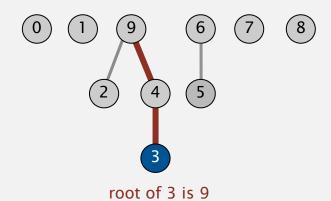
Quick-union [lazy approach]

Data structure.

- Integer array id[] of length N.
- Interpretation: id[i] is parent of i.
- Root of i is id[id[id[...id[i]...]]].

id[] 0 1 2 3 4 5 6 7 8 9
id[] 0 1 9 4 9 6 6 7 8 9

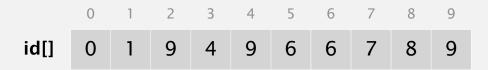
keep going until it doesn't change (algorithm ensures no cycles)



Quick-union [lazy approach]

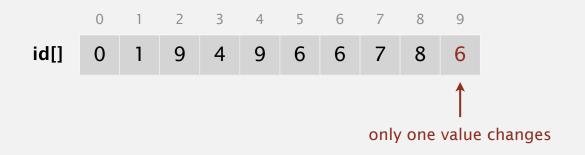
Data structure.

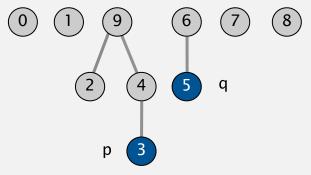
- Integer array id[] of length N.
- Interpretation: id[i] is parent of i.
- Root of i is id[id[id[...id[i]...]]].



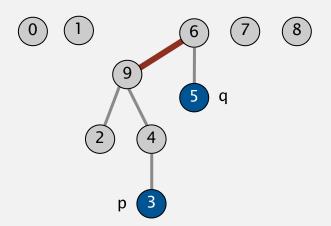
Find. Check if p and q have the same root.

Union. To merge components containing p and q, set the id of p's root to the id of q's root.





root of 3 is 9
root of 5 is 6
3 and 5 are not connected

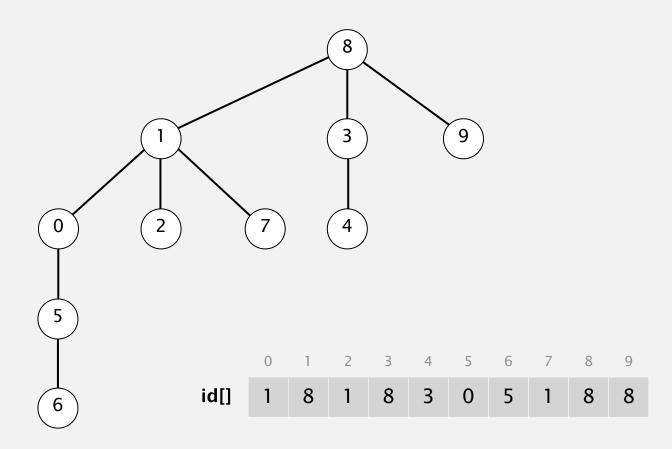




0 1 2 3 4 5 6 7 8 9

id[] 0 1 2 3 4 5 6 7 8 9

id[] 0 1 2 3 4 5 6 7 8 9



Quick-union: Java implementation

```
public class QuickUnionUF
   private int[] id;
   public QuickUnionUF(int N)
                                                                set id of each object to itself
       id = new int[N];
                                                                (N array accesses)
      for (int i = 0; i < N; i++) id[i] = i;
   private int root(int i)
                                                                chase parent pointers until reach root
      while (i != id[i]) i = id[i];
                                                                (depth of i array accesses)
       return i;
   public boolean connected(int p, int q)
                                                                check if p and q have same root
       return root(p) == root(q);
                                                                (depth of p and g array accesses)
   }
   public void union(int p, int q)
      int i = root(p);
                                                                change root of p to point to root of q
       int j = root(q);
                                                                (depth of p and q array accesses)
       id[i] = j;
```

Quick-union is also too slow

Cost model. Number of array accesses (for read or write).

algorithm	initialize	union	find	
quick-find	N	N	1	
quick-union	N	N †	N	← worst case

† includes cost of finding roots

Quick-find defect.

- Union too expensive (N array accesses).
- Trees are flat, but too expensive to keep them flat.

Quick-union defect.

- Trees can get tall.
- Find too expensive (could be *N* array accesses).