Dynamics of a neuronal pacemaker in the weakly electric fish *Apteronotus*

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| Parameter | Lower Bound | Upper Bound | Unit |
|--|-------------|-------------|----------|
| E_{Ca} | 20. | 30. | mV |
| E_K | -90. | -80. | mV |
| E_{Leak} | -90. | -80. | mV |
| E_{Na} | 20. | 30. | mV |
| G_{Ca} | 0. | 20. | mS |
| G_K | 30. | 70. | mS |
| G_{Leak} | 0. | 3. | mS |
| G_{Na} | 30. | 70. | mS |
| $s_{	au_b}$ | 100. | 2. | ms |
| $s_{	au_g}$ | 5. | 15. | ms |
| $s_{	au_h}$ | 5. | 15. | ms |
| $s_{	au_m}$ | 100. | 2. | ms |
| $s_{	au_n}$ | 5. | 15. | ms |
| $s_{	au_q}$ | 100. | 2. | ms |
| $\sigma^1_{	au_b}$ | 10. | 20. | mV |
| $\sigma_{	au_g}^{1'}$ | 10. | 20. | mV |
| $\sigma_{	au_h}^{ec{1}}$ | 5. | 15. | mV |
| $\sigma_{	au_m}^{l}$ | 5. | 15. | mV |
| $\sigma^1_{	au_n}$ | 5. | 15. | mV |
| $\sigma_{	au_q}^{rac{arepsilon}{1}}$ | 10. | 20. | mV |
| σ_{-}^{2} | 10. | 20. | mV |
| $\sigma^{2}_{	au_{b}} \ \sigma^{2}_{	au_{g}}$ | 10. | 20. | mV |
| $\sigma_{\tau_g}^2$ | 5. | 15. | mV |
| $\sigma_{	au_n}^2 \ \sigma_{	au_n}^2 \ \sigma_{	au_n}^2 \ \sigma_{	au_n}^2 \ \sigma_{	au_q}^2$ | 5. | 15. | mV |
| $\sigma_{\tau_m}^2$ | 25. | 35. | mV |
| $\sigma_{	au_n}^2$ | 20. | 30. | mV |
| $\sigma_{	au_q}$ | 10. | 20. | |
| $\sigma_{\!b_\infty}$ | 10. | 20. | mV mV |
| $\sigma_{\!g_\infty}$ | 5. | 10. | |
| $\sigma_{h_{\infty}}$ | 5. | 10. | mV mV |
| $\sigma_{m_\infty} \ \sigma_{n_\infty}$ | 10. | 20. | mV |
| $\sigma_{n_{\infty}}$ | 5. | 15. | mV |
| $\sigma_{q_\infty} \ 	heta_{b_\infty}$ | -70. | -60. | mV |
| $	heta_{g_\infty}$ | -110. | -100. | mV |
| $	heta_{h_\infty}^{g_\infty}$ | -90. | -70. | mV |
| $	heta_{m_\infty}$ | -70. | -50. | mV |
| $	heta_{n_\infty}$ | -65. | -45. | mV |
| $	heta_{q_\infty}$ | -55. | -25. | mV |
| $	heta_{	au_b}$ | -100. | -80. | mV |
| $	heta_{	au_g}$ | -85. | -75. | mV |
| $	heta_{	au_h}^{	au_g}$ | -90. | -60. | mV |
| $	heta_{	au_m}$ | -90. | -70. | mV |
| $	heta_{	au_n}$ | -65. | -45. | mV |
| $	heta_{	au_q}$ | -55. | -35. | mV |
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Table S1. Upper and lower bounds for parameter selection in the GA

| Parameter | Canonical Fit | Model ii Fit | Model iii Fit | Model iv Fit | Unit |
|------------|---------------|--------------|---------------|--------------|------|
| E_{Ca} | 23.95 | 22.13 | 29.01 | 27.02 | mV |
| E_K | -80.87 | -87.12 | -84.49 | -89.02 | mV |
| E_{Leak} | -88.91 | -84.63 | -88.95 | -87.81 | mV |
| E_{Na} | 24.22 | 25.56 | 22.12 | 21.06 | mV |
| G_{Ca} | 14.28 | 4.13 | 1.99 | 2.57 | mS |
| G_K | 59.27 | 50.16 | 39.90 | 33.16 | mS |
| G_{Leak} | 1.13 | 1.98 | 1.11 | 2.17 | mS |
| G_{Na} | 63.13 | 52.48 | 48.66 | 61.82 | mS |

Table S2. Ionic Parameters for model fits. Canonical Model maps to Figure 1A, Model B-D maps to Figure 1B-D

| Parameter | Canonical Fit | Model ii Fit | Model iii Fit | Model iv Fit | Unit |
|---|---------------|--------------|---------------|--------------|------|
| $S \tau_b$ | 0.62 | 1.38 | 1.65 | 1.07 | ms |
| $s_{	au_g}$ | 8.28 | 11.36 | 11.95 | 14.02 | ms |
| $s_{	au_h}$ | 10.29 | 11.36 | 9.71 | 9.62 | ms |
| $s_{	au_m}$ | 0.50 | 0.47 | 1.08 | 1.33 | ms |
| s_{τ_n} | 6.56 | 9.69 | 7.18 | 6.35 | ms |
| $s_{	au_q}$ | 1.01 | 0.72 | 1.15 | 0.96 | ms |
| $\sigma^1_{	au_b}$ | 11.27 | 11.31 | 13.50 | 18.50 | mV |
| $\sigma_{	au_arrho}^{ m f}$ | 17.94 | 17.33 | 17.63 | 17.60 | mV |
| $\sigma_{	au_h}^{ m l^\circ}$ | 11.15 | 7.27 | 13.49 | 13.01 | mV |
| $\sigma_{\tau_m}^{1''}$ | 11.98 | 7.20 | 8.86 | 8.94 | mV |
| $\sigma_{	au_n}^{	ilde{1}^n}$ | 7.17 | 12.68 | 10.72 | 13.23 | mV |
| $\sigma_{	au_a}^{\hat{\Gamma}}$ | 13.14 | 13.41 | 17.87 | 17.79 | mV |
| $\sigma_{\tau_{b}-\tau_{c}}^{1}$ $\sigma_{\tau_{b}-\tau_{c}}^{1}$ $\sigma_{\tau_{b}-\tau_{c}}^{1}$ $\sigma_{\tau_{b}-\tau_{c}}^{1}$ $\sigma_{\tau_{b}-\tau_{c}}^{1}$ $\sigma_{\tau_{b}-\tau_{c}}^{1}$ $\sigma_{\tau_{b}-\tau_{c}}^{1}$ $\sigma_{\tau_{c}-\tau_{c}}^{1}$ $\sigma_{\tau_{c}-\tau_{c}}^{1}$ $\sigma_{\tau_{c}-\tau_{c}}^{1}$ $\sigma_{\tau_{c}-\tau_{c}}^{1}$ $\sigma_{\tau_{c}-\tau_{c}}^{1}$ $\sigma_{\tau_{c}-\tau_{c}-\tau_{c}}^{1}$ | 12.62 | 15.89 | 17.79 | 18.41 | mV |
| $\sigma_{	au_{\sigma}}^{2}$ | 14.99 | 17.95 | 15.38 | 17.56 | mV |
| $\sigma_{	au_{k}}^{\hat{z}}$ | 10.26 | 7.80 | 11.14 | 8.17 | mV |
| $\sigma_{	au_{\cdots}}^{2^n}$ | 13.52 | 7.70 | 12.87 | 14.10 | mV |
| $\sigma_{	au_n}^{2^n}$ | 26.62 | 32.07 | 33.81 | 31.13 | mV |
| $\sigma_{	au_a}^{2^i}$ | 25.15 | 25.97 | 28.51 | 22.07 | mV |
| $\sigma_{\!b_\infty}^{^{^{q}}}$ | 11.55 | 15.12 | 16.80 | 12.37 | mV |
| $\sigma_{\!g_\infty}$ | 18.38 | 12.71 | 16.72 | 18.55 | mV |
| $\sigma_{\!h_\infty}$ | 9.48 | 9.03 | 8.51 | 6.92 | mV |
| $\sigma_{\!m_\infty}$ | 8.78 | 6.91 | 6.33 | 9.08 | mV |
| $\sigma_{n_{\infty}}$ | 12.05 | 12.99 | 11.33 | 18.22 | mV |
| $\sigma_{\!q_{\scriptscriptstyle\infty}}$ | 8.03 | 6.71 | 11.40 | 10.39 | mV |
| $	heta_{b_\infty}$ | -67.10 | -64.67 | -67.86 | -65.61 | mV |
| $	heta_{g_\infty}$ | -106.52 | -106.48 | -102.24 | -106.40 | mV |
| $	heta_{h_\infty}$ | -85.67 | -84.66 | -76.30 | -72.08 | mV |
| $	heta_{m_{\infty}}$ | -55.85 | -66.36 | -58.86 | -55.27 | mV |
| $	heta_{n_\infty}$ | -52.16 | -59.15 | -56.39 | -59.78 | mV |
| $	heta_{q_\infty}$ | -41.48 | -42.43 | -33.52 | -43.99 | mV |
| $	heta_{	au_b}$ | -83.44 | -96.35 | -88.60 | -94.56 | mV |
| $	heta_{	au_g}$ | -82.37 | -83.12 | -77.18 | -82.55 | mV |
| $	heta_{	au_h}$ | -82.53 | -76.68 | -77.66 | -84.61 | mV |
| $	heta_{	au_m}$ | -77.87 | -85.17 | -72.28 | -85.84 | mV |
| $	heta_{	au_n}$ | -52.65 | -59.64 | -47.93 | -49.18 | mV |
| $oldsymbol{	heta}_{	au_q}$ | -47.45 | -46.91 | -44.41 | -45.09 | mV |

Table S3. Gating Parameters for model fits. Canonical Model maps to Figure 1A, Model B-D maps to Figure 1B-D