1. Show that every function defined by,

$$f(x) = 2 + ce^{-2x^2}$$
 (CO4)

Where c is an arbitrary constant, is a solution of the differential equation,

$$\frac{dy}{dx} + 4xy = 8x$$

2. Find the explicit solution of the initial value problem

$$\frac{dy}{dx} = -\frac{x}{y}, \quad y(3) = 4$$

Given that the differential equation has a one-parameter family of solutions which may be written in the form,

$$x^2+y^2=\ c^2$$

$$y^2 dx + (3xy-1) dy = 0, x(-1) = \frac{1}{2}$$