

# Logic Gates

Logic gates are basic building blocks of digital circuits that perform logical operations on one or more binary inputs to produce a single binary output.

Each gate implements a specific logic function, such as **AND**, **OR**, **NOT**, **NAND**, **NOR**, **XOR**, or **XNOR**, which determines how the output is derived from the inputs.

These gates are used in various combinations to perform complex computational tasks in electronic devices.

## 1) AND GATE

### **Definition:**

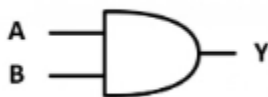
An AND gate is a digital logic gate that outputs a 1 (true) only if all of its inputs are 1 (true). If any input is 0 (false), the output will be 0 (false).

### **Boolean expression:**

$$Y = A \cdot B$$

### **Logic symbol: ^**

### **Logical diagram:**



### Truth Table:

Inputs		Output
A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

## 2) OR GATE

### Definition:

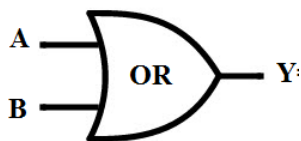
An OR gate is a digital logic gate that outputs true (1) if at least one of its inputs is true (1). If all inputs are false (0), the output is false (0).

### Boolean expression:

$$Y = A + B$$

### Logic symbol: ∨

### Logical diagram:



**Truth table:**

Inputs		Output
A	B	$Y=A+B$
0	0	0
0	1	1
1	0	1
1	1	1

### 3) NOT GATE

**Definition:**

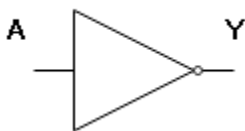
A NOT gate, also known as an inverter, is a logic gate that takes a single binary input and produces the opposite binary output. If the input is 0, the output is 1; if the input is 1, the output is 0.

**Boolean expression:**

$$Y = \text{NOT } A$$

**Logic symbol:** ~

**Logical diagram:**



**Truth table:**

Truth Table	
A	A'
1	0
0	1

#### 4) NAND GATE

**Definition:**

- A **NAND** gate is a type of logic gate that produces an output which is false only if all its inputs are true; otherwise, the output is true.
- It is the inverse of the **AND** gate.
- It combines the functions of an **AND** gate followed by a **NOT** gate.
- In binary terms, if the inputs are both 1 (true), the output is 0 (false); for any other combination of inputs, the output is 1 (true).

**Boolean Expression:**

$$Y = \overline{A.B}$$

Or ,  $Y = \text{NOT}(A.B)$

**Logic symbol: (same as AND gate with a circle at the output)**

**Logical diagram:**



**Truth table:**

Inputs		Output
A	B	Y
0	0	1
0	1	1
1	0	1
1	1	0

## 5) NOR GATE

**Definition:**

- A **NOR** gate is a type of logic gate that produces an output which is false (0) if at least one of its inputs is true (1).
- In other words, it gives a true (1) output only when all of its inputs are false (0).
- It is the inverse of the **OR** gate.
- It is the combination of an **OR** gate followed by a **NOT** gate.

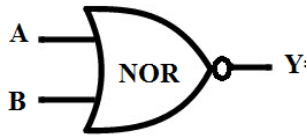
**Boolean expression:**

$$Y = \overline{A+B} \text{ or,}$$

$$Y = \text{NOT } (A+B)$$

**Logic symbol: (same as OR gate with a circle at the output)**

Logical diagram:



Truth table:

Inputs		Output
A	B	$Y = \overline{A + B}$
0	0	1
0	1	0
1	0	0
1	1	0

## 6) X-OR GATE

**Definition:**

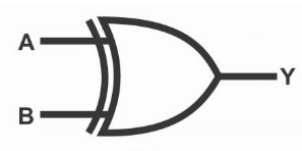
- An **XOR** (exclusive **OR**) gate is a digital logic gate that outputs true or 1 only when the number of true or 1 inputs is odd.
- For a two-input **XOR** gate, it outputs 1 if exactly one of the inputs is 1, and 0 if both inputs are the same (both 0 or both 1).
- In simpler terms, it outputs 1 when the inputs are different and 0 when they are the same.

**Boolean expression:**

$$A \oplus B = A\bar{B} + \bar{A}B$$

**! important**

Logical diagram:



Logic symbol:  $\oplus$

Truth table:

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

Note: if input(A,B) are same output: 0, otherwise:1

## 7) X-NOR GATE

**Definition:**

- An **X-NOR** gate (exclusive **NOR** gate) is a type of logic gate that outputs true (1) only when the number of true inputs is even.
- In simpler terms, for two inputs, an **X-NOR** gate outputs true (1) if both inputs are the same (both 0 or both 1) and false (0) if the inputs are different (one 0 and one 1).
- It is the opposite of an **X-OR** gate.

**Boolean expression:**

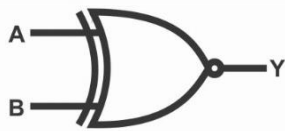
$$Y = \overline{(A \oplus B)} = (A.B + \overline{A}.\overline{B})$$

**! Important**

$$Y = A \odot B$$

**Logic symbol:**  $\odot$

**Logical diagram:**



**Truth table:**

A	B	Output
0	0	1
1	0	0
0	1	0
1	1	1

**Note: if input(A,B) are different output:0, otherwise 1**



The diagram illustrates the NOT Gate and the 7 basic logic gates. On the left, a NOT Gate is shown with an input 'A' and an output 'A-bar'. On the right, a table lists the 7 basic logic gates: AND, NAND, OR, NOR, XOR, and XNOR. Each gate is associated with its Boolean expression. The gates are labeled as 'logic gates' and the expressions as 'boolean expressions'.

Logic Gate	Boolean Expression
AND	$A \cdot B$
NAND	$\overline{A \cdot B}$
OR	$A + B$
NOR	$\overline{A + B}$
XOR	$A \oplus B$
XNOR	$\overline{A \oplus B}$

**THESE LOGIC GATES ARE COMBINED TO FORM MORE COMPLEX CIRCUITS, SUCH AS ADDER, MULTIPLEXER AND FLIPFLOP, WHICH ARE THE BUILDING BLOCKS OF DIGITAL COMPUTERS**

## THANK YOU !