# E.G.S.Pillay Engineering College

An Autonomous Institution Affiliated to Anna University,
Chennai | Approved by AICTE, New DelhiAccredited by NAAC
with A++ Grade | Accredited by NBA T1 (B.E. - CSE, B.E. - ECE

Academic Year: 2025-26 |Odd Semester|3"SemesterB.TECH Programs |Regulation: 2023

# Department of Artificial Intelligence and Data science COURSEPLAN

### COURSE SUMMARY

Course Code & Name:	2301MA301-Probability and Statistics
Semester:	III(03)
Credit Hours:	45(T)+ 15(TU)= 60Sessions (LTPC:3104)
Course Ouration:	July 2024toNov2024
Course Instructor/Coordinator:	Mrs.D.Anandhi (anandhi@egspec.org)
Domain Coordinator:	<u>Or.R.Deepa (deepa.ar@egspec.org)</u>
Course Type:	Theory
Core/Elective:	Core
Prerequisites:	2301MA102 - Engineering
	Mathematics-I 2301MA202-
	Engineering Mathematics-
	II
Course	The basic analytical concepts of probability
Description:	theory, statistical design of experiments and data
	analysis
	Probability Distribution is a key concept in
	machine learning, data engineering, and artificial
	intelligence.
	It enables businesses to make informed decisions
	based on the data available, and is used to create
	predictive models that can make predictions about future events.
	Now that data science receives a lot of attention, the
	three disciplines of data analysis, databases, and
	sciences are discussed with respect to the roles they
	play.
	In several discussions, I observed misunderstandings
	of Artificial Intelligence.
	Hence, it might be the right time to give a personal
	view of AI and the part of machine learning therein.

Since the relation between machine learning and statistics is so close that sometimes the boundaries are blurred, explicit pointers to statistical research are made.

Course Objectives:	<ol> <li>To introduce the basic concepts of probability and random variables</li> <li>To acquaint the knowledge of testing of hypothesis for small and large samples this plays an important role in real life problems</li> <li>To impart knowledge of handling random vectors which represent random variables in multidimensional</li> </ol>
Course	Use the fundamental concepts of probability
Outcomes(Statements)CO1:	and have knowledge of standard distributions
	which can describe
	real life phenomenon.(K3)
co2:	Apply the basic concept of one and two dimensional random variables in engineering applications.(K3)
CO3:	Simulate the concept of testing of hypothesis for small and large samples in real life problems.(K3).
CO4:	Apply the basic concepts of classifications of design of experiments in the field of statistical quality control (K3).
CO5:	Develop exposure to the principal component analysis of random vectors and time series. (K3)
Mapping POs/PSOs	

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4(L3 )	3	2	1	-	-	-	-	-	-	-	1		-	-	-
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C	ourse			t &Gr	ading Policy onent	:	CAT-I	(50)	CAT			Acti v i t	Act	y-	€8 €( 10 0)
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	Slight (Low) : - POs (3,12)  PSOs (1,2)Moderate(Medium) :POs (2)
i	Substantial(High) :POs(1)

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Attainment POs/											
PSOs:											
Instruction Methods:	1. P	roblem so	lving								
	2. <b>T</b>	iscussion									
	3. <b>c</b>	ritical Thi	nking								
	4. m	lind Mapp	ing								
	ı	lipped Cla	-								
(Exposure to) Modern Tools usage:	1. P	ower point	t Presenta	tion							
	2. <b>s</b>	tatistical p	package								
Scope for Problem based Learning:	Problem	based Le	arning;Sp	ecific							
	toCO1to	CO5,studer	nts will ho	we to take	up team						
	work										
Scope for Innovative Teaching:	1. €	lipped Cla	ssroom								
	2. Id	nquiry bas	ed Learnin	ng							
Course Attainment(Benchmark)	COI	CO2	CO3	CO4	COS						
Target):											
Set Benchmark:	60	60	60	60	60						
Set Target:	65	65	65	65	65						

## SESSION- WISE PLANCOI)

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Sessi on	Cumulat ive Session No	Course Content/ Topics	Content Delivery Mechanism	Pedagogy
1	1.	Course overview, Learning outcomes	Interactive Lecture	Q&A
2	2.	Random variable	Interactive Lecture,examp Les	Active Learning, Inquiry-Based Learning
3	3.	Distribution function andProperties	Interactive Lecture,examp Les	Active Learning
4	4.	Solving problems(Tutorial	Oiscussion	Practice
5	5.	Probability mass function	Interactive Lecture,examp Les	Active Learning
6	6.	Probability density function	Interactive Lecture,examp Les	Active Learning
7	7.	Moments	Interactive Lecture,examp les	Active Learning
8	8.	Solving problems(Tutorial)	Discussion	Practice
9	9.	Binomial distributions	Interactive Lecture,examp Les	Active Learning
10	10.	Poisson distributions	Interactive Lecture,examp Les	Active Learning
11	11.	Normal distributions	Interactive Lecture,examp Les	Active Learning
12	12.	Solving problems(Tutorial)	Discussion	Practice
Asse ent Stra y:	essm iteg	CAT-I(50) CAT- II(50)	1 ,	etivity- €8€(100) (5)

Mark 16 s:	-	-	-	-
Other Assessment Strategy/ Tools:	Gormative G	ssessment(As	signment)	
MeasuringCO1attainmentthr ough:	CI€=	&€€ =	C€8=	T =

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	Med	asuring  h:	CO1a	ittainm	entthr	CI	€=		<b>s</b> €€ =		ces=		τ =	
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va	variables in engineering applications.(K3)  Contents/Topics:Module2:TWO DIMENSIONAL RANDOM VARIABLES													
	Jo fo	oint dis	tribu	tions - wo var	Margi iables	nal a Corre	nd co elatio	nditio	nal dis	tributi	ions Ex	pected	values of data only) -	
maj	pping	POs/	<b>PS</b> 0	s										
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								discus	ssion			p discuss		

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Real time Scenarios

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5	17.	Expected values of functions of two variables	o <b>f</b>	lect	ractiv ure,R narios	eal tim	e	Active learning,Grou p discussions			
6	18.	Expected values of functions of two variables	o <b>f</b>	1170C1 accide					Active learning,Group discussions		
7	19.	Solving problems(Tu	torial)	Discussion (al)					Practice		
8	20.	Correlation (f discrete data		Inte	ure, ractiv mples			Active learning,Group discussions			
9	21	regression (fo discrete data		,			Active learning, Group discussions				
10	22	Correlation a	nd	d Lecture, Interactive				Active			
		regression pro	oblems	exa	mples			learnin discuss	g,Group ions		7
11	23	Central limit theorem	t	Lect	ractiv ure, mples			Active learnin	ng,Q&A		
12	24	Solving problems(Tu	torial)	Oisc	ussion	)		Practio	e		
Assess Strate		CAT-I(50)	CAT- 11(50)		Act I(5)	ivity-	Ac II(	tivity- 5)	6860	100)	
	Mark 18 s:					5		-	20		
,	Other Assessment Strategy/ Tools:	Gorma	ative f	)ssess	ment(A	ssign	nent)				
m	easuringCO20 rough:	attainment	CI€=		see	? =	ce	S=	τ =		

### SESSION- WISEPLAN(CO3)

CO3: Simulate the concept of testing of hypothesis for small and large samples in real life problems.

Bloom's level#:BL3
Applying

### Contents/Topics: Module 3: TESTING OF HYPOTHESIS

Sampling distributions - Tests for single mean, proportion and difference of means (large and small samples) Tests for single variance and equality of variances - Chi square test for goodness of fit Independence of attributes.

Map	ping T	POs/P	80s										
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Benchmark/Target:60/65 Contact Hours: (9+3)/60 (20%contributing to the course) Cumulati Pedagogy Sessio Course Content/ Content Topics ve n Delivery Mechanism Session Иo Sampling 1 25. Active lecture, distributions Interactive learning,Group discussion discussions lecture, Active Tests for single mean 2 26. learning,Q&A Interactive discussion

3	27.	Tests for single proportion	lecture, Interactive discussion	Active learning, Group discussions
4	28.	Test for difference of means	lecture, Interactive discussion	Active learning,Group discussions
5	29.	Solving problems(Tutorial)	Discussion	Practice

6	30.	Tests for si variance	ngle	lecture, Interactive examples		Active learni	ng,Q&A	
7	31.	Test for equivariances	ality of	lecture, Interactive examples		Active learni	ng,Q&A	
8	32.	Solving problems(T	utorial)	Oiscussion		Practi	ce	
9	33.	Chi square goodness of		lecture, Interactive examples		Active learning,Q&A		
10	34.	Independen attributes.	ce of	lecture, Interactive examples		Active learning,Q&A		
11	35.	More probl on chi squa test		lecture, Interactive examples		Active learni	ng,Q&A	
		Solving problems(T	utorial)	Discussion		Practi	ce	
Asso ent Stro y:	ateg	CAT-1(50)	CAT- 11(50)	Activity- I(5)	Act II(5	ivity- i)	€8€(100)	
	Marks:	16	16	-		-	20	
1	Other Assessment Strategy/ Tools:	•	Cormative Assessment(Quiz)					
	MeasuringCO3attainmentthr ough:			8€€ =	ces	<b>:=</b>	τ =	

# SESSION-WISE PLAN(CO4)

CO4: Apply the basic concepts of classifications of design of experiments in the field of statistical quality control.	Bloom's level# :Bl3
	Applying
Contents/Topics:Module4:DESIGN OF EXPERIMENTS  One way and two way classifications Completely rando  Randomized block design Latin square design - 2 facto	omized design - orial designs.
Mapping POs/PSOs	

P 0	P02	P											
1													
3	2	1	-	-	-	-	-	-	-	1	-	-	-
Contact Hours:(9+3)/60(20%contributing to the course)									Bench	mark/	Target	:60/65	

Cumulati Pedagogy Sessio Course Content/ Content Topics ve Delivery n Mechanism Session Иo One way classifications Interactive 1 37. Q&A lecture One way classifications Discussion 2 38. Active learning,Collabo r ative problemsolving two way classifications 3 Active learning, Interactive 39. Collaborativ lecture e problemsolving two way classifications Active learning, Interactive 4 40. Collaborativ lecture e problemsolving **Discussion** Solving Practice 5 41. problems(Tutorial) Completely 6 42. Active lecture, randomized design Interactive learning ,Q discussion &A, Group discussions Completely 7 Interactive 43. Active randomized design lecture learning, Q&A, Group discussions Randomized block Interactive Active learning, 8 44. design Q&A, lecture Group discussion S 9 45. Discussion Practice Solving problems(Tutorial)

10	46.	Latin square	design	Interactive Lecture		Active learning, Q&A, Group discussion s			
11	47.	2 factorial	designs.	Interactive Lecture		Active learning, Q&A, Group discussion s			
12	48.	Solving problems(T	utorial)	Oiscussion		Pract	ĭce		
Asse ent Stra y:		CAT-I(50)	CAT- 11(50)	Activity- I(5)	Activi II(5)	ity-	€8€(100)		
,	Marks:	-	16	-	-		20		
(	Other Assessment Strategy/ Tools:		formative (	Assessment(Quiz)					
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## SESSION-WISE PLAN (COS)

CO5: Develop exposure to the principal component analysis of random vectors and Time Series.										Bloom's level# :Bl3			
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Sessio n	Cumulati ve Session No	Course Content/ Topics	1	ntent Delive Necha			Pedagogy		
1	49.	Random vectors and matrices	lect	ractiv ure, nples	e		Active Learni Discus	ing,	
2	50.	Mean vectors and covariance matrices	lect	ractiv ure, nples	e		Active Learni Discus	ing,	
3	51.	Principal components	lect	ractiv ure, nples	e		Active Learni Discus	ing,	
4	52.	Solving problems(Tutorial)	Oisc	ussion	1		Pract	íce	
5	53.	Population principal components	lect	ractiv ure, nples			Active learning, Q&A		
6	54.	Principal components from standardized variables	lect	ractiv ure, nples			Active learning, Q&A		
7	55.	Time series - components	Interactive lecture, examples				Active learning ,Q &A		
8	56. Trend- Determination of trend by moving averages		Interactive Lecture, Real time Scenarios				Active learni Q&A,		

				discussions
9	57.	Solving problems(Tutorial)	Discussion	Practice
10	58.	least square method	Interactive lecture, examples	Active Learning ,Discussion
11	59.	Seasonal Variations	Interactive lecture, examples	Active Learning ,Discussion

12	60.	Solving problems(T	utorial)	Ois	cussion		Practice	
Asses ent Strat y:		CAT-I(50)	CAT- 11(50)		Activity- I(5)	Activity- II(5)		€8€(100)
	Marks :	-	18				5	20
9 8	ther ssessment trategy/ ools:		Gormati Present		ssessment(As n	sig	nment),Sen	ninar
1	MeasuringCO5attainmentthr ough:				<b>s</b> €€ =	C	ES=	τ =

# INTERNAL ASSESSMENT PLANITheory Part):

CO#/ Assess			Marl in CA T-I			Mari in CAT -II		ĭn	CTIU			Marks in ACTIVIT 9- II		TOTA L MARK
Blood Level		2	3	4	2	3	4	3	4	5	3	4	5	S
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Overall Quality of Question Paper as per Bloom's Taxonomy levels												
Bloom's level 1 2 3 4 5 6												
Marks	-	34	66	10	-	-						
% of Questions	-	30.90	60.00	09.09	-	-						
		%	%	%								

Apply the basic concepts of one and two dimensional

random variables in engineering applications.

### Objective:

This assignment aims to apply discrete and continuous random variables for solving engineering and real life problems.

Students will be assessed on their ability to:

Acquire skill in handling situation with more than one random variable with time function.

### Assignment questions:

- 1. If P(x, y)=k(2x+3y), x=0,1,2 and y=1,2,3. Simplify (i) P(x=0/y=2). (ii) Find P(x+y) and P(x+y)>3. Also find  $P(x\le 1)$ ,  $P(y\le 2)$ ,  $P(x\le 1, y\le 2)$
- 2. If the joint p.d.f of x and y is given by f(x,y)=



 A statistical survey on the Heights of fathers and sons are taken and the observed data's are given below.

Heigh t of fathe r	65	66	67	67	68	69	70	72
Hei ght of Son	67	68	65	68	72	72	69	71

Correlate the heights by designing two dimensional random variable and discuss the nature of correlation coefficient.

- 4. If the joint density function of the random variable X and Y f(x , y)= 2-x-y,  $0 \le x \le 1$ ,  $0 \le y \le 1$ . Examine the Correlation.
- $f(x,y) = \begin{cases} e^{-(x+y)}; 0 \le x \le \infty \\ 0, \text{elsewhere} \end{cases}$  5. The joint density function of  $\lambda$  was 3 is 0, elsewhere Are X and Y are independent? Find P(X < 1); P(X + Y < 1)

This assignment provides an opportunity for students to apply their knowledge of

probability and Distribution concepts to analyze real-world problems and develop critical thinking skills.

Students' can gain valuable skills and knowledge for various fields.

Scheme of Evaluation

ક.ળ	Content	Mark
o		Allocat ĭon
1.	Solution for All Problems	8
2.	Presentation	1
3.	On-time Submission	1
	Total	10

#### PROPOSED ACTIVITY-II (CO5)

Develop exposure to the principal component analysis of random vectors and Time Series.

# Objective:

The objective of time series analysis is to understand the underlying structure and function of the data points collected over time and to make informed decisions based on this analysis. Students will be evaluated on their capacity to:

· Test the hypothesis of single and difference mean

 Determine differences between research results from three or more unrelated samples or groups.

### Assignment questions:

1. i)Calculate the covariance matrix for the two random variable X and 9 their joint probability function is represented by the entries in the following table

X/9	X=0	X=1
9=-1	0.24	0.06
9=0	0.16	0.14
9=1	0.40	0.00

(ii) Compute the principle components to the matrix A=

2.

(i) Compute the quadratic trend of the form y=a+bx+cx2 for the data given below:

<b>Years</b>	198 5	1986	198 7	1988	1989	1990	1991
Producti on	10	11	12	9	10	13	11

(ii) Determine the equation of the straight line which best fits the following data:

<b>Years</b>	1984	1985	1986	1987	1988
Sales(in	35	56	79	80	40
Rs.1000					
)					

3.(i) Calculate the 3-yearly moving average of the data given below:

ye	19	19	19	19	19	19	19	198	19	19	
ars	80	81	82	83	84	85	86	7	88	89	
Sal es (mi llio ns in Rs)	3	4	8	6	7	11	9	10	14	12	

Draw a graph to represent the moving averages ,also predict the sale for 1993.

(iii) Calculate the seasonal variation by the ratio to trend method from the data given below

Year	I	II	III	IU
	Quarter	Quarter	Quarter	Quarter
1994	60	80	72	68
1995	68	104	100	88
1996	80	116	108	96
1997	108	152	136	124
1998	160	184	172	164

4.Assuming 5-yearly moving average calculate trend values from the data given below also plot the

Уe	19	19	19	19	19	19	19	19	19	19	19	19	19
96	19	19	19	19	1 19	1 19	19	19	19	19	19	19	19

ar s	71	72	73	74	75	76	77	78	79	80	81	82	83
Pr od uc tío n	10 5	10 7	10 9	11 2	11 4	11 6	11 8	12	12 3	12 4	12 5	12 7	12 9

5. (i)Compute the average seasonal movement for the following series

<b>Year</b>	Quarterly production							
	1	2	3	4				
1974	3.5	3.9	3.4	3.6				
1975	3.5	4.1	3.7	4.0				
1976	3.5	3.9	3.7	4.2				
1977	4.0	4.6	3.8	4.5				
1978	4.1	4.4	4.2	4.5				

(ii) Given below are the figures of production of a sugar factory

<b>Year</b>	1974	1975	1976	1977	1978	1979	1980
Production	77	88	94	85	91	98	90

Eit a straight by least a squares method and tabulate the trend values.

# Scheme of Evaluation

ક.ળ	Content	Mark Allocation
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1.	Solution for All	8
	Problems	

2.	Presentation	1
3.	On-time Submission	1
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Course Co-ordinatorHOD