CAAM 336

DIFFERENTIAL EQUATIONS IN SCIENCE AND ENGINEERING

Spring 2015 · Rice University

Lectures: Section 1: MWF 1:00-1:50pm, Keck 100

Section 2: MWF 1:00-1:50pm, Duncan Hall 1064

Web Site: http://www.caam.rice.edu/~caam336

Instructors: Section 1: Jesse Chan (Jesse. Chan@rice.edu), Duncan Hall 3023, (713) 348-6113

Office hours: Monday, Wednesday 2-3PM, or by appointment.

Section 2: Travis Thompson (tthompson@rice.edu), Duncan Hall 2038, (713) 348-3336

Office hours: Tuesday, Thursday 2-3PM, or by appointment

Teaching Assistants: Caleb Magruder (caleb.magruder@rice.edu), Duncan Hall 2105

Office hours: Friday 2-3PM

Charles Puelz (cpuelz@rice.edu), Duncan Hall 2108

Office hours: Tuesday 3-4PM

Recitations: (Caleb) Monday 7-9PM, Duncan Hall 1070

(Charles) Tuesday 7-9PM, Duncan Hall 1070

Text: The content of this course is based on material from:

Mark S. Gockenbach, Partial Differential Equations: Analytical and Numerical

Methods, SIAM, Philadelphia, 2011.

Grade Policy: Homework will account for 40% of the final grade and three scheduled exams will account for the

remaining 60%. The last exam will be a scheduled exam which will take place during the final exam period. Failure to attend a scheduled exam may result in a score of zero

for that exam.

Matlab: Most homework questions will require some MATLAB programming. Any MATLAB codes

that you write for the homework must be printed out and attached to the corresponding homework in order to receive credit. For assistance with parts of the homework requiring

MATLAB, please consult the class website for additional materials.

Honor Code: It is an honor code violation to turn in code or solutions which have, in all or in part, been

copied from another student. It is also an honor code violation to consult solutions to the

homework or exams from previous sections of this class.

Homework: Problem sets will be assigned roughly once a week, due at 5pm on the specified date.

Mathematically rigorous solutions are expected; strive for clarity and elegance.

You may collaborate on the problems, but your write-up must be your own independent work.

Transcribed solutions and copied MATLAB code are both unacceptable.

You may not consult solutions from previous sections of this class.

Late Policy: You may turn in two problem sets at 5pm on the next class day without penalty. Subsequent

late assignments will be penalized 20% each. Homework will not be accepted more than one

class period late. (You may not use two 'lates' on one assignment.) In exceptional circumstances, contact the instructor as soon as possible: we adhere to Student Health's

No Note policy.

Re-grade Policy: If your work has been graded incorrectly, you may submit a re-grade request. Clearly explain the

perceived error on a separate sheet of paper, staple it to the front of your graded paper, and give

it to the instructor.

Prerequisites: CAAM 210 (Introduction to Engineering Computation) and MATH 212 (Multivariable Calculus),

or permission of the instructor. Less formally: you should be able to write elementary MATLAB programs, and be comfortable with vector calculus and basic vector and matrix operations.

programs, and be comfortable with vector calculus and basic vector and matrix operations.

Course Objectives: CAAM 336 students learn to identify partial differential equations and solve canonical cases using

both analytical and computational techniques.

Course Outcomes: Upon completing this course, students should be able to:

1) explain the concept and computation of a best approximation from a subspace;

2) identify linear operators and compute their spectra in basic cases;

3) apply these concepts to obtain exact series solutions to differential equations;

4) develop finite element approximations to the exact solutions;

5) assess the stability requirement for time-dependent approximations;

6) create MATLAB programs that compute and visualize series and finite element solutions.

CAAM 336 · Manifesto and Outline

Differential equations form the heart of applied mathematics: they capture an amazing variety of phenomena in fields ranging from physical science and engineering to biology, from financial derivatives to traffic flow. As useful as these equations are, in practice they can be quite difficult to solve: as you read these words, many of the world's fastest computers are busily calculating solutions to such equations. Though the roots of this field reach back to the 18th century, many important, fascinating problems remain for you to tackle. Nearly all disciplines in science and engineering rely fundamentally on differential equations.

This course focuses on the three most famous partial differential equations: the Poisson (diffusion) equation, the heat equation, and the wave equation. There are two main approaches to solving these equations: one that constructs the exact solution as an infinite series (the 'spectral method') and another that uses numerical methods to quickly build approximations to the solution. For historical reasons these two approaches are usually taught in distinct courses—an unfortunate fissure that masks beautiful and deep connections. This course will emphasize these connections. By mastering these ideas you will not only learn elegant techniques for solving classical problems; you will also develop tools to solve the problems you will discover for yourselves as professional scientists and engineers.