

**Ahmedabad
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Strong and Weak Ties

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*Thanks to
Easley, David, and Jon Kleinberg. "Networks, crowds, and markets." Cambridge Books (2012).*

Social Network Analysis – What it does

- ❖ Networks bridge the local to the global — to offer explanations for how simple processes at the level of **individual nodes** and links can have complex effects that ripple through a **population** as a whole.

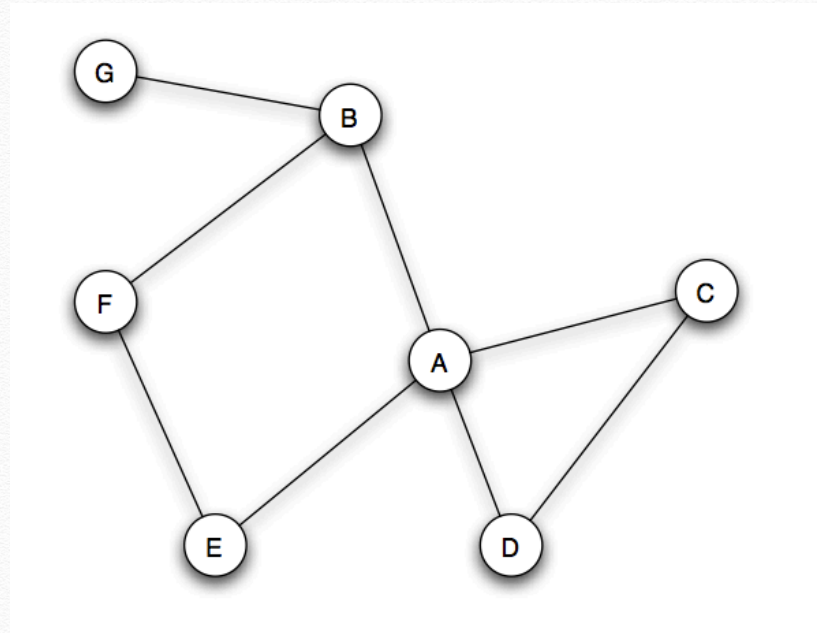
Key points

- ❖ How information **flows** through a social network..
- ❖ How different nodes can play **structurally** distinct roles in this process..
- ❖ How these **structural** considerations shape the **evolution** of the network itself over time...

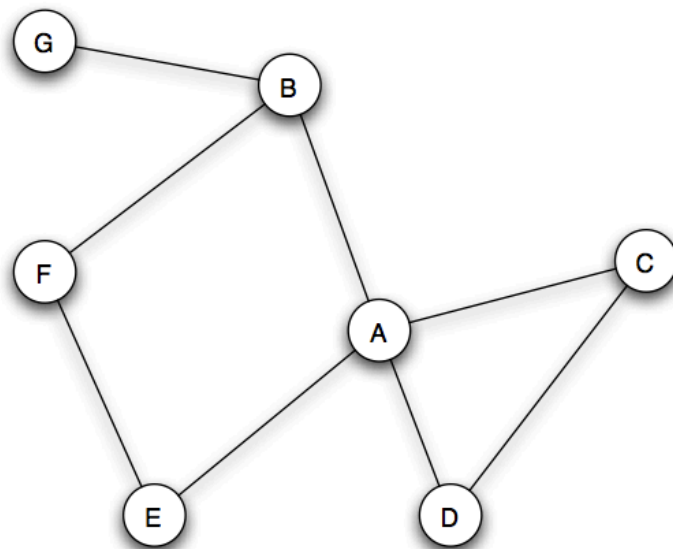
Granovetter's Problem

- ❖ How did people find new jobs?
- ❖ Through personal contacts..
- ❖ acquaintances, not close friends..
- ❖ So, how does the graph come into the picture?

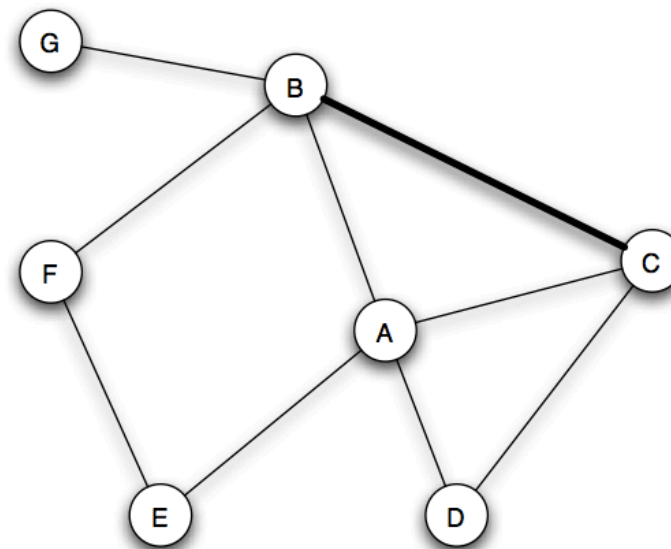
How are friendships formed?



How are friendships formed?



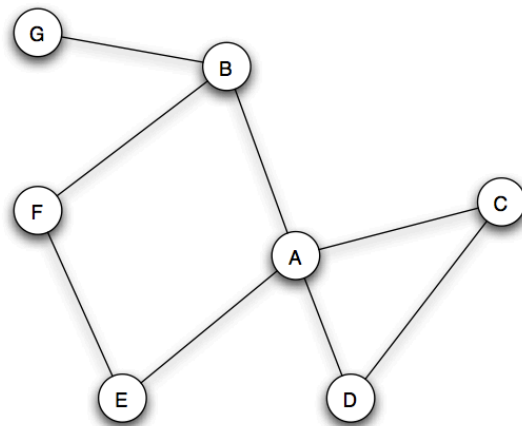
(a) Before *B-C* edge forms.



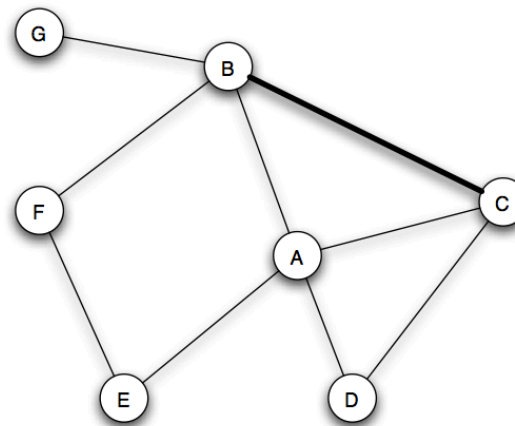
(b) After *B-C* edge forms.

What may be going on here?

Triadic Closure



(a) Before B-C edge forms.



(b) After B-C edge forms.

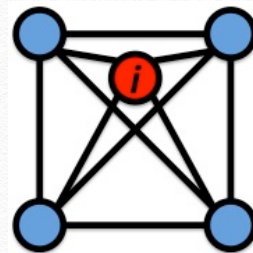
- ❖ If two people in a social network have a friend in common, then there is an increased likelihood that they will become friends themselves at some point in the future

Clustering Coefficient

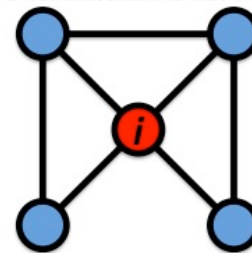
❖ What fraction of your neighbours are connected?

- Node i with degree k_i
- Clustering Coefficient C_i for a vertex i is in $[0,1]$

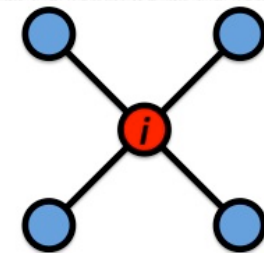
$$C_i = \frac{2e_i}{k_i(k_i - 1)}$$



$$C_i = 1$$



$$C_i = 1/2$$



$$C_i = 0$$

Clustering coefficient is a “local” property – each vertex has one.

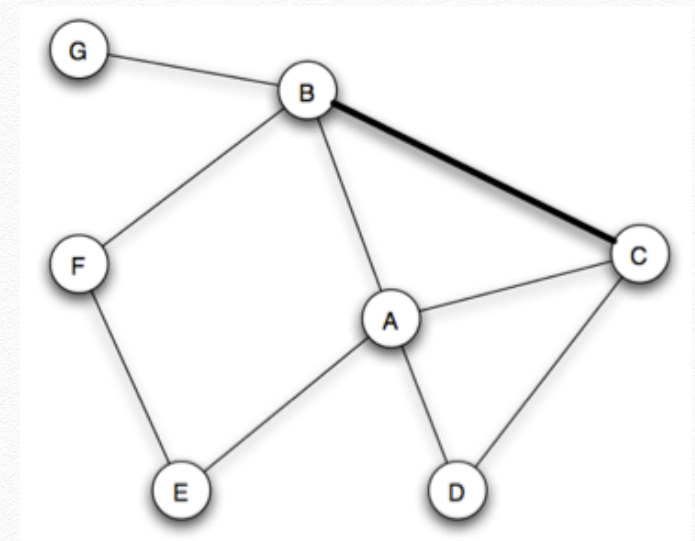
Watts & Strogatz, Nature 1998.

Clustering Coefficient

- ❖ ..is the fraction of pairs of A's friends that are connected to each other by edges.
- ❖ ..of a node A can also be defined as the probability that two randomly selected friends of A are friends with each other.
- ❖ The more the triadic closure ([dynamic](#)) is operating in the neighbourhood of a node, the higher the clustering coefficient ([static](#)) will be.

Reasons for Triadic Closure

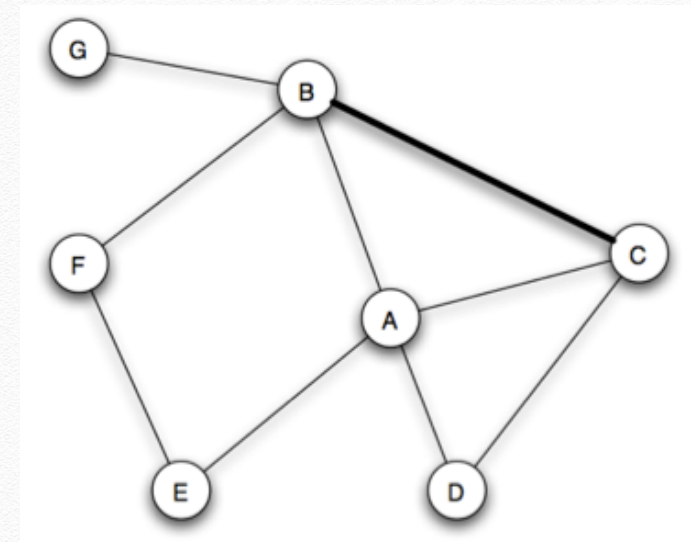
- ❖ When they have a common friend A, there is an increased **opportunity** for B and C to meet.
- ❖ Since each of B and C is friends with A (provided they are mutually aware of this) gives them a basis for **trusting** each other that an arbitrary pair of unconnected people might lack.
- ❖ A third reason is based on the **incentive** A may have to bring B and C together: if A is friends with B and C, then it becomes a source of latent stress in these relationships if B and C are not friends with each other.



The story so far...

- ❖ Acquaintances rather than friends were helpful in finding jobs.
- ❖ How friendships may be formed, and the idea of triadic closure (“formation of triangles”).
- ❖ The reasons for triadic closure.
- ❖ What are we trying to do?

Differentiate between friends and acquaintances
– strong and weak ties.

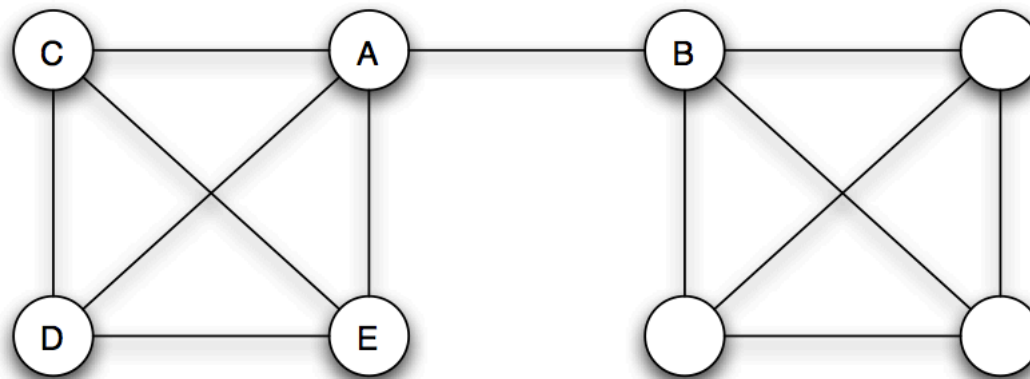


Why acquaintances...

- ❖ The close friends we have, we talk to them frequently, and share information more frequently with them.
- ❖ So, it is less likely that they have information we don't.
- ❖ The reasons for triadic closure.
- ❖ What are we trying to do?

Differentiate between friends and acquaintances – strong and weak ties.

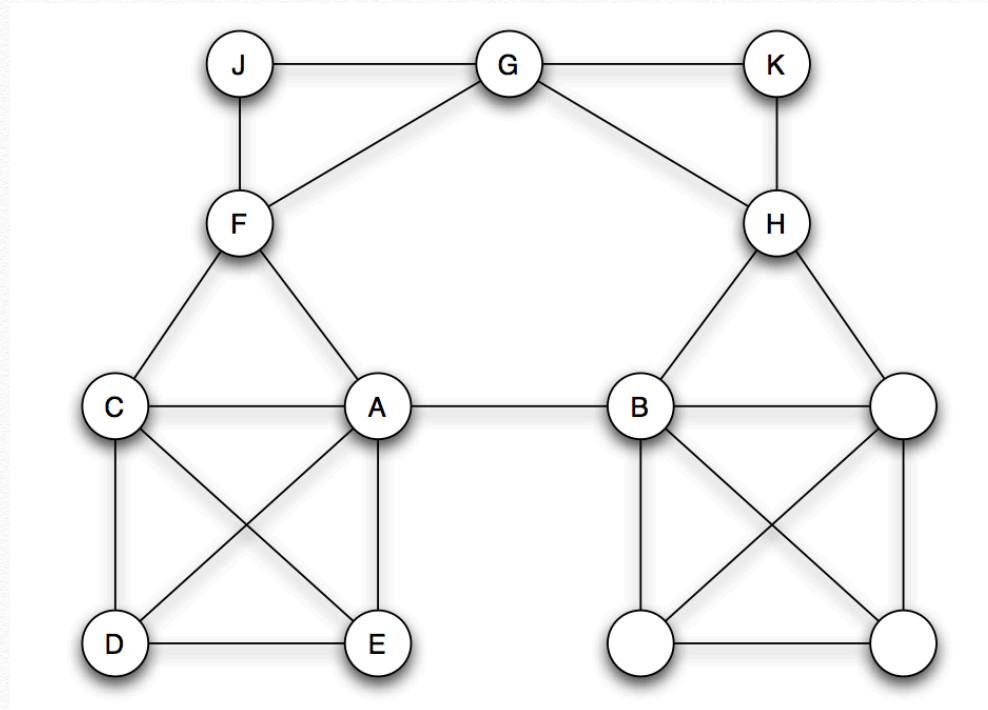
Bridges



A-B is a bridge; its removal disconnects the graph into 2 components, with A and B lying in different components.

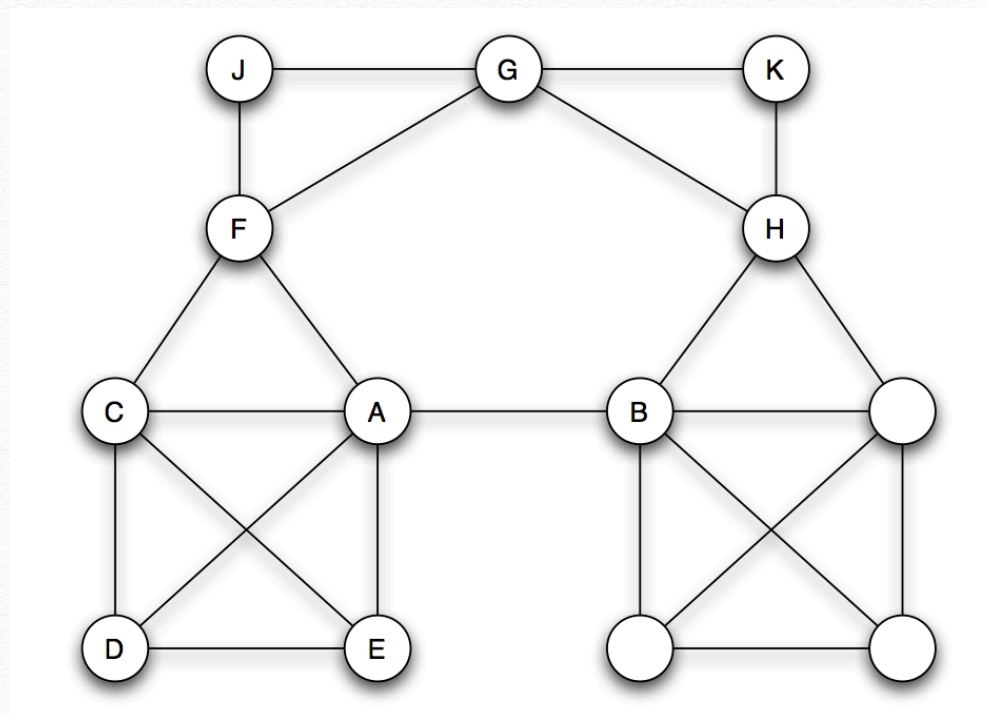
In real social networks, bridges may be rare, so...?

Local Bridges



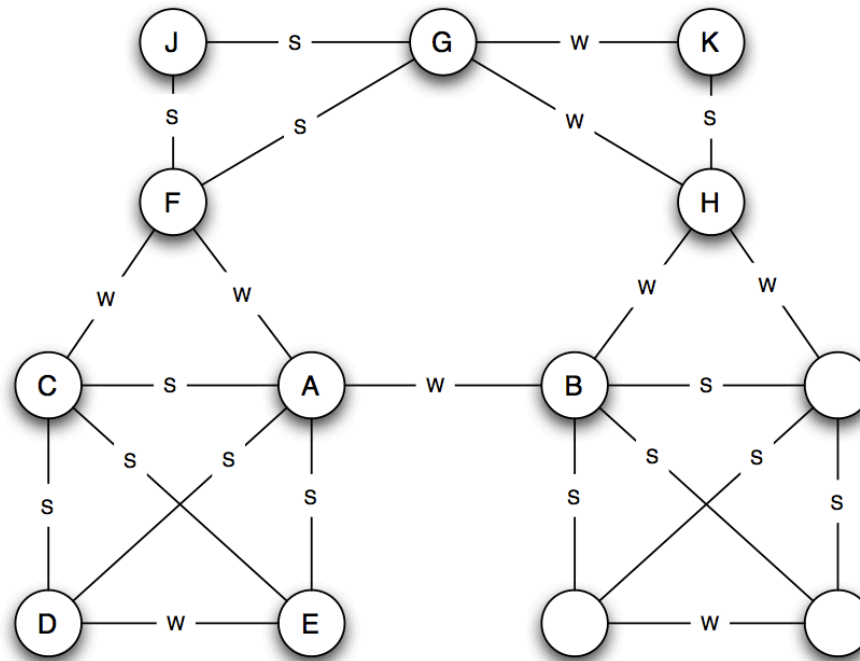
The A-B edge is a local bridge of span 4, since the removal of this edge would increase the distance between A and B to 4.

Local Bridges



We say that an edge joining two nodes A and B in a graph is a **local bridge** if its endpoints A and B have no friends in common — in other words, if deleting the edge would increase the distance between A and B to a value strictly more than two.

Local Bridges

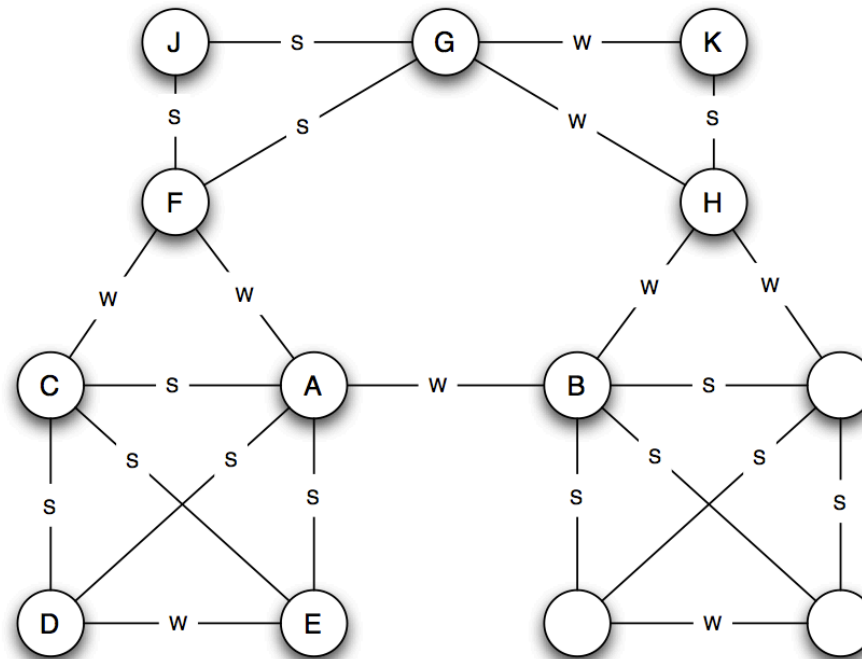


The labelling in the figure satisfies the Strong Triadic Closure Property at each node: if the node has strong ties to two neighbours, then these neighbours must have at least a weak tie between them.

Strong Triadic Closure Property

- ❖ If a node A has edges to nodes B and C, then the B-C edge is especially likely to form if A's edges to B and C are both strong ties.
- ❖ Granovetter's version:
- ❖ We say that a node A **violates** the Strong Triadic Closure Property if it has strong ties to two other nodes B and C, and there is no edge at all (either a strong or weak tie) between B and C.
- ❖ We say that a node A satisfies the Strong Triadic Closure Property if it does not violate it.

Strong Triadic Closure Property

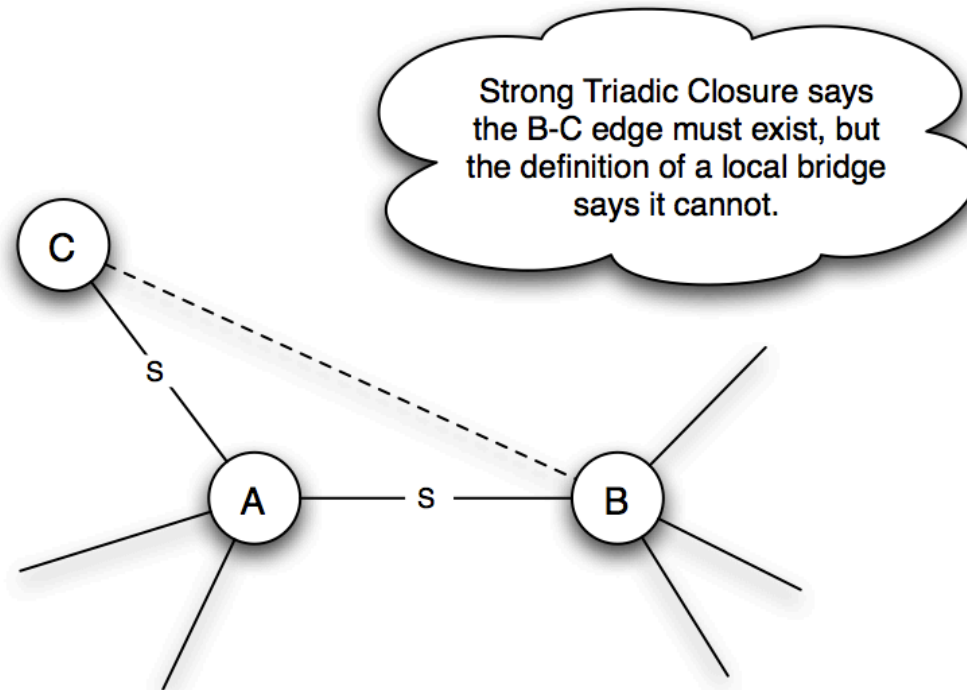


Each edge of the social network is labeled here as either a strong tie (S) or a weak tie (W), to indicate the strength of the relationship.

Local Bridges and Weak Ties

- ❖ A purely local, interpersonal distinction between kinds of links — whether they are weak ties or strong ties — as well as a global, structural notion — whether they are local bridges or not.
- ❖ What is the connection?
- ❖ Claim: If a node A in a network satisfies the Strong Triadic Closure Property and is involved in at least two strong ties, then any local bridge it is involved in must be a weak tie.
- ❖ Assuming the Strong Triadic Closure Property and a sufficient number of strong ties, the local bridges in a network are necessarily weak ties.
- ❖ *How to prove this?*

Local Bridges and Weak Ties



if the A-B edge is a strong tie, then there must also be an edge between B and C, meaning that the A-B edge cannot be a local bridge.

So, what happened?

- ❖ We found the connection between the local property of tie strength and the global property of serving as a local bridge.
- ❖ A way to think about the way in which interpersonal properties of social-network links are related to broader considerations about the network's structure.

Granovetter's Problem

- ❖ Links two different perspectives on distant relationships.
- ❖ One interpersonal, using purely local considerations of friendship between two people being strong (friend) and weak (acquaintance).
- ❖ The other structural, how friendships span different parts of the entire network.

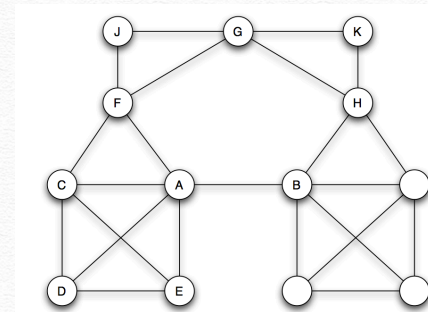
So, what did we learn?

- ❖ Simplifying assumptions (STCP) are useful when they lead to statements that are robust in practice.
 - ❖ Informally, a local bridge between nodes A and B tends to be a weak tie because if it weren't, triadic closure would tend to produce short-cuts to A and B that would eliminate its role as a local bridge.
- ❖ When the underlying assumptions are stated precisely, as they are here, it becomes possible to test them on real-world data.
- ❖ This analysis provides a concrete framework for thinking about the initially surprising fact that life transitions such as a new jobs are often rooted in contact with distant acquaintances.
 - ❖ The argument is that these are the social ties that connect us to new sources of information and new opportunities.
 - ❖ Their conceptual "span" in the social network (the local bridge property) is directly related to their weakness as social ties.
 - ❖ This dual role as weak connections but also valuable conduits to hard-to-reach parts of the network — this is the surprising strength of weak ties.

The story continues...

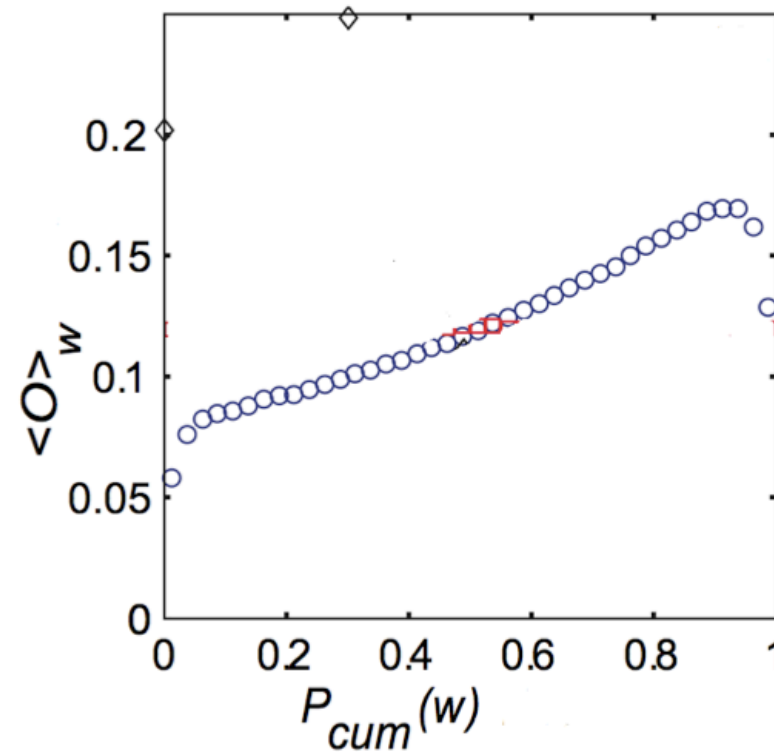
- ❖ For many years after Granovetter's work, these predictions remained untested on large social networks..
- ❖ Difficulty of finding data that would reliably capture these parameters.
- ❖ Enter digital communication data.
- ❖ Onnela et al. studied the who-talks-to-whom network maintained by a cell-phone provider that covered roughly 20% of a national population.

The story continues...

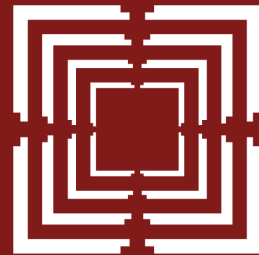


- ❖ So, how to define the metrics for a practical situation?
- ❖ Tie strength: we can make the strength of an edge a numerical quantity, defining it to be the total number of minutes spent on phone calls between the two ends of the edge.
- ❖ It is also useful to sort all the edges by tie strength, so that for a given edge we can ask what percentile it occupies this ordering of edges sorted by strength.
- ❖ *What about local bridges and “almost” local bridges?*
- ❖ Define the **neighbourhood overlap** of an edge connecting A and B as...
 - ❖
$$\frac{\text{number of nodes who are neighbours of both A and B}}{\text{number of nodes who are neighbours of at least one of A and B}}$$

Tie-strength & Network Structure in Large-Scale Data



A plot of the neighbourhood overlap (O) of edges as a function of their percentile (P) in the sorted order of all edges by tie strength. The fact that overlap increases with increasing tie strength is consistent with the theoretical predictions.



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Thank you!

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