

Linear Search

Time Complexity Analysis

The time complexity of linear search varies based on the position of the key in the list:

- **Best Case:** $O(1)$ - The key is found at the first position.
- **Average Case:** $O(n)$ - On average, the key is found halfway through the list.
- **Worst Case:** $O(n)$ - The key is at the last position or not present at all.

Binary Search

Time Complexity Analysis

Binary search has different time complexities depending on the scenario, but it is generally efficient compared to linear search for sorted lists.

- **Best Case:** $O(1)$ - The key is located at the middle of the list in the first comparison.
- **Average Case:** $O(\log n)$ - Binary search repeatedly divides the list, so the average number of comparisons is proportional to $\log n$.
- **Worst Case:** $O(\log n)$ - In the worst case, binary search will check each division until the list is reduced to one element, which takes approximately $\log n$ steps.

Comparison between Linear Search and Binary Search

Criterion	Linear Search	Binary Search
Time Complexity	Best: $O(1)$, Avg/Worst: $O(n)$	Best: $O(1)$, Avg/Worst: $O(\log n)$
Space Complexity	$O(1)$ (iterative)	$O(1)$ (iterative), $O(\log n)$ (recursive)
Efficiency on Large Datasets	Works on unsorted data	Requires data to be sorted
Efficiency on Large Datasets	Inefficient, scales linearly with n	Efficient, scales logarithmically with n
Best Use Case	Small or unsorted datasets	Large, sorted, and mostly static datasets