# Intro to (Practical) Reinforcement Learning

Dec 2019 Second Nepal Winter School in Al

#### **Course Format**

- 4 x 45min with 3min breaks in between
- Afterwards 1h lab session with quiz + python fun
- Ask questions anytime, interrupt me!

#### Goal

- Understand basic concepts around RL  $(S, A, T, R, \gamma)$
- Understand basic algorithms (policy iteration, SARSA, etc.)
- Be able to use DRL at a grad student level\*
- NOT: understand SotA algorithms / create new SotA

<sup>\*</sup> i.e. be able to download somebody else's algorithm and run it on your task

#### **Outline**

Part 1 - Intro & MDPs

(Examples, Markov stuff)

Part 2 - RL for Evaluation

(Policy Evaluation, TD(0))

Part 3 - Model-Free RL for Control

(Q learning / SARSA)

Part 4 - Practical RL

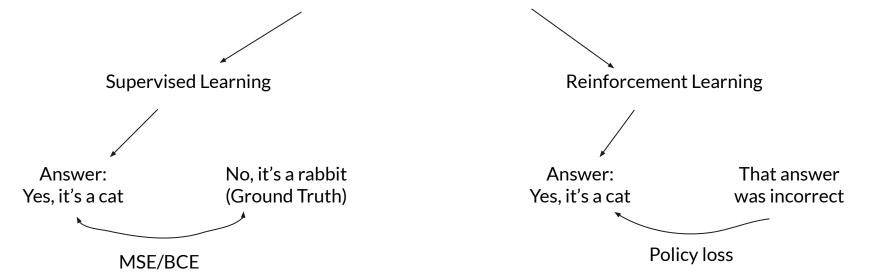
(OpenAl Gym, SotA algorithms, etc.)

# Part 1 - Introduction + MDP

## Why RL tho?



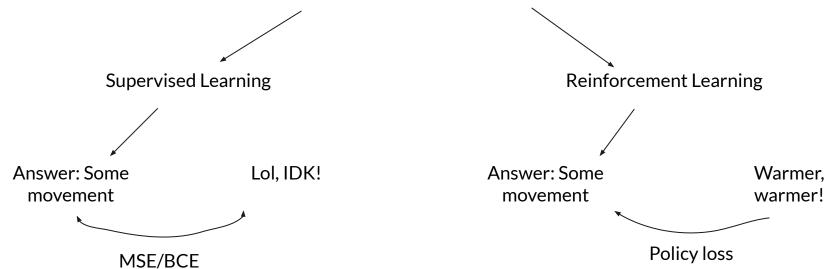
Task (e.g. is this image a cat?)



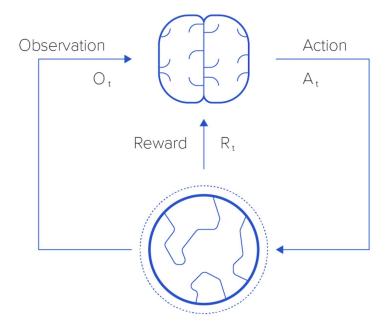


## Why RL tho?

Task (e.g. make this robot stand up & walk)

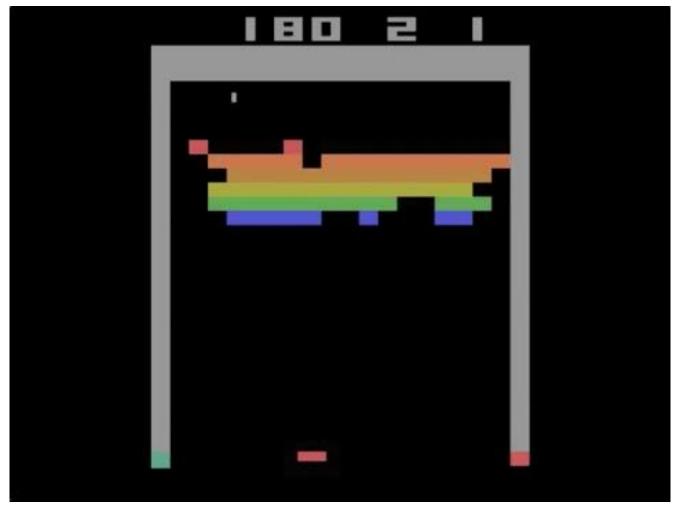


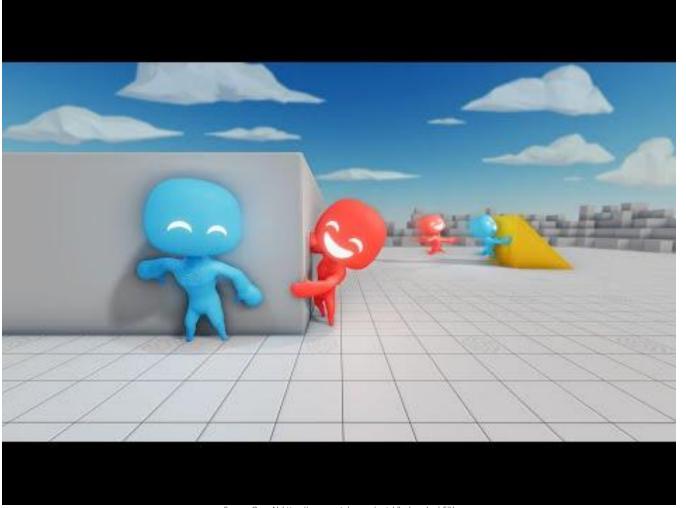
## **RL Loopdy Loop**



### What else can RL do?





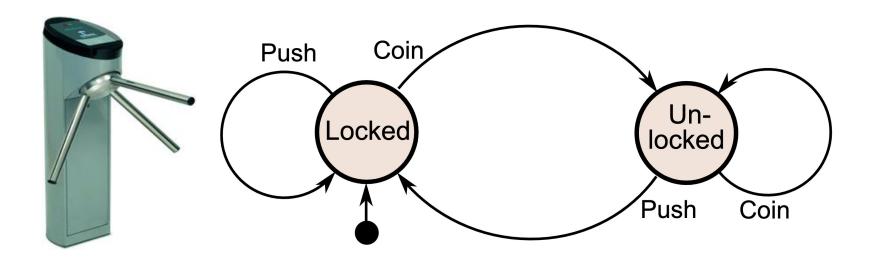


#### Resources

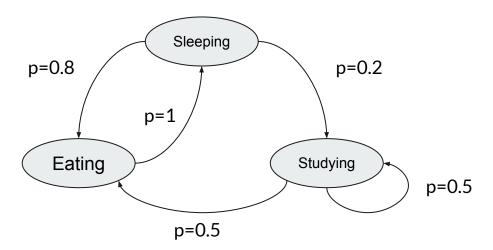
- Youtube, "RL Course by David Silver", 11 lectures x 1h30:
   <a href="https://www.youtube.com/playlist?list=PLzuuYNsE1EZAXYR4FJ75jcJseBmo4KQ9-">https://www.youtube.com/playlist?list=PLzuuYNsE1EZAXYR4FJ75jcJseBmo4KQ9-</a>
- Youtube, Abbeel & Klein, <a href="http://ai.berkeley.edu/lecture\_videos.html">http://ai.berkeley.edu/lecture\_videos.html</a>
- Sutton & Barto "Reinforcement Learning: An Introduction":
   <a href="http://incompleteideas.net/book/bookdraft2017nov5.pdf">http://incompleteideas.net/book/bookdraft2017nov5.pdf</a>
- Spinning Up in DRL: <a href="https://spinningup.openai.com/en/latest/">https://spinningup.openai.com/en/latest/</a>

Some slides/formulas were copied from the above

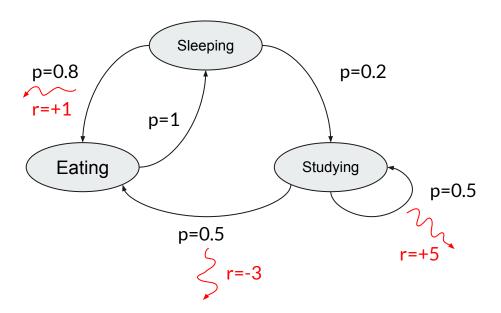
#### **Finite State Machine**

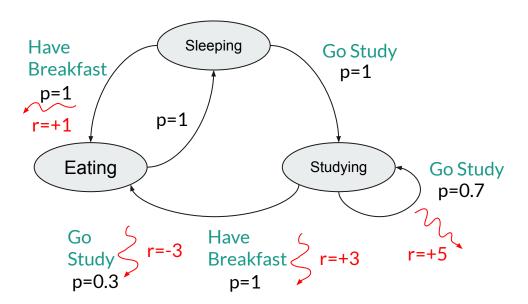


#### **Markov Chain**

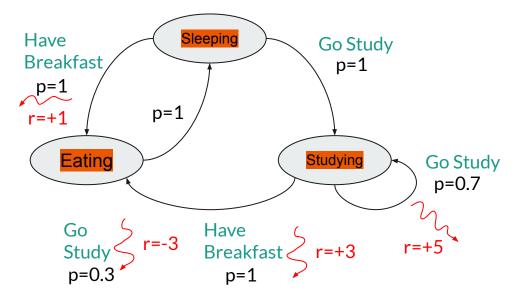


#### **Markov Reward Process**

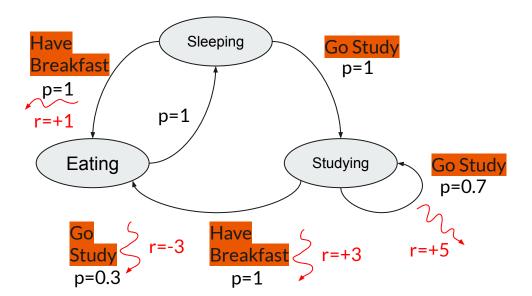




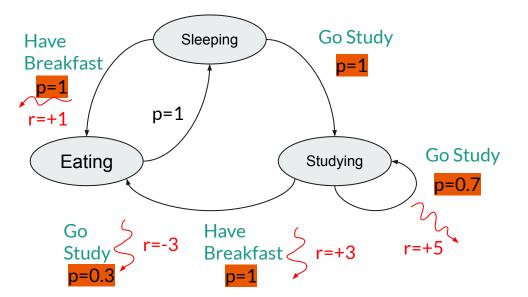
• States (S)



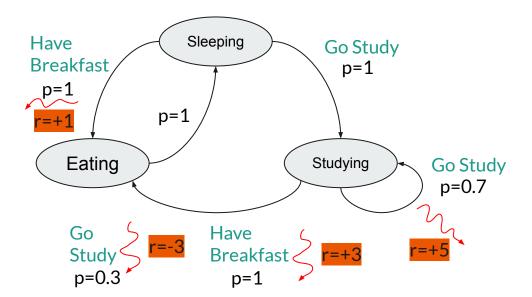
- States (S)
- Actions (A)



- States (S)
- Actions (A)
- TransitionProbabilities (T/P)



- States (S)
- Actions (A)
- TransitionProbabilities (T/P)
- Rewards (R)

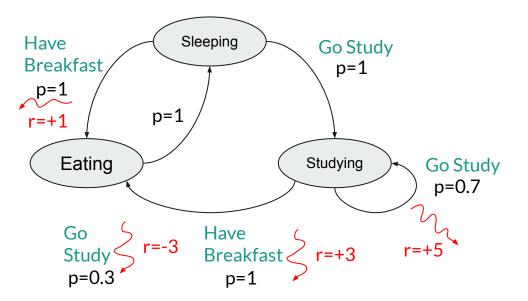


- States (S)
- Actions (A)
- Transition

Probabilities (T/P)

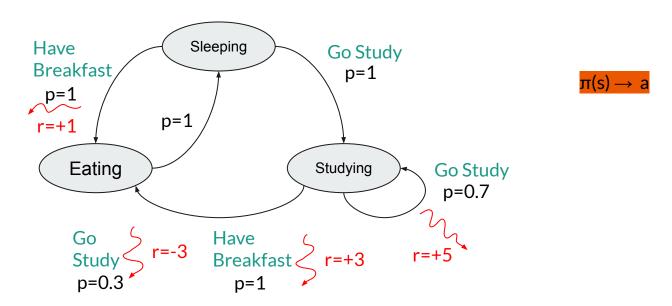
- Rewards (R)
- Discount Factor(γ)

$$(S, A, T, R, \gamma)$$



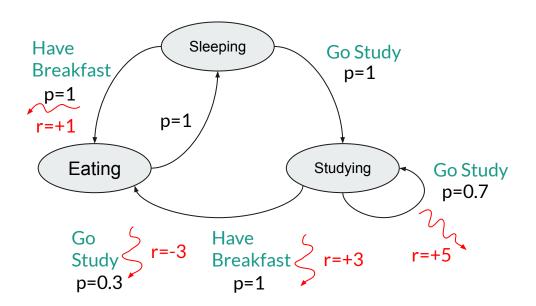
- States (S)
- Actions (A)
- TransitionProbabilities (T/P)
- Rewards (R)
- Discount Factor  $(\gamma)$

$$(S, A, T, R, \gamma)$$



- States (S)
- Actions (A)
- TransitionProbabilities (T/P)
- Rewards (R)
- Discount Factor(γ)

$$(S, A, T, R, \gamma)$$



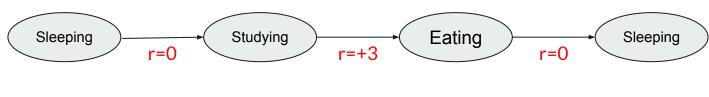
 $\pi(s) \rightarrow a$ 

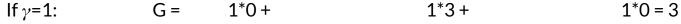
Deterministic or stochastic environment?





$$G_t = r_{t+1} + \gamma r_{t+2} + \dots = \sum_{k=0}^{\infty} \gamma^k r_{t+k+1}$$

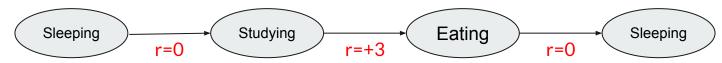






If 
$$\gamma = 1$$
:  $G = 1^*1 + 1^*0 = 1$ 

$$G_t = r_{t+1} + \gamma r_{t+2} + \dots = \sum_{k=0}^{\infty} \gamma^k r_{t+k+1}$$

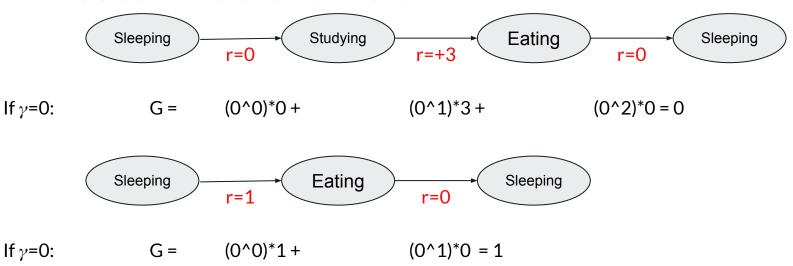


If 
$$\gamma$$
=0: G = ???



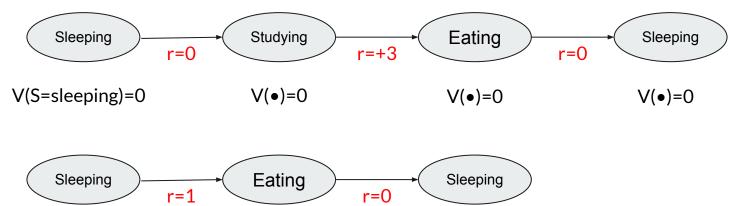
If 
$$\gamma$$
=0: G = ???

$$G_t = r_{t+1} + \gamma r_{t+2} + \dots = \sum_{k=0}^{\infty} \gamma^k r_{t+k+1}$$

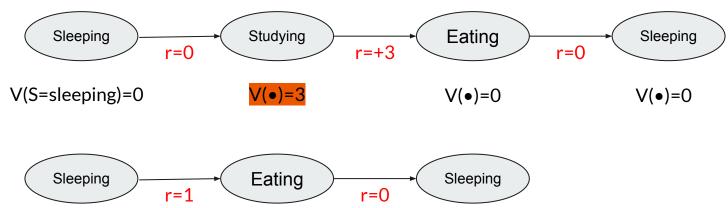


$$V^{\pi}(s) = \mathbb{E}_{\pi}[G_t|s_t = s] = \mathbb{E}_{\pi}[r_{t+1} + \gamma r_{t+2} + \gamma^2 r_{t+3} + \dots |s_t = s]$$

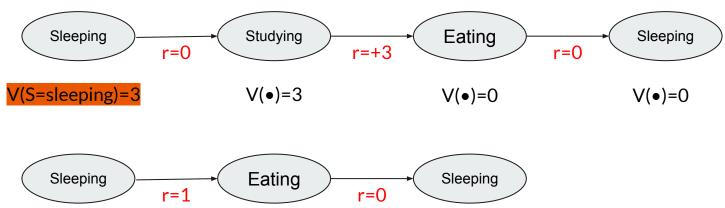
"How good is a state?"



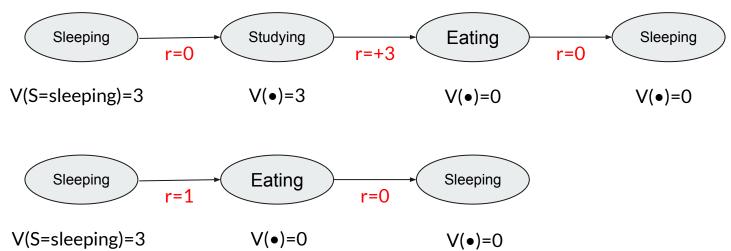
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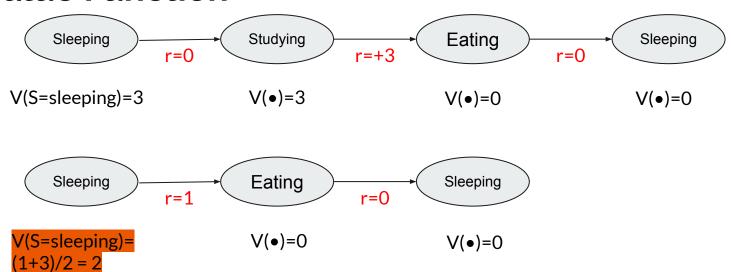
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$$V^{\pi}(s) = \mathbb{E}_{\pi}[G_t|s_t = s] = \mathbb{E}_{\pi}[r_{t+1} + \gamma r_{t+2} + \gamma^2 r_{t+3} + \dots |s_t = s]$$



## **Bellman Equation**

from s under  $\pi$ 

## Part 2 - Model-based RL

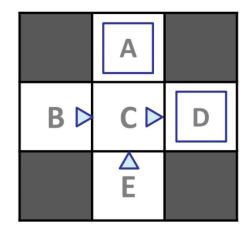
#### Model-based RL Idea

- 1. Build (or have) a model of the environment dynamics: transitions (T), rewards (R)
- 2. "Solve" the environment: via planning or value estimation
- 3. ...
- 4. Profit

## **Learning the Model**

T & R can be learned by averaging observations from trajectories.

#### Input Policy $\pi$



Assume:  $\gamma = 1$ 

#### Observed Episodes (Training)

#### Episode 1

B, east, C, -1 C, east, D, -1 D, exit, x, +10

#### Episode 3

E, north, C, -1 C, east, D, -1 D, exit, x, +10

#### Episode 2

B, east, C, -1 C, east, D, -1 D, exit, x, +10

#### Episode 4

E, north, C, -1 C, east, A, -1 A, exit, x, -10

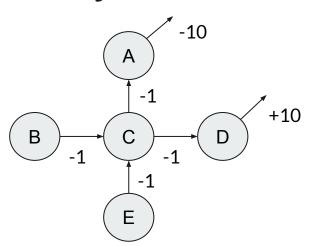
#### Learned Model

$$\widehat{T}(s, a, s')$$
T(B, east, C) = \_\_\_\_
T(C, east, D) = \_\_\_\_
T(C, east, A) = \_\_\_\_

$$\hat{R}(s, a, s')$$

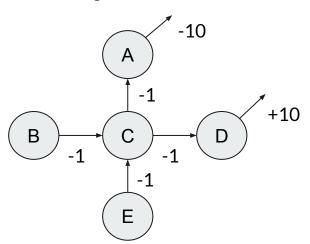
(Goal: get value function everywhere)

- 1. Initialize VF everywhere at 0
- 2. Iterate over all states; update their value with the reward from all reachable states + their current value function
- 3. GOTO 2



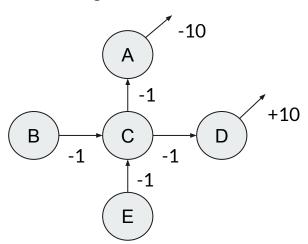
	0	
0	0	0
	0	

Assume  $T(\bullet) = 1$ ,  $\gamma = 1$ , uniform random policy



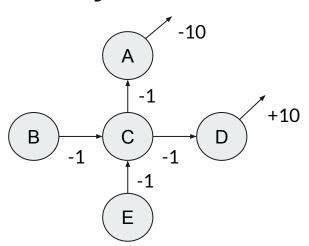
	-10	
-1	-1	+10
	-1	

Assume  $T(\bullet) = 1$ ,  $\gamma = 1$ , uniform random policy



Assume  $T(\bullet) = 1$ ,  $\gamma = 1$ , uniform random policy

	-10	
-1+(-1)	½ (-1-10)+½ (-1+10) = -1	+10
	-1+(-1)	

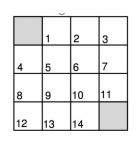


	-10	
-2	-1	+10
	-2	

Assume  $T(\bullet) = 1$ ,  $\gamma = 1$ , uniform random policy

#### And another one

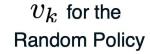




r = -1 on all transitions

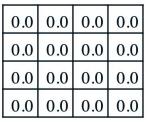
- Undiscounted episodic MDP  $(\gamma = 1)$
- Nonterminal states 1, ..., 14
- One terminal state (shown twice as shaded squares)
- Actions leading out of the grid leave state unchanged
- $\blacksquare$  Reward is -1 until the terminal state is reached
- Agent follows uniform random policy

$$\pi(n|\cdot) = \pi(e|\cdot) = \pi(s|\cdot) = \pi(w|\cdot) = 0.25$$



Greedy Policy w.r.t. 
$$v_k$$

$$k = 0$$



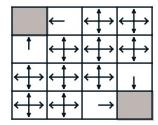
random policy

$$k = 1$$

Chance of going there under current policy  $^*$  k=2 (Reward of transition + V(s'))

0.0	-1.0	-1.0	-1.0
-1.0	-1.0	-1.0	-1.0
-1.0	-1.0	-1.0	-1.0
-1.0	-1.0	-1.0	0.0

0.0	-1.7	-2.0	-2.0
-1.7	-2.0	-2.0	-2.0
-2.0	-2.0	-2.0	-1.7
-2.0	-2.0	-1.7	0.0

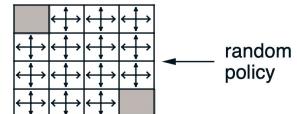


	<b>←</b>	<b></b>	$\longleftrightarrow$
1	7	$\Rightarrow$	<b>↓</b>
†	$\leftrightarrow$	₽	ļ
$ \Longleftrightarrow $	$\rightarrow$	$\rightarrow$	

## $v_k$ for the Random Policy

0.0 | 0.0 | 0.0 | 0.0

Greedy Policy w.r.t.  $v_k$ 



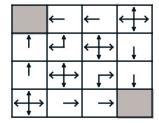
$$k = 1$$

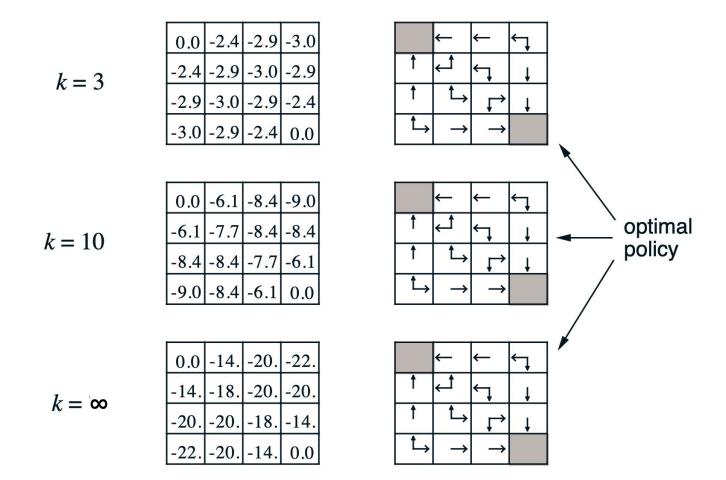
$$\begin{vmatrix}
0.0 & -1.0 & -1.0 & -1.0 \\
-1.0 & -1.0 & -1.0 & -1.0 \\
-1.0 & -1.0 & -1.0 & -1.0 \\
-1.0 & -1.0 & -1.0 & 0.0
\end{vmatrix}$$

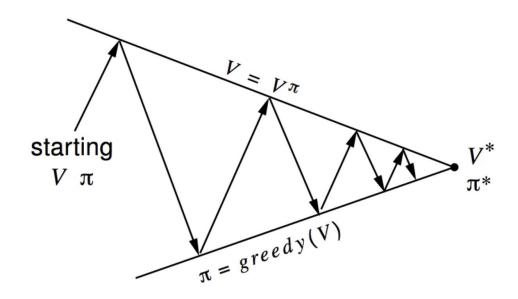
	<b>←</b>	$\longleftrightarrow$	$\longleftrightarrow$
<b>†</b>	$\Leftrightarrow$	$\leftrightarrow$	$\longleftrightarrow$
$\Leftrightarrow$	$\Leftrightarrow$	$\leftrightarrow$	ţ
$\leftrightarrow$	$\leftrightarrow$	$\rightarrow$	

$$k = 2$$

$$\begin{vmatrix}
0.0 & -1.7 & -2.0 & -2.0 \\
-1.7 & -2.0 & -2.0 & -2.0 \\
-2.0 & -2.0 & -2.0 & -1.7 \\
-2.0 & -2.0 & -1.7 & 0.0
\end{vmatrix}$$

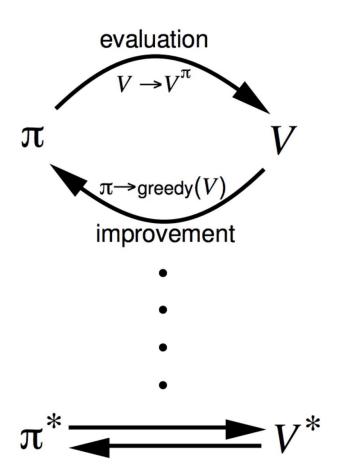






Policy evaluation Estimate  $v_{\pi}$  Iterative policy evaluation

Policy improvement Generate  $\pi' \geq \pi$ Greedy policy improvement



### **Problems:**

- Costly (synchronous update of all states + every state vs. every accessible state)
- Need transition function

 $\rightarrow$  how about asynchronous updates as we go? (MC/TD(0))

## Part 2 - Model-free RL

## **Monte-Carlo Policy Evaluation**

#### Idea:

- When an episode is over, store actual mean return (G) for each state
- Update value function to approximate this G for each state

**Learning Rate** 

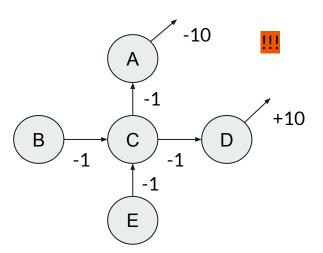
$$V(S_t) \leftarrow V(S_t) + \alpha(G_t - V(S_t))$$

## Incremental Updates

New value = old value + learning rate \* (measurement - old value)

If measurement == old value, then no change, otherwise small increase/decrease

### **MCPE**



	0	
0	0	0
	0	

Assume  $\gamma$  = 1,  $\alpha$  = 0.1

#### **MCPE**

 $\bigcirc$ A

 $\left( \mathsf{B} \right)$ 



 $\left( \mathsf{D} \right)$ 

E

	0	
0	0	0
	0	

Trajectory 1

 $B\rightarrow C$ , -1  $C\rightarrow D$ , -1

 $D\rightarrow x,+10$ 

G(B): +8

G(C): +9

G(D): +10

Assume  $\gamma = 1$ ,  $\alpha = 0.1$ 

#### **MCPE**

A

 $\left(\mathsf{B}\right)$ 



 $\left(\mathsf{D}\right)$ 

E

	0	
0+0.1*8 =.8	0+0.1*9 =.9	0+0.1*10 =1
	0	

Trajectory 1

 $B \rightarrow C$ , -1  $C \rightarrow D$ , -1

 $D\rightarrow x,+10$ 

G(B): +8

G(C): +9

G(D): +10

Assume  $\gamma = 1$ ,  $\alpha = 0.1$ 

#### **MCPE**

A

 $\left( \mathsf{\,B\,} \right)$ 



 $\left( \mathsf{D} \right)$ 

E

	0	
.8	.9	1
	0	

Trajectory 1 Trajectory 2

$$B\rightarrow C, -1$$
  $B\rightarrow C, -1$   
 $C\rightarrow D, -1$   $C\rightarrow A, -1$   
 $D\rightarrow x, +10$   $A\rightarrow x, -10$ 

Assume  $\gamma = 1$ ,  $\alpha = 0.1$ 

#### **MCPE**

A

 $\left( \mathsf{\,B\,} \right)$ 



 $\left(\mathsf{D}\right)$ 

 $\left(\mathsf{E}\right)$ 

	0+.1*-10 =1	
.8+.1* (-128) = -0.48	.9+.1* (-119) = -0.29	1
	0	

Trajectory 1 Trajectory 2

$$B\rightarrow C, -1$$
  $B\rightarrow C, -1$   
 $C\rightarrow D, -1$   $C\rightarrow A, -1$   
 $D\rightarrow x, +10$   $A\rightarrow x, -10$ 

Assume  $\gamma = 1$ ,  $\alpha = 0.1$ 

## Temporal Difference Learning

#### Idea:

- Same thing but we don't wait for the episode's end
- Use single step (reward+V(s') to update  $\rightarrow$  single step = TD(0)

$$V(S_t) \leftarrow V(S_t) + \alpha \left( G_t - V(S_t) \right)$$

$$\downarrow$$

$$V(S_t) \leftarrow V(S_t) + \alpha \left( R_{t+1} + \gamma V(S_{t+1}) - V(S_t) \right)$$
Source: David Silver reinforcement learning lecture series,

## Part 3 - RL for Control

## **Summary so far**

- Learned about MDP/(S,A,T,R, $\gamma$ )
- Policy Eval learns value func. (given T,R,π)
- Monte-Carlo Policy Eval learns value func (given π)
- Temporal Difference Learning learns value func (given  $\pi$ )
- Can use greedy  $\pi$  if we have T, but what if we don't?
  - $\rightarrow$  Q function to the rescue

## **Q** Learning

Similar to value function, but also taking actions into consideration:

#### Definition

The action-value function  $q_{\pi}(s, a)$  is the expected return starting from state s, taking action a, and then following policy  $\pi$ 

$$q_{\pi}(s,a) = \mathbb{E}_{\pi}\left[G_t \mid S_t = s, A_t = a\right]$$

## **Q Learning Policy**

$$\pi'(s) = \operatorname*{argmax} q_{\pi}(s, a)$$
 $a \in \mathcal{A}$ 

At each state, check the Q value of all the actions; Pick action with highest Q

#### How to learn Q?

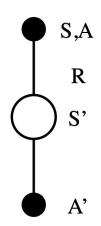
- Use Monte-Carlo algorithm ("Monte-Carlo Q Learning")
- Use Temporal Difference algorithm ("Sarsa") same as TD(0) but with Q
   function instead of value function

## Monte-Carlo Q Learning

■ For each state  $S_t$  and action  $A_t$  in the episode,

$$N(S_t, A_t) \leftarrow N(S_t, A_t) + 1$$
Simple counter (start at 0)  $Q(S_t, A_t) \leftarrow Q(S_t, A_t) + rac{1}{N(S_t, A_t)} \left(G_t - Q(S_t, A_t)\right)$ 

#### Sarsa - State-action-reward-state-action



$$Q(S,A) \leftarrow Q(S,A) + \alpha \left(R + \gamma Q(S',A') - Q(S,A)\right)$$

## **BUT: exploration**



"Behind one door is tenure - behind the other is flipping burgers at McDonald's."

- There are two doors in front of you.
- You open the left door and get reward 0 V(left) = 0
- You open the right door and get reward +1V(right) = +1
- You open the right door and get reward +3V(right) = +2
- You open the right door and get reward +2V(right) = +2

•

Are you sure you've chosen the best door?

## **€-Greedy Exploration**

- lacksquare With probability  $1-\epsilon$  choose the greedy action
- lacktriangle With probability  $\epsilon$  choose an action at random

You can decrease  $\epsilon$  slowly as you go

#### How to Neural-network this?

- Q function: a neural network, in: observation, action, out: scalar float
- π: testing each action + picking highest Q value
- "Actor-Critic" = Q network + policy network

#### Continuous actions:

•  $Q(s,a) = Q(s, \pi(s)) \rightarrow backprop through Q into both nets$ 

## Part 4 - Practical RL

## OpenAl gym

- De-facto standard RL environment(s)
- Contains variety of tasks (text adventures, Atari games, robotic tasks...)
- → Show <a href="https://gym.openai.com/envs/#classic\_control">https://gym.openai.com/envs/#classic\_control</a>
  - Only tasks, no learning algorithms
  - Homogenous API

```
import gym
env = gym.make("Pendulum-v0")
obs = env.reset()
env.render()
done = False
while not done:
    action = env.action_space.sample()
    obs, rew, done, misc = env.step(action)
    env.render()
```

## obs, rew, done, misc = env.step(action)

```
Observation as
                             Scalar float
                                                              Dictionary
                                              Bool
List, Tuple, Numpy array
                                                              Ex: { }
                             Ex: +10
                                              Ex: True
Ex: img,
                             Ex: -0.001
                                              Ex: False
np.array((128,128,3),
                                                              Ex:
dtype=np.uint8)
                                                              {"success": True,
                                                              "steps": 420}
Ex: robot joints + velocities
list(0.4, 1.0, -0.3, 0.0)
                                                              Ex:
                                                              {"reward pos": 69,
                                                              "reward vel": 1,
                                                              "reward rules": -10.4}
```

```
import gym
env = gym.make("Pendulum-v0")
policy = Policy() # <-- not part of Gym</pre>
replay_buf = ReplayBuffer() # <-- also not part of Gym</pre>
while True:
    obs = env.reset()
    done = False
    while not done:
        action = policy.select_action(obs)
        new_obs, rew, done, misc = env.step(action)
        replay_buf.add((obs, action, new_obs, rew, done))
    replay_batch = replay_buf.sample()
    policy.train(replay_batch)
```

Find

the

error!

• Normalize observations & actions to be in [-1,1] or [0,1]:

```
np.array(-100, 5, 30) \rightarrow np.array(-1, 0.05, .3)
```

(normalize by max/range or by mean/std)

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Limit/scale rewards

-100 on failure, +1 on success, -0.00001 per step  $\rightarrow$  -5, +1, -0.01

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• Make sure environment is markovian

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np.array(-100, 5, 30) 
$$\rightarrow$$
 np.array(-1, 0.05, .3) (normalize by max/range or by mean/std)

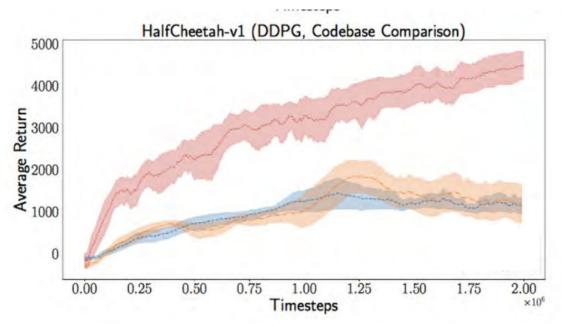
And LOTS OF SEEDS

Limit/scale rewards

-100 on failure, +1 on success, -0.00001 per step  $\rightarrow$  -5, +1, -0.01

• Make sure environment is markovian

# Reproducibility



Example:

Flying a helicopter

Observation:
 (position\_xyz, velocity\_xyz)

Example:

Flying a helicopter

```
Observation:
  (position_xyz, velocity_xyz)
```

Better:
 (position\_xyz, velocity\_xyz,
 rotation\_quat, goal\_xyz)

Example:

Flying a helicopter

Observation:

(position\_xyz, velocity\_xyz)

Better:

(position\_xyz, velocity\_xyz,
rotation\_quat, goal\_xyz)

Example:

Driving a car

Observation:

Image, (256, 256, 3)

Example:

Flying a helicopter

Observation:

(position\_xyz, velocity\_xyz)

Better:

(position\_xyz, velocity\_xyz,
rotation\_quat, goal\_xyz)

Example:

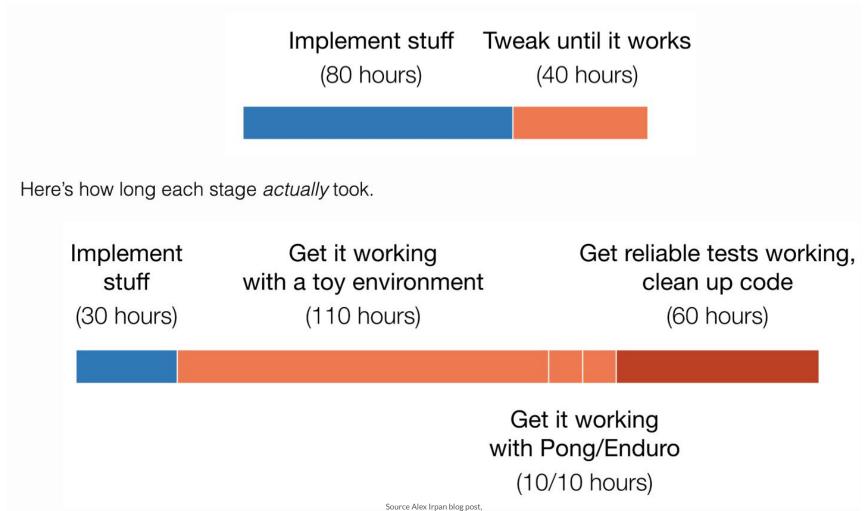
Driving a car

Observation:

Image, (256, 256, 3)

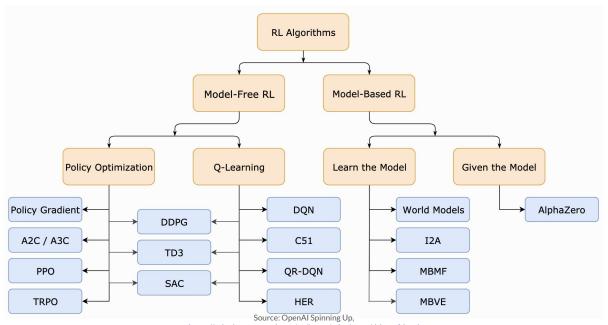
Better:

Image stack (last 4 images) + depth images (4, 256, 256, 3) + (4, 256, 256, 1)





# State-of-the-Art DRL algos

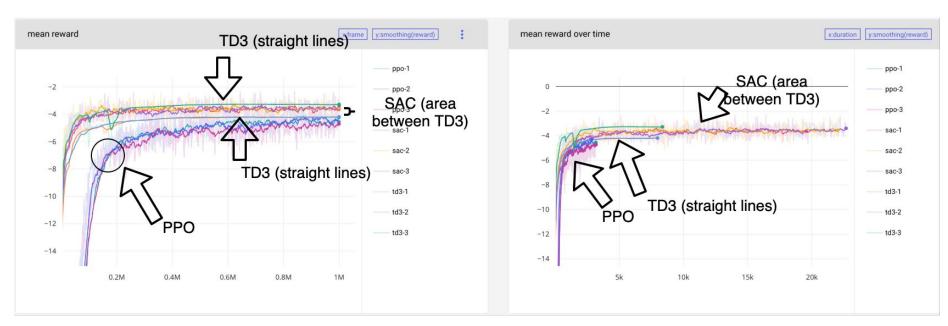


# How to pick?

9/10 times: PPO works (discrete or continuous actions)

+ few HP adjustments (episodes, stacked frames, hidden rep size)

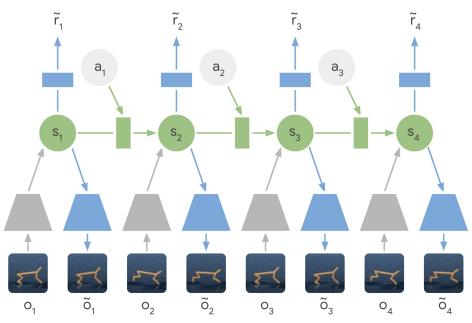
Otherwise, try SAC (slow but stable) or TD3 (fast, easy, sensitive to seed)



X axis: steps in the environment (every time the "env.step()" function is called)

X axis: compute time in seconds

# **Bonus: Modern Planning via PlaNet**



## **Bonus: Imitation Learning**

Naive: behavior cloning

- Can be used as initialization for RL policy
- But overfits to training data

Better: DAgger / Deeply AggreVaTeD, see <a href="http://videolectures.net/DLRLsummerschool2018\_daume\_imitation\_learning/">http://videolectures.net/DLRLsummerschool2018\_daume\_imitation\_learning/</a>

# Thanks, questions?