Problem 1

$$\frac{1}{2}(u_{n+1}+u_{n-1}) D_{c} V_{n} + \frac{1}{2}(V_{n+1}+V_{n-1}) D_{c} U_{n} \qquad D_{c} U_{n} = U_{n+1}-U_{n-1}$$

$$\frac{1}{2}(u_{n+1}+u_{n-1}) \frac{1}{2}(v_{n+1}+v_{n-1}) \frac{1}{2}(v_{n+1}+v_{n-1}+v_{n-1}) \frac{1}{2}(v_{n+1}+v_{n-1$$

fj + Zak Gith = O(?) (central -differences) F'(x0) = f, - Zfo - f-, Taylor Table Thyma to replicate this a, 5, 1 a, -a, h a, h/2 -a, h/6 a-124 anti an o o a, Fire a, a, h a, 12/2 a, 45/6 a, h /24 Fit + Zaxfirk = (a, +a, +a, ) F; + (1-a, +a, 1) F; + (a, 1/2 + a, 1/2) 5" + (a, 1/6 - 2, 1/6) f" (a, n2/2 + a, n2/2) fj = (a, +a0+a,) fj + (a,h-a,h) fj + (0,1/6-9, 1/6) fj (a-1 + a,) f"= = (a, +a, +a,) f' + = (a, -a-1) f' + = (a, -a,) f"  $f_{j}^{11} = \frac{2}{h^{2}} \frac{(a_{-1} + a_{0} + a_{1})}{(a_{-1} + a_{1})} f_{j} + \frac{2}{h} \frac{(a_{1} - a_{-1})}{(a_{-1} + a_{1})} f_{j}^{1} + \frac{h}{3} \frac{(a_{1} - a_{-1})}{(a_{-1} + a_{1})} f_{j}^{111}$  $\frac{1}{12} \frac{h^{2}(a_{1} + a_{-1})f^{(n)}}{(a_{1} + a_{1})} \qquad a_{1} = a_{-1}$ a-1+a0+a1=0 I am missing a third equation to solve For any as, a,

ghen X, Nr, Xrz, get accurate f's using one sided deviative formula. fj + Zakfirk = 0(?) Taylor Table t' t', t'. t'. aof: ao o o o a, a,h a,h a,h a,h 02 2haz 022 076 fit & antite = (ao + a, +az) f + (1 + a, h + 2haz) fi + (a, h2, az (zh)2)f," + (a, h3, az (zh)3)f" + ... solve for a, az, aa set low-order terms to o  $a_1 = \frac{2}{h}$   $a_2 = \frac{1}{2h}$   $a_0 = \frac{3}{2h}$ do ta, taz =0 1+a,h+2haz=0 0, h2/2 + Zazh2 = 0 f' = -3f, +4/H-fi+2 + 0(42) leading truncation term 15 hz f"