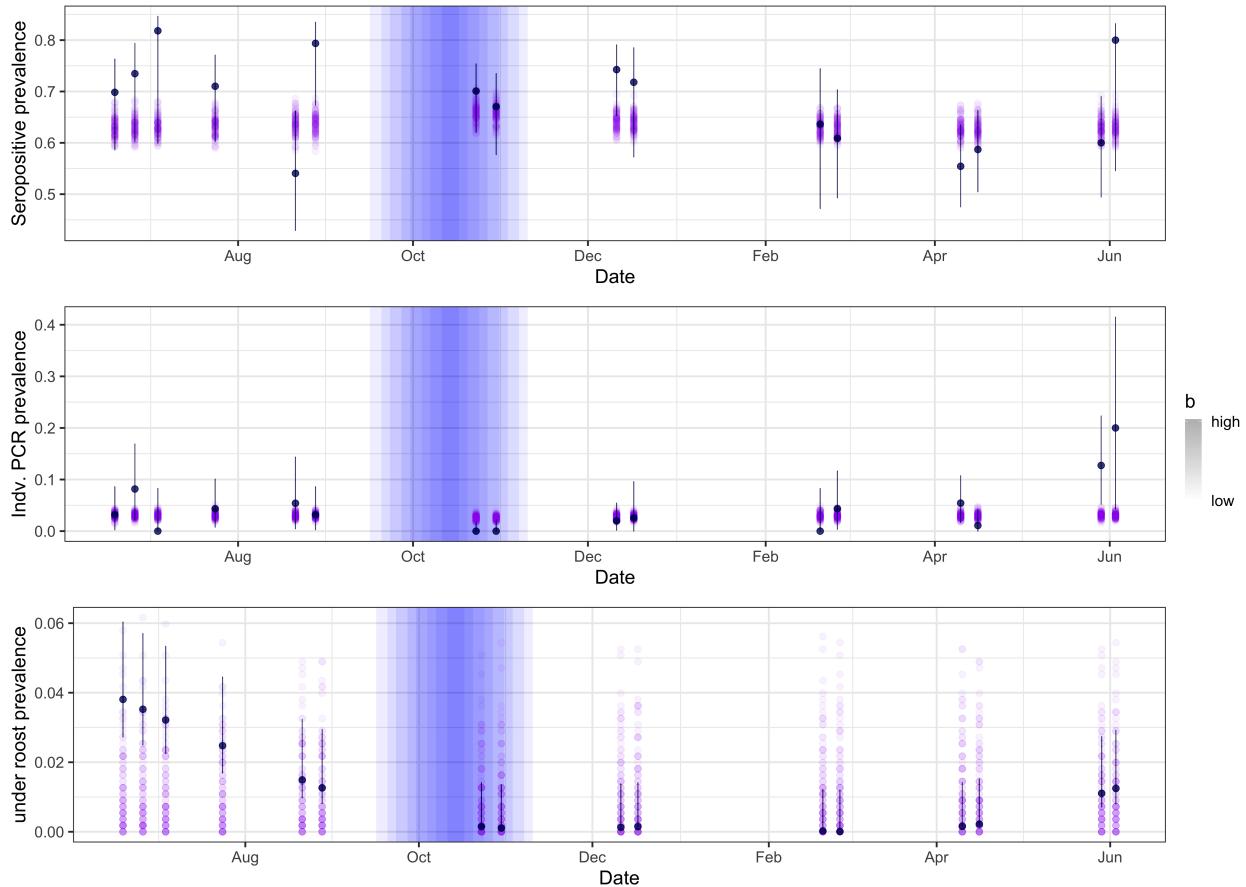


Figure 2: 100 repeat runs of the maternal immunity SILI model without seasonal forcing (model 2 in table 1), parameterised using the median values from the posterior estimates of each parameter. Dark blue points show the observed data, purple points show the model outputs for each run of the model at the corresponding observed time period. The top figure shows the simulated and observed serological prevalence, the middle figure shows the simulated and observed virus RNA prevalence from individual urine samples, and the bottom figure shows the simulated and predicted (using observed data and contributing bats parameter d) virus RNA prevalence from the under-roost samples. Confidence intervals on observed data are calculated as binomial confidence intervals, with a beta prior on the binomial distribution; the shape of the beta prior for individual samples is uninformative and for under-roost data is derived from the corresponding fitted overdispersion parameters for each data-type.

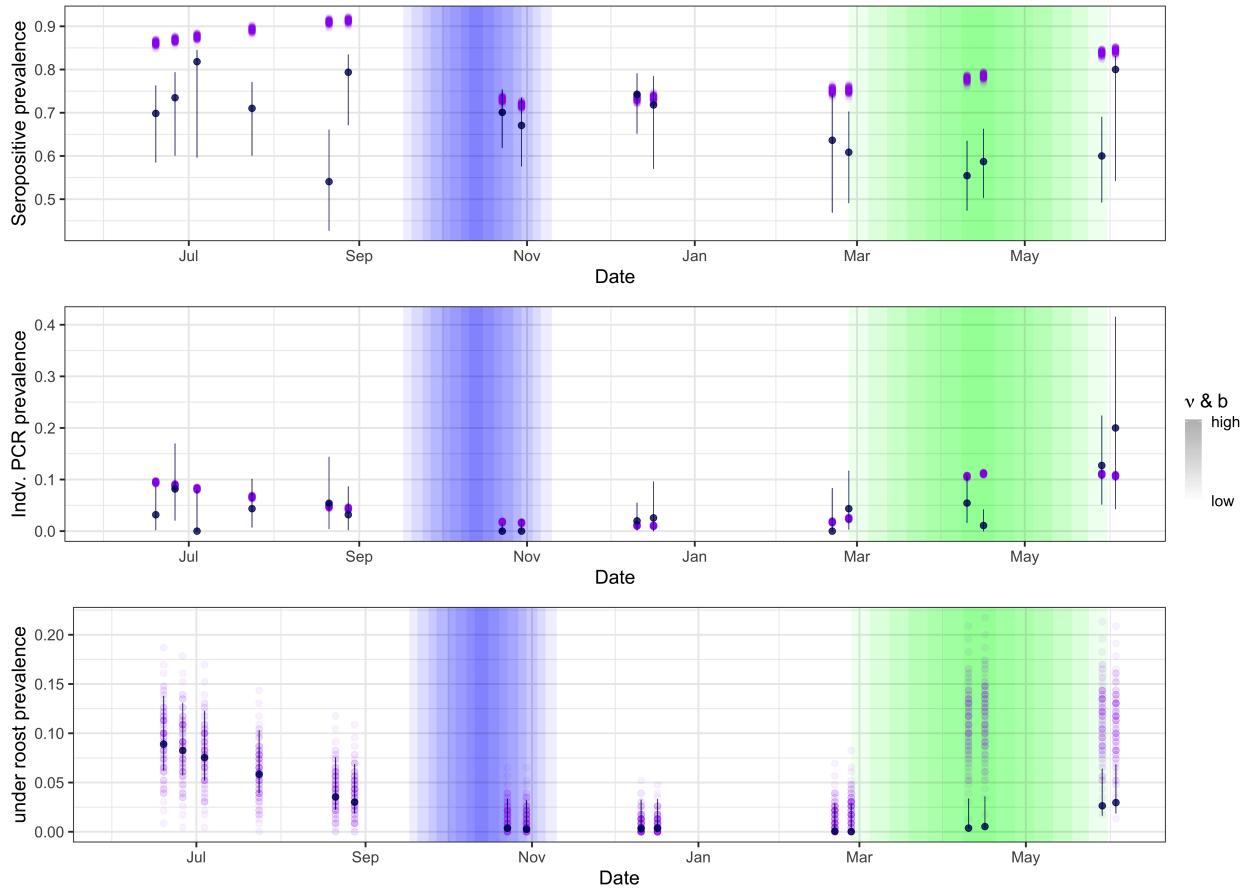


Figure 3: 100 repeat runs of the SILI model with seasonal forcing and without maternal immunity (model 3 in table 1), parameterised using the median values from the posterior estimates of each parameter. Dark blue points show the observed data, purple points show the model outputs for each run of the model at the corresponding observed time period. The top figure shows the simulated and observed serological prevalence, the middle figure shows the simulated and observed virus RNA prevalence from individual urine samples, and the bottom figure shows the simulated and predicted (using observed data and contributing bats parameter d) virus RNA prevalence from the under-roost samples. Confidence intervals on observed data are calculated as binomial confidence intervals, with a beta prior on the binomial distribution; the shape of the beta prior for individual samples is uninformative and for under-roost data is derived from the corresponding fitted overdispersion parameters for each data-type.

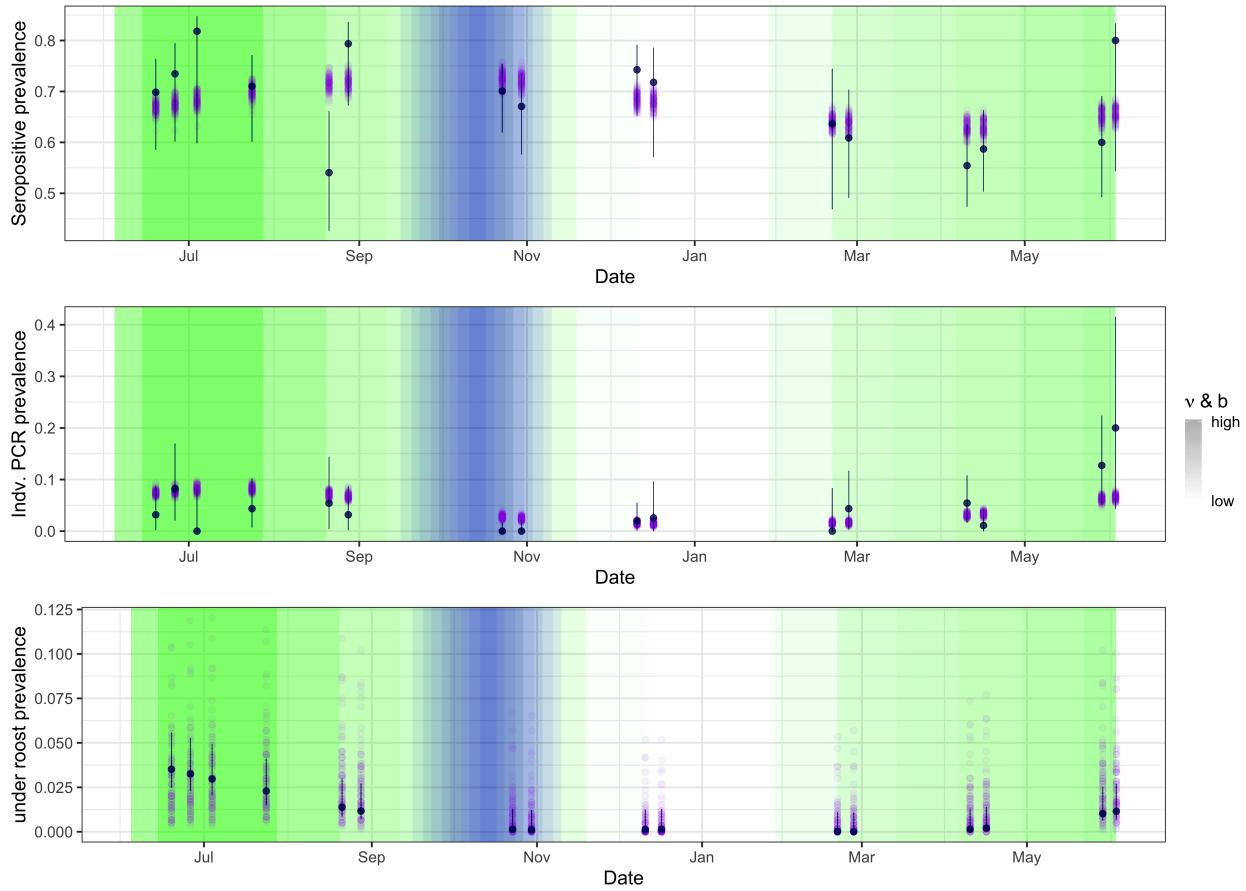


Figure 4: 100 repeat runs of the maternal immunity SILI model with seasonal forcing (model 4 in table 1), parameterised using the median values from the posterior estimates of each parameter. Dark blue points show the observed data, purple points show the model outputs for each run of the model at the corresponding observed time period. The top figure shows the simulated and observed serological prevalence, the middle figure shows the simulated and observed virus RNA prevalence from individual urine samples, and the bottom figure shows the simulated and predicted (using observed data and contributing bats parameter d) virus RNA prevalence from the under-roost samples. Confidence intervals on observed data are calculated as binomial confidence intervals, with a beta prior on the binomial distribution; the shape of the beta prior for individual samples is uninformative and for under-roost data is derived from the corresponding fitted overdispersion parameters for each data-type.

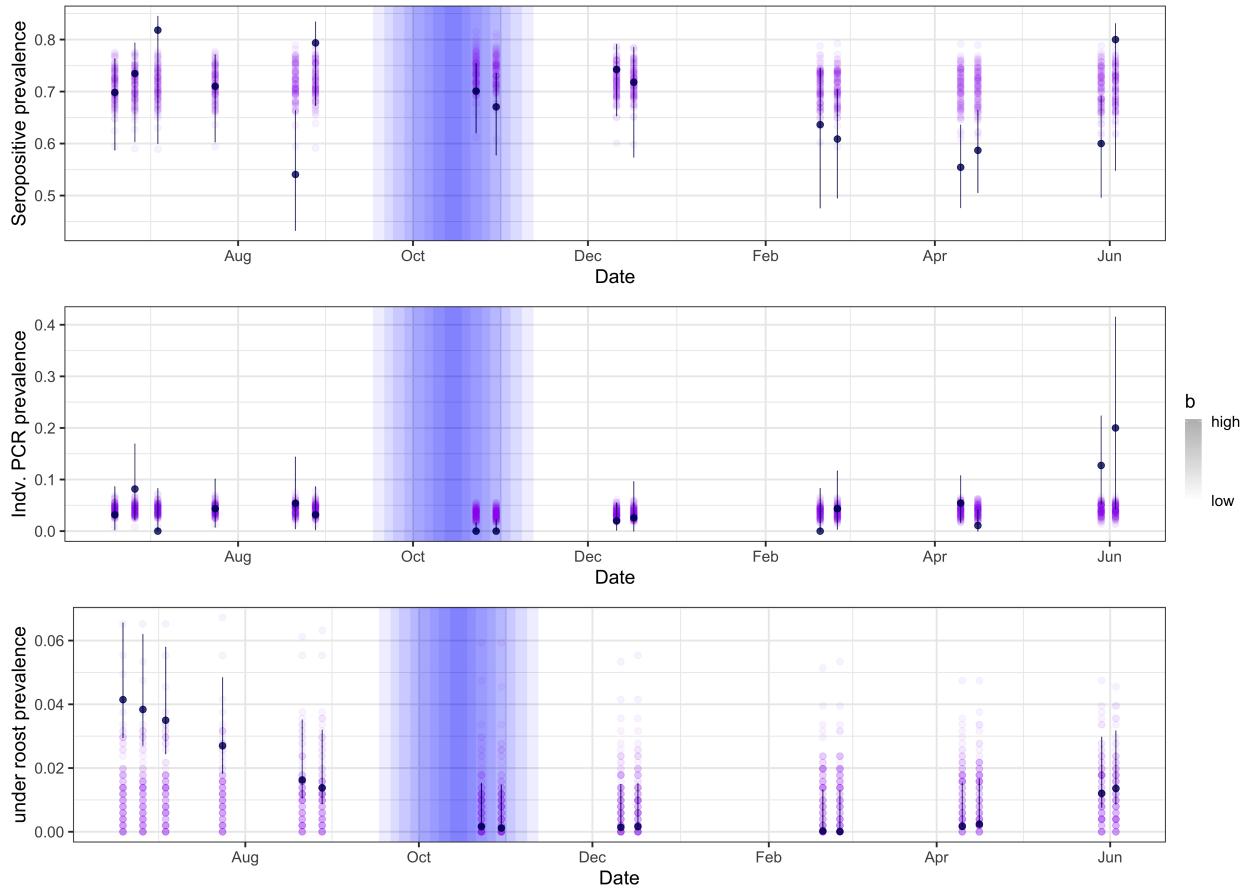


Figure 5: 100 repeat runs of the SIR model without seasonal forcing (model 5 in table 1), parameterised using the median values from the posterior estimates of each parameter. Dark blue points show the observed data, purple points show the model outputs for each run of the model at the corresponding observed time period. The top figure shows the simulated and observed serological prevalence, the middle figure shows the simulated and observed virus RNA prevalence from individual urine samples, and the bottom figure shows the simulated and predicted (using observed data and contributing bats parameter d) virus RNA prevalence from the under-roost samples. Confidence intervals on observed data are calculated as binomial confidence intervals, with a beta prior on the binomial distribution; the shape of the beta prior for individual samples is uninformative and for under-roost data is derived from the corresponding fitted overdispersion parameters for each data-type.

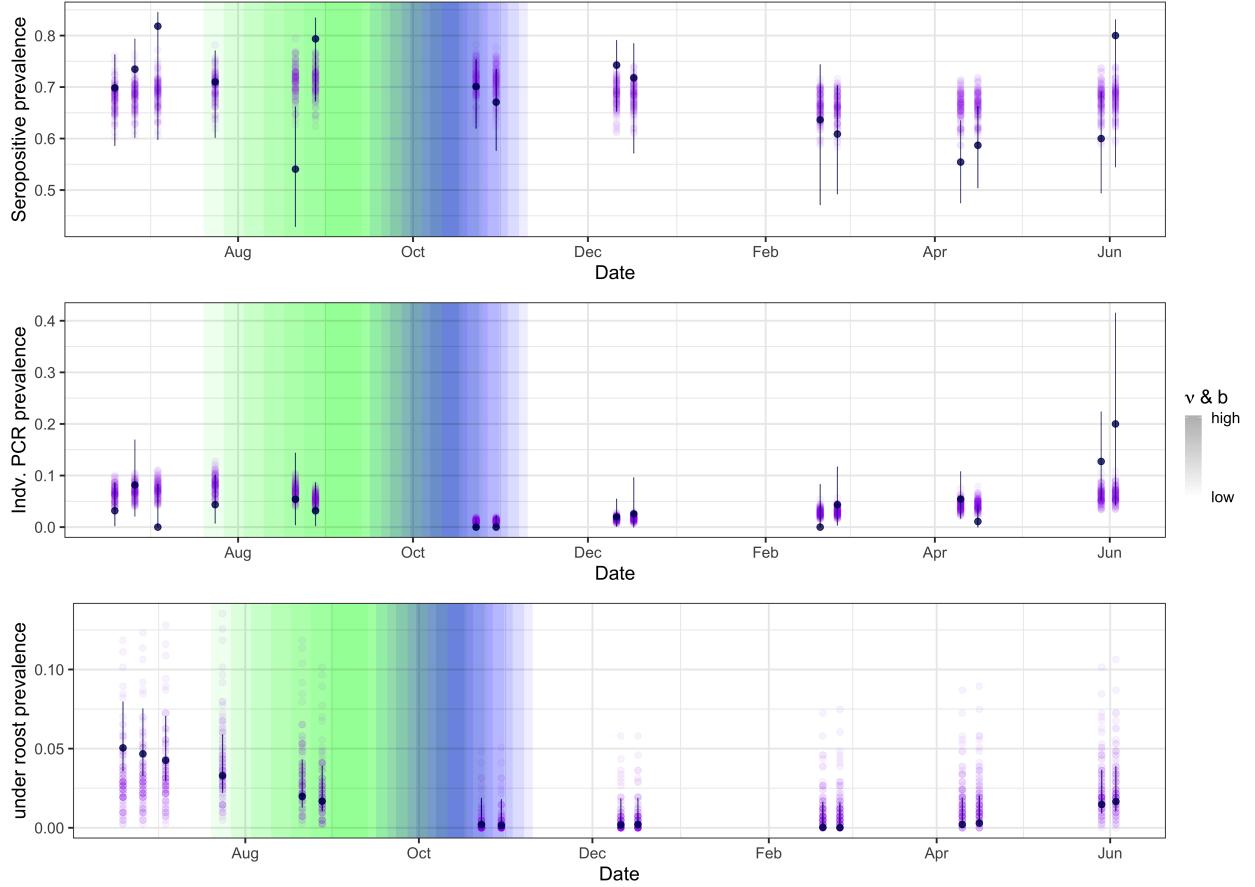


Figure 6: 100 repeat runs of the SIR model with seasonal forcing (model 6 in table 1), parameterised using the median values from the posterior estimates of each parameter. Dark blue points show the observed data, purple points show the model outputs for each run of the model at the corresponding observed time period. The top figure shows the simulated and observed serological prevalence, the middle figure shows the simulated and observed virus RNA prevalence from individual urine samples, and the bottom figure shows the simulated and predicted (using observed data and contributing bats parameter d) virus RNA prevalence from the under-roost samples. Confidence intervals on observed data are calculated as binomial confidence intervals, with a beta prior on the binomial distribution; the shape of the beta prior for individual samples is uninformative and for under-roost data is derived from the corresponding fitted overdispersion parameters for each data-type.

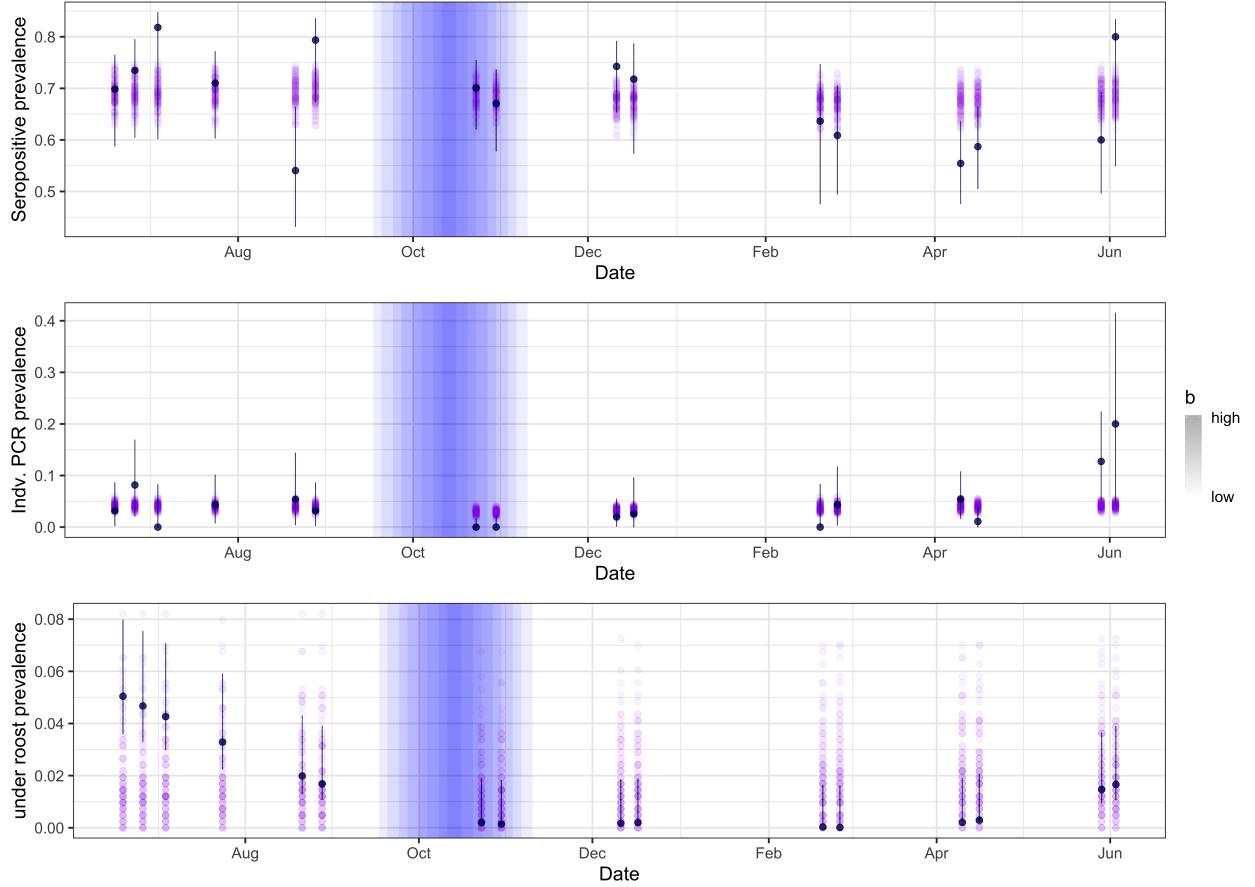


Figure 7: 100 repeat runs of the model without seasonal forcing (model 7 in table 1), parameterised using the median values from the posterior estimates of each parameter. Dark blue points show the observed data, purple points show the model outputs for each run of the model at the corresponding observed time period. The top figure shows the simulated and observed serological prevalence, the middle figure shows the simulated and observed virus RNA prevalence from individual urine samples, and the bottom figure shows the simulated and predicted (using observed data and contributing bats parameter d) virus RNA prevalence from the under-roost samples. Confidence intervals on observed data are calculated as binomial confidence intervals, with a beta prior on the binomial distribution; the shape of the beta prior for individual samples is uninformative and for under-roost data is derived from the corresponding fittedoverdispersion parameters for each data-type.

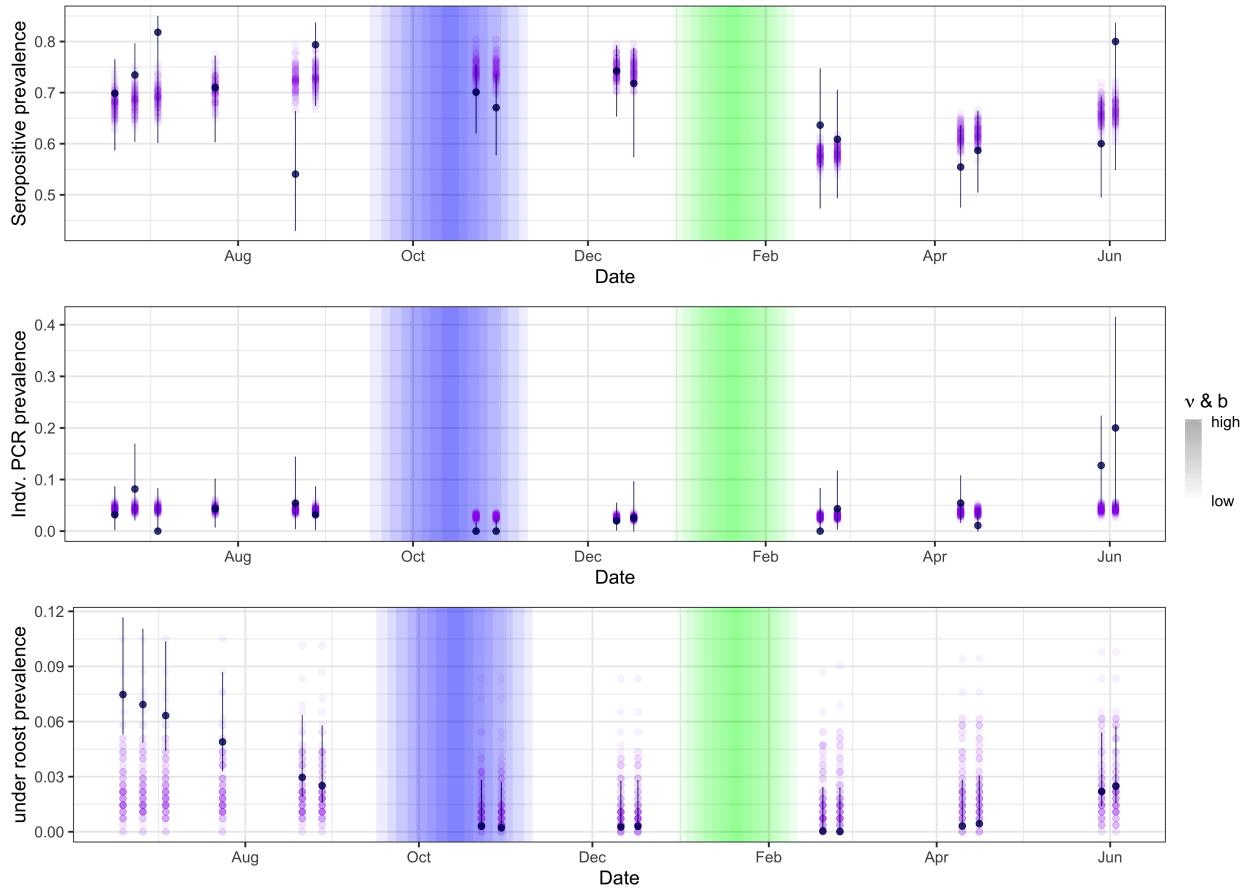


Figure 8: 100 repeat runs of the SIRS model with seasonal forcing (model 8 in table 1), parameterised using the median values from the posterior estimates of each parameter. Dark blue points show the observed data, purple points show the model outputs for each run of the model at the corresponding observed time period. The top figure shows the simulated and observed serological prevalence, the middle figure shows the simulated and observed virus RNA prevalence from individual urine samples, and the bottom figure shows the simulated and predicted (using observed data and contributing bats parameter d) virus RNA prevalence from the under-roost samples. Confidence intervals on observed data are calculated as binomial confidence intervals, with a beta prior on the binomial distribution; the shape of the beta prior for individual samples is uninformative and for under-roost data is derived from the corresponding fittedoverdispersion parameters for each data-type.

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