

```
>> F=@(t,theta)-0.5*(theta)
```

```
F =
```

```
function_handle with value:
```

```
@(t,theta)-0.5*(theta)
```

```
>> theta0=100
```

```
theta0 =
```

```
100
```

```
>> t0=0
```

```
t0 =
```

```
0
```

```
>> tf=5
```

```
tf =
```

```
5
```

```
>> (theta)exact=100*exp(-2.5)
```

```
(theta)exact=100*exp(-2.5)
```

```
↑
```

Invalid expression. Check for missing multiplication operator, missing or unbalanced delimiters, or other syntax error. To construct matrices, use brackets instead of parentheses. ✓

Did you mean:

```
>> exact=100*exp(-2.5)
```

```
exact =
```

```
8.2085
```

```
>> %(d) RK2 method:
```

```
>> h= 0.1
```

```
h =
```

```
0.1000
```

```
>> Thetah=ode2(F,t0,h,tf,theta0) %Theta at h= delta t
```

```
Thetah =
```

---

```
100.0000
 95.1250
 90.4877
 86.0764
 81.8802
 77.8885
 74.0914
 70.4795
 67.0436
 63.7752
 60.6662
 57.7087
 54.8954
 52.2193
 49.6736
 47.2520
 44.9484
 42.7572
 40.6728
 38.6900
 36.8039
 35.0097
 33.3030
 31.6794
 30.1351
 28.6660
 27.2685
 25.9392
 24.6746
 23.4717
 22.3275
 21.2390
 20.2036
 19.2187
 18.2818
 17.3906
 16.5428
 15.7363
 14.9692
 14.2394
 13.5452
 12.8849
 12.2568
 11.6593
 11.0909
 10.5502
 10.0359
  9.5466
  9.0812
```

```
8.6385
8.2174
```

```
>> Eh=8.2174-(exact) %the E value at delta t
```

```
Eh =
```

```
0.0089
```

```
>> Theta2h=ode2(F,t0,2*h,tf,theta0) %Theta at h= 2*(delta t)
```

```
Theta2h =
```

```
100.0000
90.5000
81.9025
74.1218
67.0802
60.7076
54.9404
49.7210
44.9975
40.7228
36.8541
33.3530
30.1844
27.3169
24.7218
22.3732
20.2478
18.3242
16.5834
15.0080
13.5822
12.2919
11.1242
10.0674
9.1110
8.2455
```

```
>> E2h=8.2455-(exact) %the E value at 2*(delta t)
```

```
E2h =
```

```
0.0370
```

```
>> n=ln((Eh)/(E2h))/ln(0.5)
```

```
Unrecognized function or variable 'ln'.
```

```
>> n=log((Eh)/(E2h))/log(0.5)
```

n =

2.0556

```
>> truncation_error= (h)^n
```

Unrecognized function or variable 'truncation'.

```
>> truncation_error = (h)^n
```

truncation\_error =

0.0088

```
>> truncation_error = truncation_error_RK2
```

Unrecognized function or variable 'truncation\_error\_RK2'.

```
>> %(e) using RK4
```

```
>> h= 0.1
```

h =

0.1000

```
>> Thetah=ode4(F,t0,h,tf,theta0) %Theta at h= delta t
```

Thetah =

100.0000

95.1026

90.4451

86.0156

81.8031

77.7969

73.9869

70.3635

66.9175

63.6403

60.5236

57.5595

54.7406

52.0598

49.5102

47.0855

44.7795

42.5865

40.5009

38.5174

36.6311

34.8371

```
33.1310
31.5084
29.9653
28.4978
27.1022
25.7749
24.5126
23.3121
22.1704
21.0847
20.0521
19.0700
18.1361
17.2479
16.4032
15.5999
14.8359
14.1093
13.4183
12.7612
12.1362
11.5419
10.9766
10.4391
9.9278
9.4416
8.9792
8.5395
8.1213
```

```
>> Eh=mod(8.1213-(exact)) %the E value at delta t
Error using mod
Not enough input arguments.
```

```
>> Eh=abs(8.1213-(exact)) %the E value at delta t
```

```
Eh =
```

```
0.0872
```

```
>> Theta2h=ode4(F,t0,2*h,tf,theta0) %Theta at h= 2*(delta t)
```

```
Theta2h =
```

```
100.0000
90.4044
81.7295
73.8871
66.7971
60.3875
```

```
54.5930
49.3544
44.6186
40.3371
36.4665
32.9673
29.8039
26.9440
24.3586
22.0212
19.9082
17.9978
16.2708
14.7096
13.2981
12.0220
10.8685
9.8256
8.8827
8.0304
```

```
>> E2h=abs(8.0304-(exact)) %the E value at 2*(delta t)
```

```
E2h =
```

```
0.1781
```

```
>> n=log((Eh)/(E2h))/log(0.5)
```

```
n =
```

```
1.0303
```

```
>> truncation_error_RK4 = (h)^n
```

```
truncation_error_RK4 =
```

```
0.0933
```

```
>> %explicit euler method:
```

```
>> Thetah=ode1(F,t0,h,tf,theta0) %Theta at h= delta t
```

```
Thetah =
```

```
100.0000
95.0000
95.2500
95.2375
95.2381
95.2381
```

```
>> Theta2h=ode1(F,t0,2*h,tf,theta0) %Theta at h= 2*(delta t)
```

```
Theta2h =
```

```
100.0000  
90.0000  
91.0000  
90.9000  
90.9100  
90.9090
```

```
>> Eh=mod(95.2381-(exact)) %the E value at delta t
```

```
Error using mod  
Not enough input arguments.
```

```
>> Eh=abs(95.2381-(exact)) %the E value at delta t
```

```
Eh =
```

```
87.0296
```

```
>> E2h=abs(90.9090-(exact)) %the E value at 2*(delta t)
```

```
E2h =
```

```
82.7005
```

```
>> n=log((Eh)/(E2h))/log(0.5)
```

```
n =
```

```
-0.0736
```

```
>> truncation_error_Euler = (h)^n
```

```
truncation_error_Euler =
```

```
1.1847
```

```
>>
```