CAAM 336 · DIFFERENTIAL EQUATIONS

Homework 44

Posted Friday 15 November 2013. Due 5pm Wednesday 27 November 2013.

44. [25 points] Let the norm $\|\cdot\|: \mathbb{R}^2 \to \mathbb{R}$ be defined by

$$\|\mathbf{y}\| = \sqrt{\mathbf{y} \cdot \mathbf{y}}.$$

Let

$$\mathbf{A} = \left[\begin{array}{cc} 0 & 1 \\ 1 & 0 \end{array} \right]$$

and consider the problem of finding $\mathbf{x}(t)$ such that

$$\mathbf{x}'(t) = \mathbf{A}\mathbf{x}(t), \quad t > 0$$

and

$$\mathbf{x}(0) = \left[\begin{array}{c} 2 \\ 0 \end{array} \right].$$

- (a) Compute $\mathbf{x}(t)$.
- (b) How does $\|\mathbf{x}(t)\|$ behave as $t \to \infty$?