Practice quiz on Exponents and Logarithms

PUNTOS TOTALES DE 12

1. Re write the number $784 = 2 \times 2 \times 2 \times 2 \times 7 \times 7$ using exponents.

1/1 puntos

1/1 puntos

1/1 puntos

- (2 × 7)⁶
- O (26)(76)
- (2⁴)(7²)
- \bigcirc (16⁴)(49²)

✓ Correcto

For this type of problem, count the number of times each relevant factor appears in the product. That number is the exponent for that factor.

- 2. What is $(x^2 5)^0$?
 - (x²)
 - $(x^2) 5$
 - \bigcirc -4
 - ① 1

✓ Correcto

Any real number (except zero) raised to the zeroith power = 1.

3. Simplify $((x-5)^2)^{-3}$



- (x − 5)
- $(x-5)^{-1}$
- $(x-5)^{-6}$

✓ Correcto

By Rule 2, "Power to a Power," multiply the exponents and get:

$$(x-5)^{(2\times-3)} = (x-5)^{-6}$$

By the definition of negative exponents, this is equal to $(x-5)^6$

- $^{4.} \quad \text{Simplify} (\frac{8^2}{8^7})^2$
 - $\bigcirc 8^{-1}$
 - \odot 8⁻¹⁰
 - $\odot 8^{-4}$
 - $\odot 8^{-5}$

✓ Correcto

We can first simplify what is inside the parenthesis to $8^{-5} \mbox{using the Division and Negative Powers Rule.}$

Then apply division and negative powers—the result is the same. $8^4 - e^{-10}$

$$8^4 = 8^{-10}$$

5. $\log 35 = \log 7 + \log x$

1/1 puntos

Solve for x

- ⑤ 5
- O 4
- O 28
- 0.7

✓ Correcto

$$\log(x) = \log 35 - \log 7$$

$$\log(x) = \log\left(\frac{33}{7}\right)$$

By the Quotient Rule $\log x = \log 5$

6. $log_2(x^2 + 5x + 7) = 0$

1/1 puntos

Solve for \boldsymbol{x}

- x = 3
- $\bigcirc x = 2$
- $\bigcirc x = 2 \text{ or } x = 3$

✓ Correcto

We use the property that $b^{\log_b a} = a$

Use both sides as exponent for 2.

$$2^{\log_2 x^2 + 5x + 7} = 2^0$$

$$x^2 + 5x + 7 = 1$$

$$x^2 + 5x + 6 = 0$$

$$(x+3)(x+2) = 0$$

$$x=-3 \; \mathrm{OR}$$

$$x = -2$$

- 7. Simplify $log_2 72 log_2 9$
 - O 4
 - ③ 3
 - O log2 63
 - log₂ 4

✓ Correcto

By the quotient rule, this is $\log_2 \frac{^{'2}}{^{'2}} = \log_2 2^3 = 3$

8. Simplify $\log_3 9 - \log_3 3 + \log_3 5$

- O 8
- ⊚ log₃ 15
- O 15
- log₃ 8

✓ Correcto

By the Quotient and Product Rules, this is $\log_3 \frac{9 \times 5}{3} = \log_3 15$

9. Simplify $\log_2(3^8 \times 5^7)$

- \bigcirc $(5 \times \log_2 3) + (8 \times \log_2 5)$
- $\bigcirc \ 15 \times \log_2 56$
- \bigcirc 56 $\times \log_2 15$
- (8 × log₂ 3) + (7 × log₂ 5)

1/1 puntos

1/1 puntos

1/1 puntos

- 332.19
- O 20
- 500
- 301.03

Incorrecto

Use the change of base formula, $\log_{\alpha} b = \frac{1}{\log_{\alpha} a}$

Where the "old" base is x and the "new" base is a.

$$So \frac{100}{g_{10}(2)} = \frac{100}{0.30103} = 332.19$$

11. A tree is growing taller at a continuous rate. In the past 12 years it has grown from 3 meters to 15 meters. What is its rate of growth per year?

1 / 1 puntos

- 0 10.41%
- O 11.41%
- O 12.41%
- ③ 13.41%

Correcto
$$\frac{n \frac{15}{3}}{12} = 0.1341$$

12. Bacteria can reproduce exponentially if not constrained. Assume a colony grows at a continually compounded rate of 400% per day. How many days before a colony with initial mass of 6.25 X 10-10 grams weights 1000 Kilograms?

1 / 1 puntos

- 0.875 days
- 875 days
- 8.75 days
- 87.5 days

✓ Correcto

$$6.25 \times 10^{-10} \times e^{4t} = 10^6$$

$$4t = \ln \frac{10^6}{6.25 \times 10^{-10}} = 35.00878$$

$$t = \ln \frac{10^6}{25 \times 10^{-10}} = 8.752195$$