

Lab Notes for Compressed Sensing Coding

Anthony Salerno

March 23, 2015

Contents

1	Proof of Principle (02.17.15 - 02.23.15)	2
1.1	Preamble...	2
1.1.1	Hypothesis	2
1.1.2	Notes - Unpolished	2
1.2	Simulations	4
1.2.1	Preamble	4
1.3	Hypothesis	4
2	Analysis of CS Code – Sanity Check (03.10.15)	5
2.1	Preamble...	5
2.2	Down-sampling	5
3	Simulations - (03.11.15)	7
3.1	Preamble	7
3.2	Hypothesis	7
3.3	Results	7
3.3.1	Numerical Simulations	7
3.3.2	Brain Data	7
3.4	Discussion	7

1 Proof of Principle (02.17.15 - 02.23.15)

Introduction

Beginning work on the “Proof of Principle” as per the 12.19.14 Meeting Notes - Plan 2

The notes state that we are to:

- Pick one slice - extract slice from dataset with FT on RO (i.e. in dim space) and no FT on PE1 and PE2 (aka PE and SL)
- Isotropic undersampling (I think this is a bad idea)
- Recon slices independently with Lustig code (using $\lambda_2 psi[m] + \lambda_1 TV[m]$)
- Add a directional similarity term to the recon (so we can recon similar slices simultaneously) ($\lambda_3 ||m_j - m_k||_2 f(\vec{d}_j \cdot \vec{d}_k)$)
- However, the form of $f((\vec{d}_j \cdot \vec{d}_k))$ is still unknown

Note that the git repository for this work can be found at <https://github.com/aasalerno/Lustig>. For pre-emptive notes on the code that Lustig wrote, please see `demo_SheppLoganTV_Notes.txt`.

1.1 Preamble...

1.1.1 Hypothesis

To begin, today we should be able to get a decent code running that can do Lustig’s code on any specified slice that we choose. I expect that the code will work as expected and provide a good rendition of the undersampled data with minimal alterations required. The hope is that we can use the basis of the code as an engine (that will need some optimization) in order to work with the data as we so hope.

1.1.2 Notes - Unpolished

First spent a ridiculous amount of time getting L^AT_EXup and running on this computer... But it works now!

The code is written both on my computer as well as on the lab computers – via a central git on github – using the same datasets as required. The datasets in use are Jacob’s data, reconstructed purely using the standard recon algorithm (that is, no MATLAB involved).

For all pushes and pulls, see the github repository. There are many (and it can be mapped by day!)

The code is to be written such that it is built and any values that are above 1-sampFac will be included. This means that when we are actually tacking on the r correction, we need to do it as $1 - \frac{r}{\max(r)}$

Seem to have a problem with the values that I’m getting. The outer portions of k-space seem to have almost no chance of being chosen. With a penalty threshold of only 0.25 (given a sampFac of 0.5), only 40% of values are chosen. Most of the lost points are on the corners of k -space, so this may be ok... However, I need to look into **possibly making the CS type sequence specific, for things like cylindrical acquisition.**

Date: 02/20/15

As of about 11:00 (commit 6a9cfb111c508df0af9a7222ba277ef118ba147), the code `testMap.m` is up and running. It will be used in order to actually build the map of what we are undersampling and then this will be pumped into an adapted version of Lustig's code in order to get it up and running.

Encountered a bit of an issue with how the data is obtained. Since this information is only the magnitude of the data, I'm going to make a version that can handle taking the real and imaginary parts of the data, then feeding that through to the next set of functions.

As of 12:08 PM, functionality has been added for the function to handle two files containing the real and imaginary parts of the k -space information!

Now, we want to add in the CS part of the code. Here is where things become a little painful, but we can look at the datasets and actually do what is done in CS.

For some unapparent reason, the code doesn't seem to want to work. This is really annoying and irritating as the error seems to be stemming from the raw files, which may render a tonne of previous work that I've done utterly useless. Ok, scratch that – the issue was my method of plotting. I wasn't plotting the abs of the data.

As of about 5:00 it is working. I'm going to git push it and go home.

Date: 02/23/15

Upon a first look at the code that I wrote last week (adapted from `demo_SheppLoganTV.m`, the code doesn't seem to have too great of an effect. The differences between the “im_dc” (density corrected original) and the CS reconstructed data is on the order of 10^{-9} , when the data is on the order of 1.

- One of the first things that I should try is to change the TV and L1 penalties as they are currently set to 0.01 each. This may be too low to have an effect on real data – the code that I am adapting from is using a numerical phantom.
- The next step would be to try different slices or different data. Perhaps the noisiness of this data is causing a problem, but can be fixed with some more phase corrections.

I changed the values of the two penalties (λ_1 and λ_2), increasing them by a factor of 10, each becoming 0.1. The overall residual became a little bit larger, but is still on the order of 10^{-9} , which is negligible.

In order to make the data make a bit more sense (i.e. make sure I'm not making a stupid mistake on how I'm building the filter, etc) I'm going to use Lustig's method of building the undersampling pattern.

I changed the code `testMap.m` pretty substantially, so see github for a previous version. The alterations were made to try and use the other undersampling pattern. One thing that I may do later is alter Lustig's PDF that is produced by tacking on the directionality afterwards.

After changing to Lustig's method of undersampling, we see some bigger differences, but, the undersampling kind of makes it look pretty bad. It may be how the FT (using this ‘p2DFT’) instead of just doing an FFT as it is done in MATLAB. This seems like something weird that they don't need to do, as it just makes the data look bad... Though there must be a reason for this

As it stands – 4:00PM 02/23/15 – this is as far as I can go without further understanding how well everything is going to work for the perpendicular and parallel to the gradient direction for the undersampling technique.

1.2 Simulations

1.2.1 Preamble

Here what we want to ensure is that by applying specific filters, we are obtaining what we expect. The expectation is that using a mask that is parallel to the gradient direction (applied in k -space) is going to look significantly worse than a mask applied perpendicular to the gradient direction.

1.3 Hypothesis

Using a simulation, we will be able to tell distinct differences between the use of the two different maps. The map using a perpendicular mask on the undersampled k -space will look better than the data undersampled using the parallel mask, as the smearing will not be as bad in the cross direction of the diffusion.

The code is written in `buildLambda.m`. It is currently built just to handle a 2D case and then *eventually* handled to build a 3D. In order to make it work with the code, an idea is to make it have a z -stack (in our case, a y stack, or a ‘read-out’ stack).

2 Analysis of CS Code – Sanity Check (03.10.15)

Date: 03/10/15

2.1 Preamble...

As of this point, I've finally given my seminar (which apparently went well!) and now, I'm trying to see if there's something inherently wrong with how I'm running my CS codes, as they aren't producing the effects that I would expect. The noise looks *really* weird, and isn't how I'd expect it to be.

So, for today, we are going to change things up a bit, and move on to try and understand exactly what's happening in this code – I will try to include figures where I believe it makes sense due to the simplicity of doing so.

In order to simplify things, I made a file using the raw data from Jacob's Diffusion Weighted Imaging data taken on July 29, 2014. The raw data files are located in `/projects/muisjes/asalerno/CS/data`. Specifically we are using brain 10, direction 32. This brain was chosen to be the simplest of cases, as this is a b_0 scan, thus there is no expected major differences because of the lack of diffusion weighting.

2.2 Down-sampling

One *major* thing to note is the effect that down-sampling has. We can see it here:

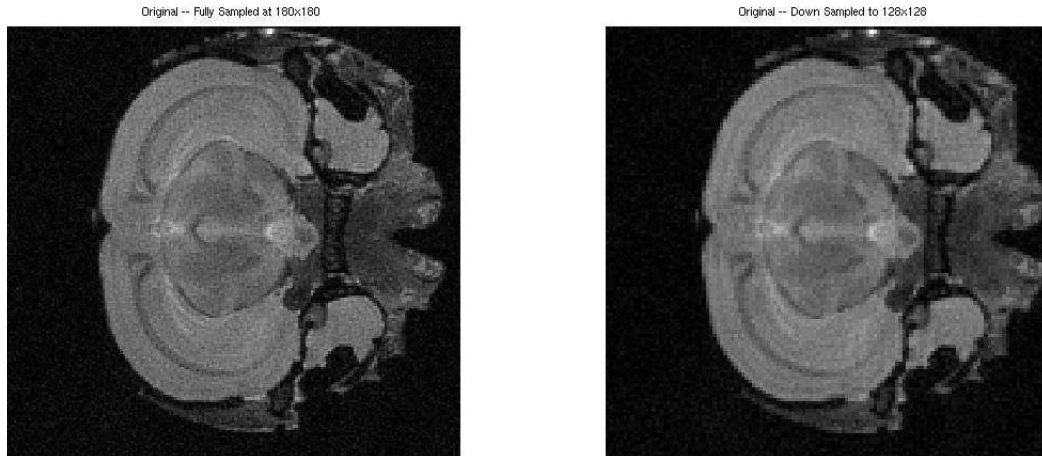


Figure 1: We can see the significant blurring effect that downsampling the figure to be 128x128 has. The blurring cannot be fixed, as in order to do this, we must sacrifice some higher spatial frequency information. Note that this is using MATLAB blurring. This is explained further in the next section and figure 2.

The downsampling is absolutely required because of how the wavelet transform is done. The 2D Wavelet transform has a 2^n size requirement in order to work (Lustig 2007, Yang 2015). We don't particularly care about the number of slices being 2^n as this will be fully sampled anyway.

It seems like MATLAB does something a little weird with how it downsamples the FFT... It produces what looks like just a blurred copy of the image (as seen above) but it doesn't seem to get the data from the center, but `instbuildLambdaead` chooses the data in the top right section (before shifting) preferentially. This can be seen in Figure 2.

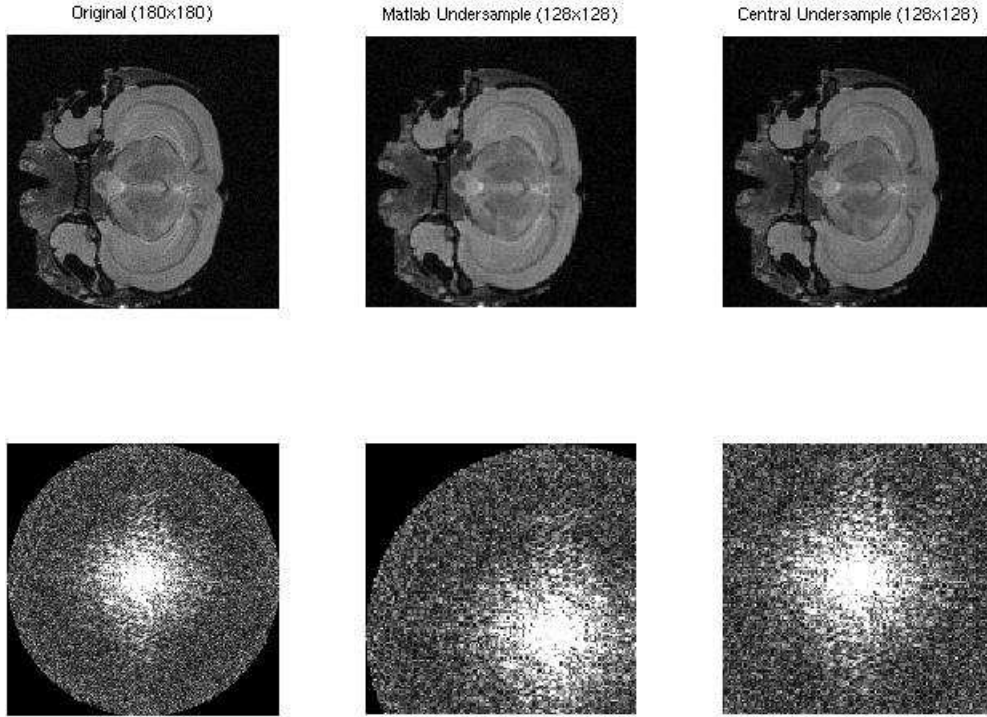


Figure 2: In this figure, we see some small differences between the method of undersampling done in MATLAB vs a logical undersampling method that takes the data from the center of k -space. All data here taken from slice 150 *after* doing a 1D FFT in the readout direction.

We can see in the above figure that MATLAB does something really weird and so, we will be using my method in order to do reconstructions that alter the number of voxels per dimension.

In order to make sure that we're using the right one, the file we must use is `kspaceDS.10.32.mat`, as this is the dataset that has been undersampled properly. For this work, what we will do right now, is look at how we can try to do a reconstruction properly using compressed sensing. We may be able to do this logically using some of the existing work here. In the angiography case, they use the previous slice as the base image as "not much is expected to change". We can do better than this, as we can try to do a combined reconstruction, where the b_0 average of the same slice (to start) would be the same.

3 Simulations - (03.11.15)

03.23.15 (work completed on and before 03.19.15)

3.1 Preamble

The point of running this simulation is to see what the best undersampling method to use would be. Our plan of attack is to do this experiment two fold, firstly with purely numerical data – i.e. a “phantom” that I design, and then afterwards using true brain data and seeing if we can get an understanding of what the best method would be.

Some of this information is noted at an earlier point in time,

3.2 Hypothesis

The expectation is that the best style would be to use the “parallel to the gradient direction” as this will give us the sharpest edge information in order to tell a cross section of the fibres that we are expecting to see. The worst should be the “perpendicular” case. It is noted that our nomenclature from before was misleading.

In order to ensure that we have it correctly, the following figure explains what is meant by each.

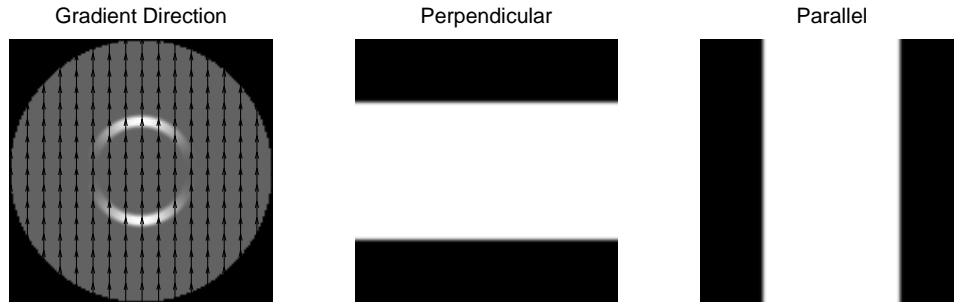


Figure 3: We can see the direction of the gradient in the left-most panel, and the definitions of the others. The parallel will give us the “cross-fibre” information mostly, and the perpendicular will give us the “along the fibre” information.

3.3 Results

3.3.1 Numerical Simulations

3.3.2 Brain Data

3.4 Discussion

Surprisingly, we didn’t particularly get what we expected. When running the simulation for the numerical phantom, the data didn’t seem very different at all – at least when comparing FA values. The data actually gave us results that were confounding... When being compared to the “standard” methods of undersampling (i.e. Circular or low resolution undersampling), the parallel and perpendicular cases fell through and were not effective. However, we may be able to find some “happy medium”, as there may be an elliptical technique that has the lower RMS error of the circular technique, but the specificity of the directionally specific techniques.