

- Longest Common Subsequence
- Travelling Salesman Problem

### **0/1 Knapsack Problem-**

In 0/1 Knapsack Problem,

- As the name suggests, items are indivisible here.
- We can not take a fraction of any item.
- We have to either take an item completely or leave it completely.
- It is solved using a dynamic programming approach.

### **0/1 Knapsack Problem Using Greedy Method-**

Consider-

- Knapsack weight capacity = w
- Number of items each having some weight and value = n

**0/1 knapsack problem is solved using dynamic programming in the following steps-**

Step-01:

- Draw a table say 'T' with (n+1) number of rows and (w+1) number of columns.
- Fill all the boxes of 0th row and 0th column with zeroes as shown-

	0	1	2	3	.....	W
0	0	0	0	0	.....	0
1	0					
2	0					
.....						
n	0					

T-Table

### **Step-02:**

Start filling the table row wise top to bottom

from left to right. Use the following formula-

$$T(i, j) = \max \{ T(i-1, j), \text{value}_i + T(i-1, j - \text{weight}_i) \}$$

Here,  $T(i, j)$  = maximum value of the selected items if we can take items 1 to i and have weight restrictions of j.

- This step leads to completely filling the table.
- Then, value of the last box represents the maximum possible value that can be put into the knapsack.

### **Step-03:**

- To identify the items that must be put into the knapsack to obtain that maximum profit,
- Consider the last column of the table.
- Start scanning the entries from bottom to top.
- On encountering an entry whose value is not same as the value stored in the entry immediately above it, mark the row label of that entry.
- After all the entries are scanned, the marked labels represent the items that must be put into the knapsack

Problem-.

For the given set of items and knapsack capacity = 5 kg, find the optimal solution for the 0/1 knapsack problem making use of a dynamic programming approach.

Item	Weight	Value
1	2	3
2	3	4
3	4	5
4	5	6

$$n = 4$$

$$w = 5 \text{ kg}$$

$$(w_1, w_2, w_3, w_4) = (2, 3, 4, 5)$$

$$(b_1, b_2, b_3, b_4) = (3, 4, 5, 6)$$

## Solution-

### Given

- Knapsack capacity ( $w$ ) = 5 kg
- Number of items ( $n$ ) = 4

Step-01:

Draw a table say 'T' with  $(n+1) = 4 + 1 = 5$  number of rows and  $(w+1) = 5 + 1 = 6$  number of columns. Fill all the boxes of 0<sup>th</sup> row and 0<sup>th</sup> column with 0.

Identifying Items To Be Put Into Knapsack

Following Step-04,

- We mark the rows labelled "1" and "2".
- Thus, items that must be put into the knapsack to obtain the maximum value 7 are **Item-1 and Item-2**

## **Time Complexity-**

- Each entry of the table requires constant time  $\theta(1)$  for its computation.
- It takes  $\theta(nw)$  time to fill  $(n+1)(w+1)$  table entries.
- It takes  $\theta(n)$  time for tracing the solution since tracing process traces the  $n$  rows.