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hw0913
<https://github.com/aaronsta/COSC311/blob/master/hw0913>
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R-4.2

A: $8n \log n$
B: $2n^2$

Solve for n , $n = 16$.

For $n_0 = 17$, B is always of greater value than A, so A is better than B for $n_0 = 17$

R-4.3

A $y = 40x^2$
B $y = 2x^3$

Solve for x , $x = 20$

$n_0 = 21$, after that B grows faster than A and thus A is better than B

R-4.8

Ordered by asymptotic growth rate

2^{10}
 $2^{(\log n)}$
 $3n + 100 \log(n)$
 $4n$
 $n * (\log(n))$
 $4n * \log(n) + 2n$
 $n^2 + 10n$
 n^3
 2^n

R-4.9

example1

The loop runs n times (doing 1 primitive operation inside), added to a constant number of primitive operations outside the loop. So the method runs in

$O(n)$

R-4.10

example2

Constant number of primitive operations outside loop plus inside loop (which again has a constant number of primitive operations) runs $\text{floor}(n/2)$ times, but $1/2$ is a constant so again the number of overall operations is:

$O(n)$

R-4.11

example3

I worked out this table of the number of iterations of the inner loop for each value of j (i.e. outer loop value):

| val of j | num of iterations of inner |
|------------|----------------------------|
| ----- | ----- |
| 0 | 1 |
| 1 | 2 |
| 2 | 3 |
| ... | ... |
| $n-1$ | n |
| n | $n+1$ |

So the primitive operation inside the inner loop runs

$$1+2+3+\dots+n + n+1 = n(n+1)/2$$

times, by Prop 4.3 of GtG book (Gauss) .

This if is of order

$O(n^2)$