

Final project system characterization

Arena (not needed for report)

for a 5 m x 5 m arena, each big tile

0.25 m x 0.25 m ← for my zoom level

The walls may have a thickness of 0.1-0.2 m?

Ultrasonic sensors

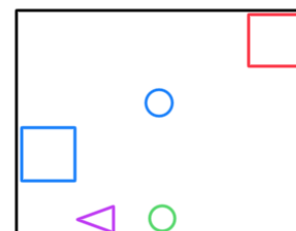
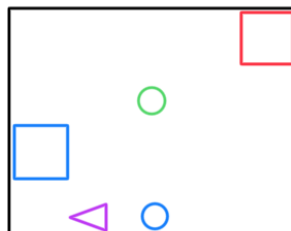
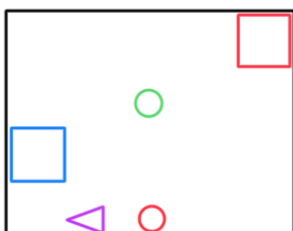
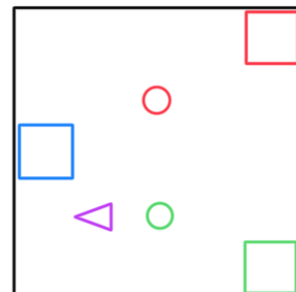
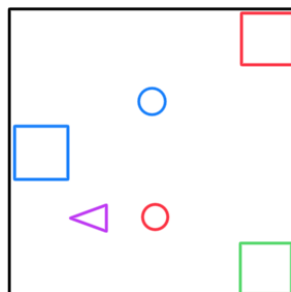
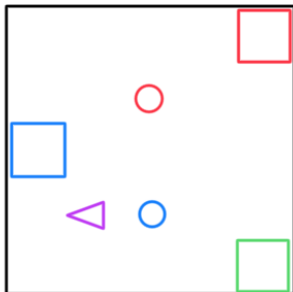
From observations

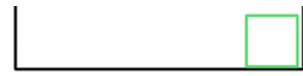
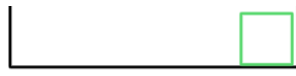
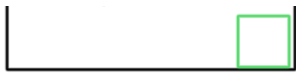
$$|d_{\text{actual}} - d_{\text{sens}}| = 0.1 - 0.2 \text{ m}$$

may relate
to wall

← thickness?

or perhaps due to
position offset





Algorithm 1 (not used)

- Spin until colored object is detected
- Given color of target object determine pre-plow-position
- Plan the path to get to pre-plow-position avoiding wall and objects. Treat objects as obstacles
- Plow object to storage-location
 - Use robot position and storage location to plan path
 - After reaching destination, move backwards a little bit to disengage from object
- Go to home position (0,0)
- Repeat loop 1 more time

Functions (not used)

- get-robot-location ()
- get-object-location(obj-distance, obj-angle)
- determine-pre-plow-position(object-location, color)
- create-map(robot-location, object-location, ...)
- determine-path(pre-plow-position, ...)

Object sensors

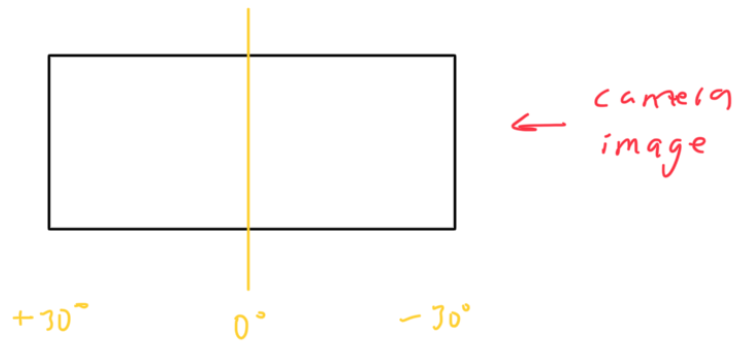
- Measure distance with respect to center of robot
- When robot is in contact with object

$d_{\min} \approx 0.38 \text{ m}$ ← minimum distance

- Maximum detected distance and angle

$d_{\max} = 2 \text{ m}$ ← NaN in $d > 2 \text{ m}$

- Angle range $(-30, 30)$

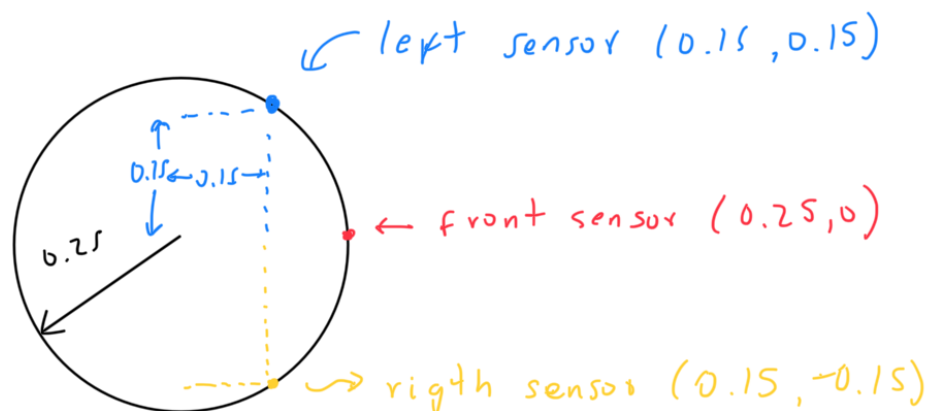


Distance sensors

- Range $(0.02, 2 \text{ m})$ ← NaN if $d > 2 \text{ m}$

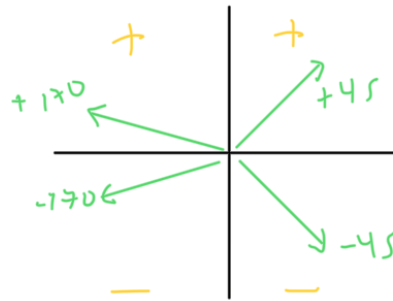
- Not affected by objects

- Position in robot :

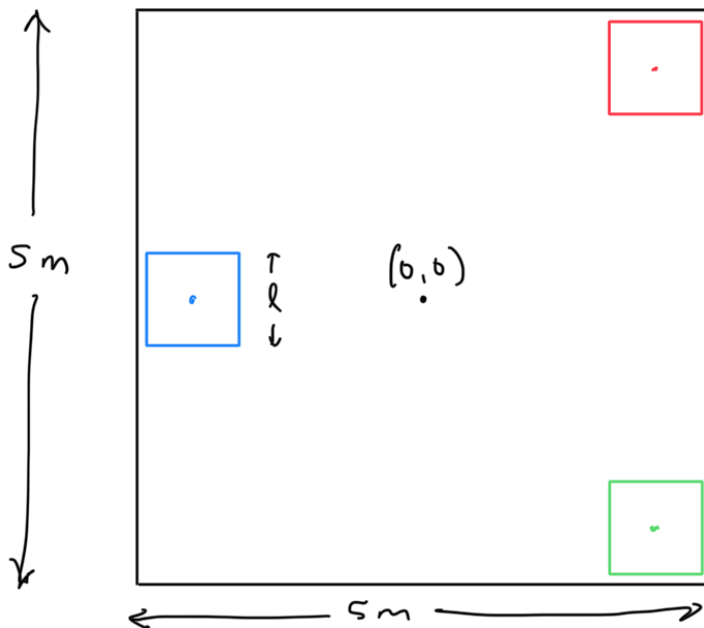


Odometer

- Provides x, y position at all times
- Angle positive counter-clockwise



Collection Zones



All zones have dimension

$$l \times l$$

where

$$l \approx 0.84$$

Red Zone Center $\rightarrow r-z-c$

$$r-z-c-x = 2.5 - 0.84/2 = 2.08$$

$$r-z-c-y = 2.5 - 0.84/2 = 2.08$$

$$r - z - c - y = 2.5 - \frac{0.84}{2} = 2.08$$

So $r - z - c = (2.08, 2.08)$

Blue Zone Center $\rightarrow b - z - c$

$$b - z - c - x = -2.5 + \frac{0.84}{2} = -2.08$$

$$b - z - c - y = 0$$

So $b - z - c = (-2.08, 0)$

Green Zone Center $\rightarrow g - z - c$

$$g - z - c - x = 2.5 - \frac{0.84}{2} = 2.08$$

$$g - z - c - y = -2.5 + \frac{0.84}{2} = -2.08$$

So $g - z - c = (2.08, -2.08)$

Determine Object Location (not used)

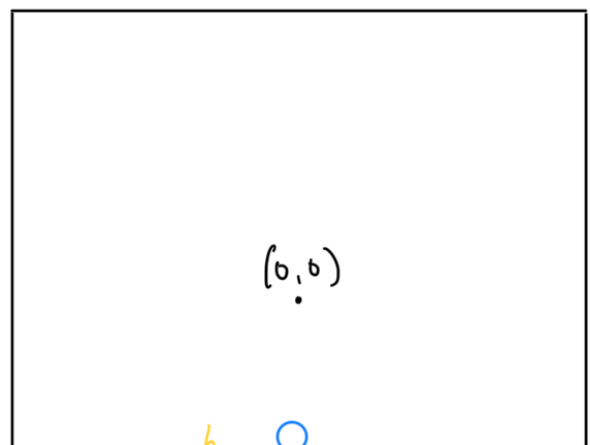
Given object angle and distance, determine location

We know α , h

$$\cos(\alpha) = \frac{op}{h}$$

$$op = h \cos(\alpha)$$

$$\sin \alpha = \frac{a}{h}$$



$$\sin \alpha = \frac{a}{h}$$

$$a = h \cdot \sin \alpha$$



Assuming object is a point

position object \rightarrow p_{obj}

position robot \rightarrow p_{rob}

$$p_{obj-x} = p_{rob-x} + h \cdot \cos \alpha$$

$$p_{obj-y} = p_{rob-y} + h \cdot \sin \alpha$$

Example

$$p_{rob} = (-2, -2)$$

$$\alpha = 30^\circ \left(\frac{\pi}{6} \right)$$

$$h = 1$$

$$p_{obj-x} = -2 + 1 \cdot \cos 30^\circ \approx -1,13$$

$$p_{obj-y} = -2 + 1 \cdot \sin 30^\circ = -1,5$$

If robot is not oriented in the x axis direction
(not used)

$$\cos(\theta + \alpha) = \frac{op}{h}$$

$$op = h \cdot \cos(\theta + \alpha)$$

$$\sin(\theta + \alpha) = \frac{a}{h}$$

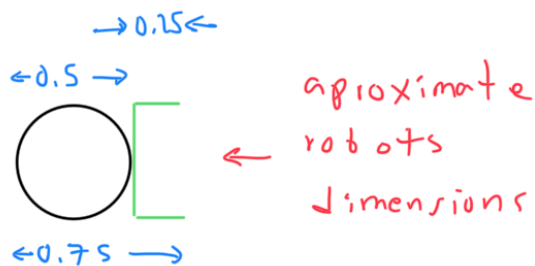


$$a = h \cdot \sin(\theta + \alpha)$$

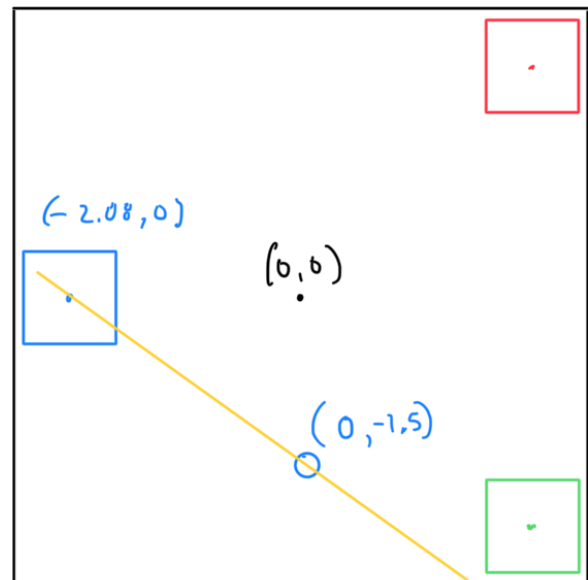


$$\begin{aligned} p_{obj-x} &= p_{rob-x} + h \cdot \cos(\theta + \alpha) \\ p_{obj-y} &= p_{rob-y} + h \cdot \sin(\theta + \alpha) \end{aligned}$$

Determine Pre-Flow Position



Let's find the $f(x)$ of a line that connects the blue object to the blue collection zone



Conditions:

$$\begin{aligned} f(x = -2.08) &= 0 \\ f(x = 0) &= -1.5 \end{aligned}$$

$f(x) = mx + c$, let's find m, c

$$f(0) = -1.5 = c$$

$$f(-2.08) = 0 = m(-2.08) - 1.5 \Rightarrow m = \frac{-1.5}{-2.08}$$

$$m = -0.72$$

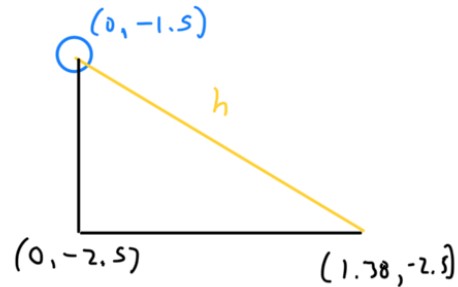
$$F(x) = -0.72x - 1.5$$

Can the robot fit between the object and the bottom wall when lining up with $f(x)$?

$$-2.5 = -0.72x_1 - 1.5$$

$$0.72x_1 = -1.5 + 2.5 = 1$$

$$x_1 = \frac{1}{0.72} = 1.38$$



$$h = \sqrt{1^2 + (1.38)^2} \approx 1.7$$

The robot should be able to fit in this position. In cases where there is not enough space for the robot we could use a different line that arrives at the collection zone but not in the centroid of the zone.

Let's choose $\frac{1.38}{2}$ as the pre-plow x position

$$f(x = \frac{1.38}{2}) = f(0.85) = -0.72 \cdot (0.85) - 1.5 = -2.11$$

So our pre-plow position is

$$p-p-p = (0.85, -2.11) \leftarrow \text{for Arena}(-, \text{blue})$$

second color is
blue

We need to determine six lines for the following

conditions:

- Arena (-, blue)
- Arena (-, red)
- Arena (-, green)
- Arena (blue, -)
- Arena (red, -)
- Arena (green, -)

test first, hardest conditions!

Let's find the line
for Arena (-, red)

Conditions

$$f(x = 2.08) = 2.08$$

$$f(x = 0) = -1.5$$

$$f(x) = mx + c$$

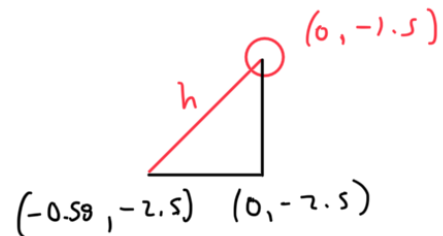
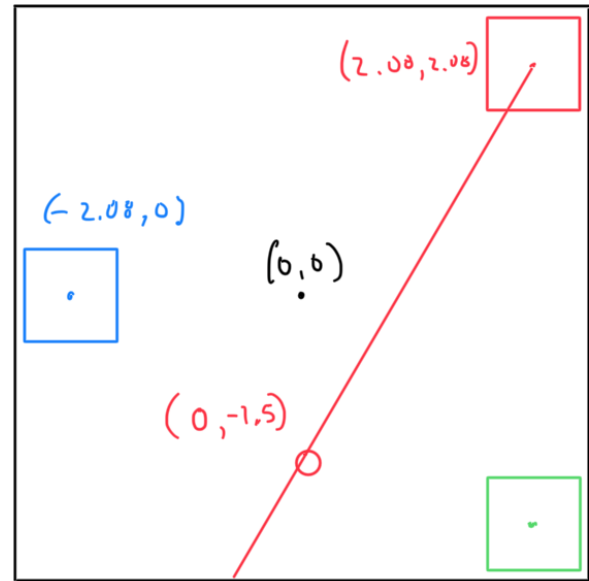
$$f(0) = -1.5 = c$$

$$f(2.08) = 2.08 = m(2.08) - 1.5$$

$$m = \frac{2.08 + 1.5}{2.08} = 1.72$$

so

$$f(x) = 1.72x - 1.5$$



$$f(x_1) = -2.5 = 1.72x_1 - 1.5 \Rightarrow x_1 = \frac{-1}{1.72} = -0.58$$

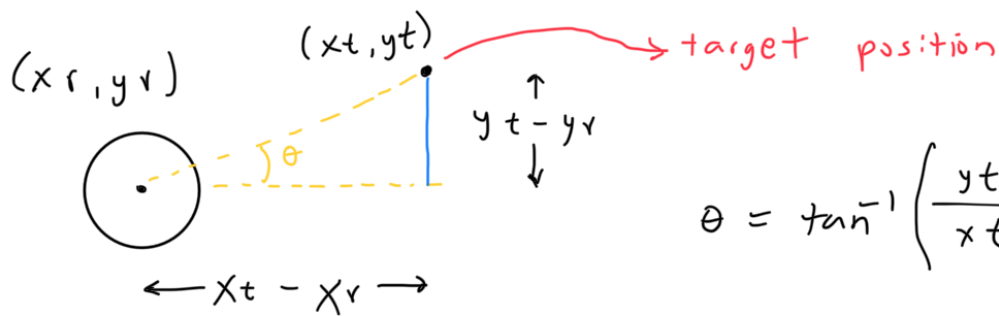
$$h = \sqrt{0.58^2 + 1} = 1.16$$

Tight fit for the robot. We need to test
our path planning algorithm in this condition

Command Movement Algorithm

- Given a path of straight segments (set of x-y coordinates)
 - Loop over each segment
 - Spin robot to point to segment end
 - Move forward until segment end is reached
 - Check if x-y are within target range
- ↳ tolerance

Determine segment end angle (not used)



$$\theta = \tan^{-1} \left(\frac{y_t - y_r}{x_t - x_r} \right)$$