

Assignment 5, CS 6363

no late homework would be accepted

- 1** (Exercise 34.4-5) Show that the problem of determining the satisfiability of Boolean formula in disjunctive normal form is polynomial-time solvable.
- 2** (Exercise 34.5-1) The subgraph-isomorphism problem takes two graphs  $G_1$  and  $G_2$  and asks whether  $G_1$  is isomorphic to a subgraph of  $G_2$ . Show that the subgraph-isomorphism problem is NP-complete.
- 3** (Exercise 34.5-7) The longest-simple-cycle problem is the problem of determining a simple cycle (no repeated vertices) of maximum length in a graph. Show that this problem is NP-hard.
- 4** Show that the following problem is NP-complete: Given a graph  $G$ , determine whether  $G$  contains a Hamiltonian path where a path is Hamiltonian if it passes every vertex exactly once.
- 5** Show that the following problem is NP-hard: Given a graph, find a spanning tree to minimize the number of leaves.
- 6** Let HALF-CLIQUE denote the problem of determining for a graph  $G$  with  $n$  vertices whether  $G$  contains a clique of size at least  $n/2$ . Prove that HALF-CLIQUE is NP-complete.
- 7** Show that the following problem is NP-hard: Given a graph, find the minimum dominating set. (A subset of vertices is called a dominating set if every vertex not in the subset is adjacent to a vertex in the subset.)