

- The Costs of Production

# Total Revenue, Total Cost, and Profit

- Assumption:
  - The goal of a firm is to maximize profit
- Total revenue,  $TR = P \times Q$ 
  - The amount a firm receives for the sale of its output
- Total cost,  $TC$ 
  - The market value of the inputs a firm uses in production
- Profit =  $TR - TC$

## EXAMPLE 1A: Jelani's Gelato Shop

Jelani owns a small gelato shop on campus. She produces 15,000 pints of gelato a year and sells them for \$5 each. If Jelani's total costs are \$65,000 a year, how much profit the shop brings in one year?

- Total revenue:  $TR = P \times Q = \$5 \times 15,000$   
 $= \$75,000$
- Profit =  $TR - TC = \$75,000 - \$65,000$   
 $= \$10,000$

# Why opportunity costs matter

- “The cost of something is what you give up to get it.”
- Explicit costs
  - Input costs that require an outlay of money by the firm (paying wages to workers)
- Implicit costs
  - Input costs that do not require an outlay of money by the firm (opportunity cost of the owner’s time)
- Total cost = Explicit + Implicit costs

## EXAMPLE 1B: Costs for Jelani's Gelato Shop

Jelani owns a small gelato shop on campus. Jelani pays \$20,000 a year for raw materials and \$12,000 in rent. Jelani could work at the local coffee shop for \$25,000 a year instead. Identify and calculate the explicit and implicit costs.

- Explicit costs: raw materials and rent  
 $= \$20,000 + \$12,000 = \$32,000$
- Implicit cost: opportunity cost of the owner's time  
 $= \$25,000$
- Total costs  $= \$32,000 + \$25,000 = \$57,000$

## EXAMPLE 1C: The cost of capital for Jelani

Jelani invested \$80,000 in the factory and equipment to start the business last year: withdrew \$30,000 from savings and borrowed \$50,000 (interest 10% for saving and borrowing). Identify and calculate the explicit and implicit costs.

- Explicit cost: the interest Jelani has to pay every year: the 10% interest on the borrowed money =  $0.10 \times 50,000 = \$5,000$
- Implicit cost: the interest Jelani could have earned if savings were saved not spent: the 10% on \$30,000 =  $0.10 \times 30,000 = \$3,000$

**The opportunity cost of capital = \$8,000 per year**

# Economic Profit vs. Accounting Profit

- Accounting profit
  - Total revenue minus total explicit costs
- Economic profit
  - Total revenue minus total costs (explicit and implicit costs)
- Accounting profit is greater than economic profit because accounting profit ignores implicit costs.

## EXAMPLE 1D: Profit for Jelani's Gelato Shop

Jelani owns a small gelato shop on campus. She produces 15,000 pints of gelato a year and sells them for \$5 each. Jelani pays \$20,000 a year for raw materials and \$12,000 in rent. Jelani could work at the local coffee shop for \$25,000 a year instead. Jelani invested \$80,000 in the factory and equipment to start the business last year: withdrew \$30,000 from savings and borrowed \$50,000 (interest 10% for saving and borrowing). Calculate accounting and economic profit.



## EXAMPLE 1D: Solutions

- Total revenue  **$TR$**  =  $\$5 \times 15,000 = \$75,000$
- Explicit costs = raw materials + rent + interest paid =  $\$20,000 + \$12,000 + \$5,000 = \$37,000$
- Implicit costs = alternative job + forgone interest =  $\$25,000 + \$3,000 = \$28,000$
- Accounting profit =  **$TR$**  – explicit costs =  $\$75,000 - \$37,000 = \$38,000$
- Economic profit =  **$TR$**  – (explicit + implicit costs) =  $\$75,000 - (\$37,000 + \$28,000) = \$10,000$   
= Accounting profit – implicit cost

## Active Learning 2: Economic vs. Accounting Profit

The equilibrium rent on office space has just increased by \$500/month.

Determine the effects on accounting profit and economic profit if:

- A. You rent your office space (you pay \$500/month)
- B. You own your office space

## Active Learning 2: Answers

The rent on office space increases by \$500/month.

**A.** You rent your office space.

- Explicit costs increase \$500/month.
- Accounting and economic profit each fall \$500/month.

**B.** You own your office space.

- Explicit costs do not change, so accounting profit does not change.
- Implicit costs increase \$500/month, so economic profit falls by \$500/month.

# Production and Costs

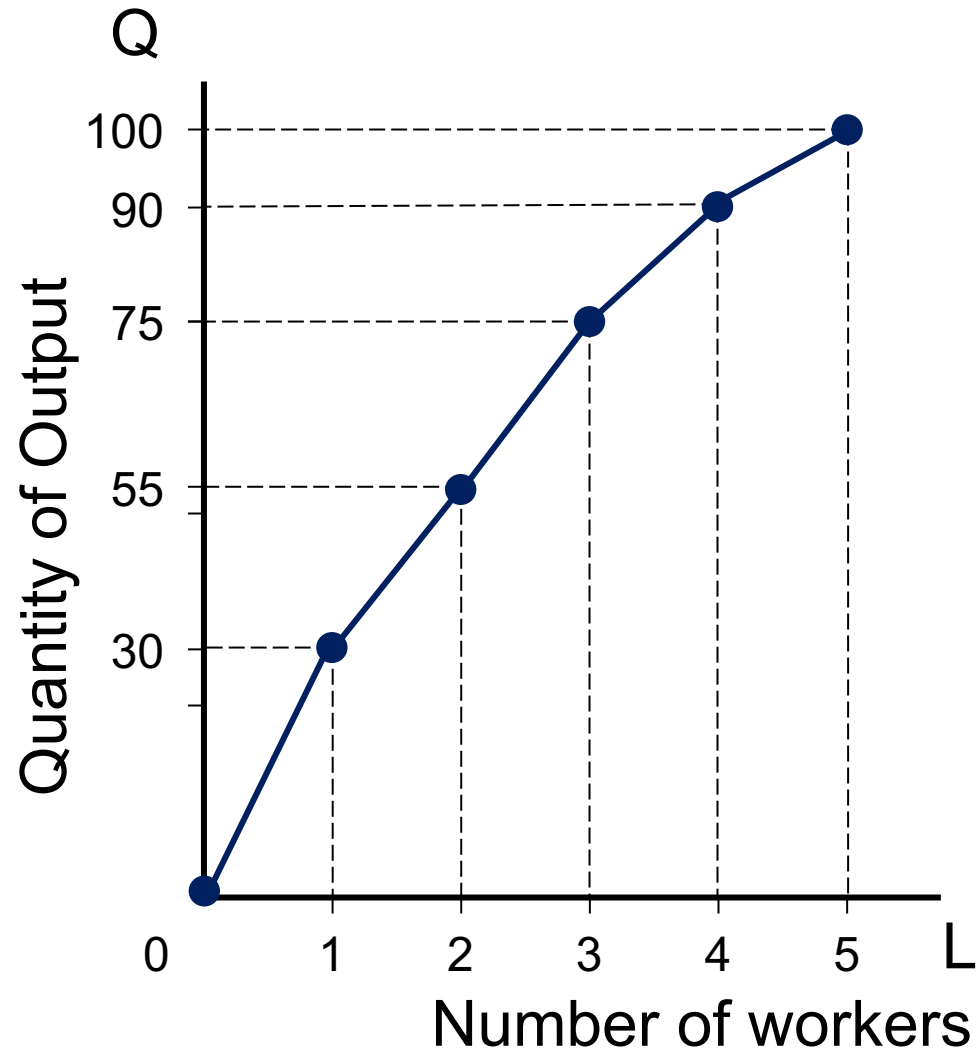
- **Assumption:**
  - Production in the short run
  - Factory size is fixed
  - To increase production: hire more workers
- **Production function**
  - Relationship between
    - Quantity of inputs used to make a good
    - And the quantity of output of that good
  - Gets flatter as production rises

## EXAMPLE 2A: Xavier's Popcorn Truck

- Xavier has a popcorn truck (fixed resource) that he takes to fairs and sporting events.
- He can hire as many workers as he wants
  - The quantity of output produced varies with the number of workers
  - If Xavier hires only 1 worker, his truck will produce 30 buckets of popcorn per day
  - If Xavier hires 2, 3, 4, or 5 workers, his truck will produce 55, 75, 90, and 100 buckets of popcorn per day, respectively

## EXAMPLE 2A: Xavier's Popcorn Production Function

L workers	Q buckets
0	0
1	30
2	55
3	75
4	90
5	100



# Marginal Product

- **Marginal product**
  - Increase in output that arises from an additional unit of input
  - Other inputs constant
  - Slope of the production function
- **Marginal product of labor,  $MPL = \Delta Q / \Delta L$** 
  - If Xavier hires one more worker, his output rises by the marginal product of labor.

## EXAMPLE 2B: Xavier's Total and Marginal Product

	<b>L</b> workers	<b>Q</b> buckets		<b>MPL</b> buckets
	0	0		
$\Delta L = 1$	1	30	$\Delta Q = 30$	30
$\Delta L = 1$	2	55	$\Delta Q = 25$	25
$\Delta L = 1$	3	75	$\Delta Q = 20$	20
$\Delta L = 1$	4	90	$\Delta Q = 15$	15
$\Delta L = 1$	5	100	$\Delta Q = 10$	10



# Diminishing MPL

- **Diminishing marginal product**
  - Marginal product of an input declines as the quantity of the input increases
  - Production function gets flatter as more inputs are being used
  - The slope of the production function decreases
- **“Rational people think at the margin”**
- **Hiring one extra worker**
  - Increases output by MPL
  - Increases costs by the wage paid

## EXAMPLE 2C: Xavier's Popcorn Truck Costs

- Xavier must pay \$200 per day for the truck, regardless of how much popcorn he produces
- The market wage for popcorn makers is \$50 per day
- So, Xavier's costs are related to how much popcorn the truck produces

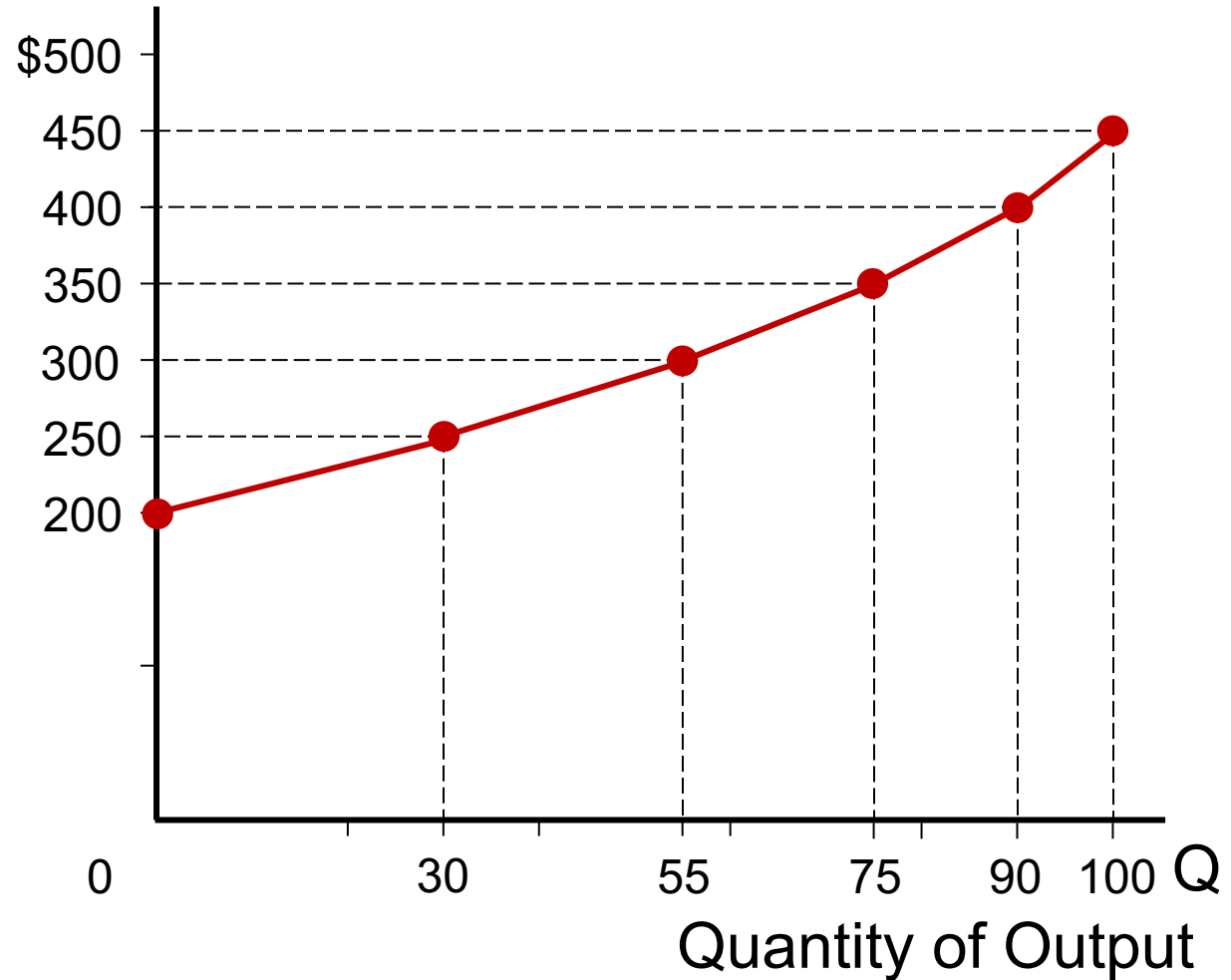
## EXAMPLE 2C: Solutions

L workers	Q buckets	Cost of the truck	Cost of labor	Total Cost
0	0	\$200	\$0	\$200
1	30	\$200	\$50	\$250
2	55	\$200	\$100	\$300
3	75	\$200	\$150	\$350
4	90	\$200	\$200	\$400
5	100	\$200	\$250	\$450

## EXAMPLE 2D: Xavier's Total Cost Curve

Q buckets	Total Cost
0	\$200
30	\$250
55	\$300
75	\$350
90	\$400
100	\$450

Total Cost



## Active Learning 2: Diminishing MPL

Number of workers	Output	<i>MPL</i>
0	0	
1	45	45
2	85	40
3	115	30
4	135	20
5	145	10

A. What is the marginal product of the second worker?

**40**

B. What is the marginal product of the fourth worker?

**20**

C. Does this production function exhibit diminishing marginal returns?

**Yes**

# The Various Measures of Cost

- Total cost,  $TC = FC + VC$ 
  - Total cost of producing a given amount of output
- Fixed costs,  $FC$ 
  - Do not vary with the quantity of output produced
  - Incur even if production is zero
- Variable costs,  $VC$ 
  - Vary with the quantity of output produced

## EXAMPLE 3: Angel's Knitted Scarves Business

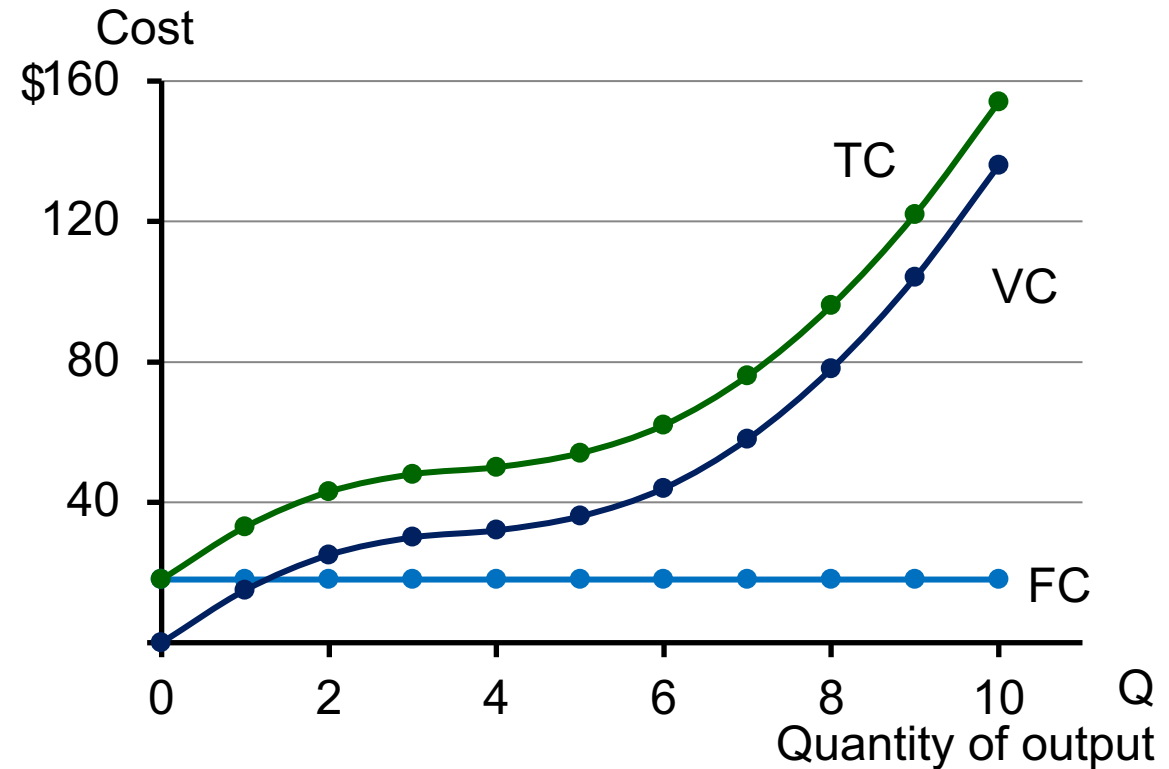
Q	FC	VC	TC
0	18	0	18
1	18	15	33
2	18	25	43
3	18	30	48
4	18	32	50
5	18	36	54
6	18	44	62
7	18	58	76
8	18	78	96
9	18	104	122
10	18	136	154

Angel loves to knit scarves:

- Angel paid \$18 for two pairs of knitting needles
- To produce more scarves, Angel needs more yarn and more workers

## EXAMPLE 3A: Angel's **FC**, **VC**, and **TC** curves

Q	FC	VC	TC
0	18	0	18
1	18	15	33
2	18	25	43
3	18	30	48
4	18	32	50
5	18	36	54
6	18	44	62
7	18	58	76
8	18	78	96
9	18	104	122
10	18	136	154



The **TC** and **VC** curves are parallel  
The **FC** curve is a horizontal line



# Average and Marginal Cost

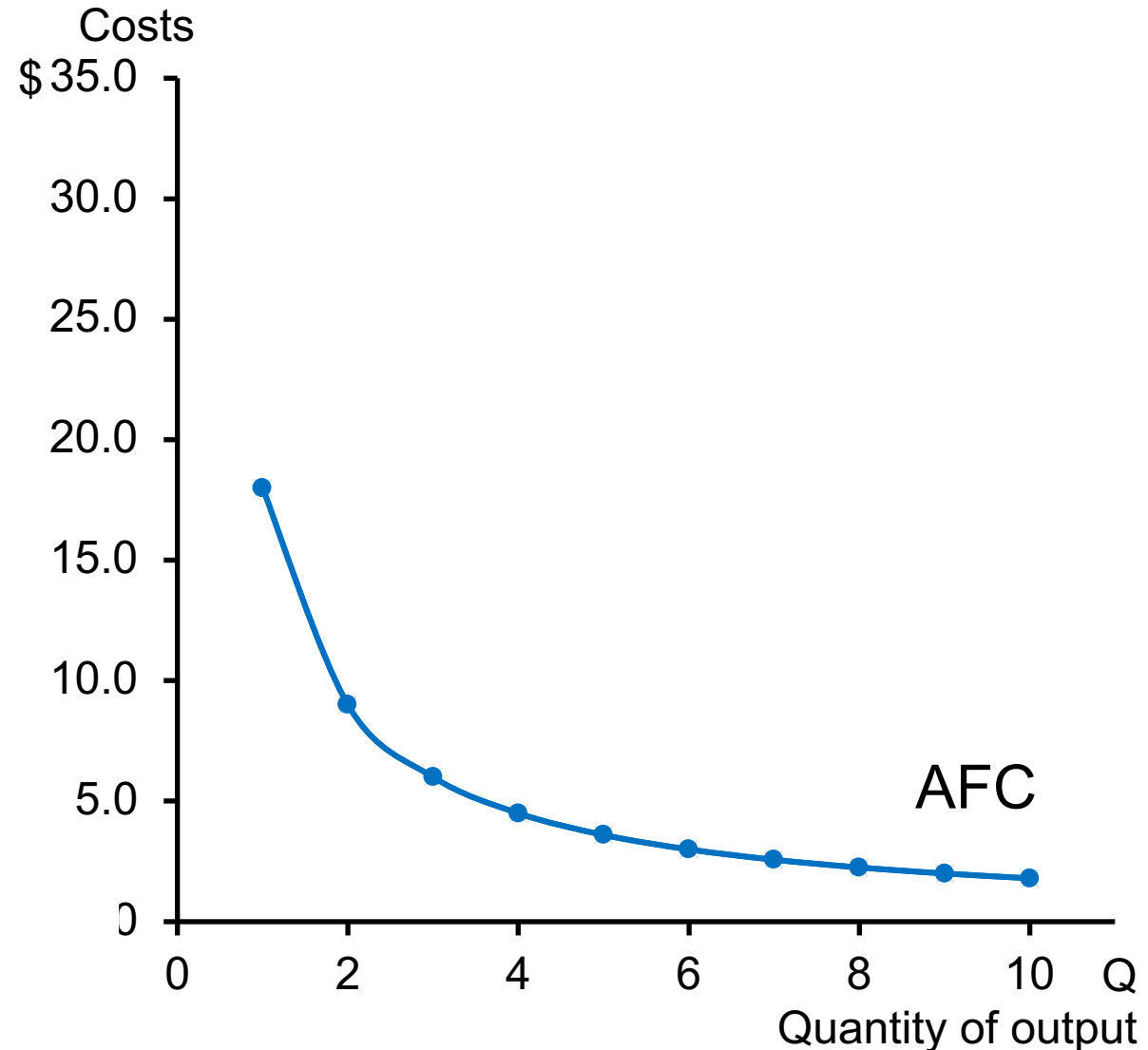
- Average fixed cost,  **$AFC = FC / Q$**
- Average variable cost,  **$AVC = VC / Q$**
- Average total cost,  
 **$ATC = TC / Q = AFC + AVC$** 
  - The cost of the typical unit produced
  - Total cost divided by the quantity of output
- Marginal cost,  **$MC = \Delta TC / \Delta Q$** 
  - The increase in total cost that arises from an extra unit of production

## EXAMPLE 3B: Angel's Average and Marginal Cost

Q	FC	VC	TC	AFC	AVC	ATC	MC
0	\$18	\$0	\$18	-	-	-	
1	18	15	33	\$18.0	\$15.0	\$33.0	\$15.0
2	18	25	43	9.0	12.5	21.5	10.0
3	18	30	48	6.0	10.0	16.0	5.0
4	18	32	50	4.5	8.0	12.5	2.0
5	18	36	54	3.6	7.2	10.8	4.0
6	18	44	62	3.0	7.3	10.3	8.0
7	18	58	76	2.6	8.3	10.9	14.0
8	18	78	96	2.3	9.8	12.0	20.0
9	18	104	122	2.0	11.6	13.6	26.0
10	18	136	154	1.8	13.6	15.4	32.0

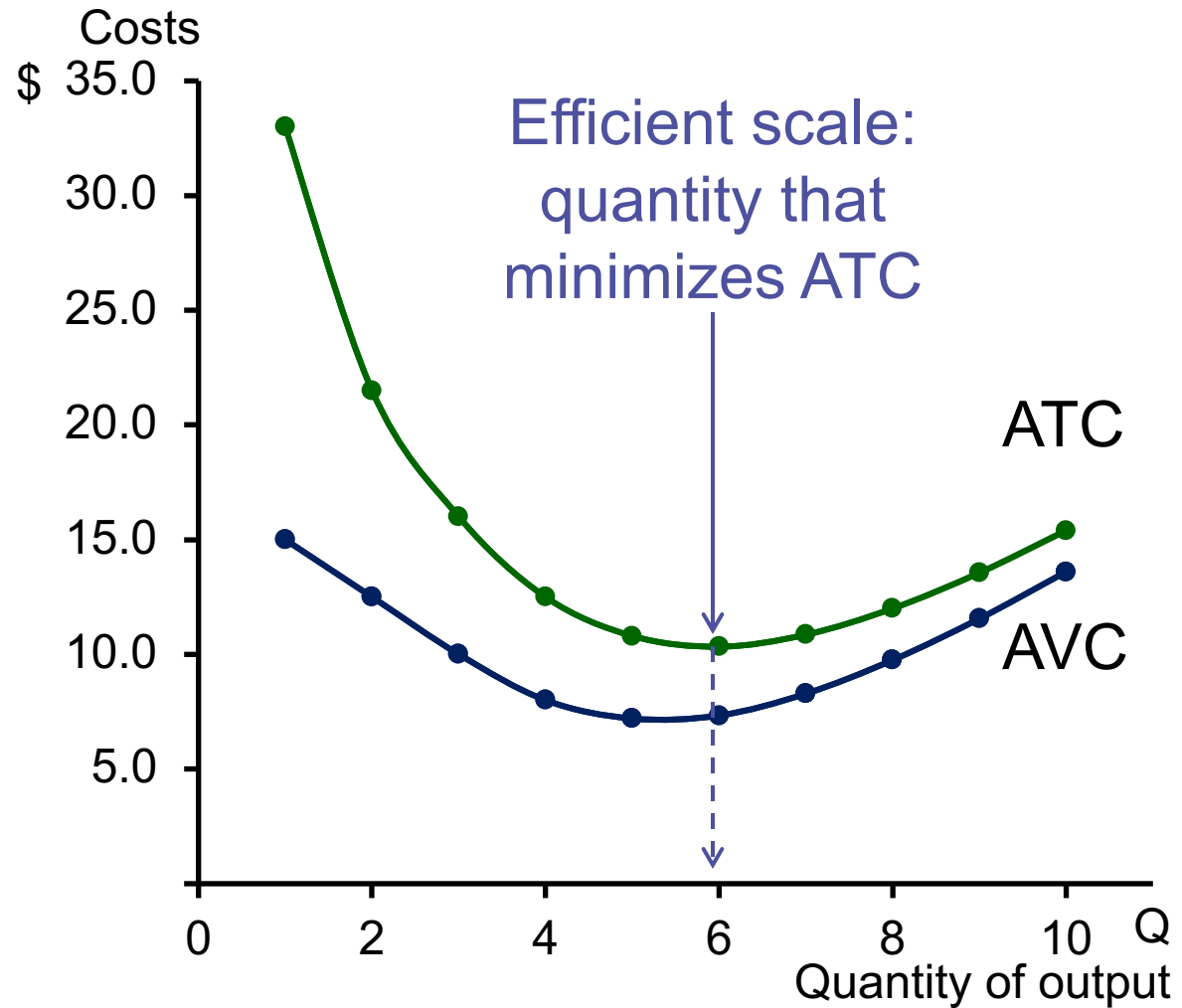
## EXAMPLE 3C: Angel's **AFC** curve

Q	FC	AFC
0	18	-
1	18	18.0
2	18	9.0
3	18	6.0
4	18	4.5
5	18	3.6
6	18	3.0
7	18	2.6
8	18	2.3
9	18	2.0
10	18	1.8



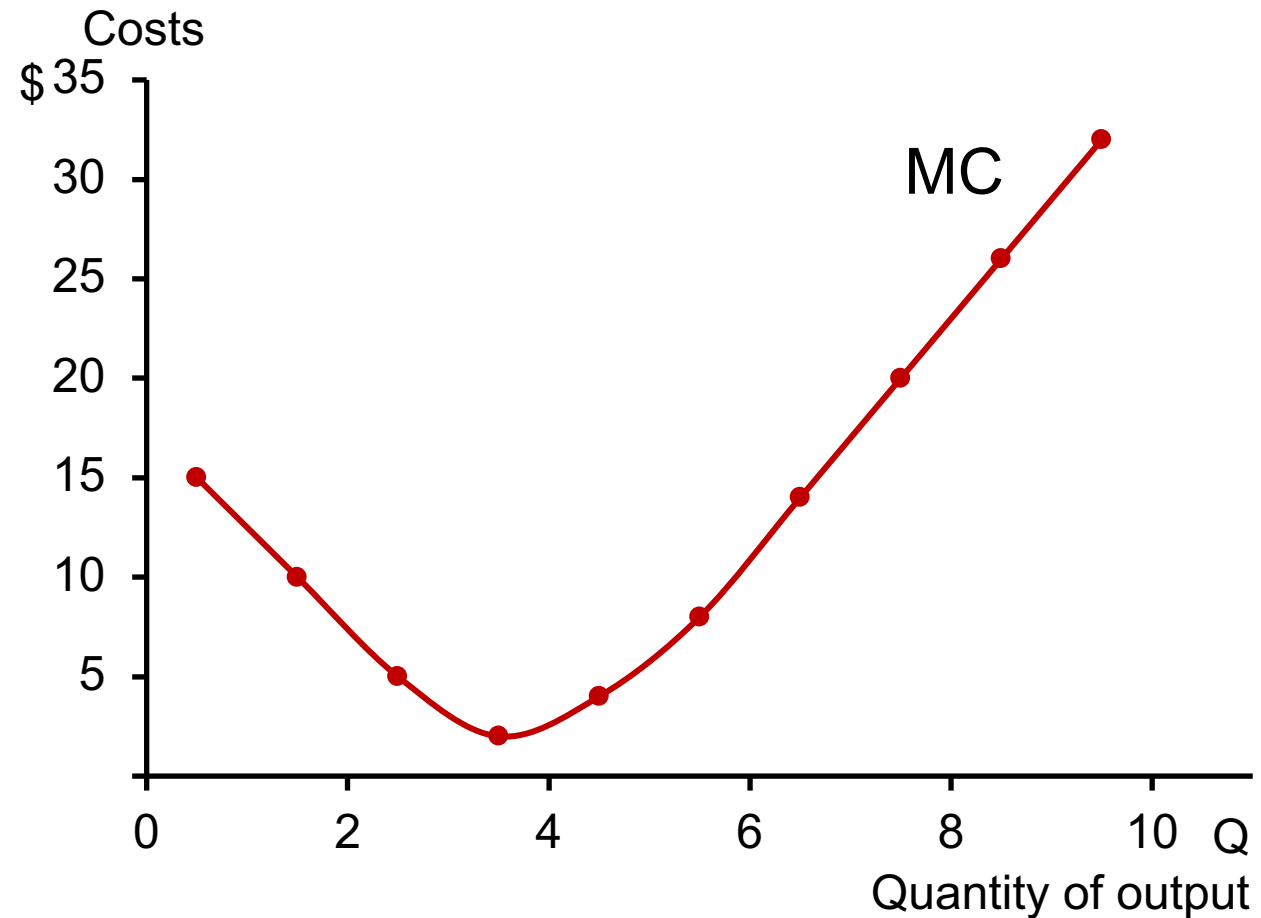
## EXAMPLE 3C: Angel's **AVC** and **ATC** curves

Q	VC	TC	AVC	ATC
0	\$0	\$18	-	-
1	15	33	15.0	33.0
2	25	43	12.5	21.5
3	30	48	10.0	16.0
4	32	50	8.0	12.5
5	36	54	7.2	10.8
6	44	62	7.3	10.3
7	58	76	8.3	10.9
8	78	96	9.8	12.0
9	104	122	11.6	13.6
10	136	154	13.6	15.4

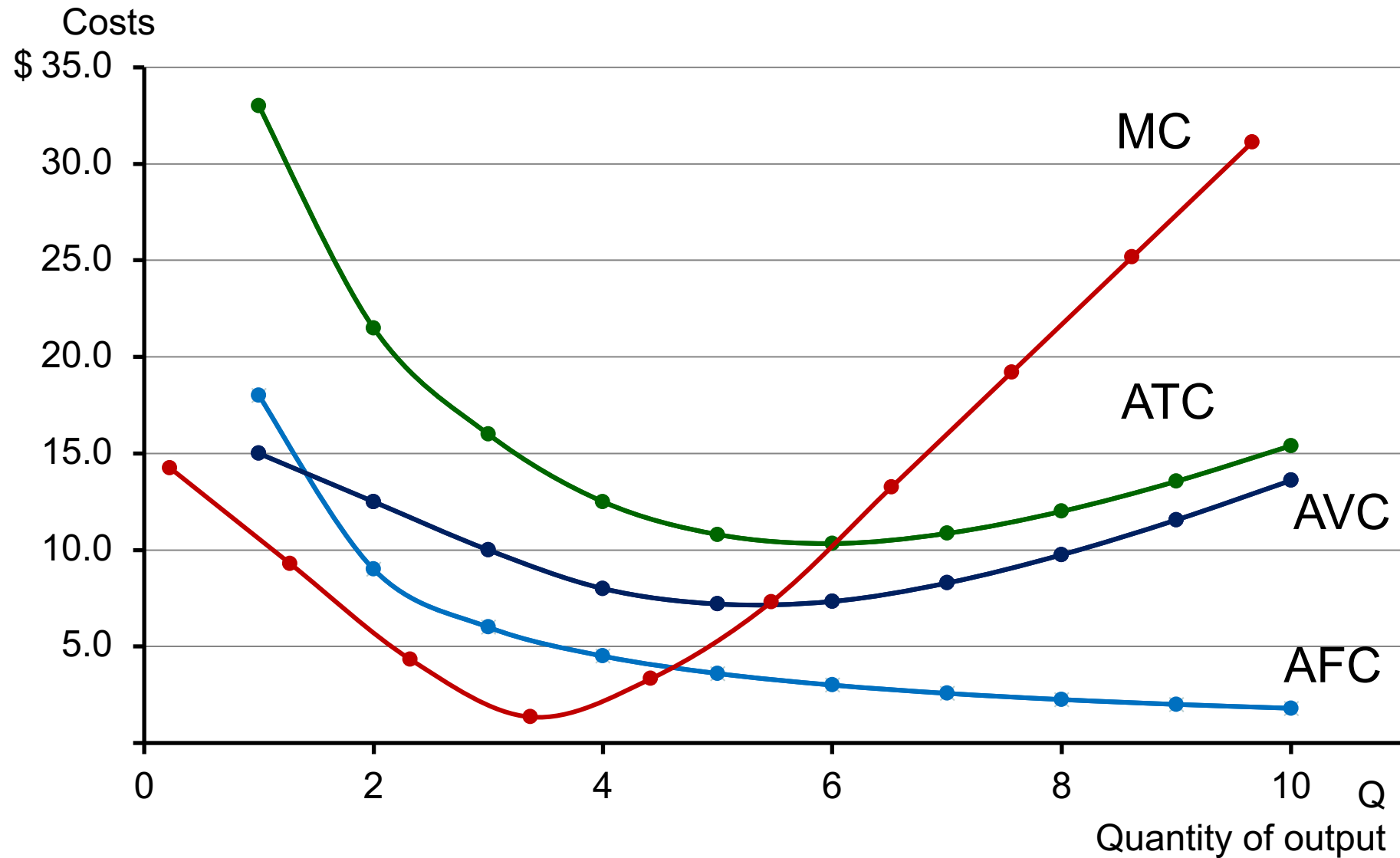


## EXAMPLE 3C: Angel's Marginal Cost Curve

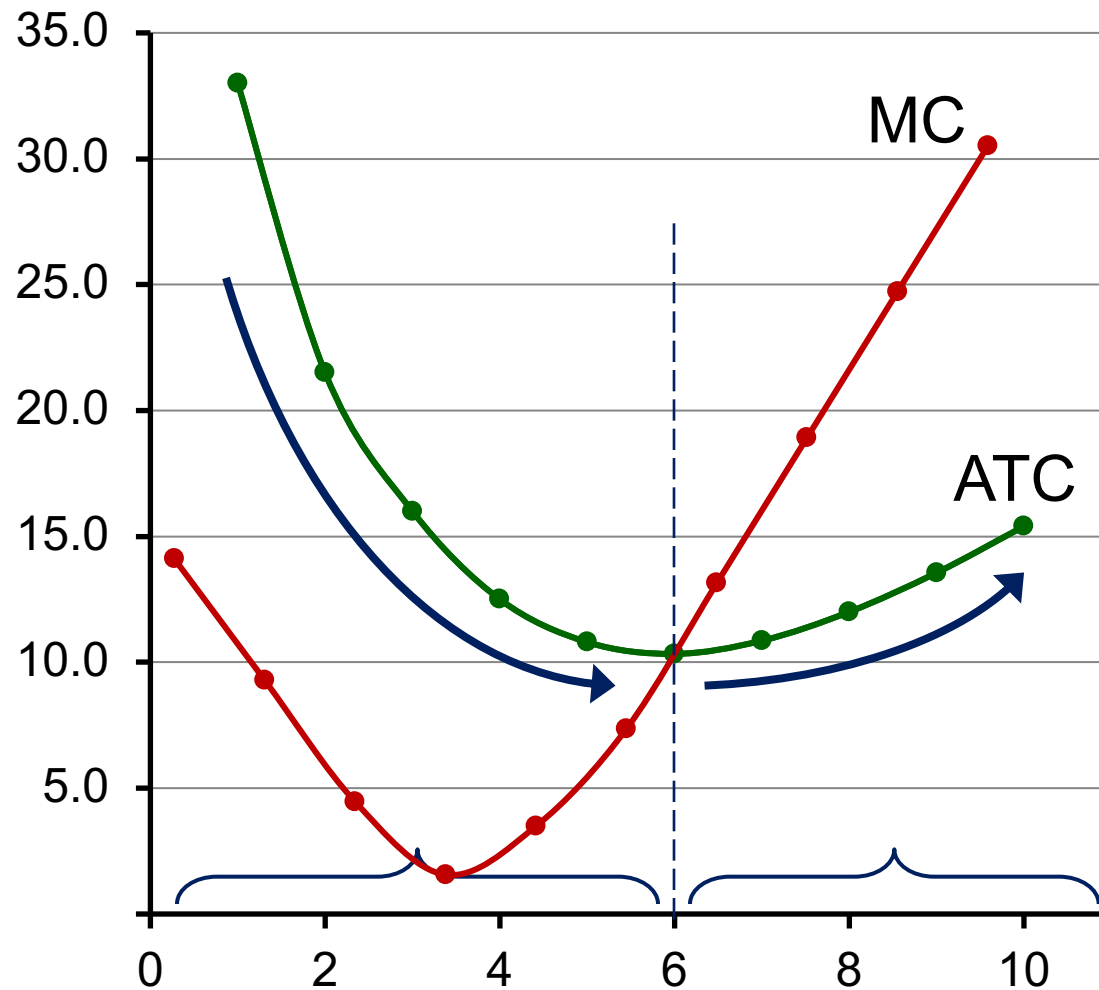
Q	TC	MC
0	\$18	
1	33	\$15.0
2	43	10.0
3	48	5.0
4	50	2.0
5	54	4.0
6	62	8.0
7	76	14.0
8	96	20.0
9	122	26.0
10	154	32.0



## EXAMPLE 3C: Angel's Knitting Cost Curves



## EXAMPLE 3D: Angel's **ATC** and **MC** curves



- When  $MC < ATC$ ,  $ATC$  is falling.
- When  $MC > ATC$ ,  $ATC$  is rising.
- The  $MC$  curve crosses the  $ATC$  curve at the  $ATC$  curve's minimum.

# Active Learning 3: Calculating costs

Fill in the blank spaces of this table.

Q	VC	TC	AFC	AVC	ATC	MC
0		\$50	n/a	n/a	n/a	
1	10			\$10	\$60.00	\$10
2	30	80				
3			16.67	20	36.67	30
4	100	150	12.50		37.50	
5	150			30		
6	210	260	8.33	35	43.33	60



# Active Learning 3: Answers

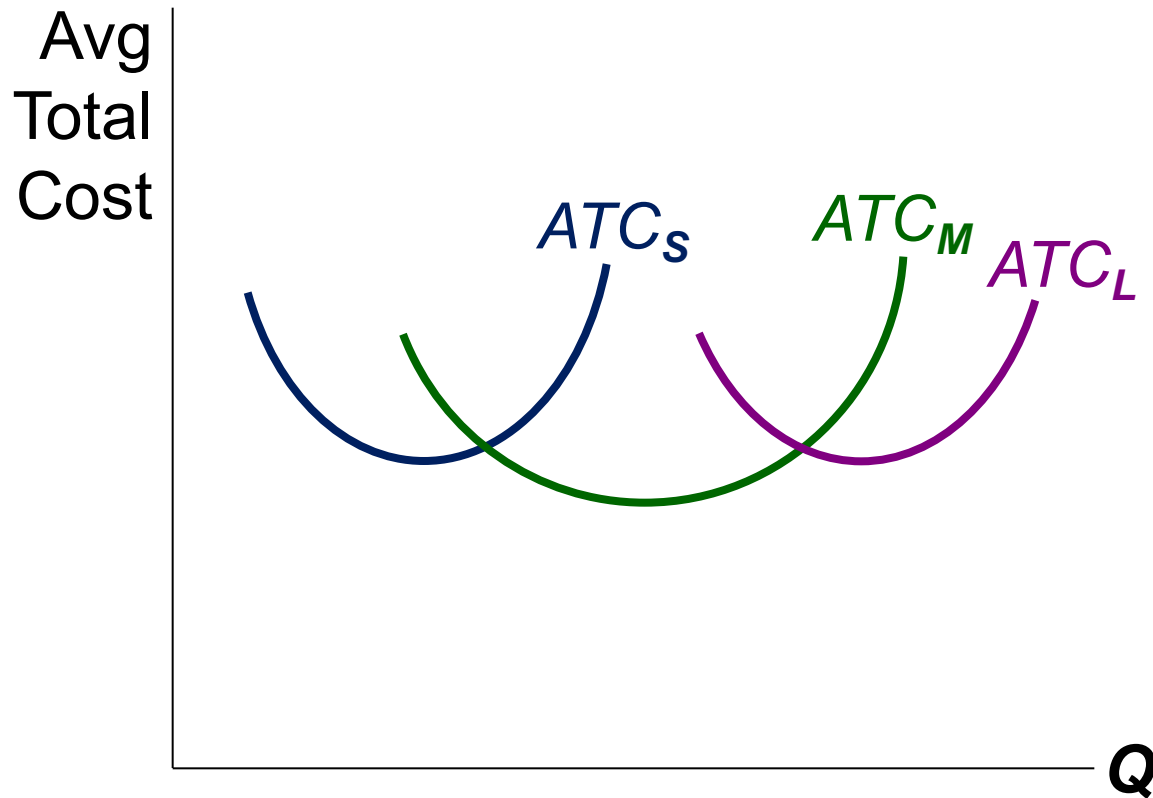
First, deduce  $FC = \$50$  and use  $FC + VC = TC$ .

Q	VC	TC	AFC	AVC	ATC	MC
0	\$0	\$50	n/a	n/a	n/a	
1	10	60	\$50.00	\$10	\$60.00	\$10
2	30	80	25.00	15	40.00	20
3	60	110	16.67	20	36.67	30
4	100	150	12.50	25	37.50	40
5	150	200	10.00	30	40.00	50
6	210	260	8.33	35	43.33	60

# Costs in the Short Run & Long Run

- Short run, **SR**:
  - Some inputs are fixed (e.g., factories, land)
  - The costs of these inputs are **FC**
- Long run, **LR**:
  - All inputs are variable (e.g., firms can build more factories or sell existing ones)
- In the long run
  - **ATC** at any **Q** is the cost per unit using the most efficient mix of inputs for that **Q** (e.g., the factory size with the lowest **ATC**)

# LRATC with 3 factory sizes

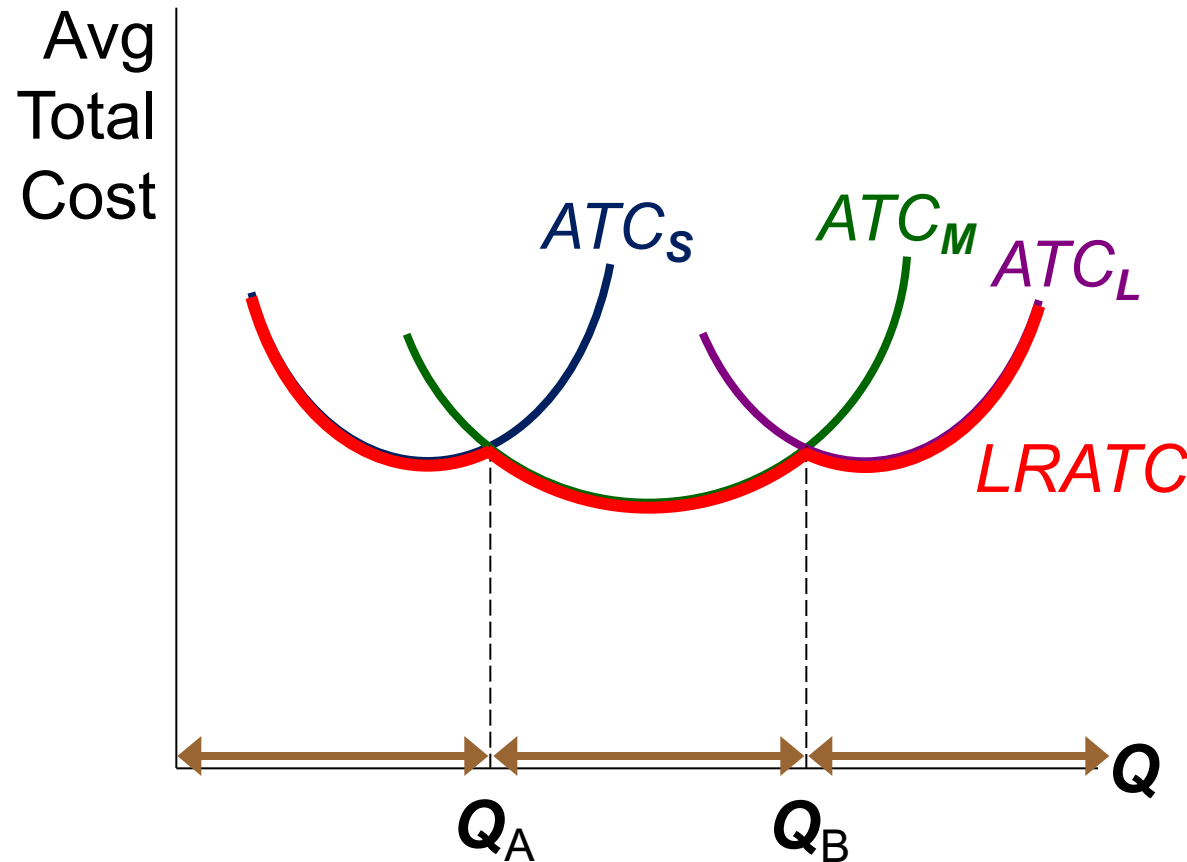


- Firm can choose from three factory sizes: S, M, L.

Each size has its own **SRATC** curve.

- The firm can change to a different factory size in the long run, but not in the short run.

# LRATC with 3 factory sizes



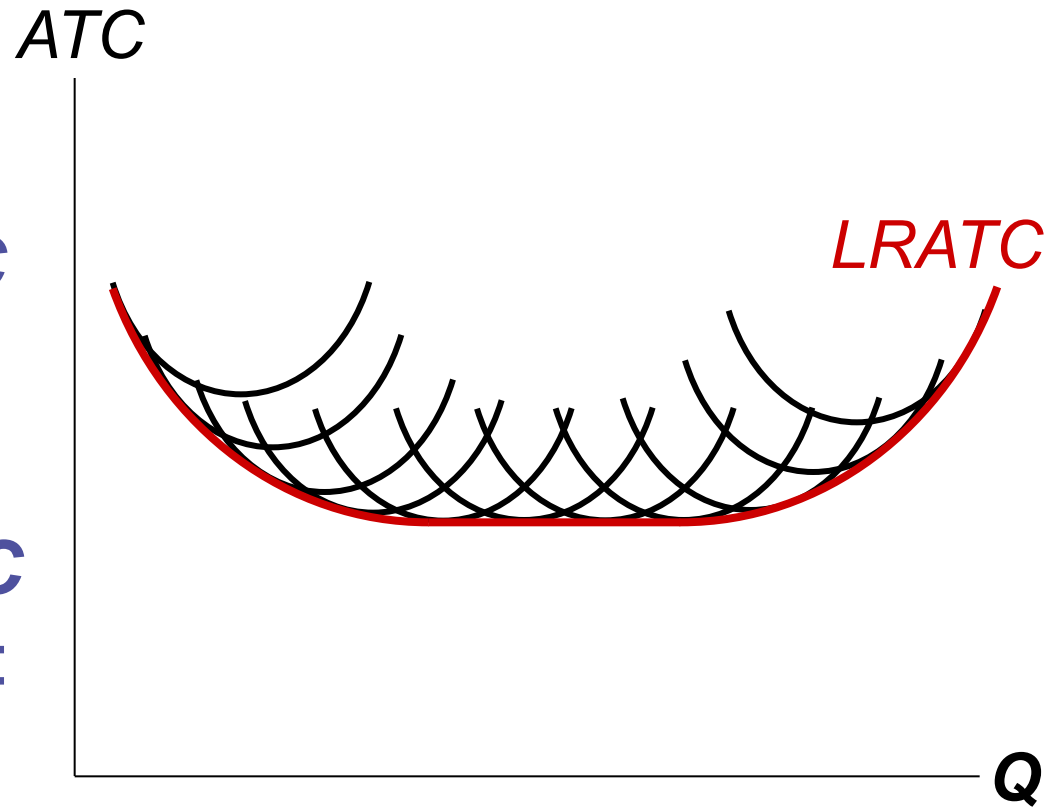
To produce less than  $Q_A$ , firm will choose size S in the long run.

To produce between  $Q_A$  and  $Q_B$ , firm will choose size M in the long run.

To produce more than  $Q_B$ , firm will choose size L in the long run.

# A typical LRATC curve

- In the real world, factories come in many sizes, each with its own **SRATC** curve.
- So, a typical **LRATC** curve looks like this:



# Costs in Short and Long Run – 1

- **Economies of scale**
  - Long-run average total cost falls as the quantity of output increases
    - Increasing specialization among workers
    - More common when  $Q$  is low
- **Constant returns to scale**
  - Long-run average total cost stays the same as the quantity of output changes

# Costs in Short and Long Run – 2

- **Diseconomies of scale**

- Long-run average total cost rises as the quantity of output increases
- Increasing coordination problems in large organizations.
  - E.g., management becomes stretched, can't control costs.
  - More common when  $Q$  is high.

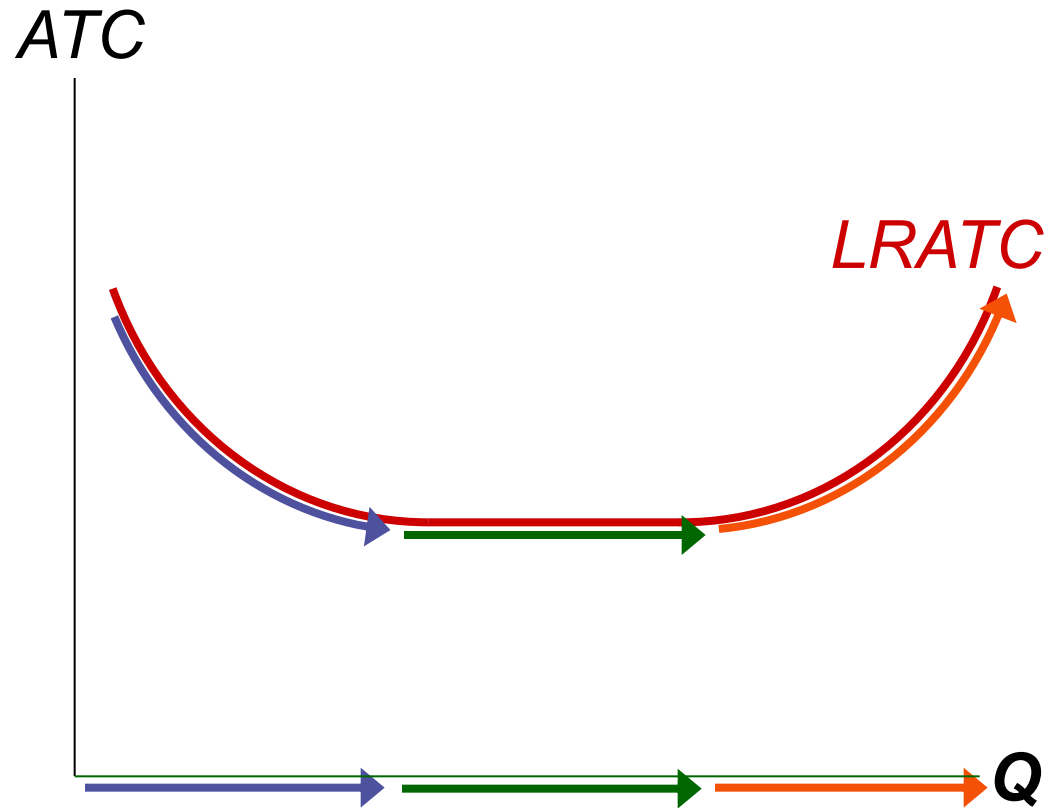
# Economies and diseconomies of scale

Economies of scale:

**ATC** falls as **Q** increases.

Constant returns to scale: **ATC** stays the same as **Q** increases.

Diseconomies of scale: **ATC** rises as **Q** increases.







# THINK-PAIR-SHARE

Your neighbor has a back-yard garden and grows fresh fruit and vegetables to be sold at a local “farmer’s market.” He comments, “I hired a college student who was on summer vacation to help me this summer and my production more than doubled. Next summer, I think I’ll hire three helpers and my output should go up more than three- or fourfold.”

- A. What can explain why the production more than doubled when your neighbor hired a helper?
- B. Will production increase three- or fourfold if your neighbor hires 3 helpers next summer?

# CHAPTER IN A NUTSHELL

- The goal of firms is to **maximize profit**, which equals total revenue minus total cost.
- When analyzing a firm's behavior, it is important to include **all the opportunity costs of production**.
  - **Explicit cost**: wages a firm pays its workers
  - **Implicit cost**: wages the firm owner gives up by working at the firm rather than taking another job
- **Economic profit** takes both explicit and implicit costs into account, whereas accounting profit considers only explicit costs.

# CHAPTER IN A NUTSHELL

- A firm's costs reflect its production process.
  - **Diminishing marginal product**: production function gets flatter as  $Q$  of an input increases
  - Total-cost curve gets steeper as the quantity produced rises.
- Firm's **total costs** = fixed costs + variable costs.
  - **Fixed costs**: do not change when the firm alters the quantity of output produced.
  - **Variable costs**: change when the firm alters the quantity of output produced.

# CHAPTER IN A NUTSHELL

- **Average total cost** is total cost divided by the quantity of output.
- **Marginal cost** is the amount by which total cost rises if output increases by 1 unit.
- Graph average total cost and marginal cost.
  - Marginal cost rises with the quantity of output.
  - Average total cost first falls as output increases and then rises as output increases further.
  - The MC curve always crosses the ATC curve at the minimum of ATC

# CHAPTER IN A NUTSHELL

- A firm's costs often depend on **the time horizon** considered.
  - In particular, many costs are fixed in the short run but variable in the long run.
  - As a result, when the firm changes its level of production, average total cost may rise more in the short run than in the long run.