

- Electric Circuit: The closed path followed by an electric current.

$$I = \frac{d\phi}{dt} \text{ C/s or Amp}$$

$$P = \frac{dw}{dt}$$

- Electromotive Force: Voltage of an energy source.

$$V = \frac{dw}{dq}$$

$$P = \frac{dw}{dq} \cdot \frac{dq}{dt} = VI$$

$$W = \int_{-\infty}^t P dt J$$

⇒ Current entering +ve terminal → Absorbing
 " leaving " " " → Delivering

- Absorbing Power / Delivering Power

When the current is entering the +ve terminal then the element is absorbing power.

When the current is leaving the +ve terminal then the element is delivering power.

1. Active Elements :

ii When an element is capable of delivering power independently for infinite time is active element.

2. Passive E

ii When an element is having property of internal amplification, it is an active element.

2. Passive Elements :

i When an element is not capable of delivering energy independently then the element is called passive element.
Eg:- Resistor, Inductor, Capacitor, etc.

a. Resistor: Current is directly proportional to applied voltage.

$$\text{b. Capacitor : } i = C \frac{dV}{dt}$$

$$\text{c. Inductor : } V = L \frac{di}{dt}$$

2. Resistor :

$$J = \sigma E \rightarrow \text{Ohm's law 1st form}$$

$J \rightarrow$ current density in amperes per square meter
 $\sigma \Rightarrow$ conductivity of the substance which is constant for each particular substance.

$E \rightarrow$ Electric field along the conducting substance in volts per meter.

$$J = \frac{I}{A}$$

A

$$\frac{I}{A} = \rho \cdot \frac{V}{l}$$

$$\frac{I}{A} = \frac{V \cdot l}{R \cdot A \cdot l}$$

$$I = \frac{V}{R}$$

$$V = IR - \text{Ohm's law 2nd form}$$

$$I = GV \rightarrow \text{Ohm's Law 3rd form}$$

$$G = \frac{I}{V}$$

$$V = R \frac{dQ}{dt} \rightarrow \text{Ohm's law 4th form}$$

2. Capacitor:

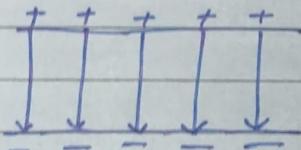


Fig: Electric field lines or lines of force
b/w two charged conductors.

$$E = \frac{F}{Q}$$

Area of the plates as A and charge on the top plate be Q

$$\text{Charge Density} = \frac{Q}{A}$$

Acc. to Gauss's Law

$$Q = \int \int_D \cos \theta dS$$

↓ ↓

→ Increment of surface
Angle b/w D and dS.
Flux Density

$$Q = DA$$

$$D = \epsilon E$$

$$E = \frac{Q}{EA}$$

$$V = Ed$$

$$\boxed{V = \frac{Qd}{EA}}$$

$$U = \frac{1}{2} Q^2$$

↪ elastance \rightarrow reciprocal of Capacitance

~~$c = \frac{Q}{V}$~~

$$\boxed{V = \frac{Q}{C}} \Rightarrow \boxed{D = CV}$$

$$\boxed{C = \frac{\epsilon A}{d}}$$

$$\frac{dq}{dt} = \frac{CdV}{dt}$$

$$i = \frac{C \cdot dV}{dt}$$

$$V = \frac{1}{C} \int_{\infty}^t i dt$$

$$P = V_i$$

$$P = VC \frac{dV}{dt}$$

$$W = \int P dt = \int VC \frac{dV}{dt} dt$$

$$W = \frac{1}{2} CV^2$$

* Linear & Non-Linear Resistors:

When the resistor follows ohm's law it is linear resistor & when the resistor doesn't follow ohm's law it is non-linear resistors.

⇒ Bidirectional \rightarrow Independent of direction of current.

\Rightarrow When $C = \infty$, $\frac{dV}{dt} = 0$
 $\therefore i = 0$

] Steady State \rightarrow open circuit

\Rightarrow Capacitor doesn't allow sudden change in voltage.

$$i = C \frac{dV}{dt}$$

$dt \rightarrow 0$ for sudden change

$i \rightarrow \infty$ \therefore it doesn't allow to change voltage suddenly

• Linear Capacitor:

When capacitance on the capacitor is independent on voltage magnitude then capacitor is called as linear capacitor.

• Non-Linear Capacitor:

When capacitance on the capacitor is dependent on voltage magnitude then capacitor is called as non-linear capacitor.

3) Inductor:

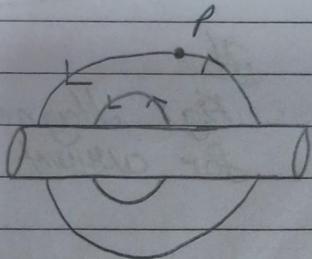
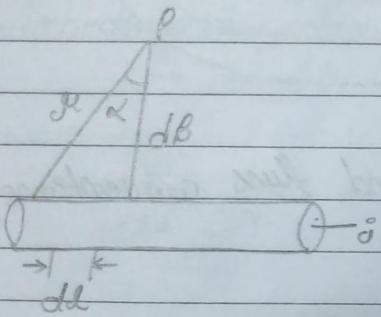


Fig: Identifying quantities which determine the magnetic field at point P.

Force per unit magnetic pole.

$$dB = \frac{\mu i \cos \alpha d\ell}{4\pi a^2} - (j)$$

μ = magnetic permeability

j = current

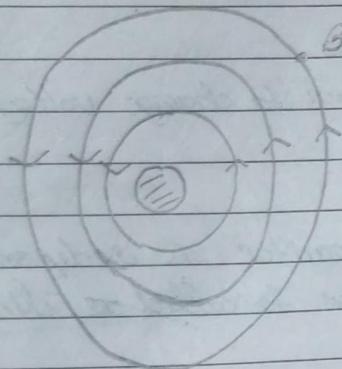


Fig: Cross-section of a current carrying inductor.

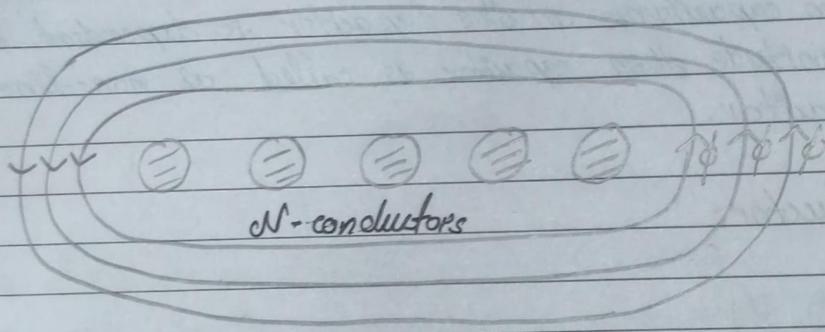


Fig: Magnetic field and flux conventions for current direction.

from (i)

- * The magnetic field density from (i) is constant for a constant distance from the current carrying conductor.

The lines of magnetic field density by the lines of magnetic flux is given by

$$\phi = \int_{\text{ds}} B \cos \theta d\theta - \text{(ii)}$$

The total no. of flux linkage

$$\Psi = \sum_{j=1}^N n_j \phi_j - \text{(iii)}$$

~~N no of conductors when linked together in a magnetic field there'll be flux linkage.~~

Flux linkage is the linking of the magnetic field with the conductors of a coil when the magnetic field passes through the loops of the coil, expressed as a value.

$$\Psi = N \int_s B \cos \theta d\theta - \text{(iv)}$$

According to Faraday's law

$$V = K \frac{d\Psi}{dt} - \text{(v)}$$

$$K = 1$$

$$V = \frac{d\Psi}{dt} - \text{(vi)}$$

$$\Psi = \int_{-\infty}^t V dt - \text{(vii)}$$

$$\Psi = \int_{-\infty}^t V dt - \text{(viii)}$$

$$\Psi = \left[N \int \left(\int \frac{\mu_0 \cos \varphi d\ell}{4\pi a^2} \right) ds \right] i \quad -ix$$

Ψ and i are inductance parameters

$$\Psi = L i \quad -x$$

$L \rightarrow$ Self Inductance \rightarrow Both Ψ and i have same physical parameters

If current i_1 produces flux linkage Ψ_2 in another circuit the parameter is one of the mutual inductance.

$$\Psi_2 = M_{21} i_1 \quad -xi$$

Substitute x in (ii)

Also

$$V = \frac{d(CLf)}{dt}$$

$$V = L \frac{di}{dt}$$

* We can't change current suddenly as $dt \rightarrow 0$

$$\text{Also } V = \frac{di}{dt}$$

$$\text{Also } V \rightarrow \infty$$

* In steady state, inductor is short circuit

$$dt \rightarrow \infty$$

$$V = 0$$

• Linear / Non-Linear Inductance:

When the inductance of the inductor depends on the current magnitude, it is known as non-linear inductor.

when the inductance of the inductor depends on the current magnitude, it is known as ^{does not} linear inductor.

• Types of Resistors:

- i) Fixed Resistors
- ii) Variable Resistors.

fixed resistor



Molded carbon composition

resistor

- (i) Carbon clay composition
- (ii) Metallized type
- (iii) Wire Wound resistor

- Q A resistor has a colour band sequence yellow violet orange and gold. Find the range in which its value must lie so as to satisfy the manufacturer's tolerance.

Ans Yellow $\rightarrow 4$

Violet $\rightarrow 7$

Orange $\rightarrow 10^3$

Gold $\rightarrow \pm 5$

$$(47 \times 10^3) \pm 5\% \\ = 44.65 \times 10^3 - 49.35 \times 10^3 \\ \text{Range} 2350 \Omega$$

1st - 2nd Band 3rd Band 4th Band

Bye	Bill	Black	0	10^0	Gold $\rightarrow \pm 5\%$
Bye	Brown	Brown	1	10^1	Silver $\rightarrow \pm 10\%$
Rasie	Realised	Red	2	10^2	No color (bare) $\rightarrow \pm 20\%$
off	only	orange	3	10^3	
Soal	Yesterday	Yellow	4	10^4	
Cro	Good	Green	5	10^5	
Bristol	Boys	Blue	6	10^6	
Via	Value	Violet	7	10^7	
Creat	Good	Grey	8	10^8	
Western	work	White	9	10^9	

Type of Capacitor: \rightarrow offers low impedance to AC & high impedance to DC

- a Fixed Capacitor
- b Variable Capacitor

Capacitor is used to couple alternating voltage from one circuit to another circuit while at the same time blocking the DC voltage from reaching the next circuit. The capacitor is called as coupling capacitor or blocking capacitor or bypass capacitor.

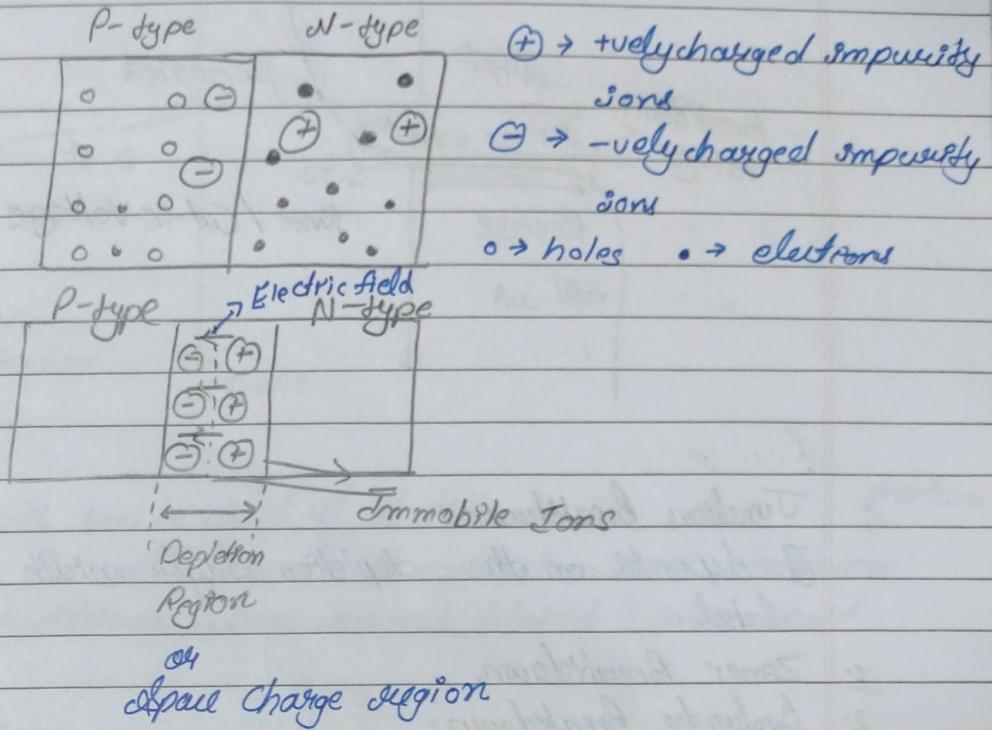
Three types of fixed capacitors:

- i NICA
 \hookrightarrow 5 pF to 10,000 pF
- ii Ceramic
 \hookrightarrow 3 pF to 2 uF
- iii Electrolyte
 \hookrightarrow more than both

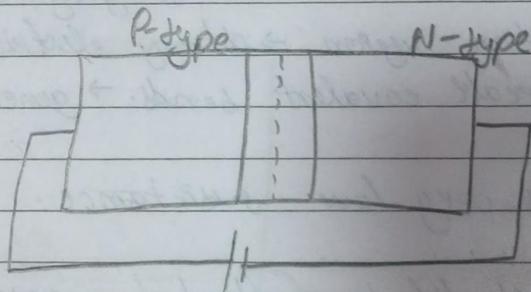
\Rightarrow Capacitance colour code:

- 1st \rightarrow Temp. Coefficient
- 2nd \rightarrow Significant Digits
- 3rd \rightarrow
- 4th \rightarrow
- 5th \rightarrow Tolerance

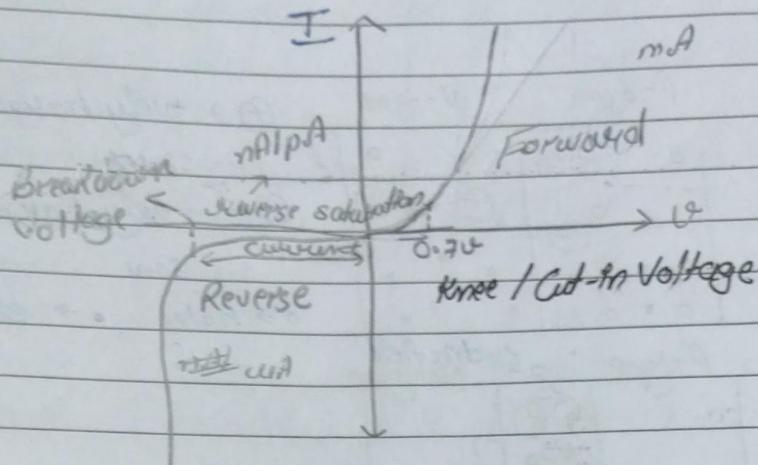
• PN Junction [No external voltage]



• Forward Bias - PN Junction



I-V characteristics of a P-N junction diode:



Junction Breakdown:

It depends on the depletion layer width and the doping level.

- 1: Zener Breakdown
- 2: Avalanche Breakdown.

1: Zener Breakdown:

It occurs when semiconductor is highly doped & we have narrow depletion region \rightarrow strong electric field \rightarrow strong enough to break covalent bonds \rightarrow generate e- hole pair

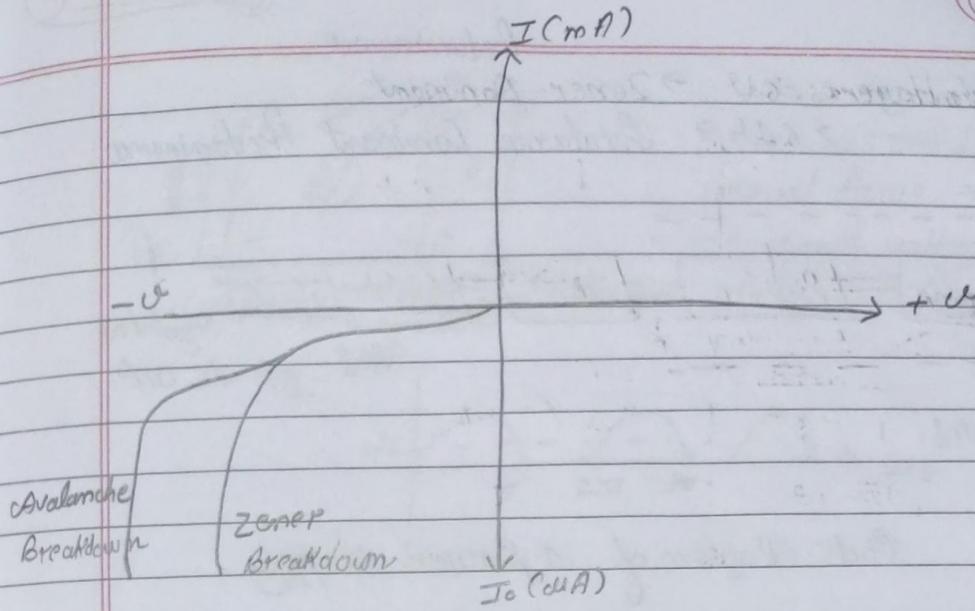
Junction has very low resistance.

2: Avalanche Breakdown : (flood of carriers)

lightly doped \rightarrow large depletion region \rightarrow not strong E^{\rightarrow} \rightarrow can't break covalent bonds.

$\underbrace{\text{high energy}}_{\text{minority carriers}} \leftarrow \text{increase of} \leftarrow$

have ability to break covalent bonds \rightarrow generate carriers accelerated by E^{\rightarrow} \rightarrow more collisions \rightarrow more generation.

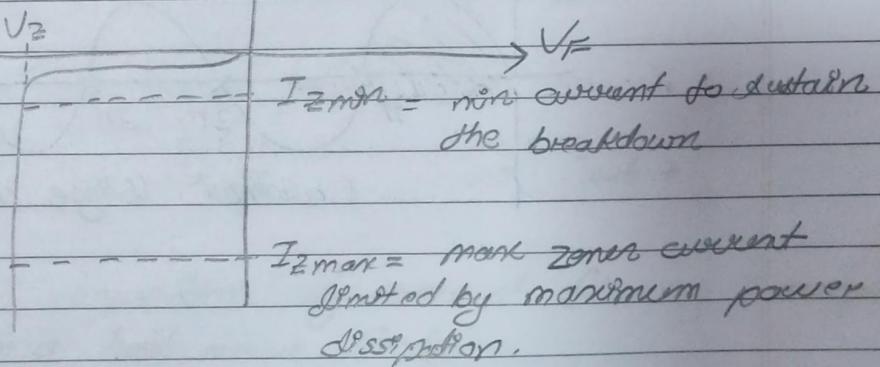


- * Ideal diode can be defined as follows:
 - i When its forward biased it conducts with a resistance
 - ii Infinite resistance when reverse biased \rightarrow open circuit

^{short circuit}

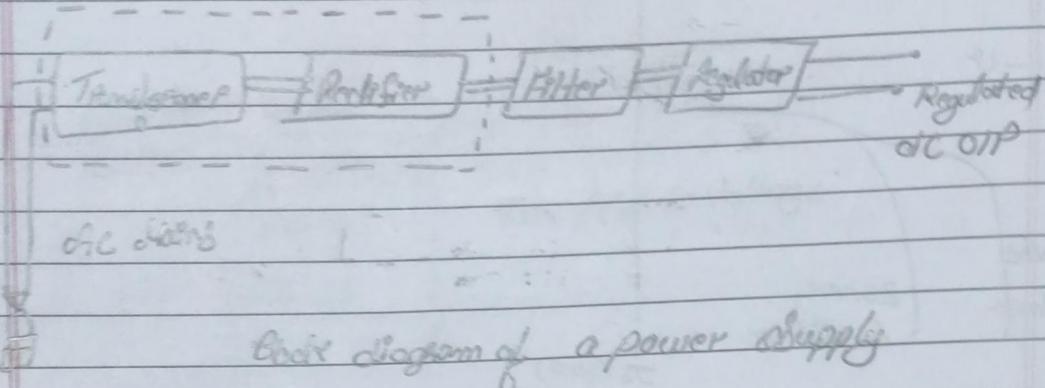
• Zener Diode:

It is a reverse biased heavily doped silicon/germanium P-N junction diode which is operated in the breakdown region where the current is limited by both external resistance.



$I_{Z\text{max}} = \text{max zener current}$
limited by maximum power dissipation.

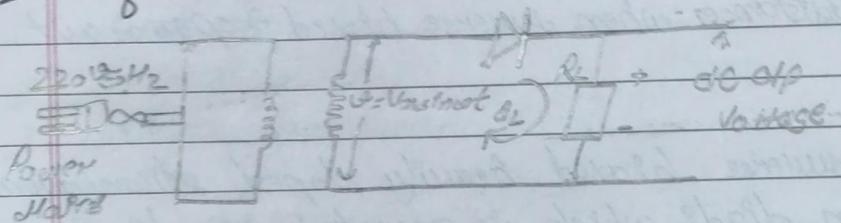
Reverse Voltage $< 6\text{V}$ \rightarrow Zener Dominant
 $> 6\text{V}$ \rightarrow Avalanche Dominant Predominance



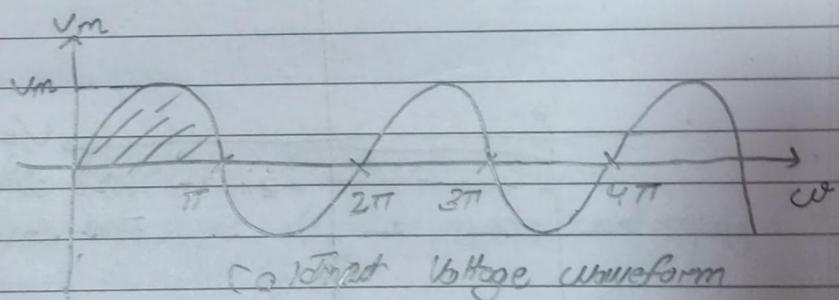
Block diagram of a power supply

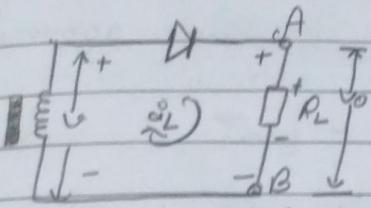
- Rectifiers:

1. Half Wave Rectifier -



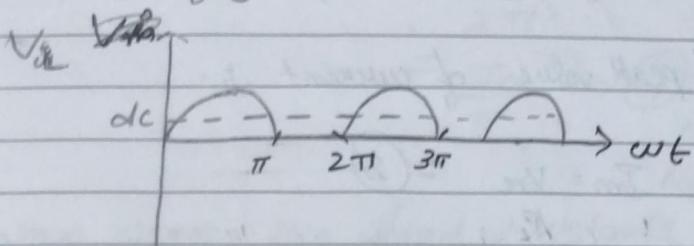
Primary is connected to AC supply \rightarrow induce current in secondary coil.





(a) During +ve half cycle

Diode acts ~~as~~ forward bias \rightarrow current flows \rightarrow low resistance \rightarrow very small voltage drop



During Reverse bias \rightarrow no current \rightarrow no voltage \rightarrow no graph / current.

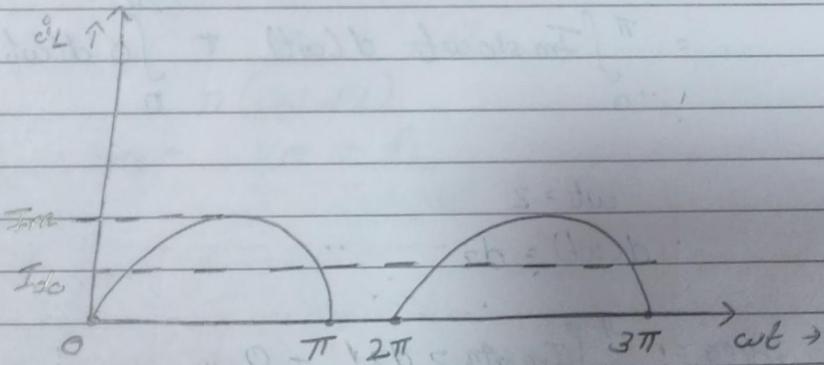
• Peak Inverse Voltage:

It will be the maximum voltage ~~induced in secondary coil~~ withstand during the -ve half cycle of input.

in which the diode must

$$\text{PIV} = V_m \cdot \text{Half cycle}$$

• Output DC Voltage



Key: Waveform of current flowing through R_L in a half wave Rectifier.

$$i_L = I_m \sin \omega t \quad \text{---(1)}$$

for $0 \leq \omega t \leq \pi$

$$i_L = 0$$

for $\pi \leq \omega t \leq 2\pi$

I_m = peak value of current i_L .

$$I_m = V_m / R_L \quad \text{---(2)}$$

To find the dc or average value of current, we can find the net area under the curve over one complete cycle i.e. for 0 to 2π and divide this area by the base i.e. 2π .

We first integrate & then use eqn. (1) and to find the area.

$$\begin{aligned} \text{Area} &= \int_0^{2\pi} i_L d(\omega t) \\ &= \pi \int_0^{2\pi} I_m \sin \omega t d(\omega t) + \int_{\pi}^{2\pi} 0 d(\omega t) \end{aligned}$$

$$\omega t = z$$

$$d(\omega t) = dz$$

$$\begin{aligned} \text{Area} &= \int_0^{\pi} I_m \sin z dz + 0 \\ &= 2 I_m \quad \text{---(3)} \end{aligned}$$

Average value of the load current

$$I_{avg} = I_{dc} = \frac{\text{area}}{\text{base}}$$

$$= \frac{2 Im}{2\pi}$$

$$= \frac{Im}{\pi}$$

$$= \frac{Im}{\pi} - (4) \cdot \text{Assumptions:-}$$

No react. in forward bias
Negl. loss. in sec. winding

DC voltage across the load resistance R_L :

$$V_{dc} = I_{dc} \times R_L = \frac{Im}{\pi} \times R_L - (5)$$

If diode res. isn't negligible & ~~load~~^{diode} resistance is comparable to R_L

$$Im = \frac{Vm}{R_L} \Rightarrow Im = \frac{Vm}{C_d + R_L}$$

$$V_{dc} = \frac{Im}{\pi} \times R_L$$

$$= \frac{Vm}{\pi(C_d + R_L)} \times R_L$$

$$V_{dc} = \frac{Vm}{\pi} \times \frac{R_L}{(C_d + R_L)}$$

$$= \frac{Vm R_L}{\pi(C_d + R_L)} = \frac{Vm}{\pi(1 + \frac{C_d}{R_L})}$$

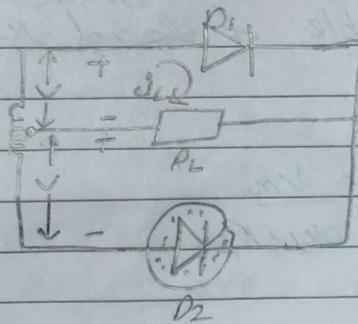
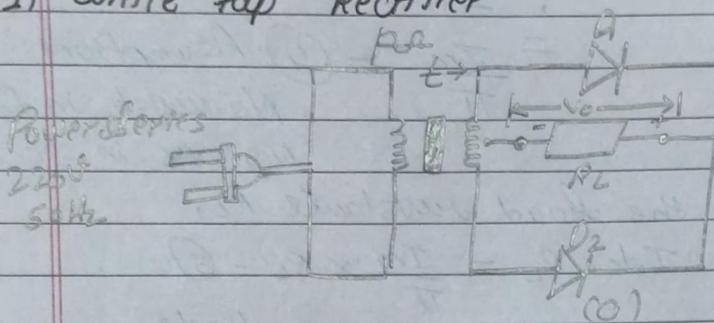
$$= \frac{Vm}{\pi} \left[\text{if } C_d \ll R_L \right]$$

• Full-Wave Rectifier:

(1) Centre tap Rectifier

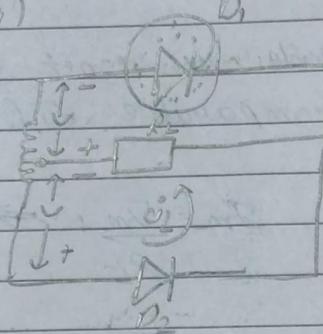
(2) Full Bridge Rectifier

(1) Centre tap Rectifier



(b)

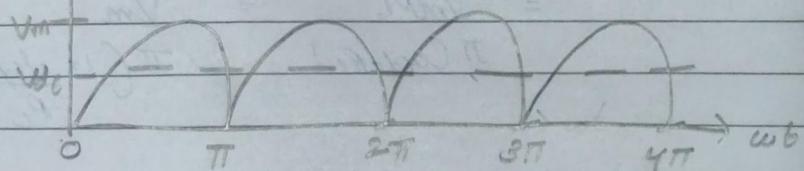
+ve half cycle



(c)

-ve half cycle

v_o



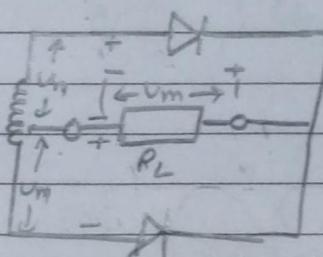
During the +ve half cycle of secondary voltage the diode O_1 is forward biased and O_2 is reverse biased.

The current flows through the diode O_1 , load resistor R_L and the upper half of the winding as shown in the figure no.(b).

During the -ve half cycle diode O_2 is forward biased and O_1 is reverse biased. Then O_2 will conduct.

The load resistor current in (b) & (c) is same.

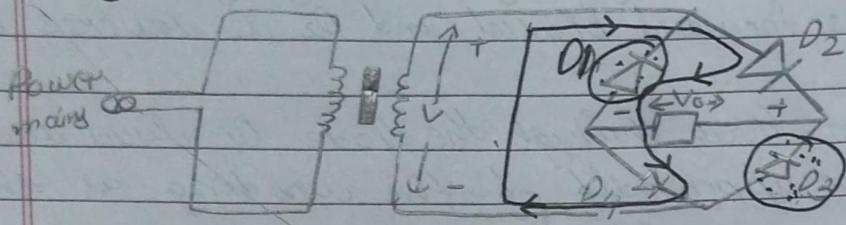
PIV for Center Tap:



$$\text{PIV} = 2V_m$$

The reverse voltage that appears across the non-conducting diode is the summation of the voltage across the load resistor R_L .

2: Bridge wave Rectifier:

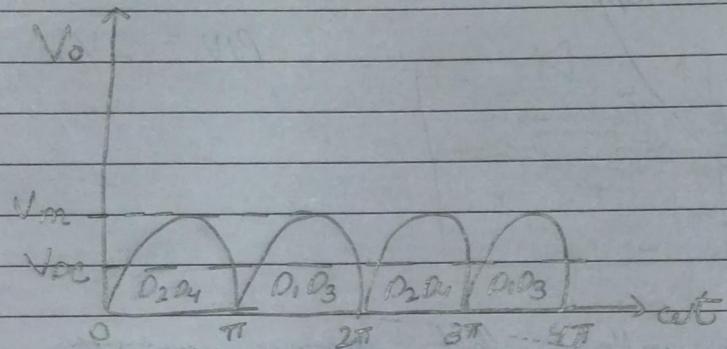


Positive Half Cycle $D_2 \& D_4 \rightarrow$ forward bias \rightarrow Conduct

$D_1 \& D_3 \rightarrow$ Reverse Bias \rightarrow Do not conduct

Negative Half Cycle $D_1 \& D_3 \rightarrow$ Reverse bias \rightarrow Do not conduct

$D_2 \& D_4 \rightarrow$ forward bias \rightarrow Conduct



PIV: V_m

- * V_m is the max. voltage across secondary winding in bridge wave & V_m is the max. voltage across half the secondary winding in centre tap.

- Output dc voltage in voltage rectifiers:

$$V_{dc} = \frac{2 V_m}{\pi}$$

The output voltage of a full-wave rectifier is described as:

$$V_o = V_m \sin \omega t \quad 0 \leq \omega t \leq \pi \\ = -V_m \sin \omega t \quad \pi \leq \omega t \leq 2\pi$$

The average or the dc value of voltage is

$$V_{dc} = \frac{1}{2\pi} \int_0^{2\pi} V_o d(\omega t)$$

$$= \frac{1}{2\pi} \int_0^{\pi} V_m \sin \omega t d(\omega t) + \int_{\pi}^{2\pi} V_m \sin \omega t d(\omega t)$$

$$= \frac{1}{2\pi} V_m \left[\int_0^{\pi} \sin \omega t dt - \int_{\pi}^{2\pi} \sin \omega t dt \right]$$

~~$$= \frac{1}{2\pi} - \cos \omega t + [\cos \omega t]_{\pi}^{2\pi}$$~~

$$= (+2+2) \frac{V_m}{2\pi}$$

$$= \frac{2V_m}{\pi}$$

Ripple Factor:

Ripple factor is a measure of purity of dc output of a rectifier

$\text{Rf} = \frac{\text{rms value of components of wave}}{\text{average or dc value}}$

- Rectification efficiency:

It tells us what percentage of total input AC power is converted into DC output power.

$$\eta = \frac{\text{DC power delivered to load}}{\text{AC input power from Transformer } (T_x) \text{ secondary}}$$

$$= \frac{P_{dc}}{P_{ac}}$$

- Performance of half-wave rectifiers:

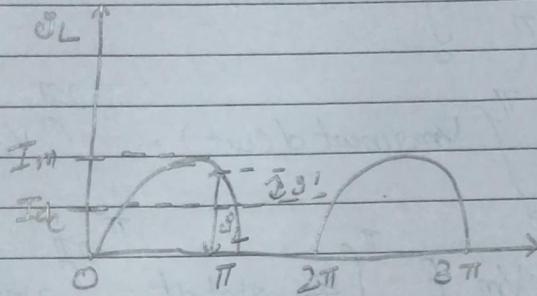


Fig Half-Wave Rectified Current value.

The instantaneous AC component of current is the difference b/w instantaneous total current & DC current i.e.

$$i' = i_L - i_{dc}$$

$$i_L = I_m \sin \omega t \text{ for } 0 \leq \omega t \leq \pi$$

0 for $\pi \leq \omega t \leq 2\pi$

⇒ RMS value of current -

The rms or effective value of the current flowing through the load is given by,

$$I_{\text{rms}} = \sqrt{\frac{1}{2\pi} \int_0^{2\pi} j_L^2 dt}$$

$$= \frac{I_m}{\sqrt{2\pi}} \sqrt{\int_0^\pi 1 - \cos 2wt \frac{dt}{2}}$$

$$= \frac{I_m}{\sqrt{2\pi}} \sqrt{\frac{\pi}{2} - \left[\frac{\sin wt}{2} \right]_0^\pi}$$

$$= \frac{I_m}{2}$$

$$j' = j_L - j_{dc}$$

The sum value of ac component.

$$I'_{\text{rms}} = \sqrt{\frac{1}{2\pi} \int_0^{2\pi} (j_L - j_{dc})^2 dt}$$

$$I'_{\text{rms}} = \sqrt{I_{\text{rms}}^2 - I_{dc}^2}$$

$$\mathcal{H} = \frac{I'_{\text{rms}}}{I_{dc}}$$

$$= \sqrt{I_{\text{rms}}^2 - I_{dc}^2}$$

$$= \sqrt{\frac{I_{\text{rms}}^2}{I_{dc}} - 1}$$

$$= \sqrt{(1.57)^2 - 1}$$

$$\boxed{j_{dc} = 1.21}$$

- Rectification efficiency of half-wave rectifier:

The dc power delivered to the load,

$$P_{dc} = I^2 R_L = \left(\frac{I_m}{\pi}\right)^2 R_L$$

The total ac input power is

$$\begin{aligned} P_{ac} &= I_{rms}^2 (C_0 d + R_L) \\ &= \left(\frac{I_m}{2}\right)^2 (C_0 d + R_L) \end{aligned}$$

$$\text{So } \eta = \frac{P_{dc}}{P_{ac}} = \left(\frac{I_m}{\pi}\right)^2 \times \left(\frac{2}{I_m}\right)^2 \times \frac{R_L}{C_0 d + R_L}$$

$$= \frac{4}{\pi} \frac{\times 100\%}{(1 + \frac{R_L}{C_0 d})}$$

$$= \frac{90\%}{\pi} \frac{40.6\%}{1 + \frac{R_L}{C_0 d}}$$

- Performance of full-wave rectifier.

RMS value of current

~~$$I_{rms} = \frac{1}{\sqrt{2\pi}} \sqrt{\int_0^{\pi} I_m^2 \cos^2 \omega t + \int_0^{\pi} I_m^2 \sin^2 \omega t}$$~~

~~$$= \frac{I_m \times \sqrt{2}}{\sqrt{2\pi}} \sqrt{\int_0^{\pi} \cos^2 \omega t}$$~~

~~$$= \frac{I_m}{\sqrt{\pi}} \sqrt{\pi - \sin 2\omega t}$$~~

~~$$= \frac{I_m}{\sqrt{2}} \cdot \frac{I_m}{\sqrt{2}}$$~~

RMS value of current

$$\begin{aligned} I_{\text{rms}} &= \frac{1}{\sqrt{2\pi}} \int_0^{\pi} I_m^2 \sin^2 \omega t \\ &= \frac{I_m}{\sqrt{2\pi}} \times \sqrt{\pi} \\ &= \frac{I_m}{\sqrt{2}} \end{aligned}$$

$$\begin{aligned} i' &= i_1 - i_{dc} ; i_{dc} = \frac{2I_m}{\pi} \\ I'_{\text{rms}} &= \sqrt{I'^2_{\text{rms}} - I_{dc}^2} = \sqrt{I^2_{\text{rms}} - \frac{4I_m^2}{\pi^2}} \end{aligned}$$

$$\begin{aligned} \mu &= \frac{I'_{\text{rms}}}{I_{dc}} \\ &= \sqrt{\frac{I^2_{\text{rms}} - 1}{I_{dc}}} \\ &= \sqrt{\left(\frac{I_m}{\sqrt{2}}\right)^2 \times \frac{\pi^2}{4I_m^2} - 1} \\ &= \sqrt{\frac{\pi^2}{8} - 1} \\ &= 0.482 \end{aligned}$$

\Rightarrow Rectification efficiency:

$$P_{dc} = I^2_{dc} R_L = \left(\frac{2I_m}{\pi}\right)^2 R_L$$

$$\begin{aligned} \text{Total ac Power} &= I^2_{\text{rms}} (\text{ac load } P_L) \\ &= \frac{I_m^2}{2} \text{ ac load } P_L \end{aligned}$$

$$\begin{aligned} \eta &= \frac{\frac{4I_m^2}{\pi^2} \times R_L \times 100}{\frac{I_m^2}{2} (\text{ac load } P_L)} = \frac{8}{\pi^2} \times 100 \times \frac{1}{\frac{\text{ac load}}{R_L} + 1} \\ &= 81.2\% \end{aligned}$$

$$1 + \frac{I_{dc}}{R_L}$$

• Comparison of different rectifiers

Half-Wave Rectifier

Full-Wave Rectifiers

1 Centre tap

2 Full Wave

1: No. of
diodes

1

2

4

2: Tx No
necessary

Yes No

3: Peak V_m 2V_m V_m
Sec. Volt

4: Peak $\frac{V_m}{2R_d + R_L}$ $\frac{V_m}{R_d + R_L}$ $\frac{V_m}{4R_d + R_L}$
load current (A) (Jm)

5: I_{avg} $\frac{I_m}{2}$ $\frac{3I_m}{\sqrt{2}}$ $\frac{I_m}{\sqrt{2}}$

6: I_{dc} $\frac{I_m}{\pi}$ $\frac{2I_m}{\pi}$ $\frac{2I_m}{\pi}$

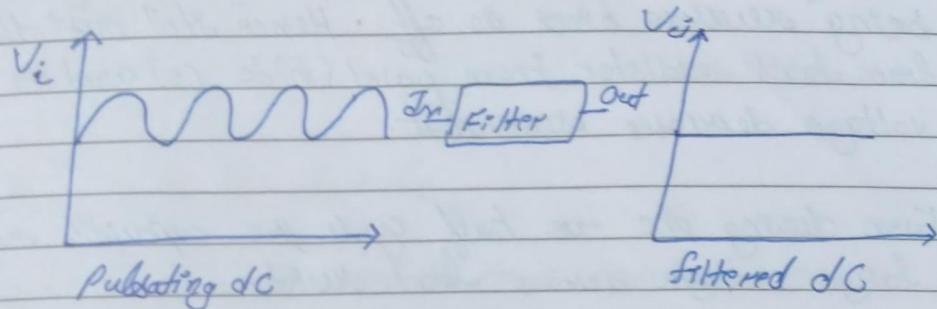
7: R 1.21 0.482 0.482

8: η 40-61% 81-21% 81-2%

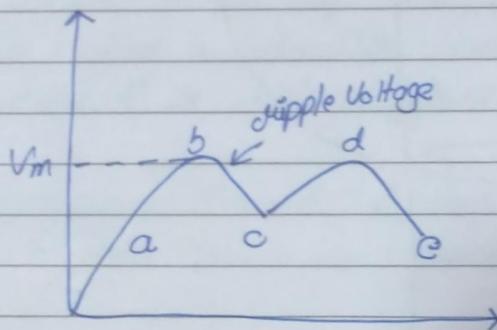
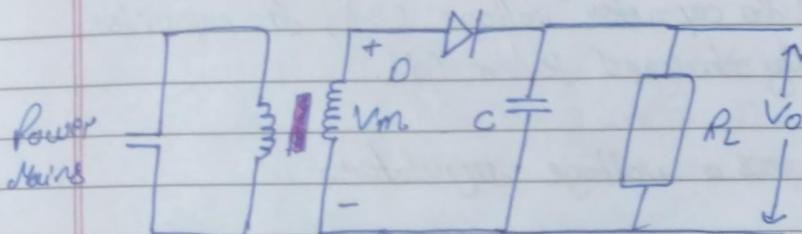
Transformer may be used for isolation even if not required for stepping up or down the input ac.

- Filters:

To minimise the ripple content.

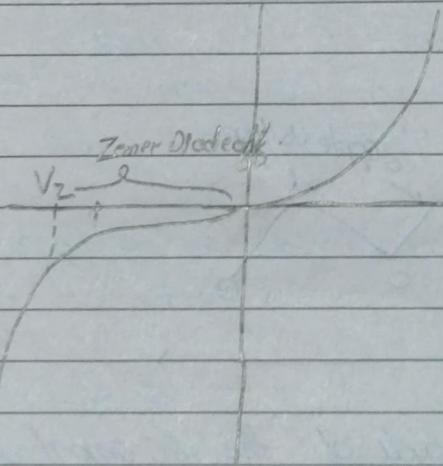


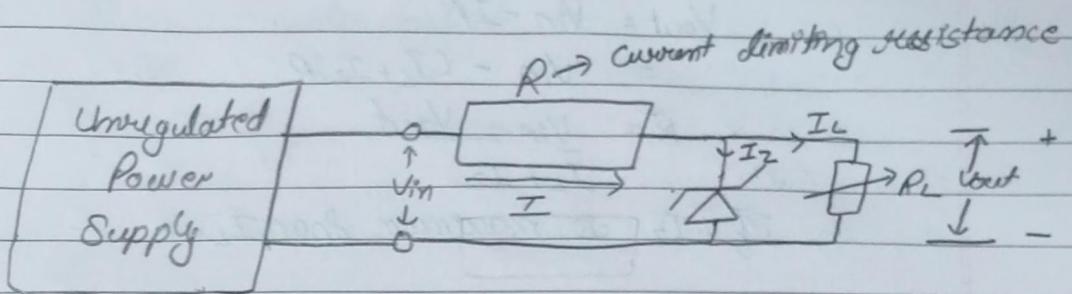
- Shunt Capacitor Filter \rightarrow



3 When the negative half cycle of the AC input is applied the diode is in forward bias and hence it'll conduct. So this allows the capacitor to quickly charge upto V_m , i.e., upto (b).

- iii After we fully charge, the capacitor holds the charge till the input ac supply to the rectifier goes negative.
- iv During the -ve half cycle the capacitor attempts to discharge. However, it can't discharge through diode being reverse bias is off. Hence still ~~not~~ discharge from load resistor from point (b) to (c) and its voltage decreases somewhat.
- v Even during the -ve half cycle the capacitor maintains large voltage across load resistor.
- vi During the next +ve half cycle when the rectifier voltage exceeds the capacitor voltage (cc), the capacitor is again quickly charged to V_m (d).
- Zener diode as a voltage regulator:





Voltage Regulator is used to keep constancy in the dc voltage

Case I Suppose R is kept fixed but supply voltage V_{in} is slightly increased.

- i The increase in current I will be absorbed by zener diode without affecting I_L .
- ii The increase in V_{in} will be dropped across R thereby keeping V_{out} constant.
- iii On the other hand, if the supply voltage decrease the diode takes a smaller current and voltage drop across R is reduced, thus again keeping V_{out} constant.
- iv When V_{in} changes I and IR drop changes in such a way as to keep $V_{out} = V_2$ constant

2. Case II: V_{in} is fixed but I_L is changed.

- i When I_L increases, diode current I_Z decreases thereby keeping I and IR drop constant. In this way V_{out} remains unaffected.
- ii When I_L decreases, diode current I_Z increases thereby keeping I and IR drop constant. In this way V_{out} remains unaffected.

$$V_{out} = V_{in} - IR$$

$$= V_{in} - (I_L + I_2)R$$

$$R = \frac{V_{in} - V_{out}}{I_L + I_2}$$

If I_2 is maximum then $I_L = 0$

$$\text{So } R = \frac{V_{in} - V_{out}}{I_{2(\max)}}$$

- Half Wave Rectifier:

$$\text{Ripple factor} = 1$$

$$2\sqrt{3}fR_LC$$

- Full wave Rectifier:

$$\text{Ripple factor} = \frac{1}{4\sqrt{3}fR_LC}$$

- In a centre tap full wave rectifier the load resistance $R_L = 1k\Omega$. Each diode has forward bias resistance of 10^{-2} . The voltage across half the secondary winding is $220 \sin 314t$ volt. Find
 - i) Peak value of current
 - ii) DC average value of current
 - iii) RMS value of current.
 - iv) Ripple factor
 - v) Rectification efficiency.

$$\text{v} = 220 \sin 100\pi t$$

$$2\pi f = 100\pi$$

$$f = 50 \text{ Hz}$$

$$R_L = 1000 \Omega$$

$$\text{Im} = \frac{220}{1010} = 0.217 \text{ A}$$

$$\text{iii } \frac{2\text{Im}}{\pi} = \frac{2 \times 0.217}{3.14} = 0.138 \text{ A}$$

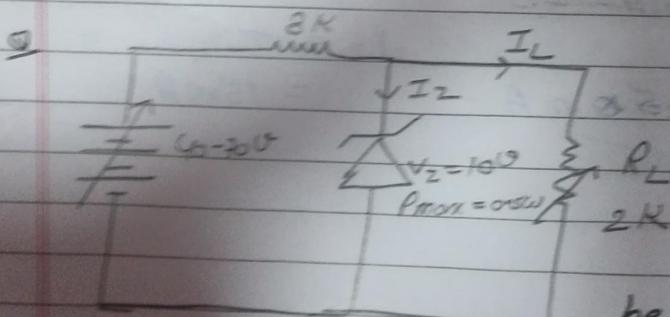
$$\text{iv } \frac{0.217}{\sqrt{2}} = 0.157$$

$$\text{v } \cancel{0.478} \quad R = \sqrt{\frac{I_{\text{rms}}^2}{I_{\text{dc}}} - 1}$$

$$= 0.478$$

$$\text{vi } \eta = \frac{P_{\text{dc}}}{P_{\text{ac}}} = \frac{(I_{\text{dc}})^2 R_L}{I_{\text{rms}}^2 (R_L + R_d)}$$

$$\approx 81.2 \%$$



Neglect zener resistance.

Calculate the battery current I , I_Z and I_L in the circuit. How will these values be affected if source voltage increases to 70V.

~~$P_{max} = I_2 \cdot V_2$~~

~~$0.5 = I_2 \times 10$~~

~~$0.05 A = I_2$~~

~~$5 \times 10^{-2} A = I_2$~~

~~$\therefore I = 40.8$~~

~~8×10^3~~

~~$I = 8 \times 10^{-3} A$~~

~~To~~

~~$IR = 30V$~~

~~$\frac{30}{3} \times 10^{-3} = I$~~

~~$10mA = I$~~

~~$V_{RL} = 30V$~~

~~$\therefore V = IR$~~

~~$\frac{30}{3} \times 10^3 = I_L$~~

~~$I_2 = I - I_L$~~

~~$= 5mA$~~

~~$10 \times 10^{-2} = I_L$~~

~~$I_2 + I_L = I \quad \therefore V_{in} = 70V$~~

~~$(8 \times 10^{-3}) \times 5$~~

~~$IR = 60$~~

~~$= \frac{60}{3} \times 10^{-3}$~~

~~When $V_{in} = 40V$~~

~~$V_2 = 10V$~~

~~$30V = IR$~~

~~$30 = I \times 3 \times 10^3$~~

~~$10 \times 10^{-3} = I$~~

~~$10mA = I$~~

~~$9.5mA = I_L$~~

~~$I_L = \frac{10}{2000} = 5mA$~~

~~$I_2 = I - I_L$~~

~~$= 15mA$~~

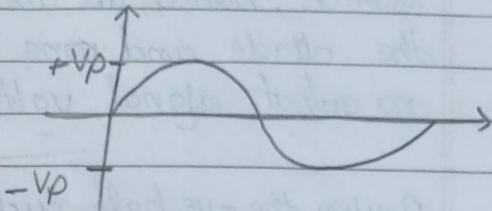
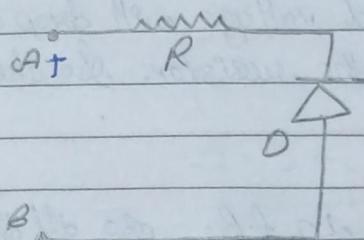
~~$I_2 = 5mA$~~

Clippers and Clampers:

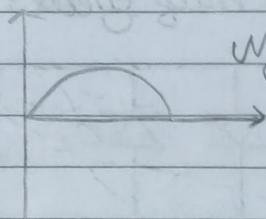
portion of input signal is clipped off

lift up or lift down the input signal to a different DC circuit level.

Clipper circuit:



Input Sine Wave Signal

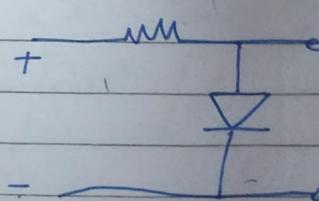


Negative Clipper

During the +ve half cycle of the signal is applied on the clipper A is +ve cut B the diode D is reverse biased. Hence it acts as an open circuit.

During the -ve half cycle O is forward biased, hence it acts a closed switch.

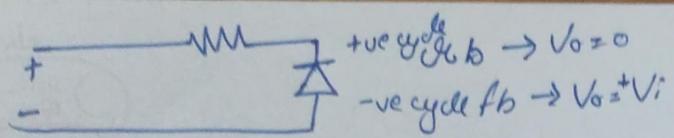
Actual-vc clipper:



+ve half cycle
f.b. $V_o = V_0$

-ve half cycle
o.b. $V_o = 0$

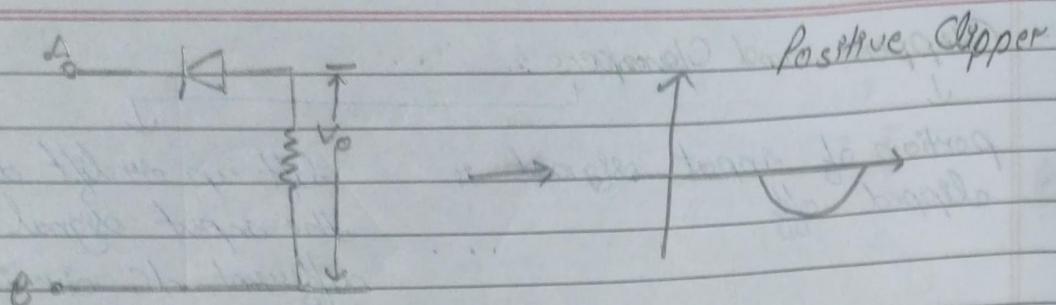
+ve
clipper



classmate

Date _____

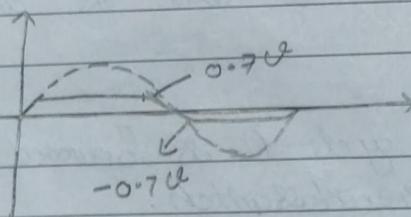
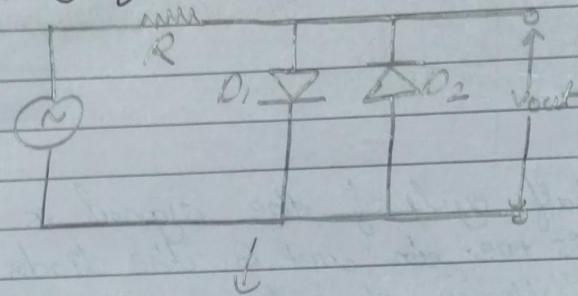
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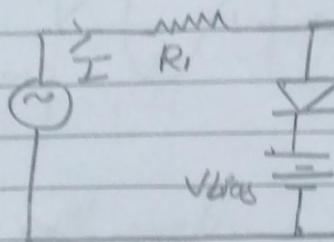
During the +ve half cycle of signal V_{in} , diode D is open switch, hence, all the applied voltage will drop across the diode and none across the resistor. So there's no output signal voltage.

During the -ve half cycle D is in f.B. so all the voltage is across R.

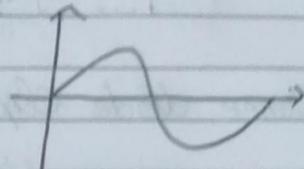
- clipping of both half cycles:



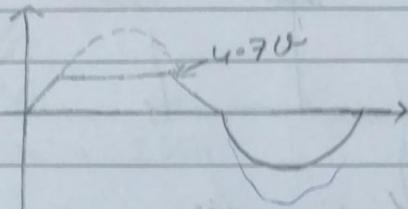
• Bias diode Clipping Circuits:



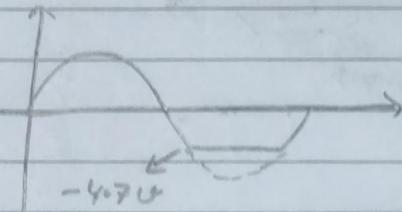
Positive bias diode



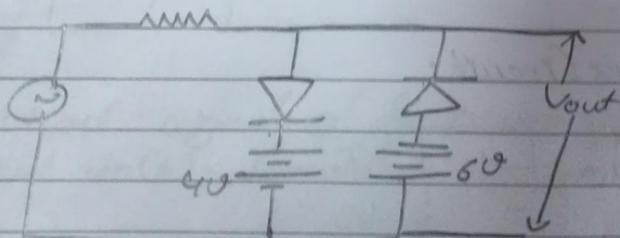
$$V_{bias} + V_{diode} \ll V_{AC}$$

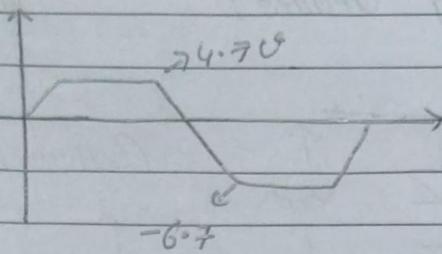


Negative bias

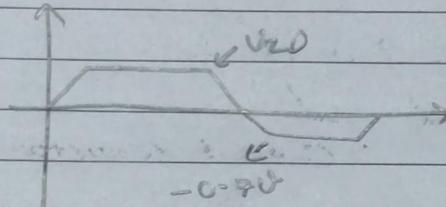
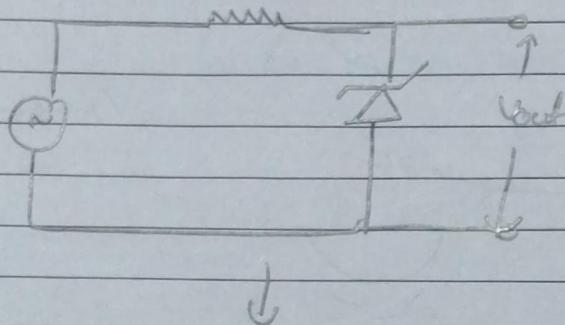


Q find o/p wave form.





- Zener diode Clipping:

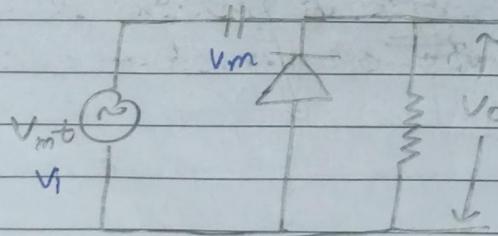


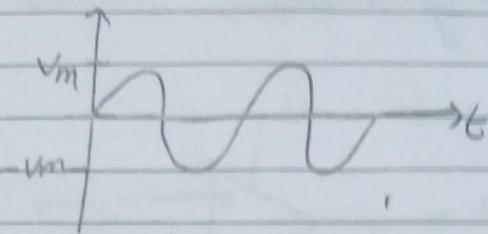
- Clampers:

time constant $\rightarrow \tau = CR$

$\tau \gg \frac{T}{2}$, where T = time period of the signal

1. Positive Clamper Circuit:





-ve half cycle:

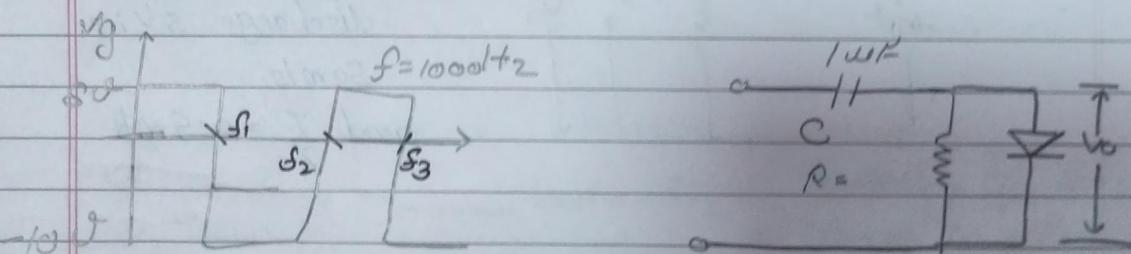
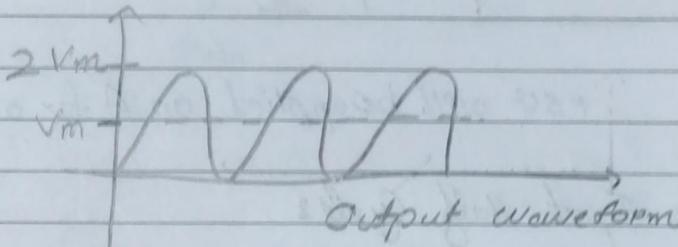
Diode \rightarrow F.B.

Capacitor \rightarrow Fully charge do +ve V_m .

+ve half cycle:

Diode \rightarrow R.B.

$$O/p \rightarrow V_i + V_m = 2V_m$$



The input signal of fig. (a) is applied to clamping circuit in (b). Draw the o/p waveform of o/p voltage V_o .

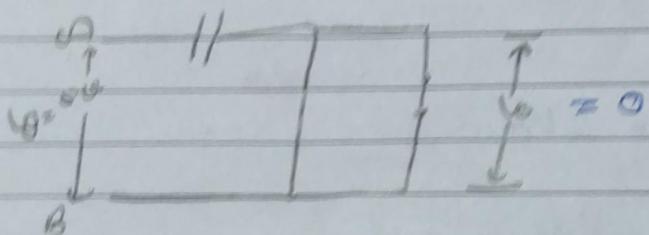
$\text{Time period of signal} = \frac{T}{f} = 1\text{ms}$

$$\frac{T}{2} = 0.5\text{ms}$$

$$\Delta = 1\text{ms}$$

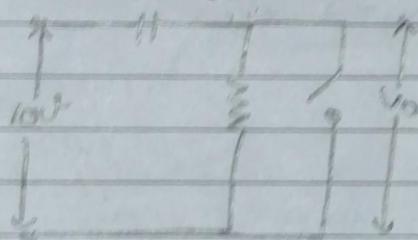
$$\Delta > \frac{T}{2}$$

→ Positive Input Half-Cycles



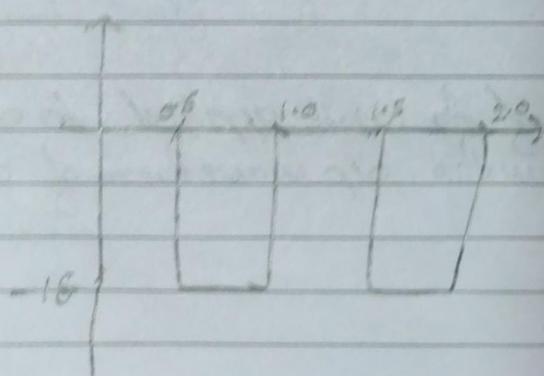
+5V will be applied on A for 0.5ms

→ Negative Input Half Cycles

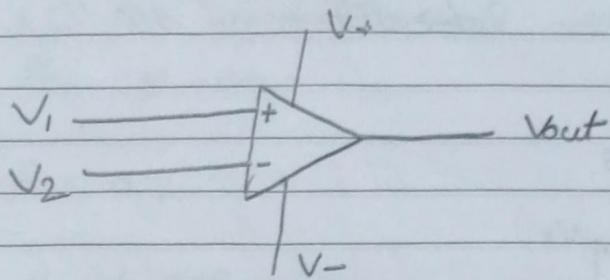


C needs 5A &
Discharge 5V i.e.
5mJ.

$$\text{and } \frac{I}{2} = 0.5\text{mA}$$



• Operational Amplifier (Op Amp):

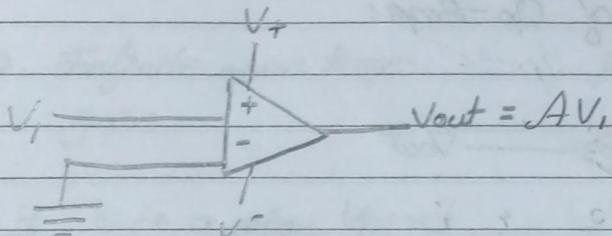


⇒ Two types:

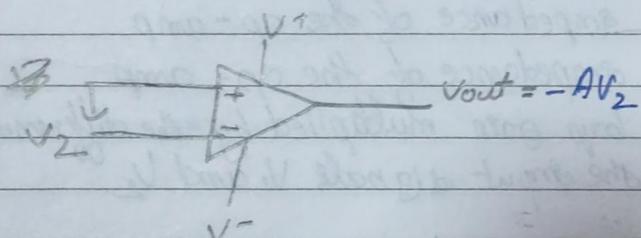
- i Non-Inverting
- ii Inverting

$$V_{out} = A \downarrow (V_1 - V_2)$$

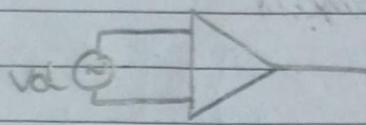
\downarrow
Gain



Non-Inverting Op Amp
* No change in phase



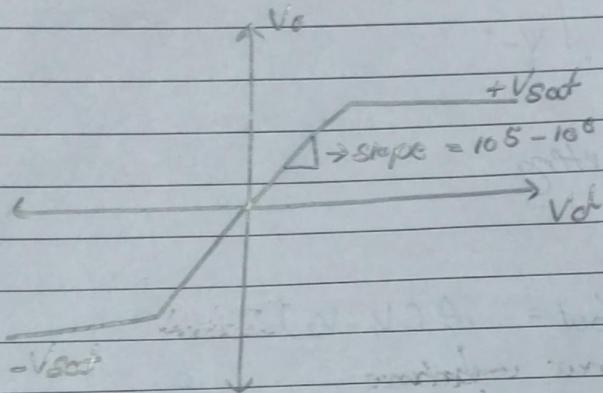
~~V1~~ $V_{out} = -AV_2$ Inverting Op Amp
* change in phase = 180°



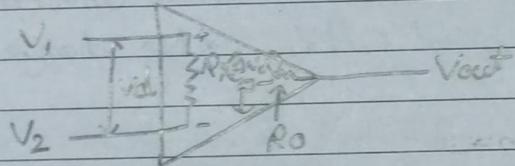
$$V_{out} = A V_{ol}$$

\hookrightarrow differential o/p v

$$A \approx 10^4 - 10^6$$



\Rightarrow Equivalent circuit of Op-Amp:



R_i = input impedance of the op-amp

R_o = output impedance of the op-amp

V_{out} = open loop gain multiplied by the difference b/w the input signals V_1 and V_2 .

• Characteristics of an Ideal Op-Amp:

1. $R_i = \infty$, so that the input voltage applied between the input terminals will be directly applied to the op-amp.

2. $R_o = 0$,

3. Bandwidth = ∞ .

4. $A = \infty$

\Rightarrow

1. Infinite Input Impedance

Ideal

$R_i = \infty$

Practical

10^2

2. Zero o/p Impedance

$R_o = 0$

10^2

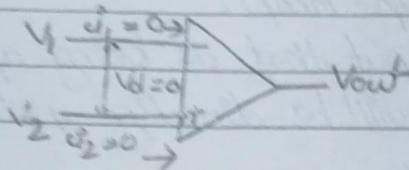
3. Infinite open loop gain

$A = \infty$

$10^5 - 10^6$

4. $V_{out} = 0$ when $V_{in} = 0$

mV



$$i_1 = i_2 = 0 \Rightarrow R_i \text{ is } \infty$$

- ⇒ Op-Amp draws no current at both the input terminals
i.e. $i_1 = i_2 = 0$
- ⇒ As the gain is infinite the Voltage b/w the inverting and non-inverting terminals is i.e. differential input voltage i.e. $V_d = (V_1 - V_2)$ is essentially zero, for the output o/p voltage V_o .

• Feedback in Ideal op-amp:

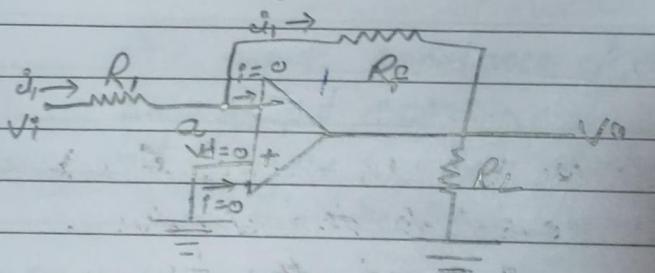
⇒ -ve feedback:

→ 2 basic feedback connection used.

Realistic i The current drawn by the either of the o/p Assumption terminals is negligible.

ii The differential o/p Voltage b/w non-inverting & inverting input terminal is zero.

⇒ The Inverting Amplifier:



(a) Inverting Amplifier

$$i_1 = \frac{V_i}{R_i}$$

$$V_o = -i_1 R_f = -\frac{V_i}{R_i} R_f$$

Gain of the inverting amplifier (Closed loop gain):

$$A_{CL} = \frac{V_o}{V_i} = -\frac{R_f}{R_i}$$

The nodal eqn. at the node 'a' is

$$\frac{V_a - V_i}{R_i} + \frac{V_a - V_o}{R_f} = 0$$

V_a is the Voltage at node 'a'.

a is grounded, so $V_a = 0$

$$\frac{V_o}{V_i} = -\frac{R_f}{R_i}$$

Q Design an amplifier with the gain of -10 and input resistance $10\text{ k}\Omega$.

Ans $-10 = -\frac{R_f}{R_i}$

$$R_i = 100\text{ k}\Omega$$

Q $R_i = 10\text{ k}\Omega$, $R_f = 100\text{ k}\Omega$, $V_i = 1\text{ V}$, A load of $25\text{ k}\Omega$ is connected to the output terminal. Calculate i_1 , V_o , i_L and the total current i_o on o/p.

Ans $i_1 = \frac{V_i}{R_i} = 10^{-4}\text{ A}$

~~$i_L = \frac{V_o}{R_f} = \frac{10}{100 \times 10^{-4}}$~~

$$V_o = -\frac{R_f}{R_i} \times V_i = -10\text{ V}$$

$$\begin{aligned}
 i_L &= \frac{10}{25 \times 10^3} \\
 &= \frac{1 \times 10^{-2}}{25} \\
 &\approx 4 \times 10^{-4} \\
 &= 0.4 \text{ mA}
 \end{aligned}$$

$$\begin{aligned}
 i_T &= (0.4 + 0.1) \text{ mA} \\
 &= 0.5 \text{ mA}
 \end{aligned}$$

Practical Inverting Amplifier:

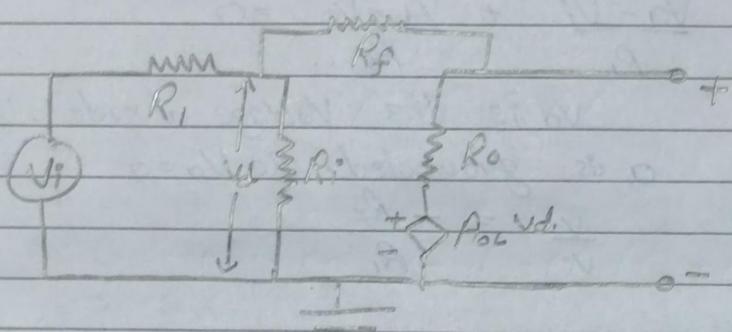


Fig : Equivalent circuit of a practical op-amp inverting amplifier

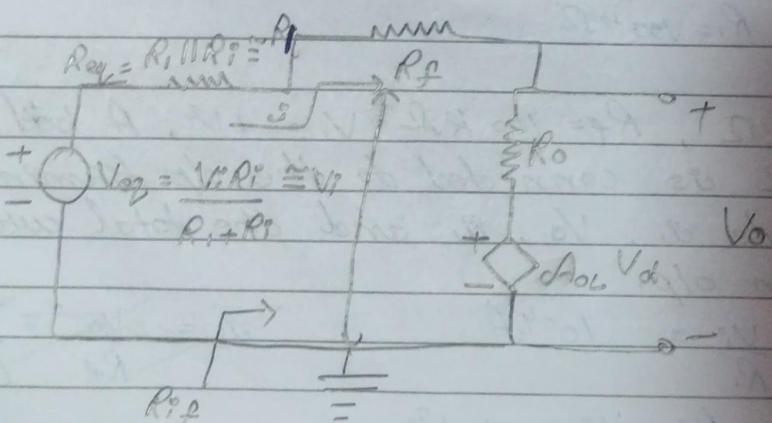


Fig: Simplified circuit by using Thevenin's Equivalent

from the o/p loop:

$$V_o = \alpha R_o + A_{OL} V_d - \textcircled{1}$$

open loop gain

Also

$$V_d + jR_f + V_o = 0 - \textcircled{2}$$

Putting the value of V_d from $\textcircled{2}$ to $\textcircled{1}$ and simplifying.

$$\underline{V_o - jR_o - A_{OL} V_d}$$

$$A_{OL} V_o + jR_f A_{OL} + jR_o = 0$$

$$V_o = \frac{(R_o - R_f A_{OL})j}{1 + A_{OL}} - \textcircled{3}$$

$$\frac{V_o - jR_o}{A_{OL}} = V_d$$

$$V_o - jR_o + j$$

Also, the KVL loop eqn.

$$V_i = j(R_f + R_o) + V_o - \textcircled{4}$$

Put the value of j from $\textcircled{3}$ into $\textcircled{4}$ and solve for closed loop gain,

$$A_{CL} = \frac{V_o}{V_i}$$

$$i = \frac{V_o (1 + A_{OL})}{R_o - A_{OL} R_f}$$

$$V_i = V_o \frac{(1 + A_{OL})(R_f) + V_o}{R_o - A_{OL} R_f}$$

$$V_i = V_o \left[\frac{1 + A_{OL} + R_o - A_{OL} R_f}{R_o - A_{OL} R_f} \right]$$

$$\frac{V_o}{V_i} = \frac{R_o - A_{OL} R_f}{1 + A_{OL} + R_o - A_{OL} R_f}$$

$$\frac{V_o}{V_i} = \frac{R_o - A_{OL} R_f}{1 + A_{OL}(1 - R_f) + R_o}$$

$$V_i = V_o \left[\frac{R_i + R_f + A_{OL}(R_i + R_f) + R_o - A_{OL} R_f}{R_o - A_{OL} R_f} \right]$$

$$\begin{aligned} \frac{V_o}{V_i} &= \frac{R_o - A_{OL} R_f}{R_i + R_f + R_o + R_i A_{OL}} \\ &= \frac{R_o - A_{OL} R_f}{R_i(1 + A_{OL}) + R_o + R_f} \end{aligned}$$

If $A_{OL} \gg 1$, $A_{OL} R_i \gg R_o + R_f$ and neglecting R_o ,

$$A_{OL} = \frac{V_o}{V_i} = -\frac{R_f}{R_i}$$

\Rightarrow Input resistance, R_{if}

$$R_{if} = \frac{V_d}{i}$$

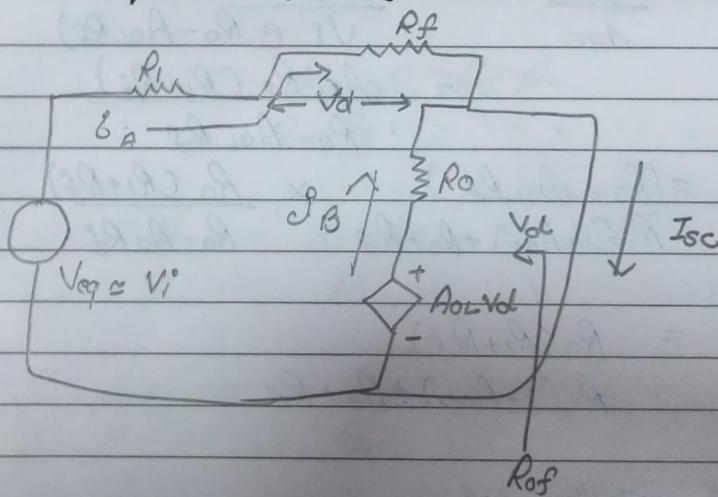
Writing the loop eqn. and solving for R_{if} .

$$V_d + i(R_f + R_o) + A_{OL}V_d = 0$$

$$V_d(1 + A_{OL}) = -i(R_f + R_o)$$

$$R_{if} = \frac{V_d}{i} = \frac{(R_f + R_o)}{1 + A_{OL}}$$

\Rightarrow Output impedance, R_{of}



$$i_A = \frac{V_d}{R_f + R_o} \quad \text{--- (1)}$$

$$i_B = \frac{A_{OL}V_d}{R_o} \quad \text{--- (2)}$$

$$V_d = -i_A R_f$$

$$i_B = -\frac{A_{OL}i_A R_f}{R_o}$$

$$\begin{aligned}
 i_{sc} &= i_p + i_B \\
 &= i_p - A_{OL} \frac{i_A R_f}{R_o} \\
 &= i_p \left(1 - \frac{A_{OL} R_f}{R_o} \right) \\
 &= \frac{V_i (C_{R_o} - A_{OL} R_f)}{(R_i + R_f) R_o}
 \end{aligned}$$

$$A_{CL} = \frac{V_{oc}}{V_i}$$

$$A_{CL} V_i = V_{oc}$$

$$\begin{aligned}
 R_{of} &= \frac{V_{oc}}{i_{sc}} = \frac{A_{CL} \cdot V_i R_o (R_i + R_f)}{V_i C_{R_o} - A_{OL} R_f} \\
 &= \frac{A_{CL} R_o (R_i + R_f)}{R_o - A_{OL} R_f} \\
 &= \frac{(R_o - A_{OL} R_f)}{R_i (1 + A_{OL}) + R_o + R_f} \times \frac{R_o (R_i + R_f)}{R_o - A_{OL} R_f}
 \end{aligned}$$

$$R_{of} = \frac{R_o (R_i + R_f)}{R_i (1 + A_{OL}) + R_o + R_f}$$

R_f can be written as,

$$\begin{aligned}
 R_{of} &= \frac{R_o (R_i + R_f)}{R_o + R_i + R_f} \\
 &\quad \frac{1 + \frac{R_i A_{OL}}{R_o + R_i + R_f}}{1 + \frac{R_i A_{OL}}{R_o + R_i + R_f}}
 \end{aligned}$$

- The Non-Inverting Amplifier:

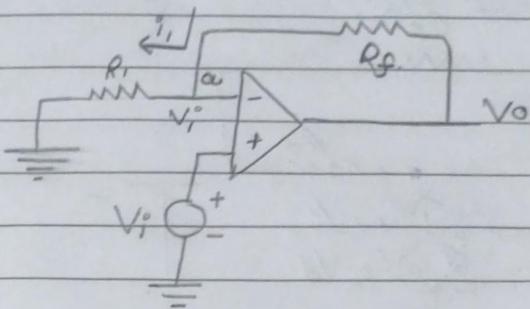


Fig. Non-Inverting Amplifier

Two assumptions:

i Input current = 0

ii $V_{OL} = 0$

$$V_i = \frac{V_o}{R_1 + R_f} \cdot R_f$$

$$\frac{V_o}{V_i} = \frac{R_1 + R_f}{R_1}$$

$$A_{CL} = 1 + \frac{R_f}{R_1}$$

- Practical Non-Inverting Amplifier:

• Practical Non-inverting Amplifier:

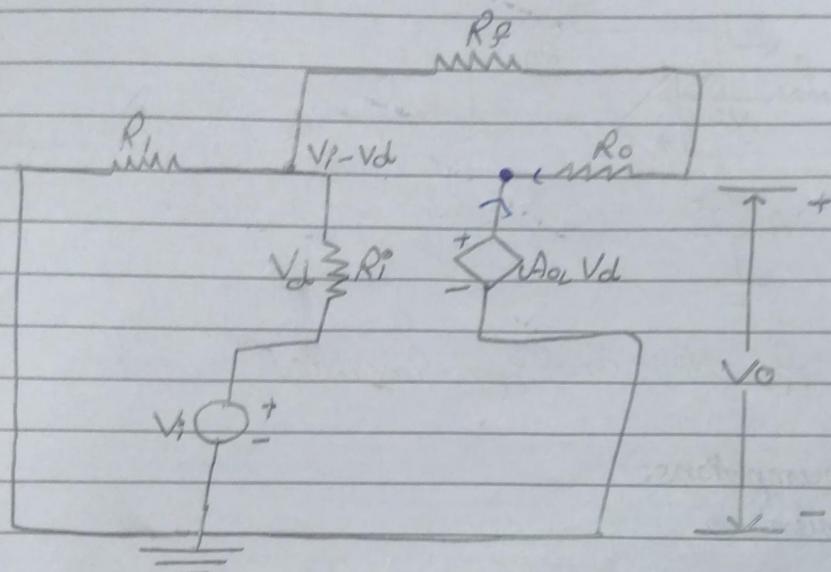


Fig. Equivalent circuit of non-inverting amplifier.

$$\cancel{V_i + V_d = gR_1}$$

$$\frac{V_i - V_d}{R_1} + \frac{V_d}{R_i} + \frac{V_i - V_d - V_o}{R_f} = 0$$

$$(V_i - V_d)Y_i + V_d Y_f + (V_i - V_d - V_o)Y_f = 0$$

\rightarrow Admittance

$$- (Y_i + Y_f) V_d + (Y_i + Y_f) V_i = Y_f V_o \quad \text{--- (1)}$$

$$(Y_i + Y_f) V_i = Y_f V_o = V_d (Y_i + Y_f - Y_i)$$

$$\Rightarrow V_i(Y) = V_d Y_1 + V_d Y_i + V_o Y_f - V_d Y_f - \\ V_o Y_f = 0.$$

$$\Rightarrow V_d [Y_i - Y_i - Y_f].$$

$$\Rightarrow -V_d [-Y_i + Y_i + Y_f] + V_o [Y_i + Y_f] - V_o Y_f.$$

At output node: KCL

$$Y_f (V_i^o - V_d - V_o) + (A_{oL} V_d - V_o) Y_o = 0$$

$$= V_o (Y_f + Y_o) + Y_f V_i^o + V_d (C - Y_f + A_{oL} Y_o) = 0 \quad (2)$$

$$-V_o (Y_f + Y_o) + Y_f V_i^o = V_d (A_{oL} Y_o + Y_f)$$

$$(Y_i + Y_f - Y_i) (-V_o (Y_f + Y_o) + Y_f V_i^o) = (Y_f Y_f) V_i^o - Y_f V_o$$

$$(Y_i + Y_f - Y_i) (-V_o Y_f - Y_o V_o + Y_f V_i^o) = Y_f V_i^o + Y_f V_i^o - Y_f V_o$$

$$-V_o Y_f Y_i - \underline{Y_o V_o Y_i} + Y_f V_i^o Y_i - \underline{V_o Y_f^2} - \underline{Y_o V_o Y_f} + \\ \underline{Y_f^2 V_i^o} + Y_i \underline{V_o Y_f} + Y_i \underline{Y_o V_o} - Y_f V_i^o Y_i - Y_i V_i^o - Y_f V_i^o \\ + Y_f V_o = 0$$

$$V_o (C - Y_f Y_i - Y_o Y_f - Y_f^2 - Y_o Y_f + Y_i Y_f + Y_o Y_i + \\ + Y_f) + V_i^o (C Y_f Y_i + Y_f^2 - Y_f Y_i - Y_i - Y_f) = 0$$

$$\frac{V_o}{V_i^o} = Y_f Y_i + Y_o Y_i$$

$$A_{CL} = \frac{V_o}{V_i} = \frac{(A_{OL} Y_0 (Y_I + Y_F) + Y_F Y_0)}{(A_{OL} + 1) Y_0 Y_F + (Y_I + Y_{I^o}) (Y_F + Y_0)}$$
(3)

If $A_{OL} \rightarrow \infty$

$$A_{CL} = \frac{Y_0 (Y_I + Y_F)}{Y_0 Y_F}$$

$$A_{CL} = 1 + \frac{Y_I}{Y_F}$$

$$A_{CL} = 1 + \frac{R_F}{R_I}$$

Q In the circuit of non-inverting amplifier $R_I = 5\text{ k}\Omega$, $R_F = 20\text{ k}\Omega$ and $V_p = 1\text{ V}$. A load diode of $5\text{ k}\Omega$ is connected at the output. Calculate V_o , A_{CL} , the load current and the output current i_o .

Ans $\frac{V_o}{V_i} = 1 + \frac{20}{5}$

$$V_o = 5\text{ V}$$

$$A_{CL} = 5$$

$$i_L = \frac{V_o}{R_L} = \frac{5}{5 \times 10^3} = 1\text{ mA}$$

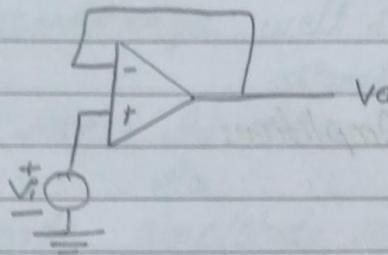
$$i_I = \frac{V_o}{5 \times 10^3} = \frac{1}{5} = 0.2 \times 10^{-3} = 0.2\text{ mA}$$

$$i_o = i_L + i_I \\ = 1.2\text{ mA}$$

- Voltage follower:

$$R_i = \infty$$

$$R_f = 0$$



$$V_o$$

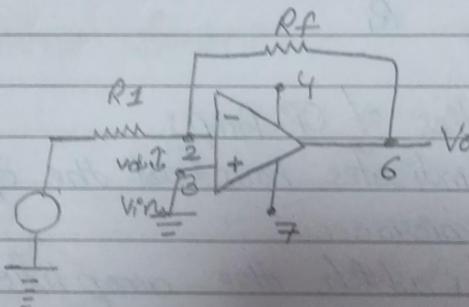
$$A_{CL} = \frac{V_o}{V_i} = 1 \text{ and } V_o = V_i$$

Output signal follows the input signals.

Ideal Non-Inverting Amplifier

- Inverting Amplifier:

Offset Null	1	8 - Not used
Inverting IIP	2	7 - V+
Non-inverting IIP	3	6 - Output
	4	5 - Offset Null
	V-	



$$\text{For } \frac{V_o - V_i}{R_f} + \frac{V_2 - V_o}{R_1} = 0$$

$$V_2 = 0$$

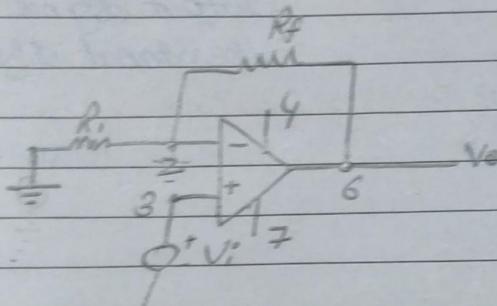
$$\frac{V_i}{R_1} = -\frac{V_o}{R_f}$$

$$\frac{V_o}{V_i} = -\frac{R_f}{R_1}$$

$$\Rightarrow V_{in} = 100, R_f = 10, R_i = 1k\Omega, V_o = ?$$

$$V_o = - \frac{10 \times 100}{10^3} = -10V$$

\Rightarrow Non-Inverting Amplifier:



$$V_i = \frac{V_o}{R_f + R_i} \cdot R_i$$

$$\frac{V_o}{V_i} = 1 + \frac{R_f}{R_i}$$

• Basic characteristics of OP-Amp:

• slew Rate: ~~It indicates how fast the op-Amp output changes to V per microsec.~~

Maximum rate at which the amplifier op can change in V/μs (microsec)

$$S = \frac{\Delta V_{out}}{\Delta t}$$

2. Common Mode Rejection Ratio:

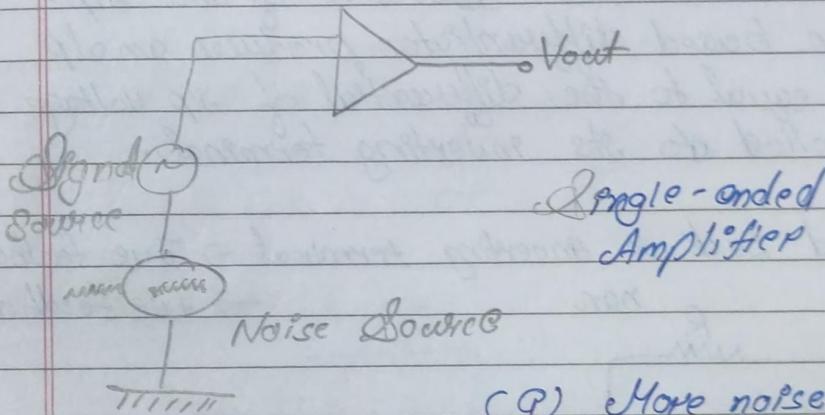
How much it rejects the common mode input & how

$CMRR = \frac{V_o}{V_i}$ well it amplifies the input
differential

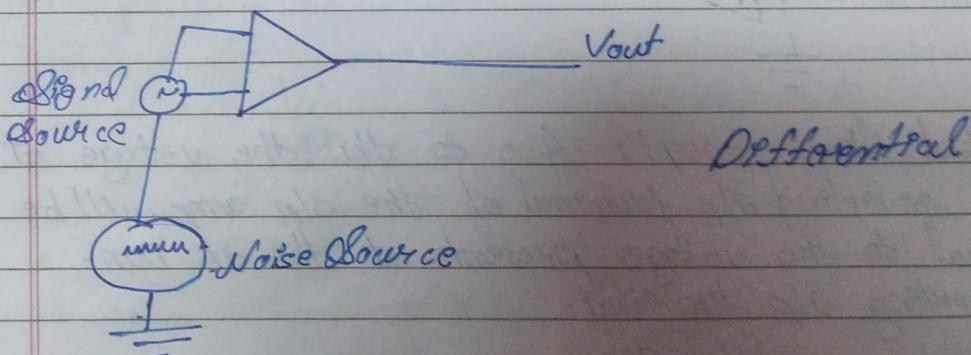
$$CMRR = \frac{A_d}{A_c} = \infty$$

In common mode amplitude remains same or if p.t
o.p. & are in phase

Differential Mode $\rightarrow -V_i = +V_o$ i.e. out of phase.



(a) More noise as the
Noisier Signal Source is input



(b) Less noise as the amplifier rejects
the common mode input i.e.
the noise source

3. Offset Voltage:

Difference b/w the inverting & non-inverting voltage.
Ideally it is zero.

4. Bandwidth:

It can amplify any frequencies without any loss.
Ideally it is ∞ .

• Applications of op-Amp:

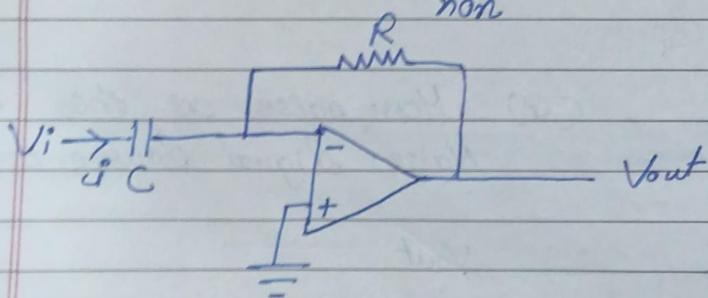
i) Differentiator:

- i) It is an electronic circuit which produces an o/p equal to the first derivative of the s/p.
- ii) An op-amp based differentiator produces an o/p which is equal to the differential of s/p voltage that is applied to its inverting terminal.

If o/p is fed back to inverting terminal \rightarrow -ve feedback

non

\rightarrow +ve feedback



Virtual Short Concept: According to this, the voltage at the inverting s/p terminal of the o/p amp will be equal to the voltage present at the s/p's non-inverting s/p terminal.

$$\cancel{V_i^o = 0}$$

$$I = \frac{dq}{dt}$$

$$q = CV$$

$$\dot{q} = \frac{dCV}{dt}$$

$$\dot{q} = C \frac{dV}{dt}$$

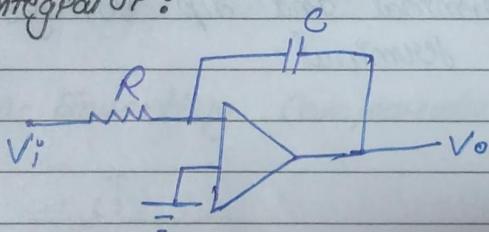
$$\frac{C d(C_0 - V_i)}{dt} + \frac{C - V_o}{R} = 0$$

$$V_o = -RC \frac{dV_i}{dt}$$

If $RC = 1 \text{ sec}$

$$V_o = -\frac{dV_i}{dt} \quad (- \text{ is out of phase})$$

2) Integrator:



$$-\frac{V_i}{R} + C \frac{d(C_0 - V_o)}{dt} = 0$$

$$-\frac{V_i}{R} = C \frac{dV_o}{dt}$$

$$-\frac{1}{RC} V_i dt = dV_o$$

$$V_o = -\frac{1}{RC} \int V_i dt$$

$$\text{If } RC = 1, V_o = - \int V_i dt \text{ (out of phase)}$$

3: Comparator:

An electronic circuit that, will compare the two inputs and give o/p after comparison.

They're of two types:

1: Inverting

2: Non-Inverting

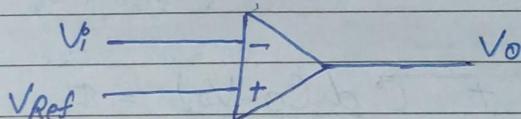
⇒ Inverting Comparator:

Reference Voltage: It is created in circuit to create a reference.

I/p voltage \rightarrow Inverting Terminal

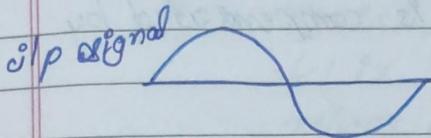
Ref. voltage \rightarrow Non-Inverting Terminal

An inverting comparator is an op-Amp based comparator for which a reference voltage is applied to its non-inverting terminal and o/p voltage is applied to its inverting terminal.

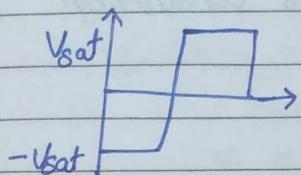


~~⇒ If Vin is greater than Vref then the o/p at the o/p will give rise to +ve saturation level i.e. Vout and vice-versa.~~

~~The o/p value of an inverting comparator will be $-V_{sat}$ for which the $V_{in} \neq V_{ref}$.~~



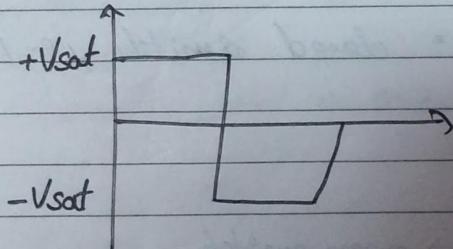
During the half cycle
o/p is $-V_{sat}$



During the +ve half cycle of the sinusoidal slip signal the Voltage present at the inverting terminal > 0 i.e. $V_{in} > V_{ref}$, hence the o/p value of the inverting comparator will $-V_{sat}$ and vice versa.

* O/p changes whenever it crosses 0 V.

⇒ Non-Inverting Comparator:



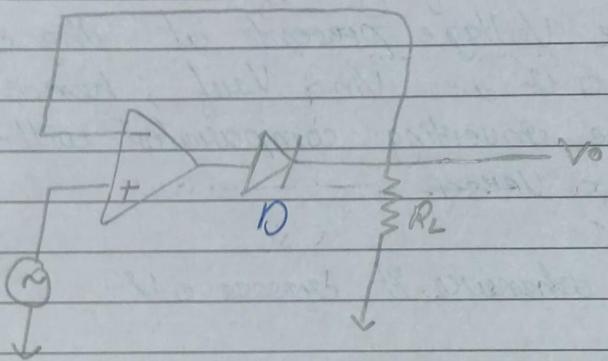
In +ve half cycle
 $V_{in} > V_{ref} \rightarrow +V_{sat}$
-ve half cycle
 $V_{in} < V_{ref} \rightarrow -V_{sat}$

- Precision Rectifier (Superdiode):

We use it to get rectified o/p (ac to dc) without loss of any signal.

The voltage drop across diode is compensated by op-amp.

When $V_{in} \gg V_{threshold}$ then only diode is conducting.
(like 0.7)



① V_{in} is +ve, $V_{in} > 0$

D in f.B. \therefore D = closed switch i.e. D is buffer.
 $V_{in} = V_o$.

② V_{in} is -ve, $V_{in} < 0$

D in R.B., \therefore D \rightarrow open switch .

$$V_o = 0$$

Effective Voltage Drop across Diode:

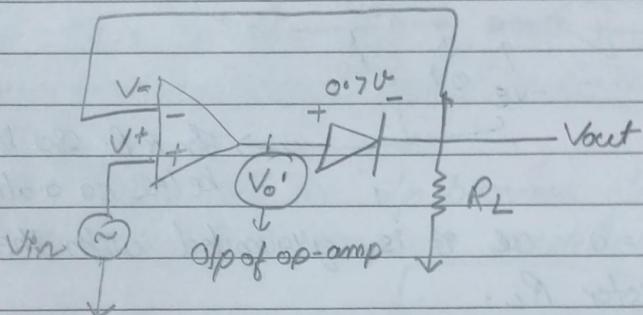
$$V_F' = V_F$$

A_{OL}

where V_F is Voltage drop across the diode

V_F' is effective forward voltage drop across the diode.

$$\begin{aligned} V_F' &= \frac{0.7}{10^5} \\ &\approx 0V \text{ (approx.)} \end{aligned}$$



$$V_{out} = V_o' - 0.7V$$

$$V_o' = V_{out} + 0.7V$$

$$V_o' = A_{OL} (V^+ - V^-)$$

$$A_{OL} (V^+ - V^-) = V_{out} + 0.7$$

$$A_{OL} (V_d) - 0.7 = V_{out} \quad V_{out} + 0.7 = V^+ - V^-$$

$$A_{OL} \gg 0.7$$

$$\therefore V_{in} = V_{out}$$

$$A_{OL}$$

$$A_{OL} \gg 0$$

$$V^+ - V^- = 0$$

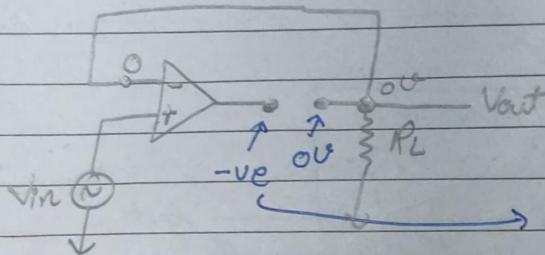
$$V^+ = V^-$$

The implies that the I/p at the +ve terminal will be equal to the -ve terminal. (if -ve terminal is connected to 0/p)

$$V_{out} = V_{in}$$

Note: The diode will conduct only when the applied I/p voltage is greater than zero.

\Rightarrow -ve input signal:

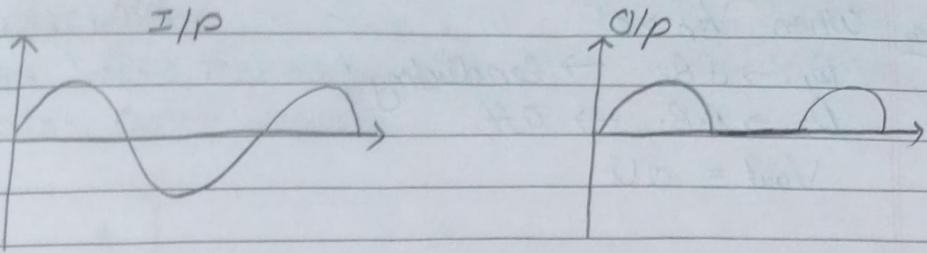


In R.B. so that p would be less so o o in then-veat p

$V_{out} = 0$ as it is grounded with the diode
resistor R_L .

$V_{at -ve\ terminal} = 0$. (as its connected to V_{out})
(* Can apply virtual short concept)

This is only possible whenever the applied I/p voltage in the diode is -ve



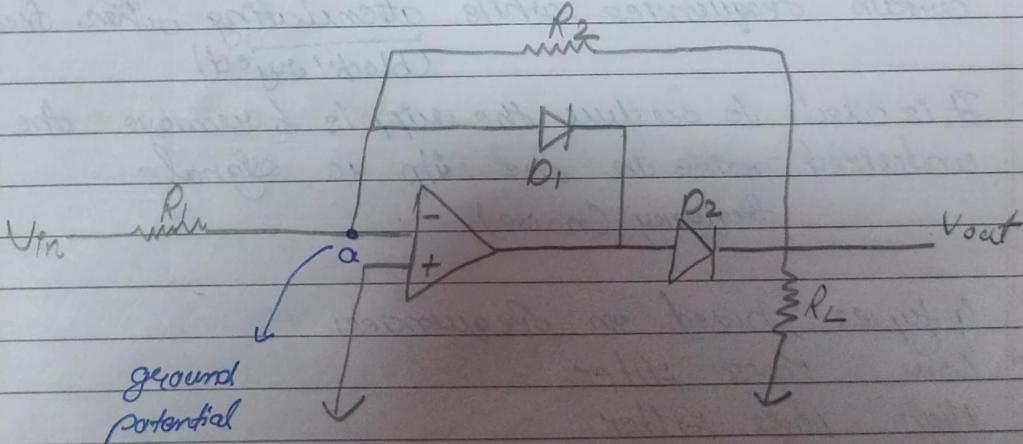
Whenever $V_{in} < 0$ then the o/p of op-amp will be in $-V_{sat}$.

And this will be open-loop configuration.

Whenever the o/p becomes +ve at that time the op-amp needs to come out from the $-V_{sat}$ (negative saturation voltage) i.e. it'll have some time to have $+V_{sat}$. This is fine for take low frequencies.
~~There'll be no delay in low frequencies~~

At high frequencies the o/p becomes distorted. So we use modified precision rectifier. To avoid the $-V_{sat}$ we use

- Modified Precision Rectifiers



3 When $V_{in} > 0$

$D_1 \rightarrow S.B. \rightarrow$ Conducting

$D_2 \rightarrow R.B. \rightarrow$ off

$$V_{out} = 0V$$

2 $V_{in} < 0$

$D_1 \rightarrow$ off

$D_2 \rightarrow$ conducting

$$V_{out} = -\frac{R_2}{R_1} V_{in}$$

\Rightarrow let us assume D_1 is conducting

\Downarrow
O/p is fed back to the I/p.

At the 'o' node we can apply virtual ground concept $V_o = 0$.

• Filters:

A filter is a circuit which is capable of amplifying certain frequencies while attenuating other frequencies.
(block/reject)

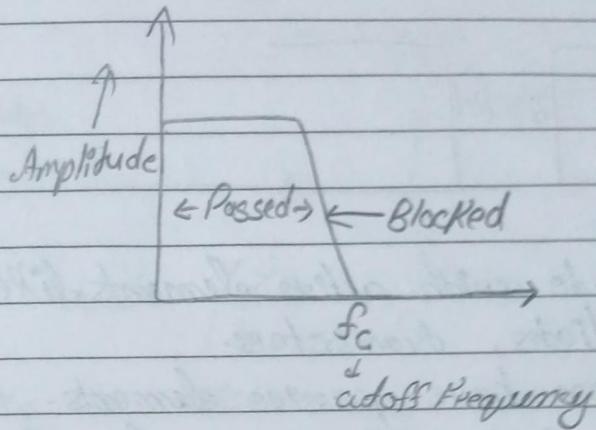
It is used to reduce the ripples & remove the undesired noise in the o/p ac signal.
(frequency noise)

\Rightarrow 4 types, based on frequencies:

1. Low Pass Filter
2. High Pass Filter
3. Band Pass Filter
4. Band Reject Filter

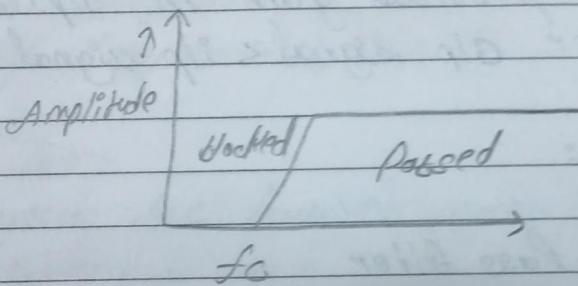
3. Low Pass Filter:

Allows low frequency signals & rejects high frequency (Cutoff frequency).



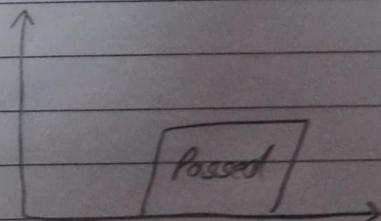
2. High Pass filter:

Allow high frequency & rejects low frequency.
(cutoff frequency \rightarrow ~~—~~ (f > f_c))



3. Band Pass filter:

Allows only a certain band & rejects others.



4 Band Reject filter:

Rejects only a certain band & accept others.



⇒ Active Filter: Made with active elements like op-amp, diodes, transistors.

Can have passive elements.

⇒ Passive Filter: Made with passive elements like resistor, capacitor (not inductor bcs of huge energy loss).

* Active filter provides gain in o/p signal.
Passive filter o/p signal < i/p signal.

5 Passive Filter:

Types:

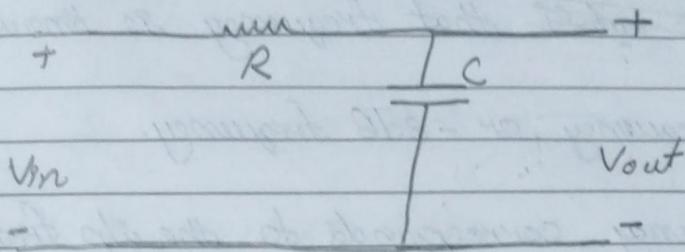
a) RC Low Pass Filter

b) RL " " "

c) RLC " " "

⇒ RC Low

⇒ RC low pass filter:



$$V_{out} = \left(\frac{X_C}{X_C + R} \right) V_{in}$$

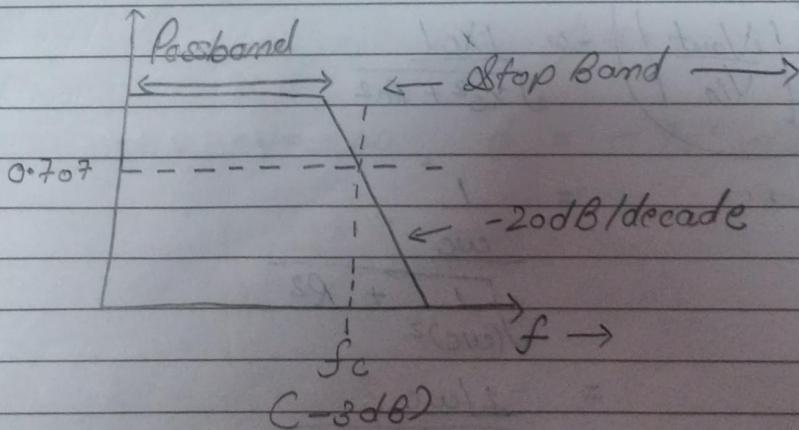
X_C is reactance of capacitor which varies with frequency.

$$|X_C| = \frac{1}{\omega C}$$

- i At low frequencies, $X_C \uparrow \rightarrow V_{out} = V_{in}$
- ii At high frequencies, $X_C \downarrow \rightarrow V_{out} = 0$

c.e. of low

It passes the low frequency signal & rejects the high frequency.



\Rightarrow The frequency at which o/p is $0.707 \left(\frac{1}{\sqrt{2}}\right)$ times i/p, is the cutoff that frequency is known as

cutoff frequency or -3dB frequency.

\Rightarrow -3dB frequency corresponds to the o/p frequency that causes the o/p signal to drop by -3dB relative to the o/p signal.

$$V_o = \frac{1}{\sqrt{2}} V_i$$

\Rightarrow The magnitude changes to $\frac{1}{\sqrt{2}}$ whenever the frequency changes to tenfold/decade.

$$S_C = \frac{1}{2\pi R C}$$

$$V_{out} = \left(\frac{X_C}{X_C + R_C} \right) V_{in}$$

Transfer function

$$\left(\frac{V_{out}}{V_{in}} \right) = \frac{|X_C|}{\sqrt{X_C^2 + R_C^2}}$$

$$= \frac{1}{$$

$$\frac{w_C}{}$$

$$\sqrt{\frac{1}{(w_C)^2} + R^2}$$

$$= \frac{1/w_C}{$$

$$\sqrt{1 + R^2 w^2 C^2}$$

$$w_C$$

$$\frac{1}{\sqrt{2}} = \frac{1}{\sqrt{1 + R^2 \omega^2 C^2}}$$

$$\frac{1}{2} = \frac{1}{1 + R^2 \omega^2 C^2}$$

$$2 = 1 + R^2 \omega^2 C^2$$

$$1 = R^2 \times 4\pi^2 f^2 C^2$$

$$\frac{1}{R^2} = f^2$$

$$4\pi^2 R^2 C^2$$

$$\boxed{\frac{1}{2\pi RC} = f_c}$$

If $f_c \uparrow$ the output signal & phase will change.

$$\boxed{\phi = -\tan^{-1}(wCR)} \rightarrow \text{Phase}$$

$\Rightarrow w = 0, \phi = 0^\circ$ i.e. o/p in phase with i/p

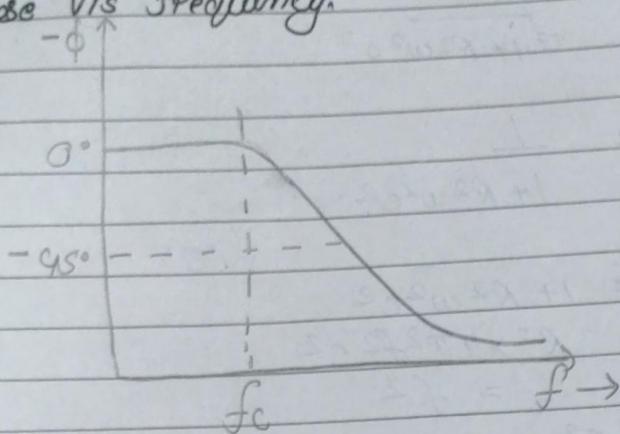
$$\text{At } f_c, w = w_c \Rightarrow \phi = -\tan^{-1}\left(\frac{2\pi \times R C}{2\pi R C}\right)$$

$$\phi = -\tan^{-1}(1)$$

$$\phi = -45^\circ$$

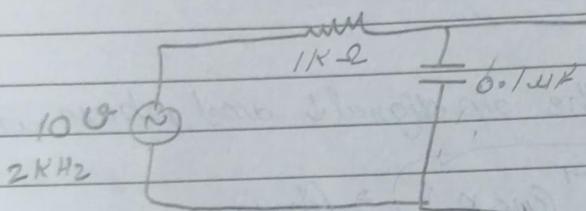
$w = \infty, \phi = -90^\circ$; o/p lags i/p with 90°

Phase vs frequency.



Q Find -3dB frequency and o/p voltage at 2 KHz.

Ans



$$\frac{1}{\sqrt{2}} = \frac{1}{\sqrt{1+R^2 \omega^2 C^2}} = \frac{1}{2\pi RC}$$

$$\frac{1}{2} = \frac{1}{2\pi \times 3.14 \times 10^3 \times 10^{-6}} = \frac{1}{6.28 \times 10^{-3}}$$

$$= \frac{1}{6.28} = \frac{100}{6.28}$$

$$= 1.59 \text{ KHz}$$

~~$$V_o = \left(\frac{X_C}{X_C + R} \right) V_{in}$$~~

~~R~~

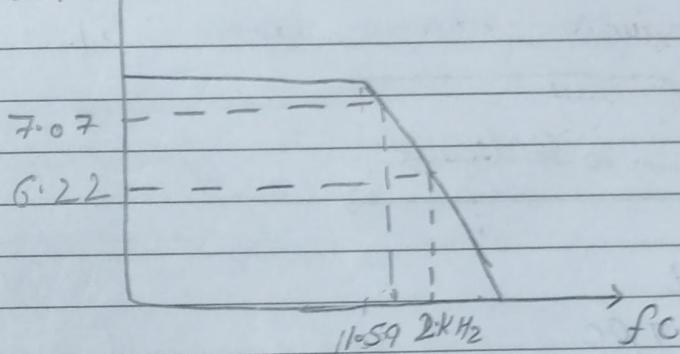
$$X_C = 1592.356 \cdot 6 \quad X_C = 796.17$$

$$X_C = 1.59 \text{ M}\Omega$$

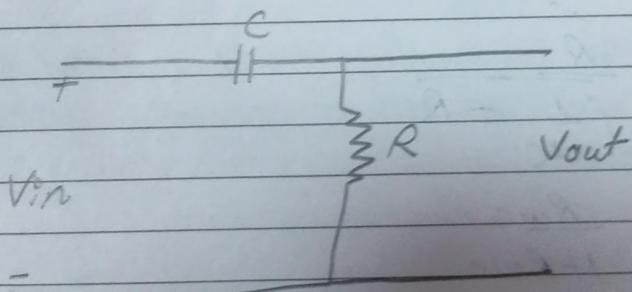
$$V_o = \left(\frac{796}{796 + 1000} \right) \times 10 \quad V_o = \left(\frac{|Y_{o1}|}{\sqrt{X_C^2 + R^2}} \right) \cdot V_{in}$$

$$\begin{aligned} V_o &= \frac{796}{\sqrt{633616 + 10^8}} \times 10 \\ &= \frac{796}{1278.12} \times 10 \\ &= 6.227 \text{ V} \end{aligned}$$

Amplitude



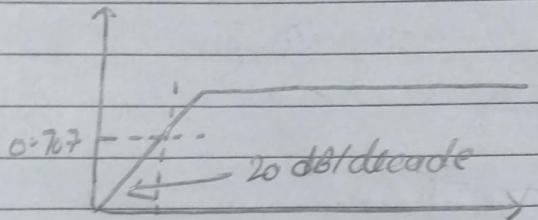
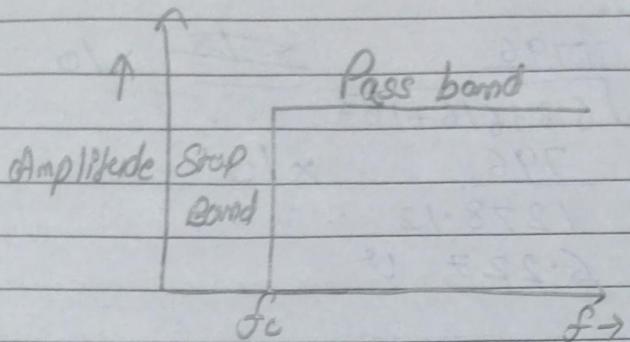
• RC High Pass Filter:



$$V_{out} = \left(\frac{R}{X_C + R} \right) V_{in}$$

$$|X_C| = \frac{1}{\omega_C}$$

- j At $\omega = 0$, $|X_C| = \infty$, $V_o = 0$
 ii At $\omega = \infty$, $|X_C| = 0$, $V_o = V_{in}$



$$f_c = \frac{1}{2\pi RC}$$

$$V_o = \frac{1}{\sqrt{2}} V_{in}$$

$$\frac{1}{\sqrt{2}} = \frac{R}{\sqrt{L + R^2 \omega^2}}$$

$$\frac{1}{2} = \frac{R_{wc}}{1 + R_{wc}}$$

$$2R_{wc} = 1 + R_{wc}$$

$$R_{wc} = \pm$$

$$2\pi f R C = 1$$

$$\frac{1}{2\pi R C} = f_c$$

As $f_s \uparrow$ o/p signal \uparrow and phase will also change.

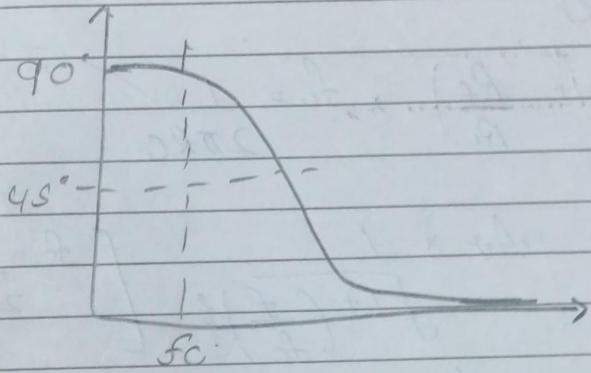
$$\Rightarrow \phi = \tan^{-1} \left(\frac{L}{wCR} \right)$$

at $\omega = 0$, $\phi = 90^\circ \rightarrow$ o/p leads s/p by 90°

$\omega = \infty$, $\phi = 0$

$\omega = \omega_c$, $\phi = 45^\circ$

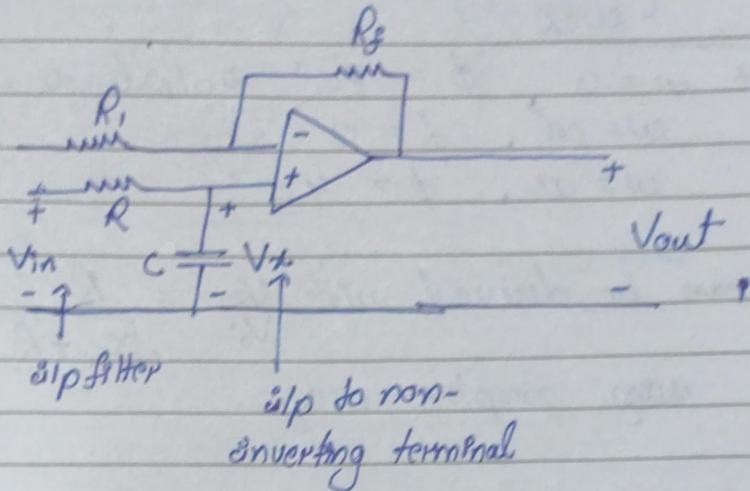
* Phase can be derived with $\frac{V_o}{V_i} = \frac{R}{\sqrt{Lc + R}}$ by using complex wCj .



passive

* When we cascade many filters it'll effect the cut off frequency thus affecting the ~~per~~ load. That's why we use active filter.

- Active Low Pass Filter & High Pass Filter:



$$A_v = \left(1 + \frac{R_f}{R_1} \right), \quad f_c = \frac{1}{2\pi R C}$$

$$\left| \frac{V_o}{V_i} \right| = A_v \times \underbrace{\frac{1}{\sqrt{1 + \left(\frac{f}{f_c} \right)^2}}}_{\left[f_c = \frac{1}{2\pi R C} \right]}$$

Response of a low pass filter

for a low pass filter

$$V_o = \left(\frac{X_C}{X_C + R} \right) \cdot V_{in}$$

Multiply the numerator and denominator by ωC .

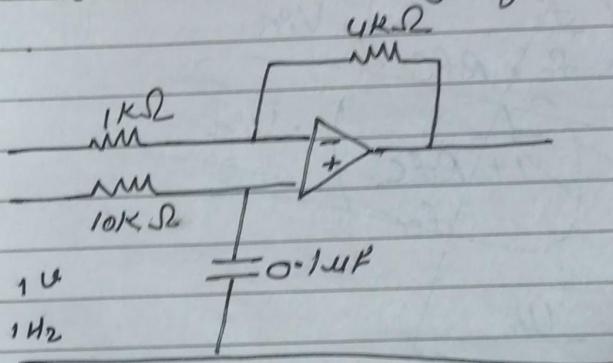
$$V_o = \frac{X_0}{X_0 + R} \cdot V_{in} \Rightarrow \frac{1}{1 + \omega_c R} \cdot V_{in} \Rightarrow \frac{1}{1 + 2\pi f C R} \cdot V_{in}$$

$$= \frac{1}{\frac{1}{2\pi C R}} \cdot V_{in} = \frac{\omega_c}{\omega_c + f} \cdot V_{in} \Rightarrow \frac{1}{1 + \frac{f}{\omega_c}} \cdot V_{in}$$

$$\frac{1}{2\pi C R} + f$$

$$\left| \frac{V_o}{V_i} \right| = \sqrt{\frac{1}{\left(\frac{f}{\omega_c} \right)^2}}$$

Q) Find the cutoff frequency of the given filter.

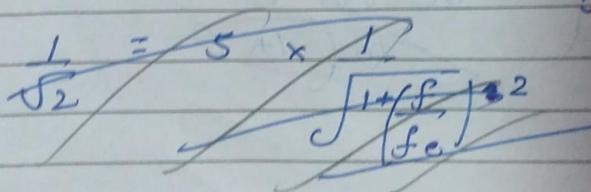


CASE

$$A_v = 1 + \frac{R_f}{R_i} = 5$$

$$\omega_c = \frac{1}{2\pi R C}$$

$$= \frac{1}{2\pi \times 10^3 \times 0.1 \times 10^{-6}} = 159 \text{ rad/s}$$



$$V_o = 5 \times \frac{1}{\sqrt{1 + \left(\frac{f}{159}\right)^2}} \times 1$$

$$V_o = 4.99 \approx 5 \text{ V}$$

⇒ Active high pass filter.

$$V_o = \frac{R}{R + jC} \cdot V_{in}$$

$$V_o = \frac{R}{\frac{1}{j\omega C} + R} \cdot V_{in}$$

$$\frac{V_o}{V_{in}} = \frac{R}{1 + R\omega C}$$

$$\frac{V_o}{V_{in}} = \frac{R}{1 + 2\pi f R C}$$

$$\frac{V_o}{V_{in}} = \frac{R}{2\pi f R C}$$

$$= \frac{1}{2\pi f C}$$

$$= -\frac{R}{2\pi f C} \cdot \frac{R}{R + jC}$$

$$= \frac{R}{2\pi f C}$$

$$= \frac{1}{2\pi f C} + f$$

$$= \frac{R f_c}{f_c + f}$$

$$\frac{V_o}{V_{in}} = \frac{R}{1 + \frac{f}{f_c}}$$

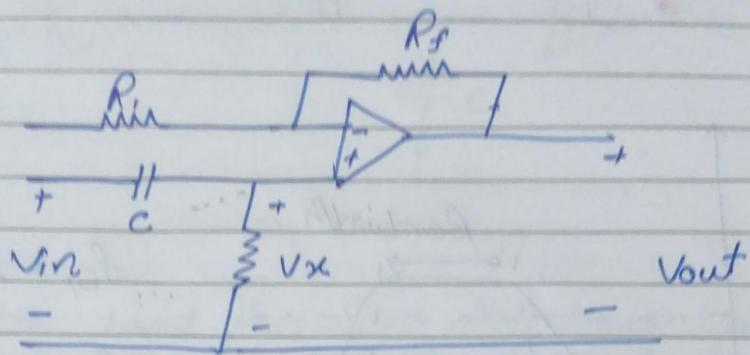
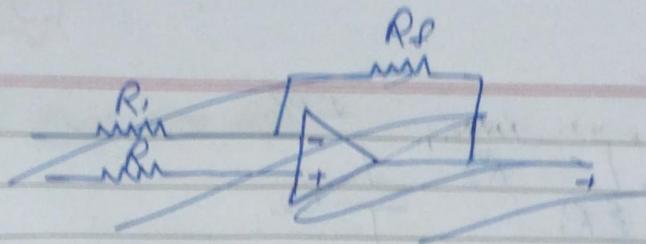
$$V_o =$$

• Active high pass filter:

$$\begin{aligned}
 \frac{V_o}{V_i} &= \frac{R}{X_C + R} = \frac{R_{wg}}{\frac{1}{\omega_c} + R} \\
 &= \frac{R_{wg} \times \omega_c}{\omega_c + R_{wg} \times \omega_c} = \frac{R_{wg}}{\frac{1}{2\pi f_c} + R_{wg}} \\
 &= \frac{R_{wg} \times 2\pi}{\frac{2\pi}{2\pi R_C} + R_{wg} \times 2\pi} = \frac{R_{wg} \times 2\pi}{\frac{2\pi f_c}{2\pi R_C} + R_{wg} \times 2\pi} \\
 &= \frac{\omega}{\omega_c + \omega} = \frac{f}{f_c + f} \\
 V_o &= \left(\frac{f}{f_c} \right) \cdot V_{in}
 \end{aligned}$$

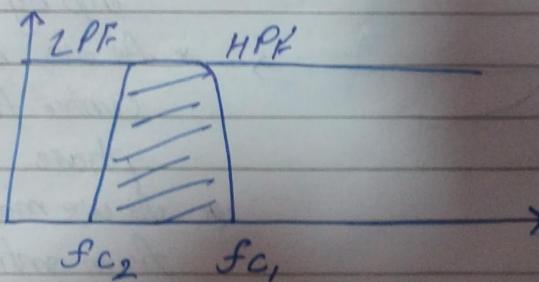
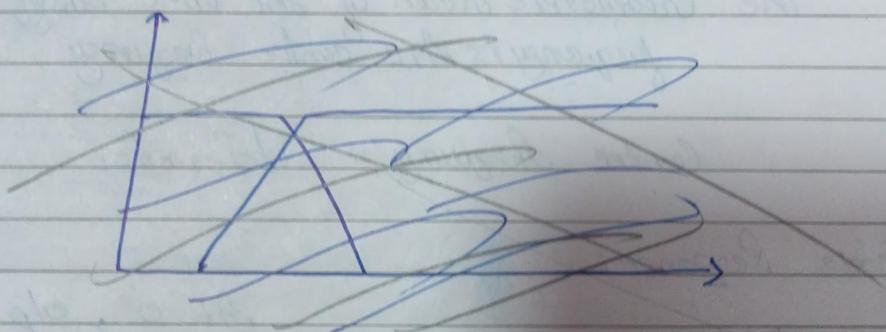
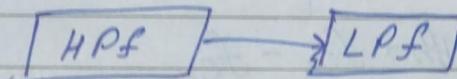
$$\left| \frac{V_o}{V_i} \right| = \frac{(f/f_c)}{\sqrt{1 + (f/f_c)^2}} \quad \text{Response of filter} \rightarrow \text{high pass}$$

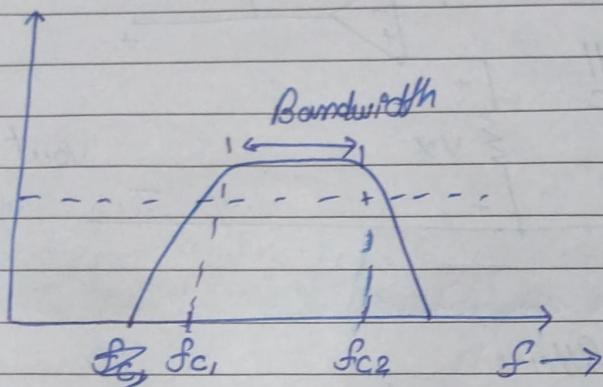
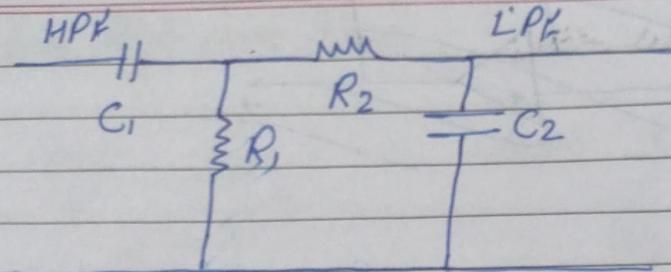
$$\text{So } V_o = A_v \times \frac{f/f_c}{\sqrt{1 + (f/f_c)^2}}$$



• Band Pass Filter:

Cascade high pass & low pass filter.





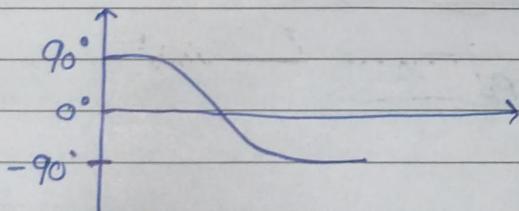
f_{c1} = Low cut-off frequency
 f_{c2} = High cut off freq.

$$\text{Bandwidth} = f_{c2} - f_{c1}$$

The Geometric Mean of the two cutoff frequency is the centre frequency

$$\text{Centre frequency} = \sqrt{f_{c2} \times f_{c1}}$$

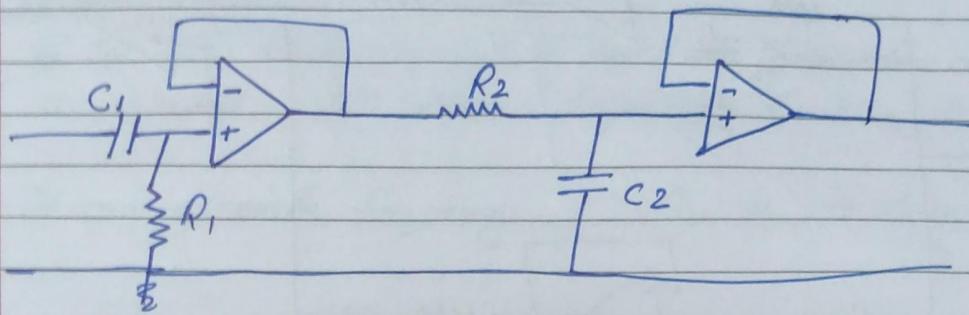
Phase Response:



At 0° , o/p leads s/p by 90°

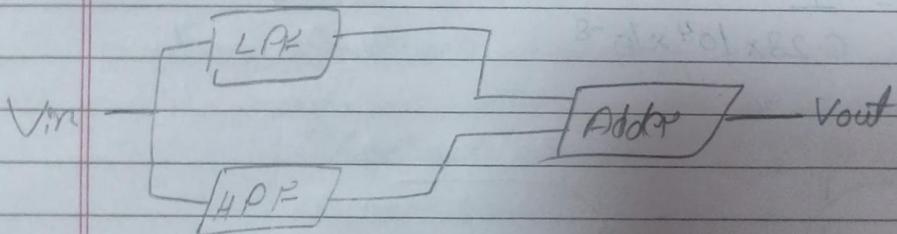
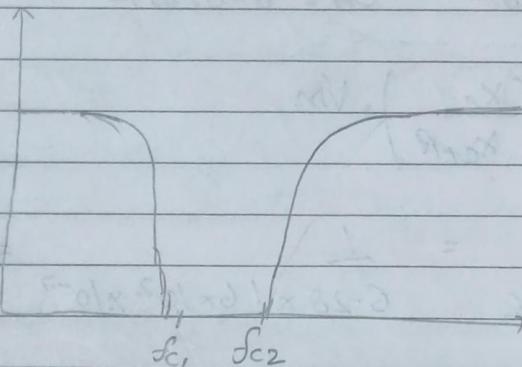
- * As we move towards centre frequency the phase response ↓.
- * As we move away from centre frequency o/p will lag the s/p. & at ∞ o/p lags by 90° .

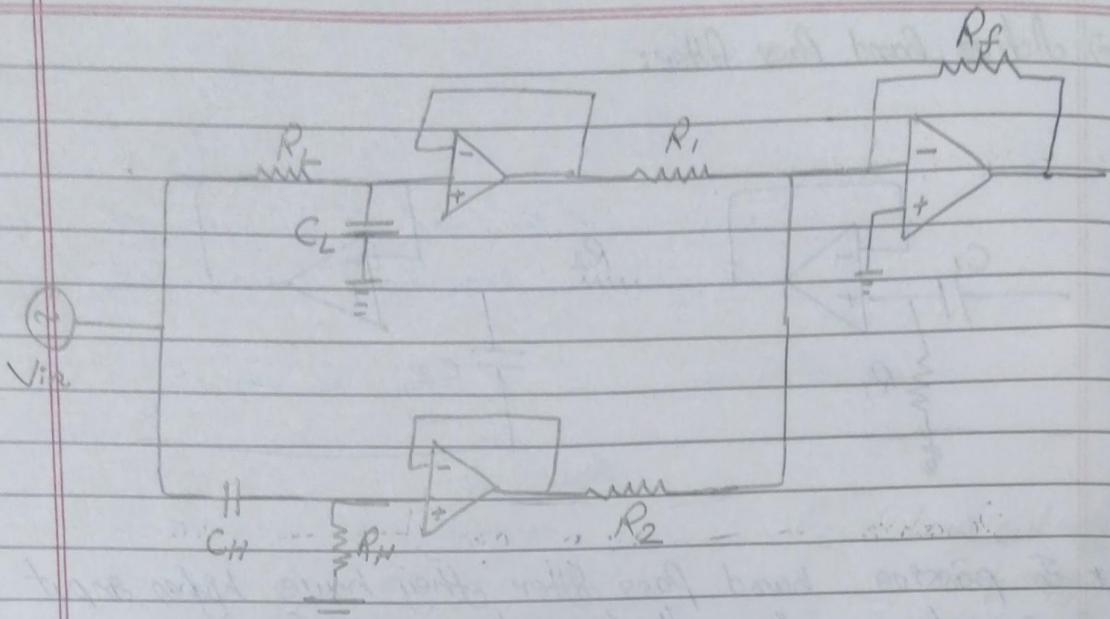
→ Active Band Pass filter:



- * In passive band pass filter they have higher input impedance thus affecting the cutoff frequency and distorting the I/P signal.

- Band-Stop/Reject Filter:





Q Find the band stop filter for the given values:

$$R_L = 1.6 \text{ k}\Omega \quad R_1 = 11\text{k}\Omega \quad R_2 = 1\text{k}\Omega$$

$$R_H = 10\text{k}\Omega \quad R_F = 1\text{k}\Omega$$

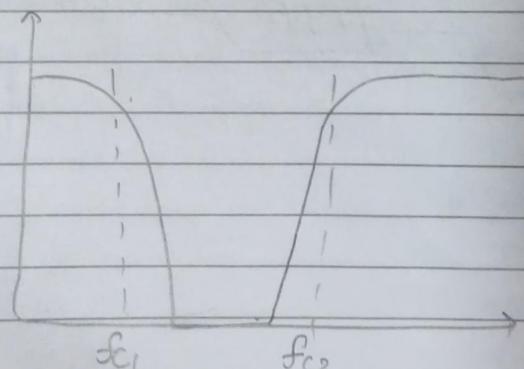
$$C_L = 0.1\mu\text{F} \quad C_H = 0.01\mu\text{F}$$

Ans

$$V_{out} = \left(\frac{X_C}{X_C + R} \right) \cdot V_{in}$$

$$(f_c)_L = \frac{1}{2\pi R C} = \frac{1}{6.28 \times 16 \times 10^2 \times 10^{-8}} = 995.2 \text{ Hz}$$

$$(f_c)_H = \frac{1}{6.28 \times 10^4 \times 10^{-8}} = 1592.3 \text{ Hz}$$



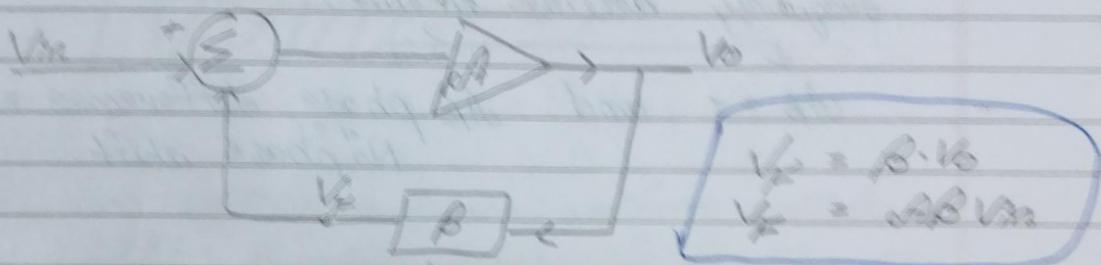
$$\omega_0 - \omega_1 = \omega_{\text{RF}}$$

- i) Oscillator:
- ii) It is an electronic circuit used to generate an op-amp oscillator with desired frequency from a dc signal.
- iii) I can generate frequency of few Hz to GHz.

Oscillator \rightarrow Amplifier \rightarrow AC op-amp

with desired frequency

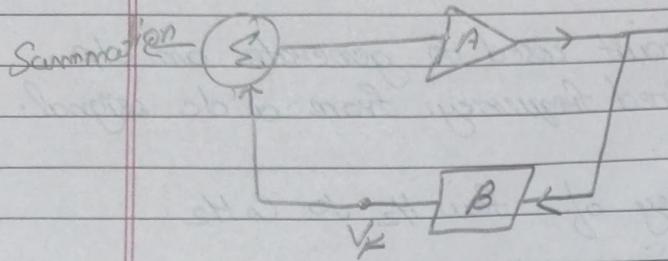
- iv) Oscillator is an amplifier with positive feedback.



Feedback \rightarrow Frequency selective circuit

B = Feedback fraction i.e. it is what fraction of op-amp signal will be given to IP of feedback circuit

When there's no o/p signal there'll be oscillations in o/p due to thermal noise.

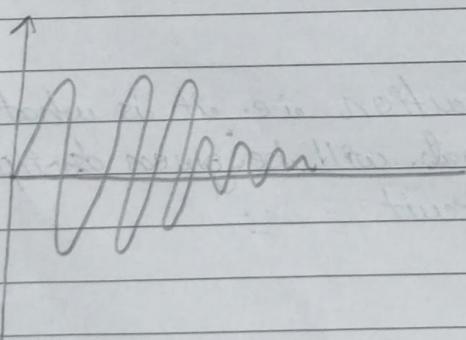


AB is the loop gain & o/p depends on this AB .

Only particular frequency will be selected on basis of AB . Only some signal with particular frequency will be passes through frequency selective circuit.

$AB = 1$ and AB phase difference = 0
No phase shift.

If $AB < 1$



If $AB < 1$, over a period of time, oscillation will die out i.e. damping.

$$AB = 0.9$$

$$V_{in} = 2V$$

$$V_F = AB V_{in} = 1.8$$

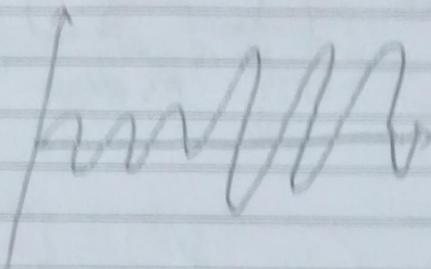
$$V_F = 1.8 \times 0.9 = 1.62$$

$$V_F = 1.62 \times 0.9 = 1.458$$

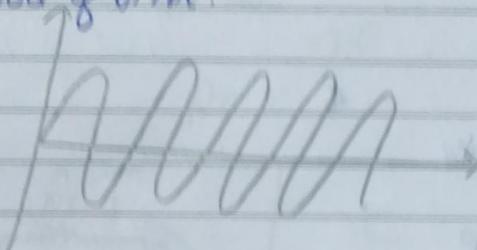
Over a period of time if there are alternating effects
will die out over a period of time.

ii) if $AB > 1$

if there are increasing



iii) if $AB = 1$, the oscillation is sustained for the period of time.



The two criteria do have uniform oscillation:

$$|AB| = \pm$$

? Barkhausen

$$\angle AB = 0^\circ \text{ (Phase Diff} = 0\text{)} \quad ? \text{ Cutters}$$

* feedback circuit can be made of RC, RL or RLC components

-> Types of oscillator based on feedback circuit:

i) RC

? sinusoidal oscillation

ii) RL

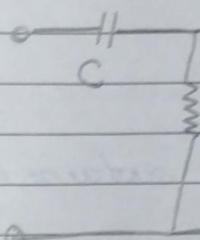
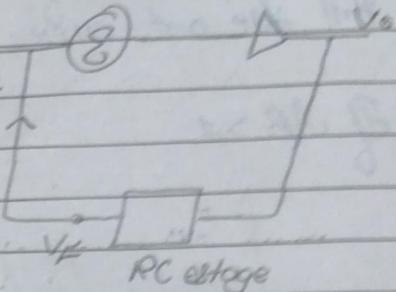
?

iii) Crystal oscillator ?

iv) Relaxation oscillator \rightarrow non-sinusoidal oscillation

• RC Phase Shift oscillator :

- i) At the no feedback op is of 180° . i.e. phase shift = 180°
- ii) RC circuit should induce 180° phase shift for sustain ability.



→ HPF or Phase lead circuit

as op decide the op signal

$$\frac{V_o}{V_{in}} = \frac{R}{R - jX_C}$$

$$\frac{V_o}{V_{in}} = \frac{R}{R - j\omega C}$$

$$\frac{V_o}{V_{in}} = \frac{R\omega C}{R\omega C - j} = \frac{1}{1 - j \frac{1}{R\omega C}}$$

$$\angle \phi = -\tan^{-1} \left(-\frac{1}{\omega CR} \right)$$

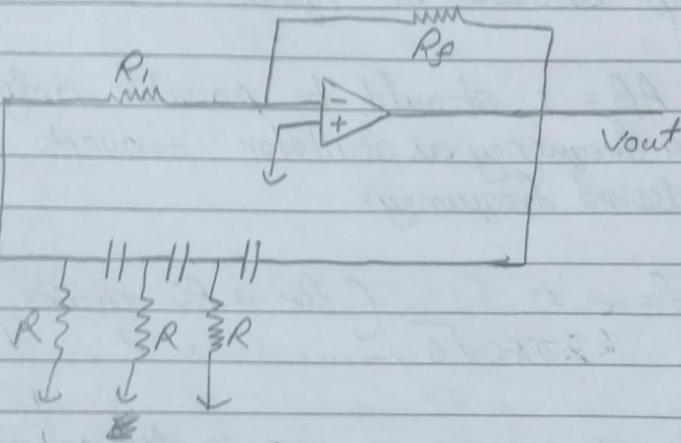
$$\angle \phi = \tan^{-1} \left(\frac{1}{\omega CR} \right)$$

$$\angle \phi = \tan^{-1} \left(\frac{X_C}{R} \right)$$

X_C very small $\angle \phi = 0^\circ$

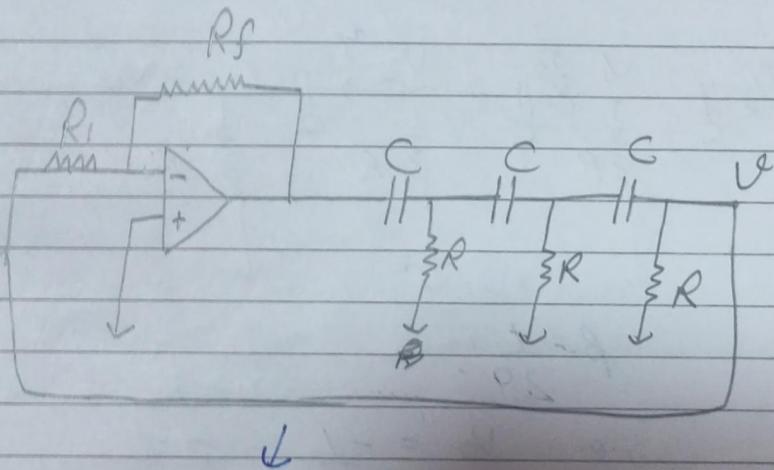
$R = 0, \angle \phi = 90^\circ$

So we cascade two RC circuits to get $180^\circ \text{ phase shift}$.
 This is theoretically correct but in actual we get three RC phase shift.



Practically one RC gives 60° phase diff.
 so three RC = 180°

OR



$$\angle AFB = 0$$

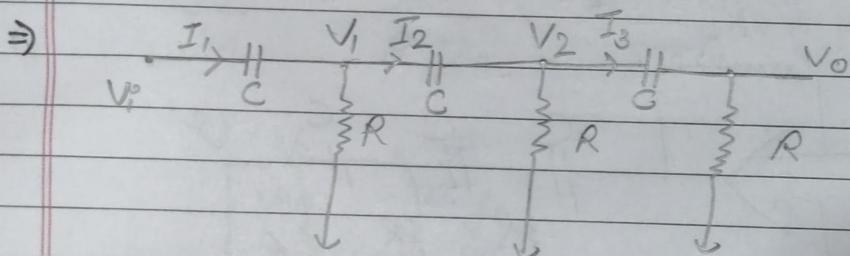
$\Rightarrow \beta = \frac{1}{29}$ i.e. the attenuation (loss of signal) produced by the feedback circuit (for this circuit) -RC

$$\text{so } A = 29$$

- \Rightarrow In RC phase shift oscillator, the attenuation introduced by feedback oscillator is $1/29$.
- \Rightarrow In order to get the unity gain the gain i.e. provided by op-amp should be equal to 29.
- * $\angle AB = 0$ & $AB = 1$ should be possible only at a particular frequency at oscillator converts DC to AC with desired frequency.

$$f = \frac{1}{2\pi RC \sqrt{6}} \quad (\text{for } 3 \text{ RC circuits})$$

$$f = \frac{1}{2\pi RC \sqrt{2n}} \quad , n \text{ is the no. of Phase lead circuit}$$



$$\beta = \frac{1}{29}$$

$$\text{i.e. } \frac{V_o}{V_i} = -\frac{1}{29}$$

Proof:

At node V_2 ,

$$V_2 = (-jI_2 \times C) + V_o$$

$$V_o = I_2 R$$

$$I_2 = \frac{V_o}{R}$$

$$V_2 = \left(-j \frac{V_o}{R} \times C \right) + V_o$$

$$C = \frac{1}{\omega_C}$$

$$V_2 = \left(-j \frac{V_o}{R} \frac{1}{\omega_C} \right) + V_o$$

$$V_2 = V_o - j \frac{V_o \cdot 1}{R \omega_C} \times j \frac{1}{\omega_C}$$

$$V_2 = V_o + \frac{V_o}{j R \omega_C}$$

$$V_2 = V_o \left[1 + \frac{1}{j R \omega_C} \right]$$

Apply KCL at V_2 ,

$$I_2 = \frac{V_2}{R} + I_3$$

$$I_2 = \frac{V_o}{R} \left[1 + \frac{1}{j R \omega_C} + 1 \right] \quad \left[\because I_3 = \frac{V_o}{R} \right]$$

$$I_2 = \frac{V_o}{R} \left[2 + \frac{1}{j R \omega_C} \right]$$

At node V_1

$$V_1 = V_2 + I_2$$

$$= V_o \left[1 + \frac{1}{j R \omega_C} \right] + \frac{V_o}{R} \left[2 + \frac{1}{j R \omega_C} \times \frac{1}{j R \omega_C} \right]$$

$$= V_0 \left[1 + \frac{3}{j\omega CR} + \frac{2}{j\omega CR} - \frac{1}{\omega^2 C^2 R^2} \right]$$

$$V_I = V_0 \left[1 + \frac{3}{j\omega CR} - \frac{1}{\omega^2 C^2 R^2} \right]$$

Applying KCL at V_I

$$I_1 = \frac{V_I}{R} + I_2$$

$$I_1 = \frac{V_0}{R} \left[1 + \frac{3}{j\omega CR} - \frac{1}{\omega^2 C^2 R^2} \right] + \frac{V_0}{R} \left[\frac{2+1}{j\omega CR} \right]$$

$$= \frac{V_0}{R} \left[3 + \frac{4}{j\omega CR} - \frac{1}{\omega^2 C^2 R^2} \right]$$

$$V_I^o = V_I + \frac{I_L}{j\omega C}$$

$$= V_0 \left[1 + \frac{3}{j\omega CR} - \frac{1}{\omega^2 C^2 R^2} \right] + \frac{V_0}{R} \left[3 + \frac{4}{j\omega CR} - \frac{1}{\omega^2 C^2 R^2} \right] \times \frac{1}{j\omega C}$$

$$= V_0 \left[1 + \frac{3}{j\omega CR} - \frac{1}{\omega^2 C^2 R^2} + \frac{3}{j\omega CR} + \frac{-4}{\omega^2 C^2 R^2} - \frac{1}{j\omega^3 C^3 R^3} \right]$$

$$V_I^o = V_0 \left[1 + \frac{6}{j\omega CR} - \frac{5}{\omega^2 C^2 R^2} - \frac{1}{j\omega^3 C^3 R^3} \right]$$

$$\text{So } I_{\text{mg}} = 0$$

$$\frac{6}{wCR} - \frac{6}{w^3 C^3 R^3} = 0$$

$$6 = \frac{1}{w^2 C^2 R^2}$$

$$w = \frac{RC}{\sqrt{6}}$$

$$\text{So } f = \frac{1}{2\pi RC\sqrt{6}}$$

$$\text{So } I_{\text{mg}} = 0$$

So

$$V_i = V_0 \left[1 - \frac{5}{GR^2C^2 \times R^2C^2} \right]$$

$$V_i = V_0 \left[\frac{1}{R^2C^2} \right]$$

$$V_i = V_0 \left[1 - \frac{5}{GR^2C^2} \times \frac{1}{R^2C^2} \right]$$

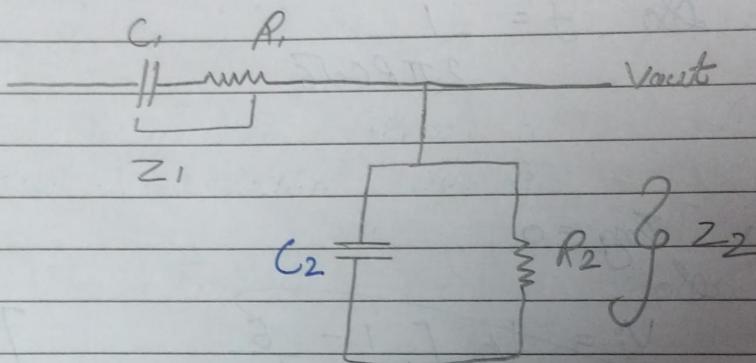
$$V_i = V_0 [1 - 30]$$

$$\frac{V_0}{V_i} = \frac{-1}{29}$$

• Wien Bridge Frequency oscillator:

$$f_c = \frac{1}{2\pi\sqrt{R_1 R_2 C_1 C_2}}$$

$$\beta = \frac{1}{3}$$



$$V_o = \frac{z_2}{z_1 + z_2} \cdot V_{in}$$

$$z_2 = R_2 \parallel \frac{1}{j\omega C_2} \Rightarrow \frac{R_2}{j\omega C_2}$$

$$z_1 = R_1 + \frac{1}{j\omega C_1} \Rightarrow \frac{j\omega C_1}{R_1 + \frac{1}{j\omega C_1}} = \frac{j\omega C_1}{j\omega C_1 + R_1}$$

$$\frac{R_2}{j\omega C_2 + 1}$$

$$\frac{R_2}{j\omega C_2 + 1}$$

$$\frac{V_o}{V_{in}} = \frac{\frac{R_2}{R_2 j\omega C_2 + 1}}{\frac{R_2}{R_2 j\omega C_2 + 1} + \frac{R_1 j\omega C_1 + 1}{j\omega C_1}}$$

$$= \frac{\frac{R_2}{R_2 j\omega C_2 + 1}}{\frac{R_2 j\omega C_1 + 1 - R_1 R_2 \omega^2 C_1 C_2 + R_2 j\omega C_2 + 1}{(R_2 j\omega C_2 + 1) C_1 j\omega C_1}}$$

$$\frac{V_o}{V_i} = \frac{\frac{R_2 j\omega C_1}{R_2 j\omega C_1 + 1 - R_1 R_2 \omega^2 C_1 C_2 + R_2 j\omega C_2 + R_1 j\omega C_1}}{+ 1}$$

$$\frac{V_o}{V_i} = \frac{R_2 j\omega C_1}{1 - \omega^2 R_1 R_2 C_1 C_2 + j\omega [R_2 C_2 + R_1 C_1] + R_1 C_1}$$

~~R₁C₁~~

We know that phase shift = 0

~~R₂jωC₁~~ So 1 - ω²R₁R₂C₁C₂ = 0

As phase shift = 0

$$\text{So } 1 - \omega^2 R_1 R_2 C_1 C_2 = 0$$

$$1 = \omega^2 R_1 R_2 C_1 C_2$$

$$\omega^2 = \frac{1}{R_1 R_2 C_1 C_2}$$

$$\omega = \frac{1}{\sqrt{R_1 R_2 C_1 C_2}}$$

$$f = \frac{1}{2\pi\sqrt{R_1 R_2 C_1 C_2}}$$

$$\frac{V_o}{V_i} = \frac{R_2 C_1}{R_1 C_1 + R_2 C_2 + R_3 C_1}$$

If $R_1 = R_2$ and $C_1 = C_2$

$$\frac{V_o}{V_i} = \frac{R \cdot C}{3RC}$$

$$\boxed{\beta = \frac{V_o}{V_i} = \frac{1}{3}}$$

- Multivibrator:

It is an electronic oscillator that produces non-sinusoidal oscillations like triangular, square, etc.

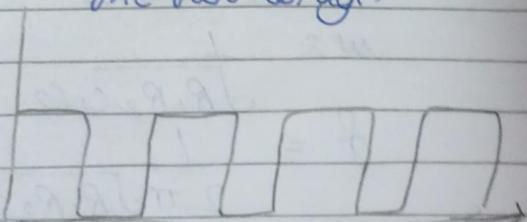
~~Q5~~ Two state solid devices: Two reference voltages in a device.

It is used to implement two state solid devices.

Three types:

1. Astable
2. Hysteretic
3. Bistable

Astable: O/P will keep on changing b/w the two states i.e. o/p not stable at any of the two stage.



555 IC timer is a type of relaxation oscillator for generating stabilised square off waveform of either a fixed frequency of upto 500 KHz or varied due to cycles from 50 to 100%.