

B. Sc. in EEE/TVE (2nd Year)
2nd Semester

Date: 12 April, 2022
Time: 10:00 am - 1:00 pm

ISLAMIC UNIVERSITY OF TECHNOLOGY (IUT)
ORGANISATION OF ISLAMIC COOPERATION (OIC)
DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING

Semester Final Examination
Course Number: Math 4221/Math 4629
Course Title: Mathematics III

Summer Semester : 2020 - 2021
Full Marks: 150
Time : 3.0 Hours

There are 06 (six) questions. Answer 06 (six) questions. The symbols have their usual meanings. Marks of each question and corresponding CO and PO are written in the brackets.

1. (a) Explain the physical significance of the divergence and curl of a vector. (12)
(CO1)
(PO1)
(b) Evaluate $\int_C \vec{F} \cdot d\vec{r}$ where C is the closed curve formed by $y=2x^2$ and $y^2=32x$ and $\vec{F}=(2x+y^2)\mathbf{i}+(3y-4x)\mathbf{j}$. (13)
(CO1)
(PO1)
2. (a) State and prove Cauchy's theorem in the plane. (12)
(CO2)
(PO2)
(b) Differentiate $f(z)=z^2-iz$ along the straight line parallel to $y=x$ (13)
(CO2)
(PO2)
3. (a) Obtain the formula to solve the equation $z^n=z_0$. Use this formula to find the roots of $z^8 = -16\sqrt{3} - 16i$ and locate them graphically. (12)
(CO1)
(PO1)
(b) Determine the region of the w plane into which the interior of the triangle $x=1$, $y=1$ and $y=-2x+1$ is mapped by the transformation $w = 5e^{\frac{i\pi}{3}}z - 2 + 4i$ (13)
(CO2)
(PO2)
4. (a) Derive Cauchy Riemann equations and find the polar form. (12)
(CO1)
(PO1)
(b) Find the Taylor series expansion for the function $f(z)=\operatorname{cosec}^2 z$ about $z = \frac{\pi}{2}$. (13)
(CO2)
(PO2)

5. (a) State Cauchy's residue theorem. Find the residue of $f(z) = \frac{z^2 - 2z}{(z^2 + 4)^3}$ (12)
at all poles and hence evaluate the integral $\int_C f(z) dz$ where C is the circle (CO1)
 $|z - i| = 2$ (PO1)

(b) From the following data find X when Y=6

(13)
(CO3)
(PO12)

X	2.3	2.5	3.9	3.6	4.1	3.2	1.4	1.1
Y	8.6	8.1	7.6	7.8	7.4	6.6	5.2	6.1

6. (a) Explain Binomial distribution and Poisson's distribution. (12)
Fifteen percent of the tools produced in a certain manufacturing process turn (CO3)
out to be defective. Find the probability that in a sample of 12 tools chosen at (PO12)
random (i) more than ten (ii) at least two will be defective by using Poisson's
distribution.
- (b) Find the area bounded by the normal curve and the horizontal axis. (13)
A manufacturer knows from experience that the resistance of resistors is (CO3)
normally distributed with mean 100 ohms and standard deviation 2 ohms. (PO12)
What percentage of resistors will have resistance between 99 ohms and 103
ohms?

$$\frac{z - \bar{x}}{s} = \frac{z - 2.2}{(2.2)^2}$$

$$\frac{x - \bar{x}}{s} = \frac{x - 2.2}{(2.2)^2}$$