



UNIVERSITÄT
LEIPZIG

Einführung in die Objekt-Orientierte Modellierung und Programmierung

Wintersemester 2025/2026

Dirk Zeckzer

Institut für Informatik



Teil XX

Rekursion

Rekursive Funktionen: Fakultät

Definition: $f(n) = n!$

► Berechnung iterativ:

$$f(n) = \prod_{i=1}^n i$$

► Beispiel

$$\begin{aligned} f(5) &= \prod_{i=1}^5 i &= 1 \cdot 2 \cdot 3 \cdot 4 \cdot 5 \\ & &= 2 \cdot 3 \cdot 4 \cdot 5 \\ & &= 6 \cdot 4 \cdot 5 \\ & &= 24 \cdot 5 \\ & &= 120 \end{aligned}$$

► Berechnung rekursiv:

$$f(n) = \begin{cases} 1 & n = 1 \\ n \cdot f(n-1) & n > 1 \end{cases}$$

► Beispiel

$$\begin{aligned} f(5) &= 5 \cdot f(4) \\ &= 5 \cdot (4 \cdot f(3)) \\ &= 5 \cdot (4 \cdot (3 \cdot f(2))) \\ &= 5 \cdot (4 \cdot (3 \cdot (2 \cdot f(1)))) \\ &= 5 \cdot (4 \cdot (3 \cdot (2 \cdot 1))) \\ &= 120 \end{aligned}$$

Rekursive Funktionen: Fakultät

Definition: $f(n) = n!$

► Berechnung iterativ:

$$f(n) = \prod_{i=1}^n i$$

```
1  public static long fakultaetForLoop(  
2      final long n  
3  ) {  
4      // Initialisierung  
5      long result = 1;  
6  
7      // Berechnung  
8      for (long i = 1; i <= n; ++i) {  
9          result *= i;  
10     }  
11  
12     // Ergebnis  
13     return result;  
14 }
```

► Berechnung rekursiv:

$$f(n) = \begin{cases} 1 & n = 1 \\ n \cdot f(n-1) & n > 1 \end{cases}$$

```
1  public static long fakultaetRecursive(  
2      final long n  
3  ) {  
4      // Fallunterscheidung  
5      if (n > 1) {  
6          // rekursiver Aufruf  
7          return n * fakultaetRecursive(n - 1);  
8      } else {  
9          // Basisfall  
10         return 1;  
11     }  
12 }
```

Odd-Even

$$\begin{aligned} \text{odd}(n) &= \begin{cases} \text{true} & n = 1 \\ \text{even}(n-1) & n > 1 \end{cases} & \text{even}(n) &= \begin{cases} \text{false} & n = 1 \\ \text{odd}(n-1) & n > 1 \end{cases} \end{aligned}$$

Beispiel:

$$\begin{aligned} \text{odd}(5) &= \text{even}(4) \\ &= \text{odd}(3) \\ &= \text{even}(2) \\ &= \text{odd}(1) \\ &= \text{true} \end{aligned}$$

Odd-Even

$$\text{odd}(n) = \begin{cases} \text{true} & n = 1 \\ \text{even}(n-1) & n > 1 \end{cases}$$

$$\text{even}(n) = \begin{cases} \text{false} & n = 1 \\ \text{odd}(n-1) & n > 1 \end{cases}$$

```
1 public static boolean odd(  
2     final int n  
3 ) {  
4     if (n > 1) {  
5         return even(n - 1);  
6     } else {  
7         return true;  
8     }  
9 }
```

```
1 public static boolean even(  
2     final int n  
3 ) {  
4     if (n > 1) {  
5         return odd(n - 1);  
6     } else {  
7         return false;  
8     }  
9 }
```

Fibonacci-Folge

1 1 2 3 5 8 13 21 34 55 ...

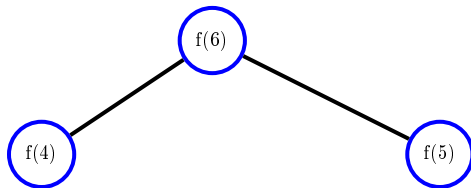
$$f(n) = \begin{cases} 1 & n = 1 \\ 1 & n = 2 \\ f(n-1) + f(n-2) & n > 2 \end{cases}$$

```
1  public static long fibonacci(  
2      final long n  
3  ) {  
4      if (n == 1) {  
5          return 1;  
6      } else if (n == 2) {  
7          return 1;  
8      } else {  
9          return fibonacci(n - 1) + fibonacci(n - 2);  
10     }  
11 }
```

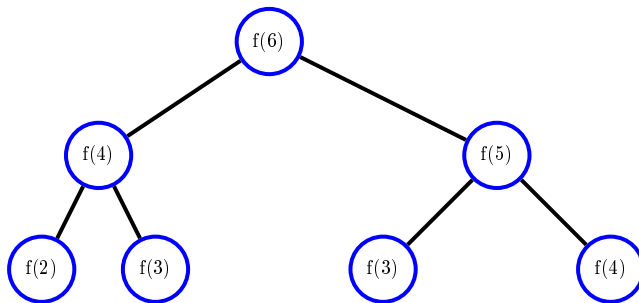
Fibonacci-Folge


$$f(6)$$

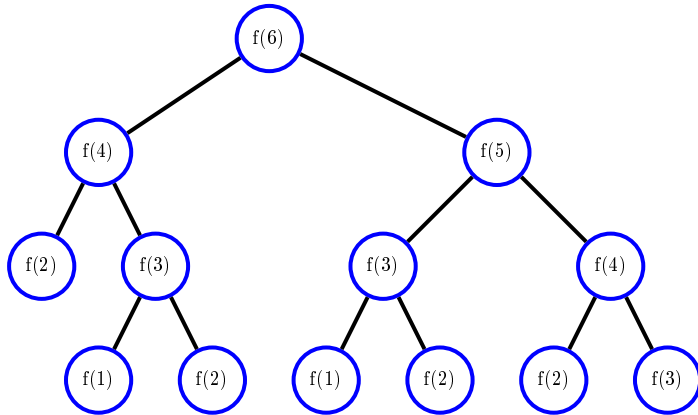
Fibonacci-Folge



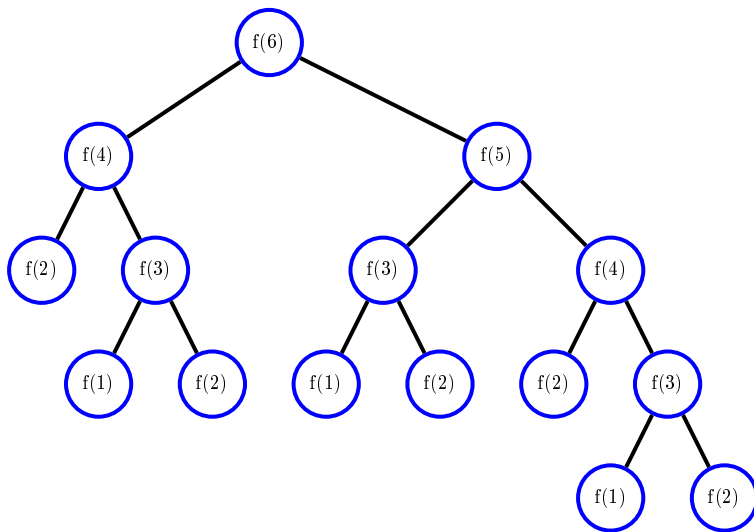
Fibonacci-Folge



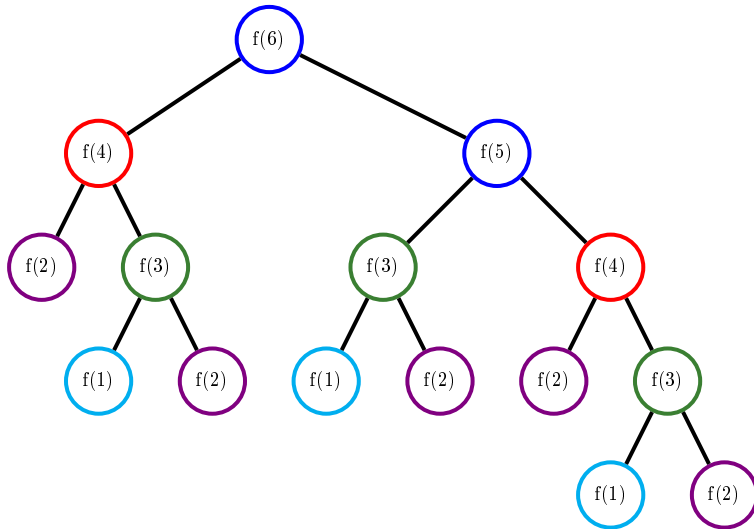
Fibonacci-Folge



Fibonacci-Folge



Fibonacci-Folge



Fibonacci-Folge

$$f(n) = \begin{cases} 1 & n = 1 \\ 1 & n = 2 \\ f(n-1) + f(n-2) & n > 2 \end{cases}$$

```
1  public static long fibonacciIterative(  
2      final long n  
3  ) {  
4      if (n == 1) {  
5          return 1;  
6      }  
7  
8      if (n == 2) {  
9          return 1;  
10     }  
  
10     long n1 = 1;  
11     long n2 = 1;  
12     long current = 2;  
13     long result = 0;  
14  
15     while (current < n) {  
16         result = n1 + n2;  
17         n1 = n2;  
18         n2 = result;  
19         ++current;  
20     }  
21  
22     return result;  
23 }
```

Ackermannfunktion

$$a(0, m) = m + 1$$

$$a(n+1, 0) = a(n, 1)$$

$$a(n+1, m+1) = a(n, a(n+1, m))$$

```
1  public static int ackermann(  
2      final int n,  
3      final int m  
4  ) {  
5      if (n == 0) {  
6          return m + 1;  
7      } else if (m == 0) {  
8          return ackermann(n - 1, 1);  
9      } else {  
10         return ackermann(n - 1, ackermann(n, m - 1));  
11     }  
12 }
```

Ackermannfunktion

$$a(0, m) = m + 1$$

$$a(n+1, 0) = a(n, 1)$$

$$a(n+1, m+1) = a(n, a(n+1, m))$$

Werte:

► $a(0, m) = m + 1$

► $a(1, m) = ?$

$$\begin{aligned} a(1, 0) &= a(0, 1) \\ &= 2 \end{aligned}$$

$$\begin{aligned} a(1, 1) &= a(0, a(1, 0)) \\ &= a(0, 2) \\ &= 3 \end{aligned}$$

$$\begin{aligned} a(1, 2) &= a(0, a(1, 1)) \\ &= a(0, 3) \\ &= 4 \end{aligned}$$

Ackermannfunktion

$$a(0, m) = m + 1$$

$$a(n+1,0) = a(n,1)$$

$$a(n+1, m+1) = a(n, a(n+1, m))$$

Werte:

$$\begin{aligned} a(4,0) &= a(3,1) \\ &= a(2, a(3,0)) \\ &= a(2,5) \end{aligned}$$

$$\begin{aligned} a(3,0) &= a(2,1) &&= a(1, a(2,4)) \\ &= a(1, a(2,0)) &&= \dots \end{aligned}$$

$$\begin{array}{llll} a(2,0) & = & a(1,1) & = & a(1,3) & = & a(1,11) \\ & = & 3 & = & 5 & = & 13 \end{array}$$

Ackermannfunktion

$$a(0, m) = m + 1$$

$$a(n + 1, 0) = a(n, 1)$$

$$a(n + 1, m + 1) = a(n, a(n + 1, m))$$

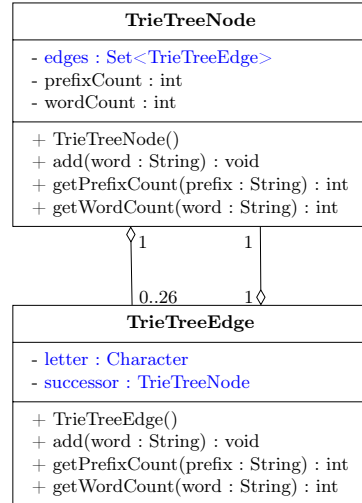
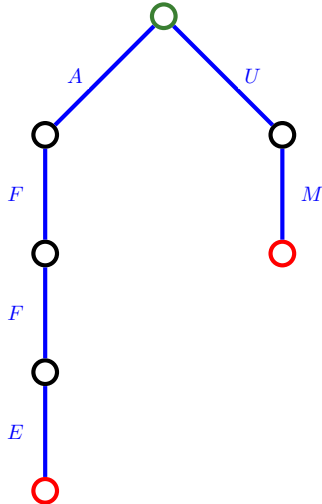
Tabelle: Werte für $a(n, m)$ [Wikipedia]

n	0	1	2	3	4	...	m
0	1	2	3	4	5	...	$m + 1$
1	2	3	4	5	6	...	$m + 2$
2	3	5	7	9	11	...	$2m + 3$
3	5	13	29	61	125	...	$8 \cdot 2^m - 3$
4	13	65533	$2^{65536} - 3$	$a(3, 2^{65536} - 3)$	$a(3, a(4, 3))$...	$2^{2^{\cdot^{\cdot^{\cdot}}}} - 3$
			$\approx 2 \cdot 10^{19728}$				(Potenztturm mit m+3 Zahlen)
5	65533	$a(4, 65533)$	$a(4, a(5, 1))$	$a(4, a(5, 2))$	$a(4, a(5, 3))$...	$a(4, a(5, m - 1))$
6	$a(5, 1)$	$a(5, a(6, 0))$	$a(5, a(6, 1))$	$a(5, a(6, 2))$	$a(5, a(6, 3))$...	$a(5, a(6, m - 1))$

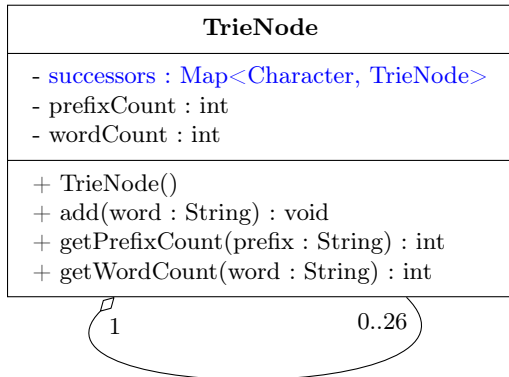
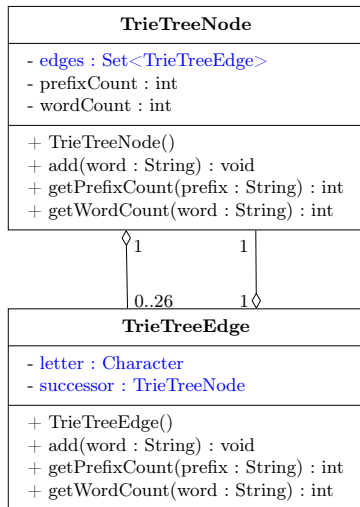
Datenstruktur Trie

- ▶ Alphabet: $\Sigma = \{A, B, C, \dots, Z\}$
- ▶ $\Sigma^+ = \{A, AA, \dots, AB, ABA, \dots, B, BA, \dots\}$
- ▶ ϵ : das **Leere Wort**, ein Wort ohne Buchstaben
- ▶ Worte: $W = \Sigma^* = \{\epsilon, A, AA, \dots, AB, ABA, \dots, B, BA, \dots\}$

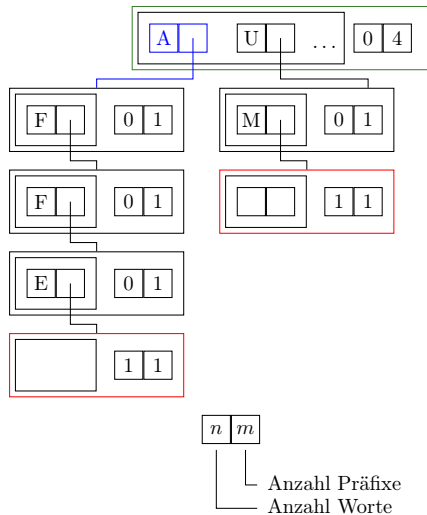
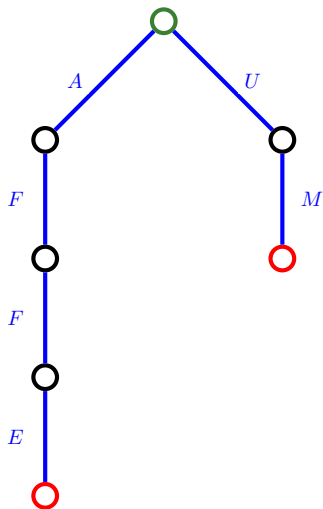
Datenstruktur Trie



Datenstruktur Trie

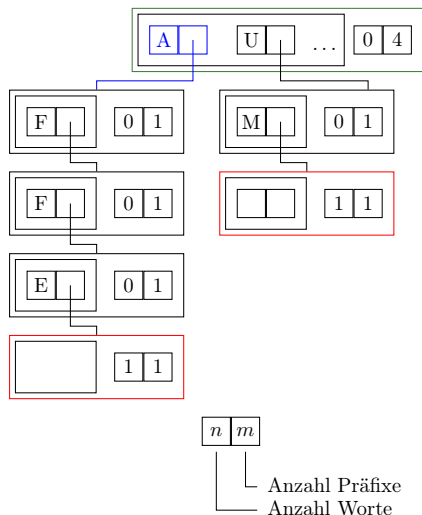


Datenstruktur Trie



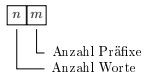
Datenstruktur Trie

- ▶ Datenstruktur zur Speicherung von Worten
- ▶ Ergebnis: Baum
- ▶ Ein Knoten im Baum entspricht einem Zeichen des Wortes



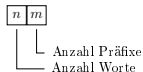
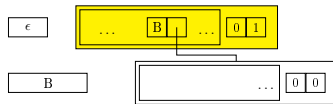
Datenstruktur Trie

Einfügen des Wortes BANANE



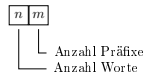
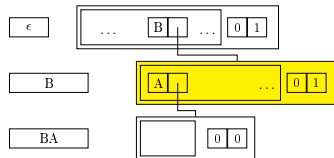
Datenstruktur Trie

Einfügen des Wortes BANANE



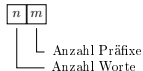
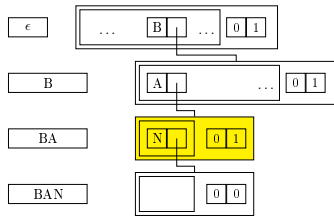
Datenstruktur Trie

Einfügen des Wortes BANANE



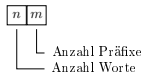
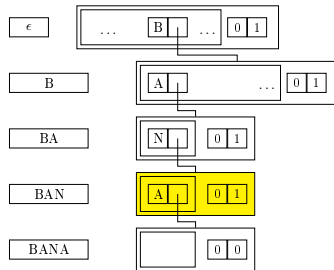
Datenstruktur Trie

Einfügen des Wortes BANANE



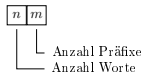
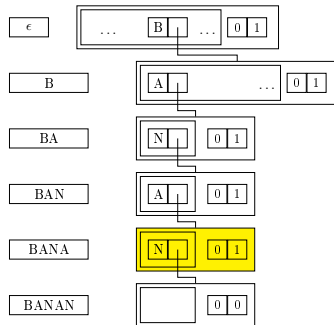
Datenstruktur Trie

Einfügen des Wortes BANANE



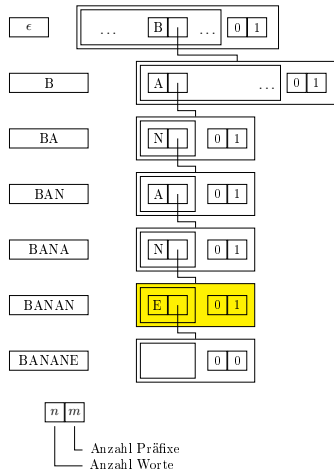
Datenstruktur Trie

Einfügen des Wortes BANANE



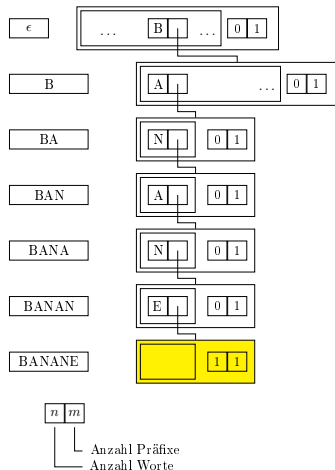
Datenstruktur Trie

Einfügen des Wortes BANANE



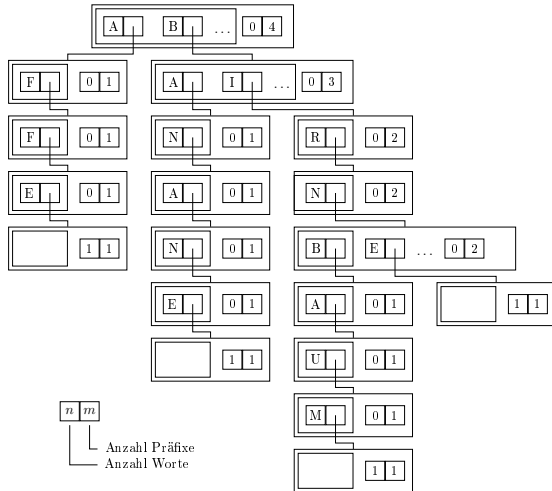
Datenstruktur Trie

Einfügen des Wortes BANANE

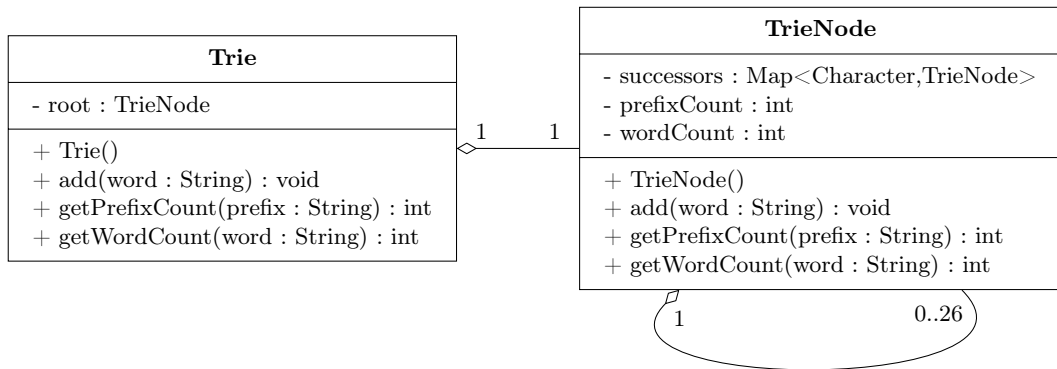


Datenstruktur Trie

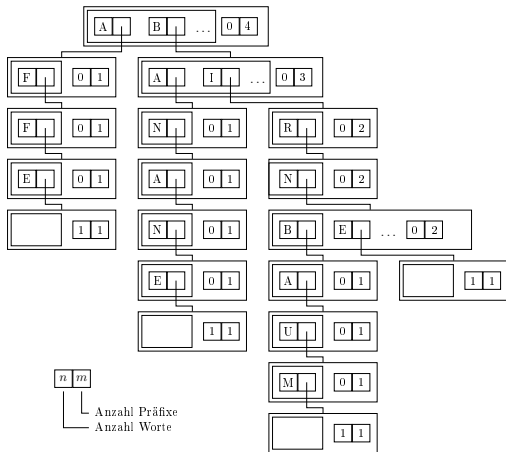
Trie nach dem Einfügen von BANANE, AFFE, BIRNE, BIRNBAUM



Datenstruktur Trie: Modell



Trie

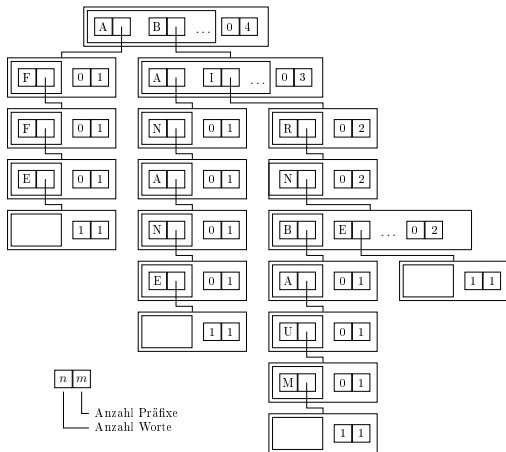


```

1  public class Trie {
2
3      private final TrieNode
4          root = new TrieNode();
5
6      public Trie() {
7      }
8
9      public void add(
10         final String word
11     ) {
12         root.add(word);
13     }
14
15     public int getPrefixCount(
16         final String prefix
17     ) {
18         return root.getPrefixCount(prefix);
19     }
20
21     public int getWordCount(
22         final String word
23     ) {
24         return root.getWordCount(word);
25     }
26 }

```

TrieNode: Attribute

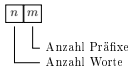
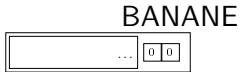


```

1  public class TrieNode {
2
3      private final Map<Character, TrieNode>
4          successors = new TreeMap<>();
5
6      private int prefixCount = 0;
7
8      private int wordCount = 0;
9
10     public TrieNode() {
11     }
12
13     ...
14 }

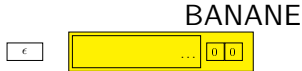
```

TrieNode: add



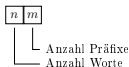
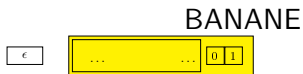
```
1 public class Trie {
2
3     private final TrieNode
4         root = new TrieNode();
5
6     public Trie() {
7     }
8
9     public void add(
10         final String word
11     ) {
12         root.add(word);
13     }
14
15     public int getPrefixCount(
16         final String prefix
17     ) {
18         return root.getPrefixCount(prefix);
19     }
20
21     public int getWordCount(
22         final String word
23     ) {
24         return root.getWordCount(word);
25     }
26 }
```

TrieNode: add



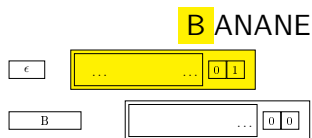
```
1 public class TrieNode {
2
3     private final Map<Character, TrieNode>
4         successors = new TreeMap<>();
5     private int prefixCount = 0;
6     private int wordCount = 0;
7
8     public void add(
9         final String word
10    ) {
11
12        ++prefixCount;
13        if (word.isEmpty()) {
14            ++wordCount;
15        } else {
16            final Character currentChar
17                = word.charAt(0);
18            TrieNode trieNode
19                = successors.get(currentChar);
20            if (trieNode == null) {
21                trieNode = new TrieNode();
22                successors.put(currentChar,
23                    trieNode);
24            }
25            trieNode.add(word.substring(1));
26        }
27    }
```

TrieNode: add



```
1 public class TrieNode {
2
3     private final Map<Character, TrieNode>
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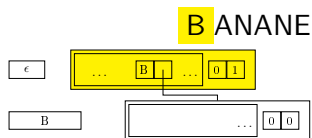
TrieNode: add



```

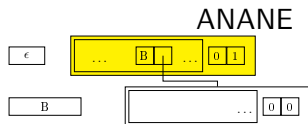
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6      private int wordCount = 0;
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9          final String word
10     ) {
11         ++prefixCount;
12         if (word.isEmpty()) {
13             ++wordCount;
14         } else {
15             final Character currentChar
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20                 trieNode = new TrieNode();
21             }
22             successors.put(currentChar,
23                             trieNode);
24             trieNode.add(word.substring(1));
25         }
26     }
27 }
    
```

TrieNode: add



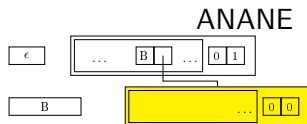
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TrieNode: add



```
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7
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9         final String word
10    ) {
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21                 successors.put(currentChar,
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23             }
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25         }
26     }
27 }
```

TrieNode: add

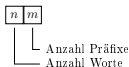
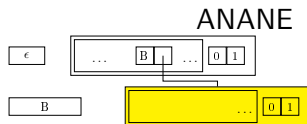


```

1 public class TrieNode {
2
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11     ) {
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19                 = successors.get(currentChar);
20             if (trieNode == null) {
21                 trieNode = new TrieNode();
22                 successors.put(currentChar,
23                     trieNode);
24             }
25             trieNode.add(word.substring(1));
26         }
27     }
28 }

```

TrieNode: add

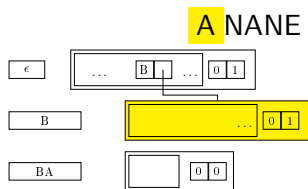


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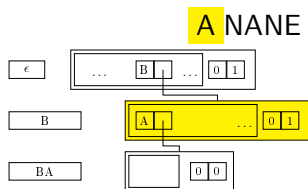
TrieNode: add



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TrieNode: add

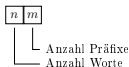
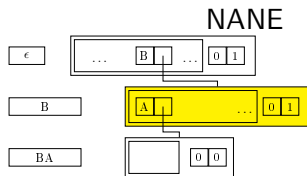


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TrieNode: add

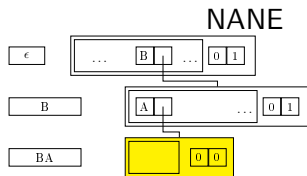


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TrieNode: add

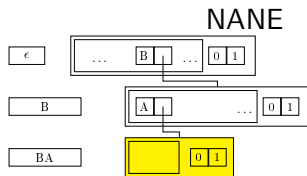


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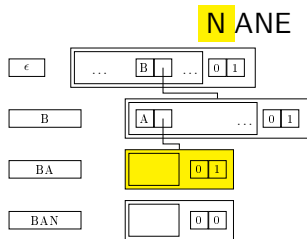
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TrieNode: add

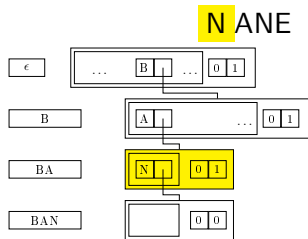


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TrieNode: add

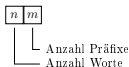
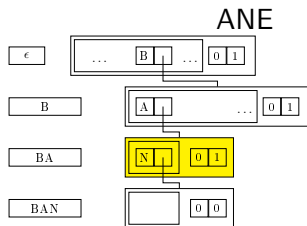


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```

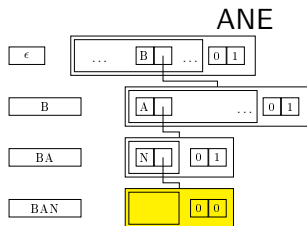
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TrieNode: add

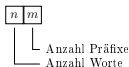
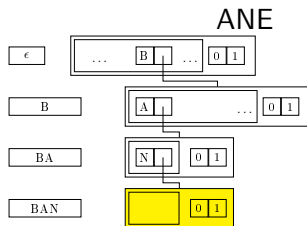


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```

TrieNode: add

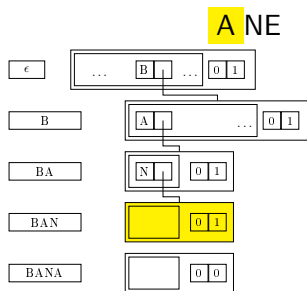


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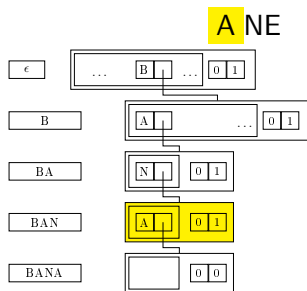
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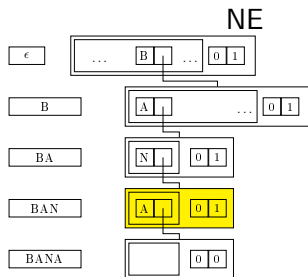
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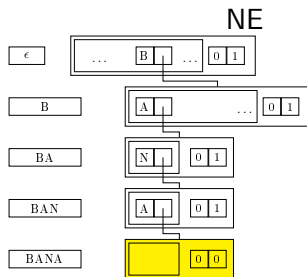
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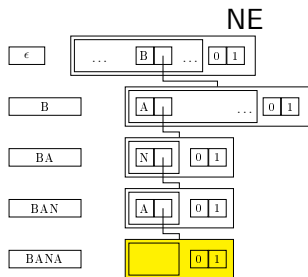


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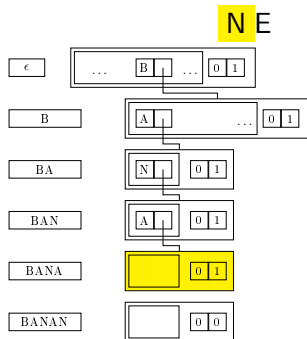
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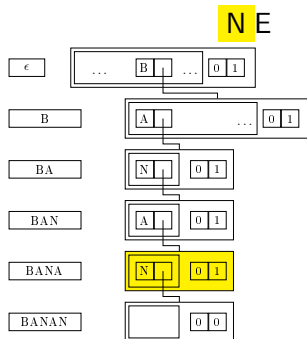


n m
 └─ Anzahl Präfixe
 └─ Anzahl Worte

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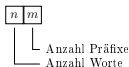
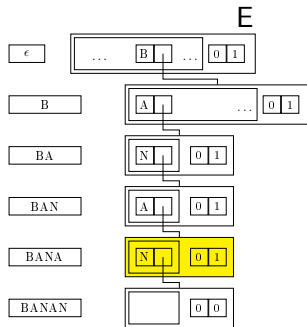


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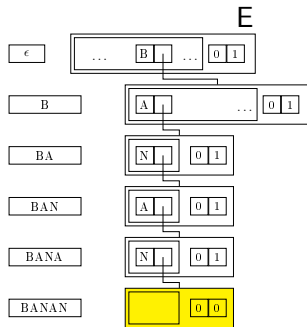
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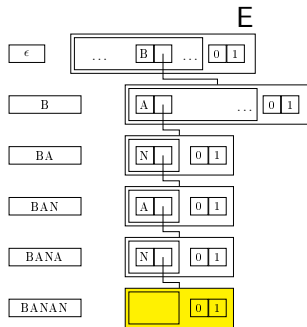


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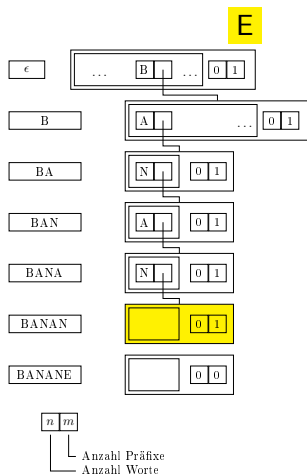


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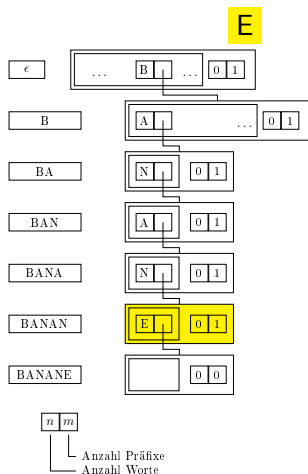


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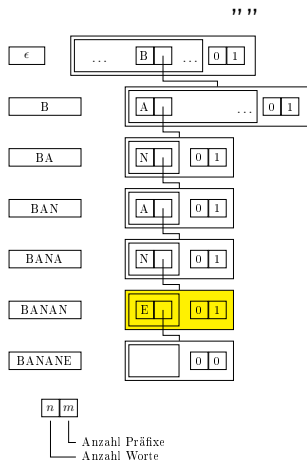


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1  public class TrieNode {
2
3      private final Map<Character, TrieNode>
4          successors = new TreeMap<>();
5      private int prefixCount = 0;
6      private int wordCount = 0;
7
8      public void add(
9          final String word
10     ) {
11         ++prefixCount;
12         if (word.isEmpty()) {
13             ++wordCount;
14         } else {
15             final Character currentChar
16                 = word.charAt(0);
17             TrieNode trieNode
18                 = successors.get(currentChar);
19             if (trieNode == null) {
20                 trieNode = new TrieNode();
21                 successors.put(currentChar,
22                             trieNode);
23             }
24             trieNode.add(word.substring(1));
25         }
26     }
27 }

```

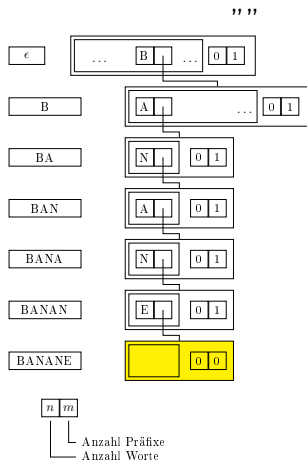
TrieNode: add



```

1  public class TrieNode {
2
3      private final Map<Character, TrieNode>
4          successors = new TreeMap<>();
5      private int prefixCount = 0;
6      private int wordCount = 0;
7
8      public void add(
9          final String word
10     ) {
11         ++prefixCount;
12         if (word.isEmpty()) {
13             ++wordCount;
14         } else {
15             final Character currentChar
16                 = word.charAt(0);
17             TrieNode trieNode
18                 = successors.get(currentChar);
19             if (trieNode == null) {
20                 trieNode = new TrieNode();
21                 successors.put(currentChar,
22                             trieNode);
23             }
24             trieNode.add(word.substring(1));
25         }
26     }
27 }
    
```

TrieNode: add

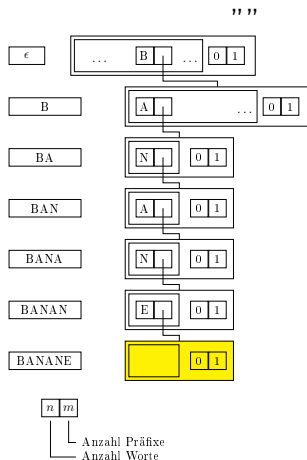


```

1  public class TrieNode {
2
3      private final Map<Character, TrieNode>
4          successors = new TreeMap<>();
5      private int prefixCount = 0;
6      private int wordCount = 0;
7
8
9      public void add(
10         final String word
11     ) {
12
13         ++prefixCount;
14         if (word.isEmpty()) {
15             ++wordCount;
16         } else {
17             final Character currentChar
18                 = word.charAt(0);
19             TrieNode trieNode
20                 = successors.get(currentChar);
21             if (trieNode == null) {
22                 trieNode = new TrieNode();
23                 successors.put(currentChar,
24                     trieNode);
25             }
26             trieNode.add(word.substring(1));
27         }
28     }
29 }

```

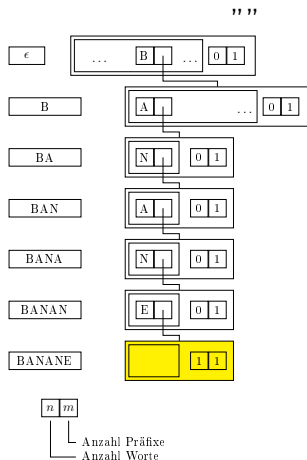
TrieNode: add



```

1  public class TrieNode {
2
3      private final Map<Character, TrieNode>
4          successors = new TreeMap<>();
5      private int prefixCount = 0;
6      private int wordCount = 0;
7
8      public void add(
9          final String word
10     ) {
11         ++prefixCount;
12         if (word.isEmpty()) {
13             ++wordCount;
14         } else {
15             final Character currentChar
16                 = word.charAt(0);
17             TrieNode trieNode
18                 = successors.get(currentChar);
19             if (trieNode == null) {
20                 trieNode = new TrieNode();
21                 successors.put(currentChar,
22                     trieNode);
23             }
24             trieNode.add(word.substring(1));
25         }
26     }
27 }
    
```

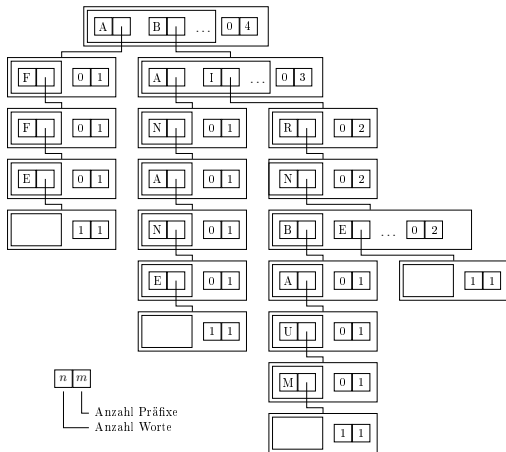
TrieNode: add



```

1  public class TrieNode {
2
3      private final Map<Character, TrieNode>
4          successors = new TreeMap<>();
5      private int prefixCount = 0;
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7
8      public void add(
9          final String word
10     ) {
11         ++prefixCount;
12         if (word.isEmpty()) {
13             ++wordCount;
14         } else {
15             final Character currentChar
16                 = word.charAt(0);
17             TrieNode trieNode
18                 = successors.get(currentChar);
19             if (trieNode == null) {
20                 trieNode = new TrieNode();
21                 successors.put(currentChar,
22                     trieNode);
23             }
24             trieNode.add(word.substring(1));
25         }
26     }
27 }
    
```

TrieNode: getPrefixCount

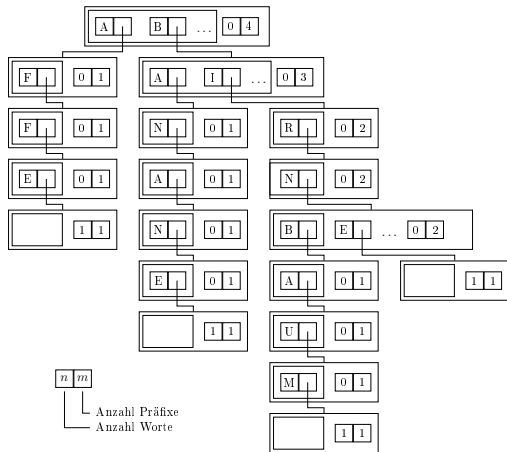


```

1  public class TrieNode {
2
3      private final Map<Character, TrieNode>
4          successors = new TreeMap<>();
5      private int prefixCount = 0;
6      private int wordCount = 0;
7
8      public int getPrefixCount(
9          final String prefix
10     ) {
11         if (prefix.isEmpty()) {
12             return prefixCount;
13         } else {
14             final Character currentChar
15                 = prefix.charAt(0);
16             final TrieNode trieNode
17                 = successors.get(currentChar);
18             if (trieNode == null) {
19                 return 0;
20             }
21             return trieNode.getPrefixCount(
22                 prefix.substring(1)
23             );
24         }
25     }
26 }

```

TrieNode: getWordCount



```

1  public class TrieNode {
2
3      private final Map<Character, TrieNode>
4          successors = new TreeMap<>();
5      private int prefixCount = 0;
6      private int wordCount = 0;
7
8      public int getWordCount(
9          final String word
10     ) {
11         if (word.isEmpty()) {
12             return wordCount;
13         } else {
14             final Character currentChar
15                 = word.charAt(0);
16             final TrieNode trieNode
17                 = successors.get(currentChar);
18             if (trieNode == null) {
19                 return 0;
20             }
21             return trieNode.getWordCount(
22                 word.substring(1)
23             );
24         }
25     }
26 }

```