

Lecture 14:

Image Segmentation

Admin: Midterm + A3 Grades

Midterm grades: Should be out tomorrow

A3 grades: Later this week or early next week

A4 Update

Will be out tomorrow (?!?)

Due 2 weeks after release – will update calendar

Last Time: Localization Tasks

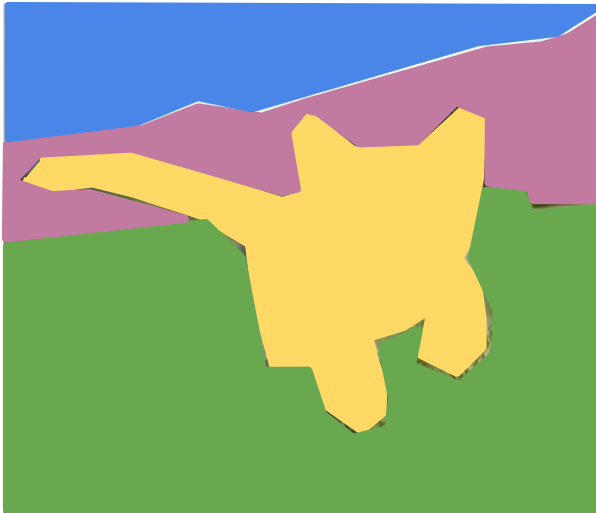
Classification



CAT

No spatial extent

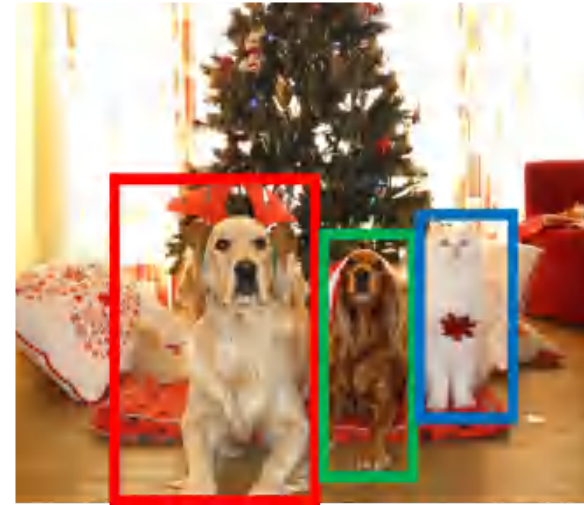
Semantic Segmentation



GRASS, CAT, TREE, SKY

No objects, just pixels

Object Detection



DOG, DOG, CAT

Multiple Objects

Instance Segmentation

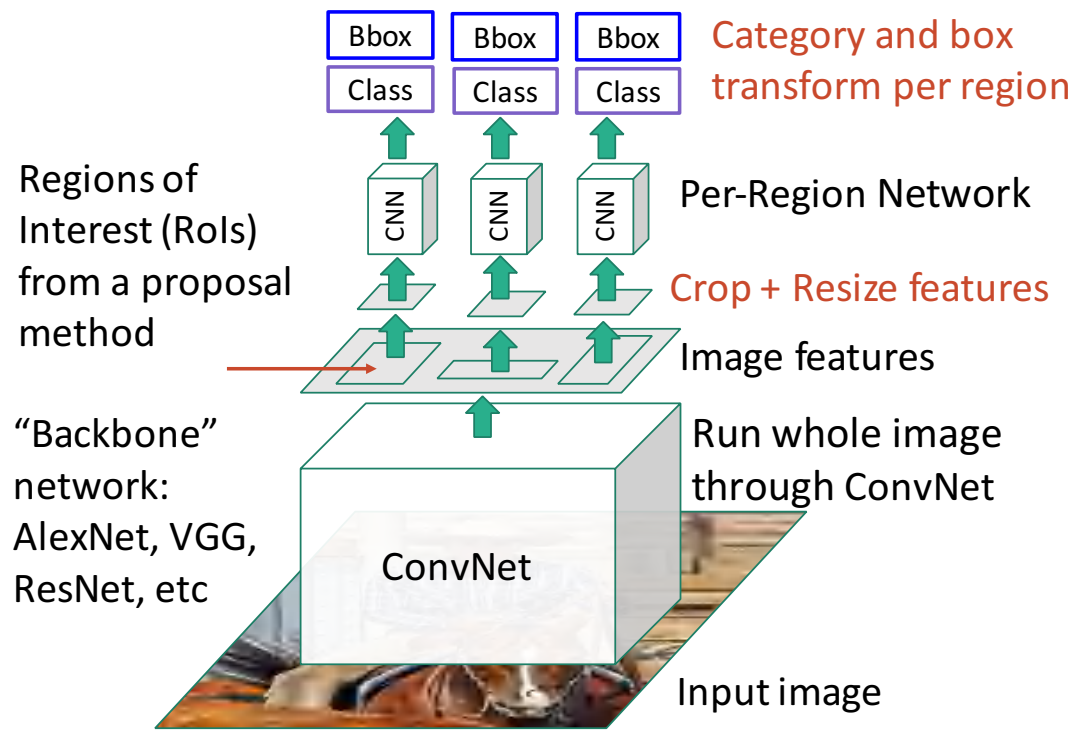


DOG, DOG, CAT

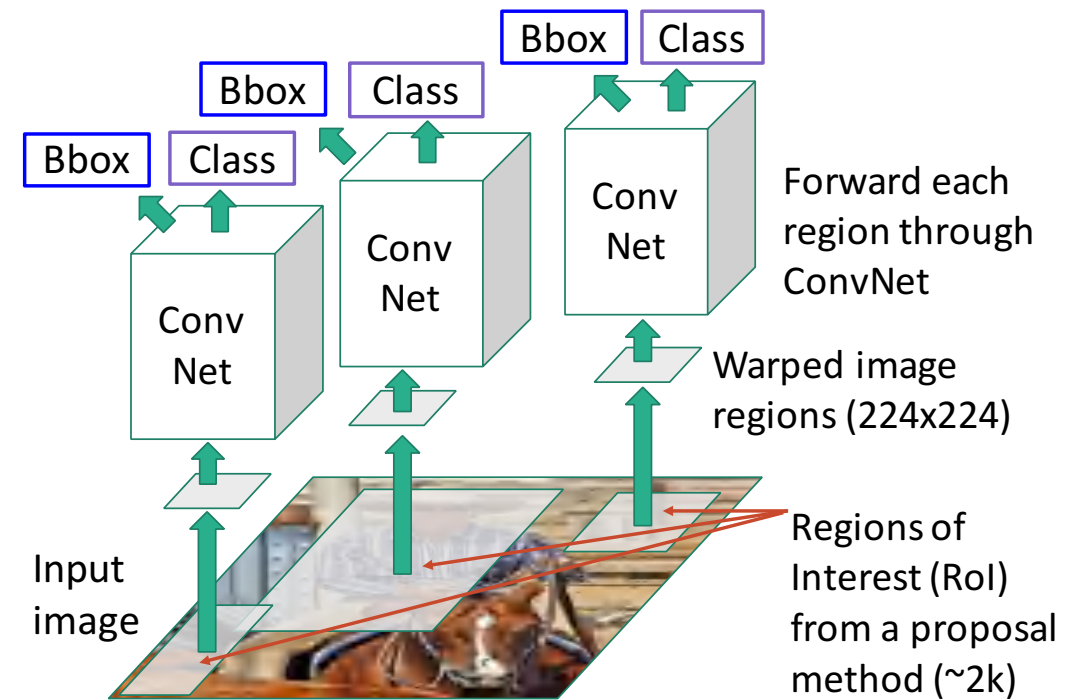
[This image is CC0 public domain](#)

Last Time: Fast R-CNN

Fast R-CNN: Apply differentiable cropping to shared image features

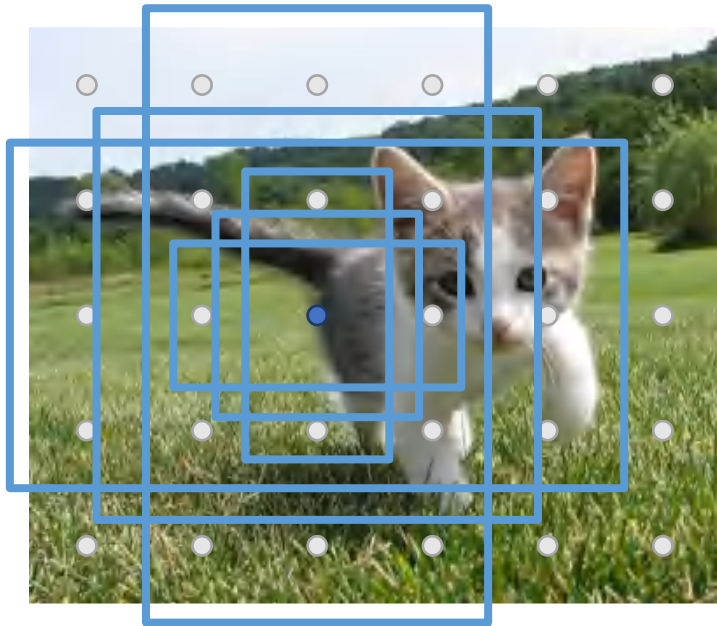


"Slow" R-CNN: Apply differentiable cropping to shared image features



Last Time: Region Proposal Network (RPN)

Run backbone CNN to get features aligned to input image



Input Image
(e.g. 3 x 640 x 480)

Each feature corresponds to a point in the input

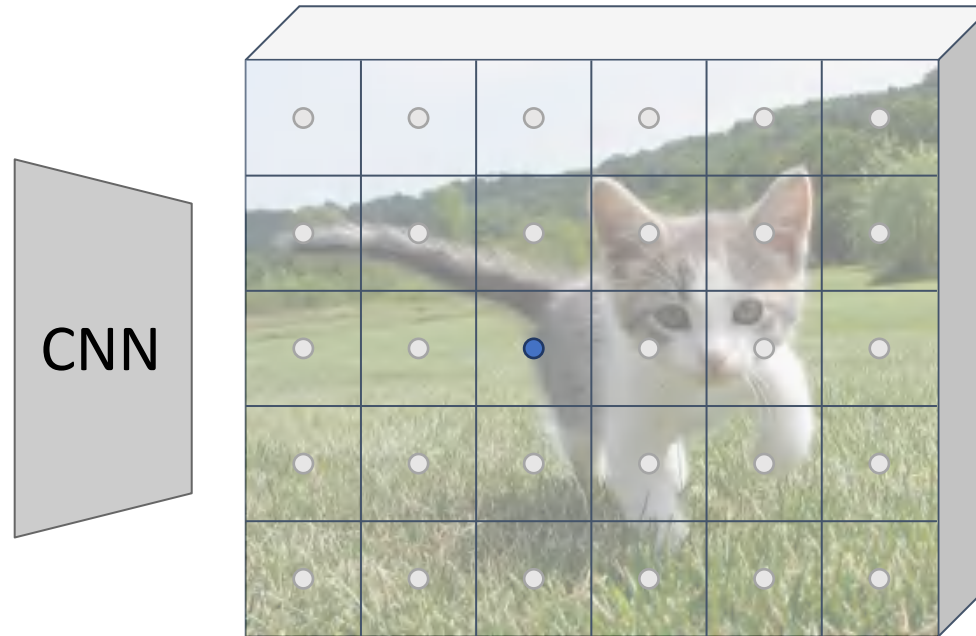


Image features
(e.g. 512 x 5 x 6)



Anchor is
object?
2K x 5 x 6

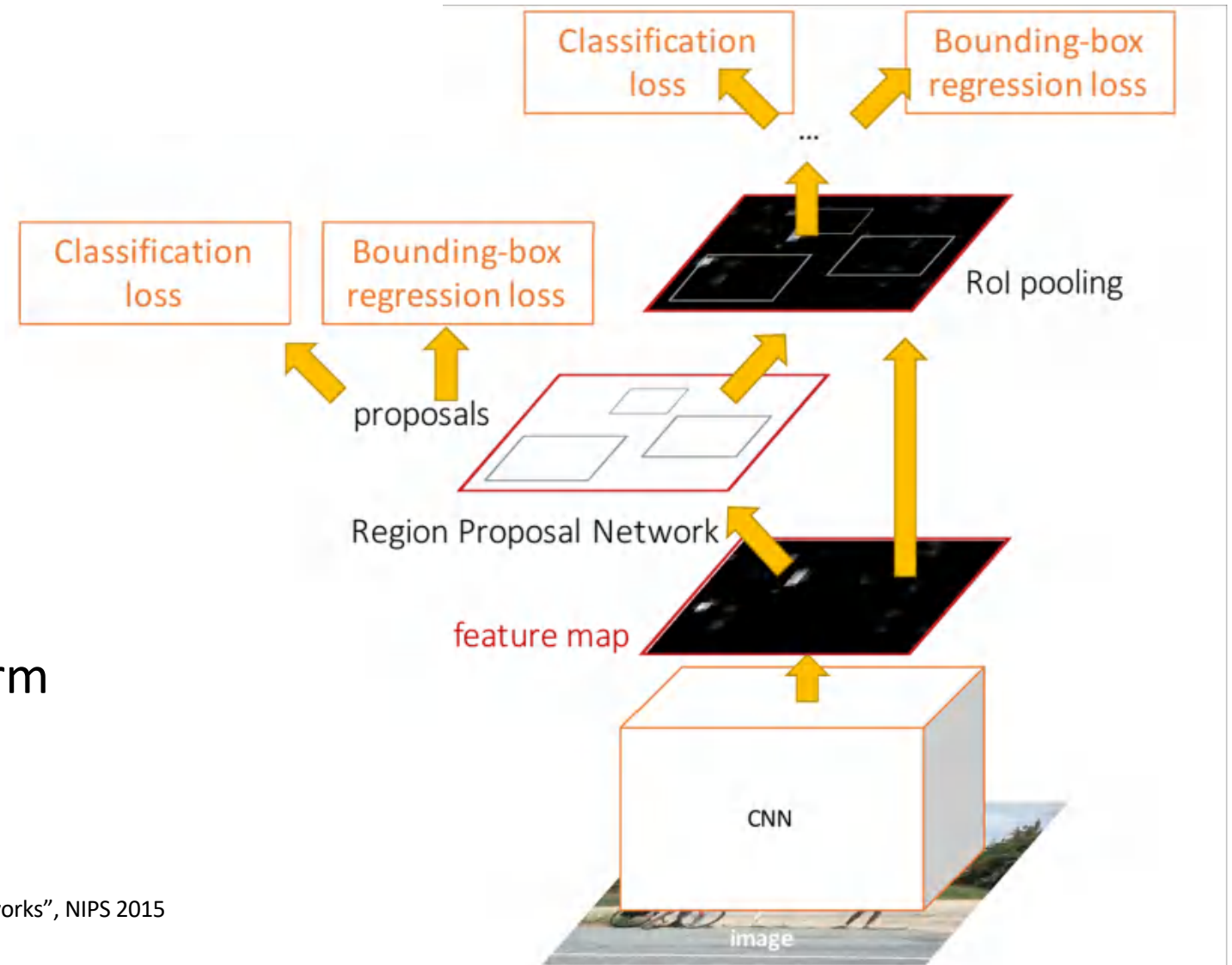
Anchor
transforms
4K x 5 x 6

At test-time, sort all $K \times 5 \times 6$ boxes by their positive score, take top 300 as our region proposals

Last Time: Faster R-CNN

Jointly train with 4 losses:

1. **RPN classification:** anchor box is object / not an object
2. **RPN regression:** predict transform from anchor box to proposal box
3. **Object classification:** classify proposals as background / object class
4. **Object regression:** predict transform from proposal box to object box

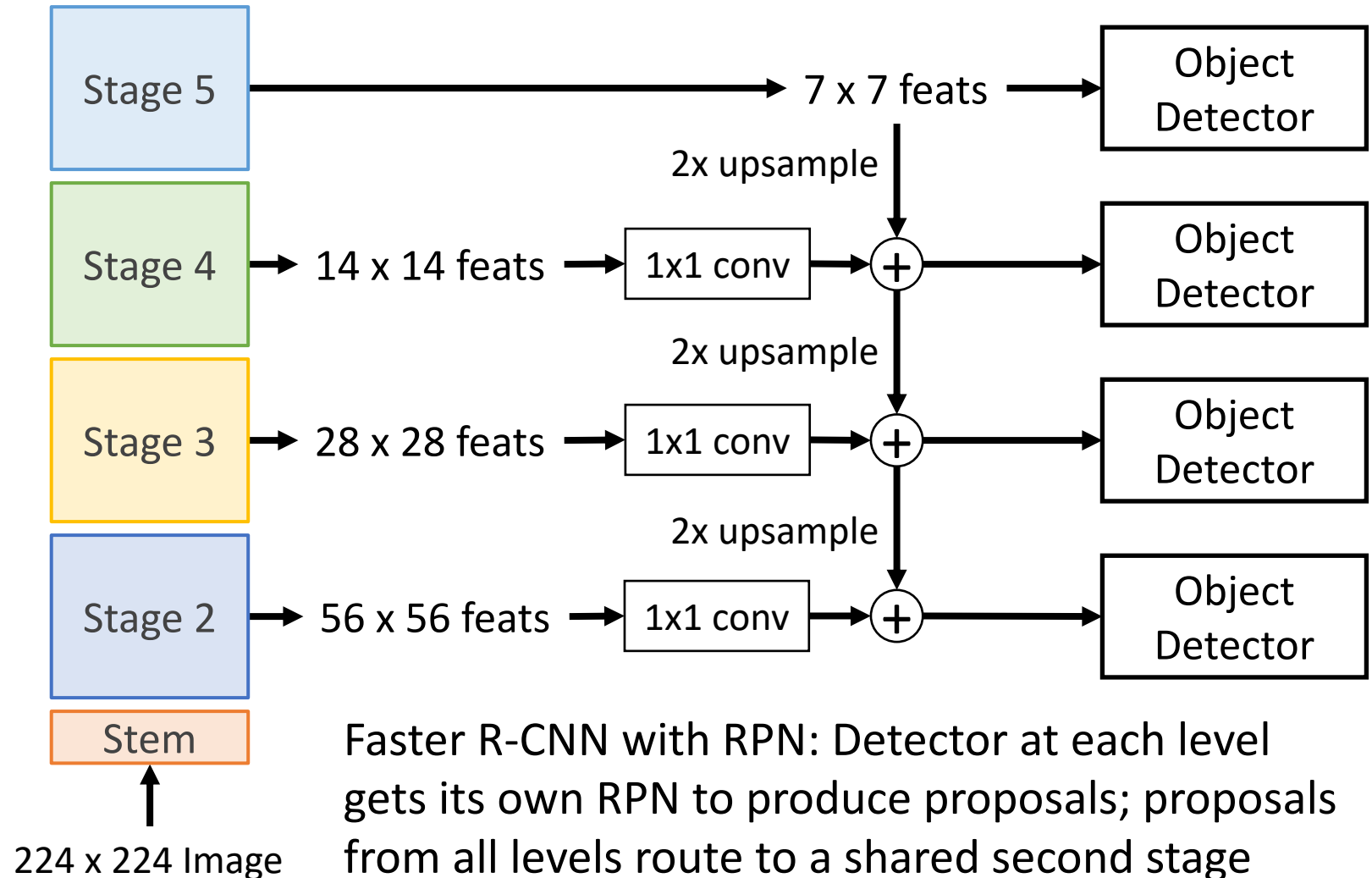


Ren et al, "Faster R-CNN: Towards Real-Time Object Detection with Region Proposal Networks", NIPS 2015
Figure copyright 2015, Ross Girshick; reproduced with permission

Last Time: Feature Pyramid Network (FPN)

Add *top down* connections that feed information from high level features back down to lower level features

Efficient multiscale features where all levels benefit from the whole backbone! Widely used in practice



Lin et al, "Feature Pyramid Networks for Object Detection", ICCV 2017

Two Stage Object Detectors

Question: Do we really need the second stage?

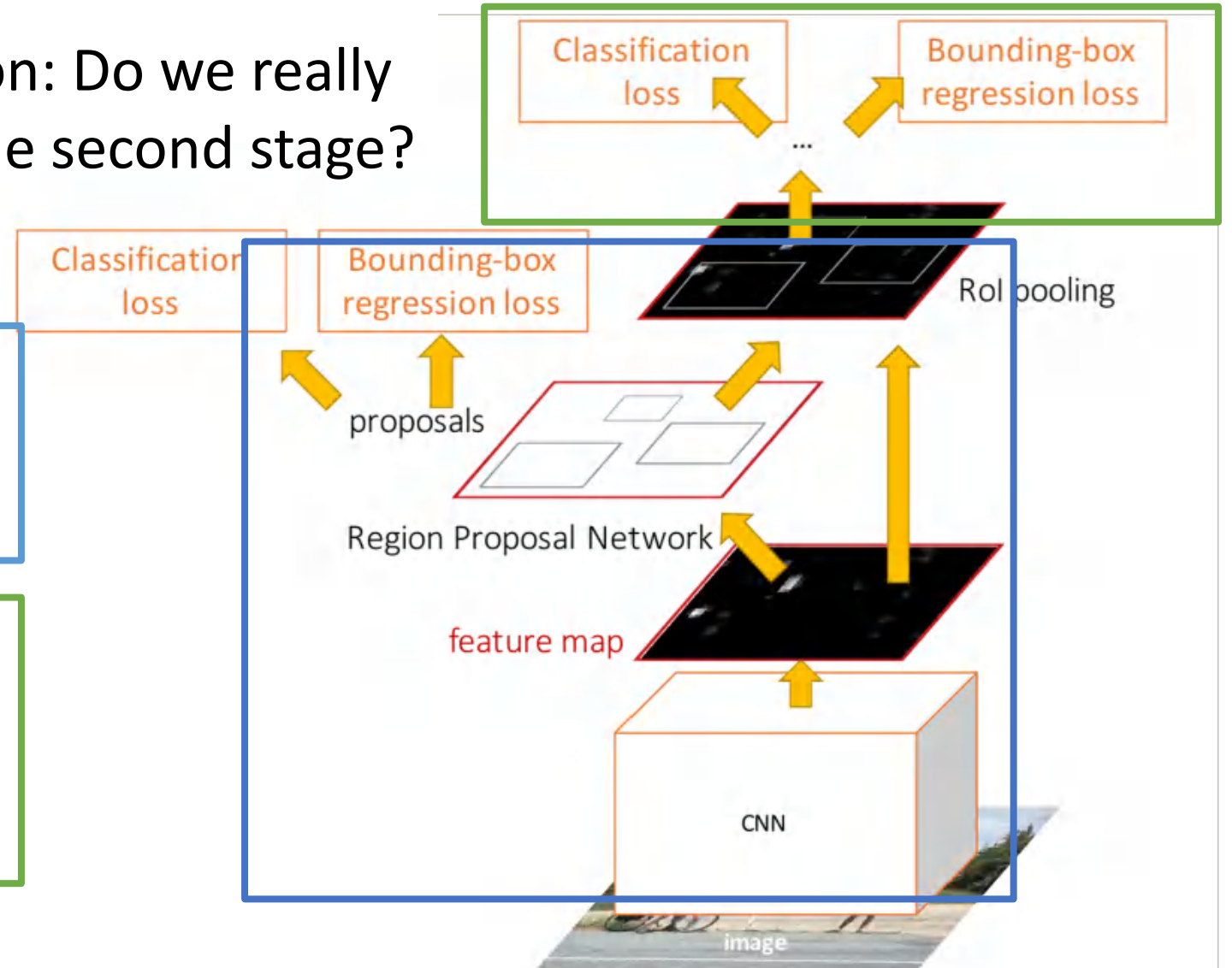
Faster R-CNN is a
Two-stage object detector

First stage: Run once per image

- Backbone network
- Region proposal network

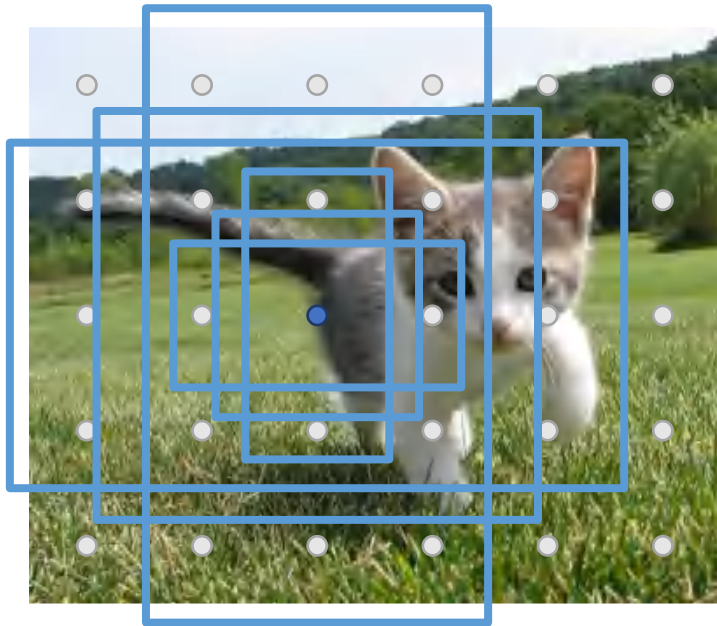
Second stage: Run once per region

- Crop features: RoI pool / align
- Predict object class
- Prediction bbox offset



Single-Stage Detectors: RetinaNet

Run backbone CNN to get features aligned to input image



Input Image
(e.g. 3 x 640 x 480)

Each feature corresponds to a point in the input

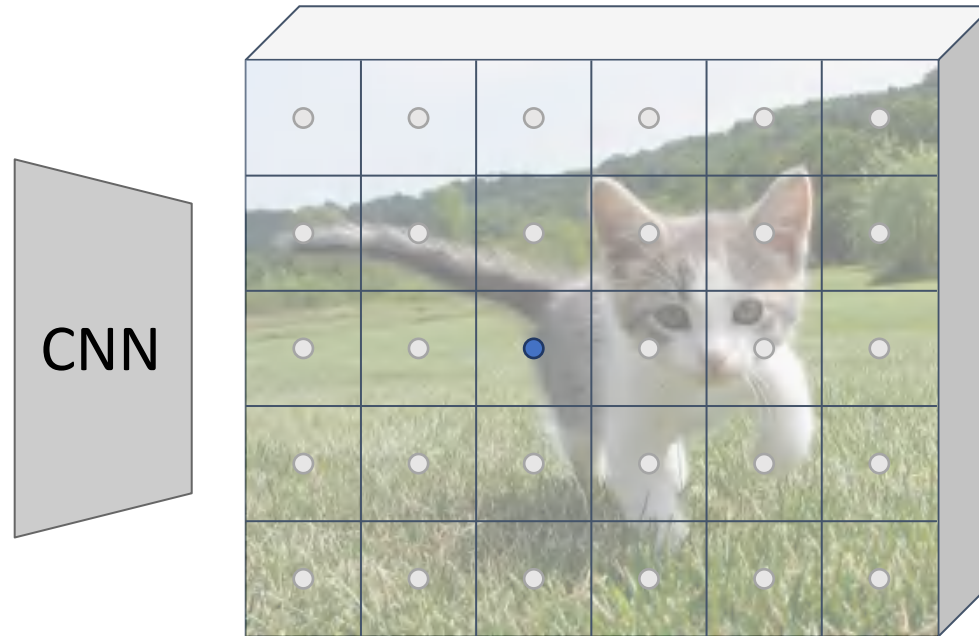


Image features
(e.g. 512 x 5 x 6)

Similar to RPN – but rather than classify anchors as object/no object, directly predict object category (among C categories) or background



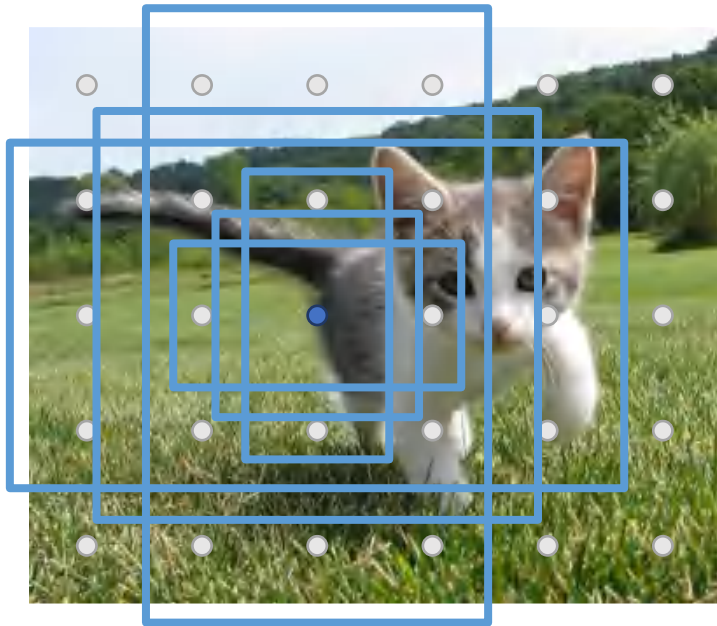
Anchor
classification
 $2K*(C+1) \times 5 \times 6$

Anchor
transforms
 $4K \times 5 \times 6$

Single-Stage Detectors: RetinaNet

Problem: class imbalance –
many more background
anchors vs non-background

Run backbone CNN to get
features aligned to input image



Input Image
(e.g. 3 x 640 x 480)

Each feature corresponds
to a point in the input

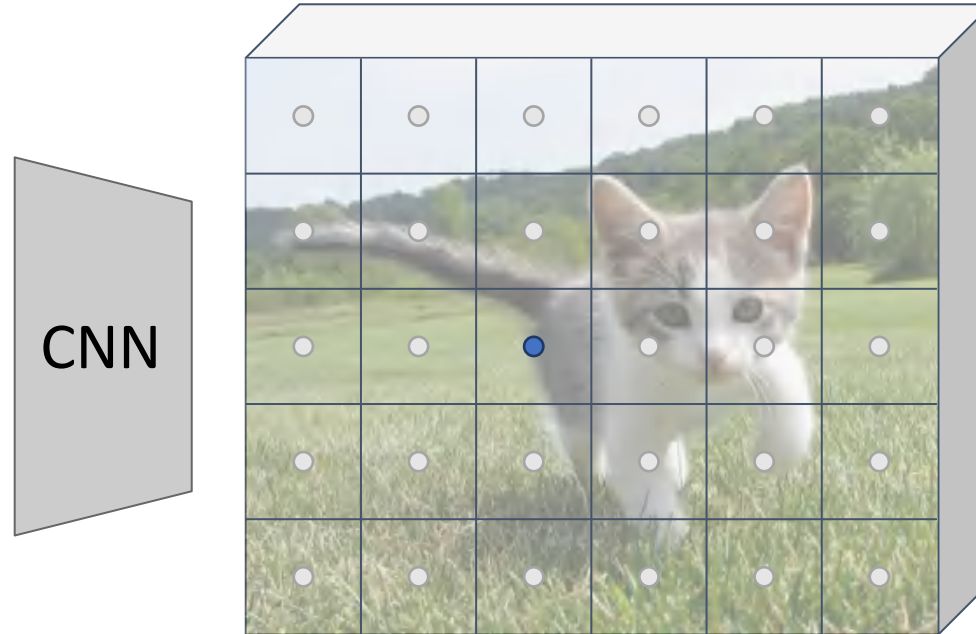


Image features
(e.g. 512 x 5 x 6)

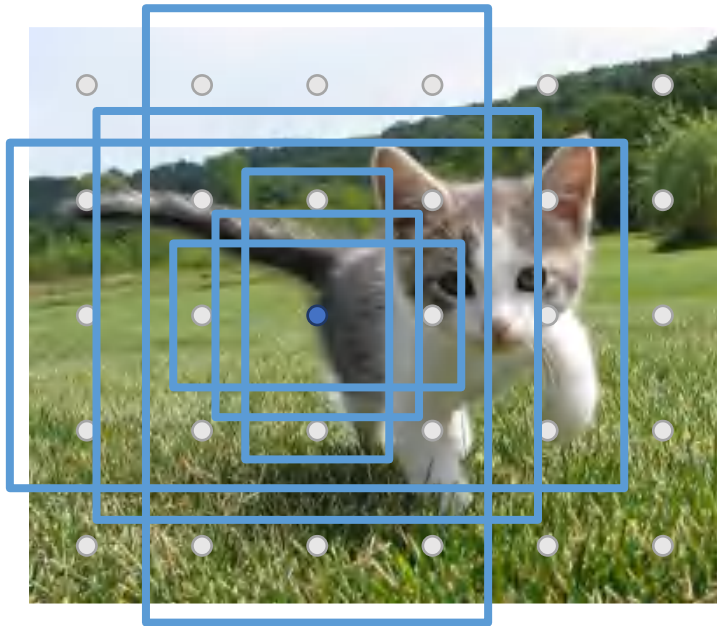


Anchor
→ classification
 $2K \times (C+1) \times 5 \times 6$

Anchor
→ transforms
 $4K \times 5 \times 6$

Single-Stage Detectors: RetinaNet

Run backbone CNN to get features aligned to input image



Input Image
(e.g. 3 x 640 x 480)

Each feature corresponds to a point in the input

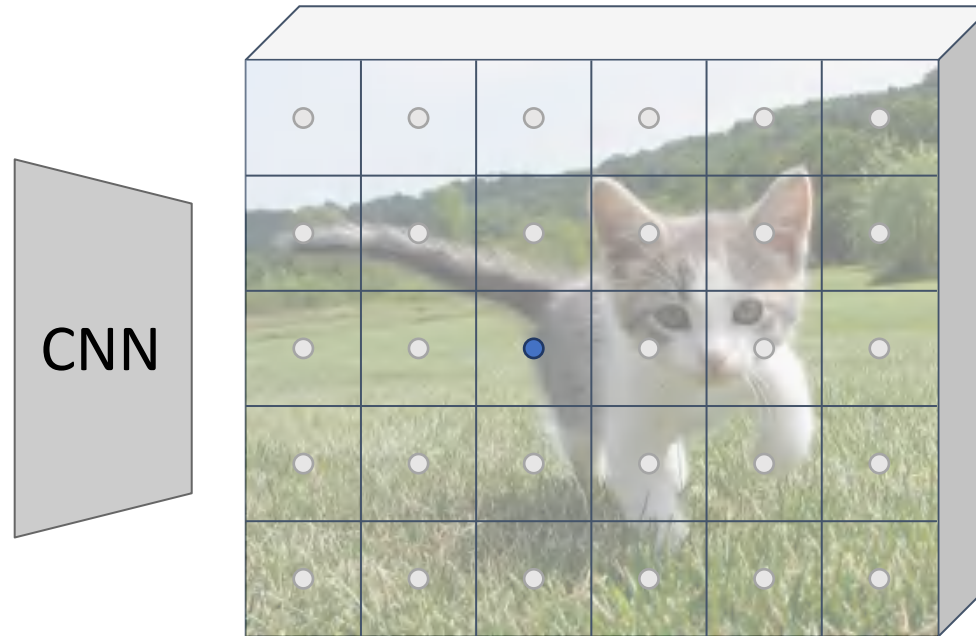


Image features
(e.g. 512 x 5 x 6)

Problem: class imbalance – many more background anchors vs non-background

Solution: new loss function (Focal Loss); see paper



Anchor
→ classification
 $2K \times (C+1) \times 5 \times 6$

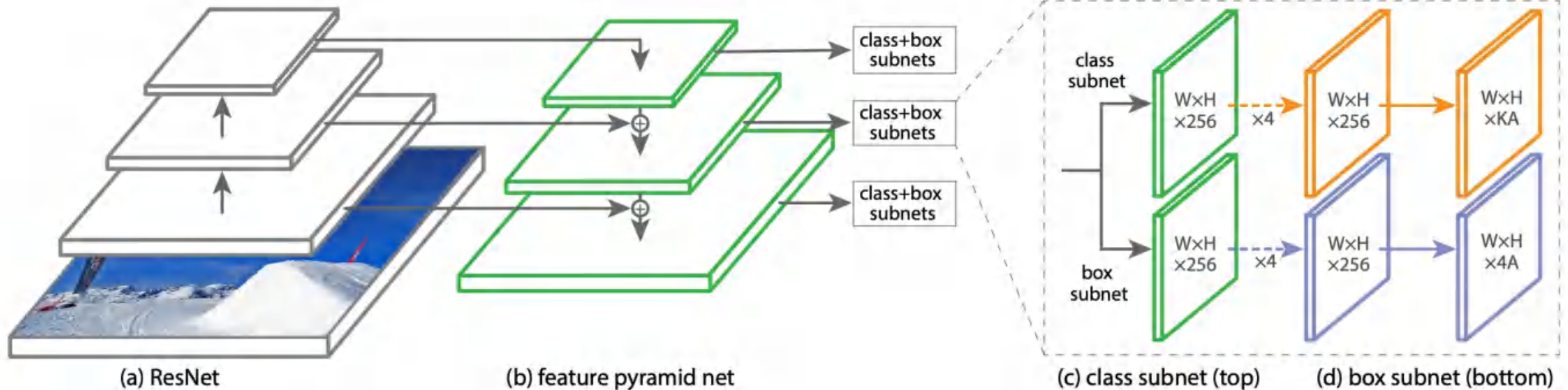
Anchor
→ transforms
 $4K \times 5 \times 6$

$$CE(p_t) = -\log(p_t)$$

$$FL(p_t) = -(1 - p_t)^\gamma \log(p_t)$$

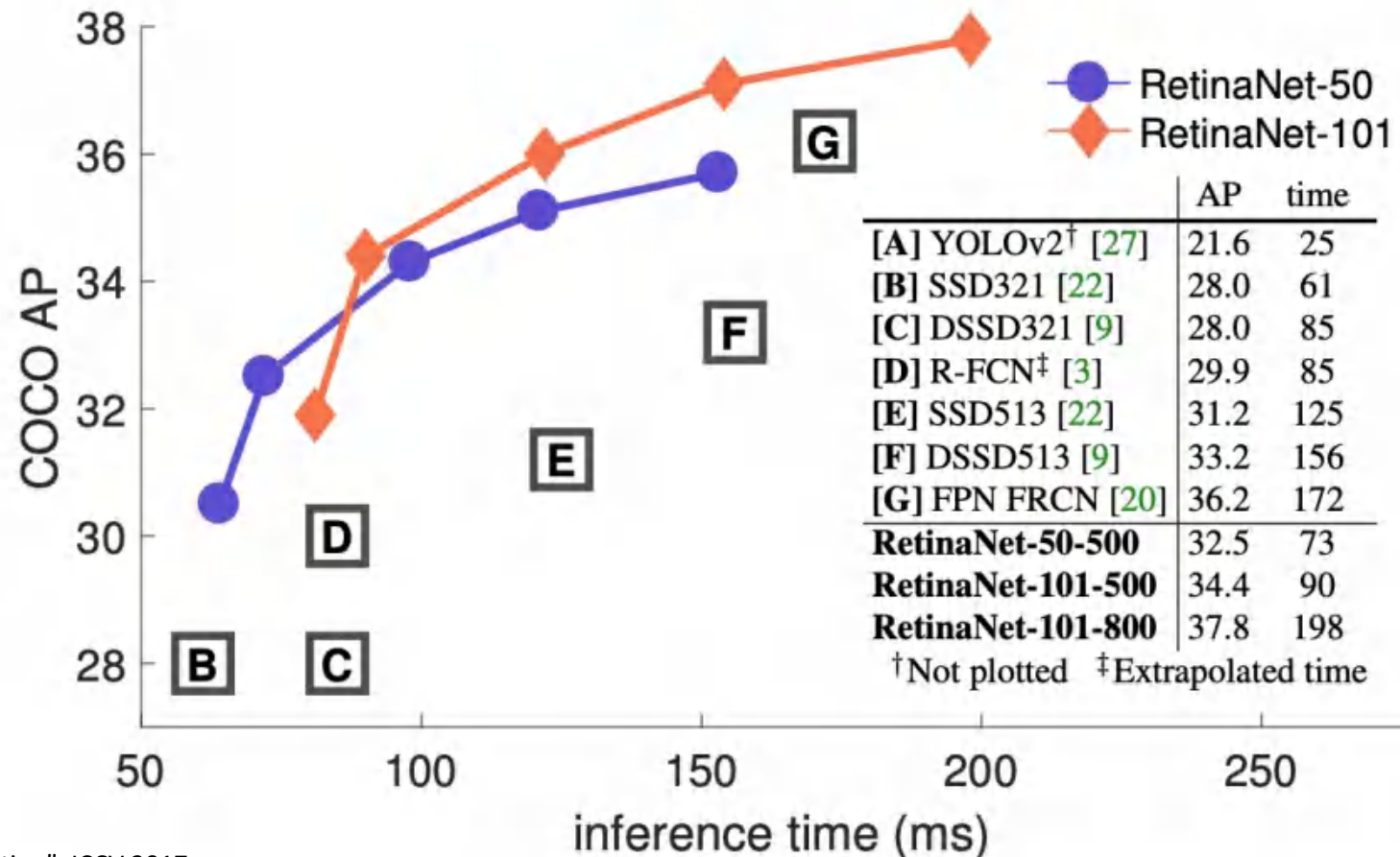
Single-Stage Detectors: RetinaNet

In practice, RetinaNet also uses Feature Pyramid Network to handle multiscale



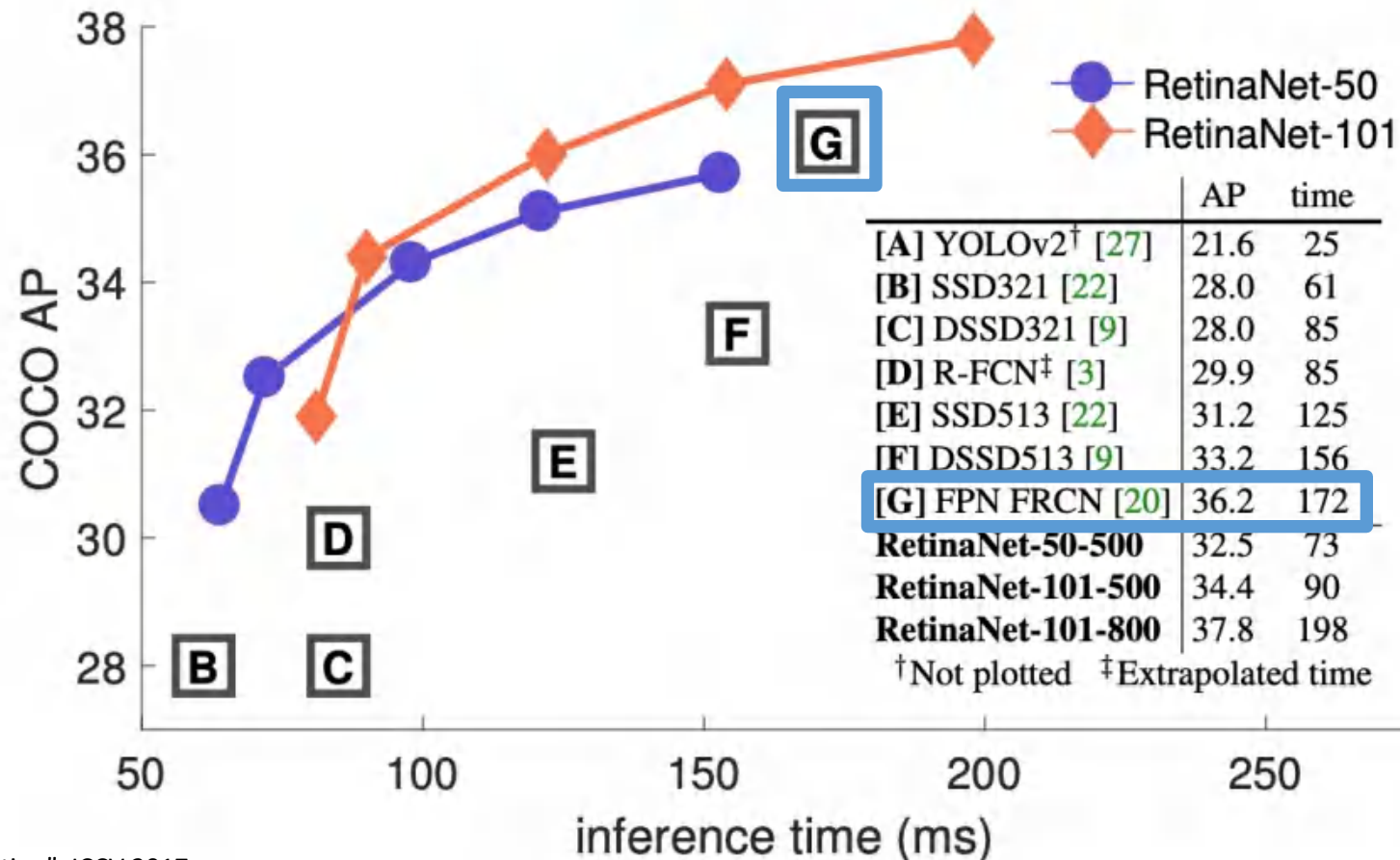
Single-Stage Detectors: RetinaNet

Single-Stage detectors can be much faster than two-stage detectors



Single-Stage Detectors: RetinaNet

Single-Stage detectors can be much faster than two-stage detectors



Faster R-CNN
with Feature
Pyramid
Network

Anchor-Free Detectors

Can we do object detection without anchors?

CornerNet: Law and Deng, “CornerNet: Detecting Objects as Paired Keypoints”, ECCV 2018

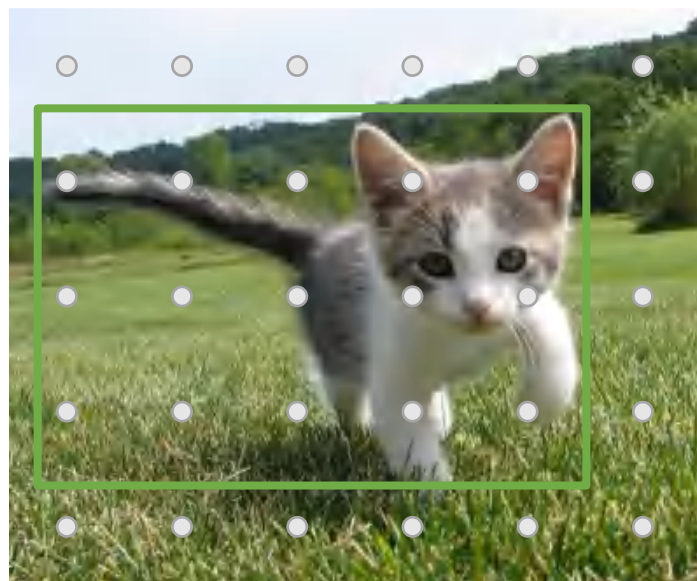
CenterNet: Zhou et al, “Objects as Points”, arXiv 2019

FCOS: Tian et al, “FCOS: Fully Convolutional One-Stage Object Detection”, ICCV 2019

Single-Stage Detectors: FCOS

“Anchor-free” detector

Run backbone CNN to get features aligned to input image



Input Image
(e.g. 3 x 640 x 480)

Each feature corresponds to a point in the input

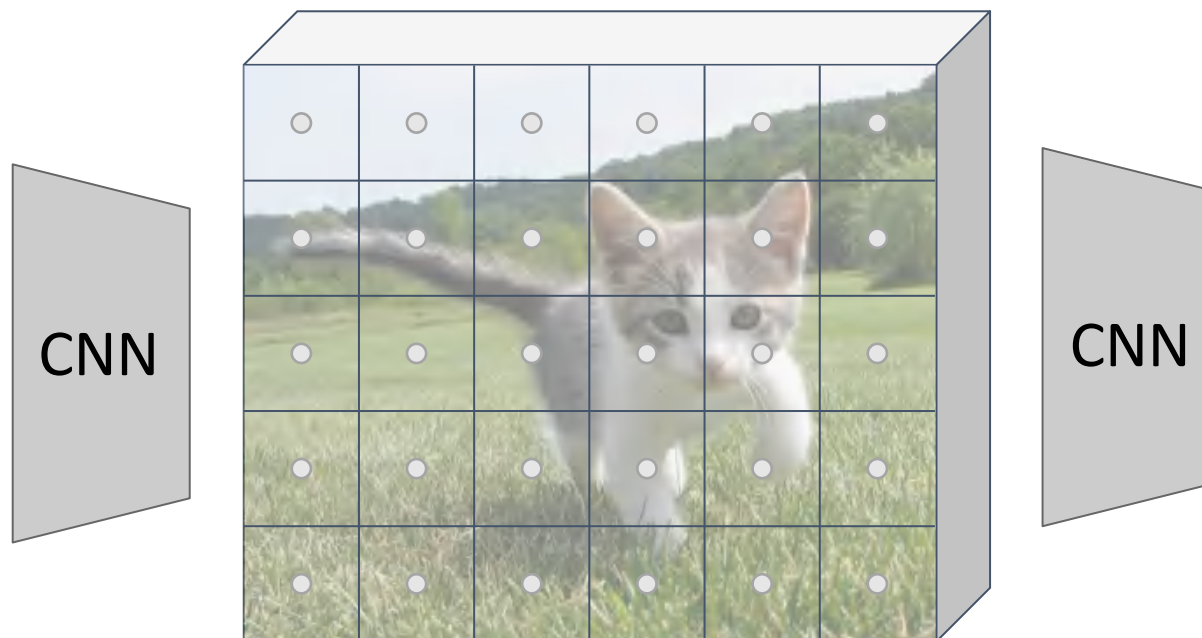
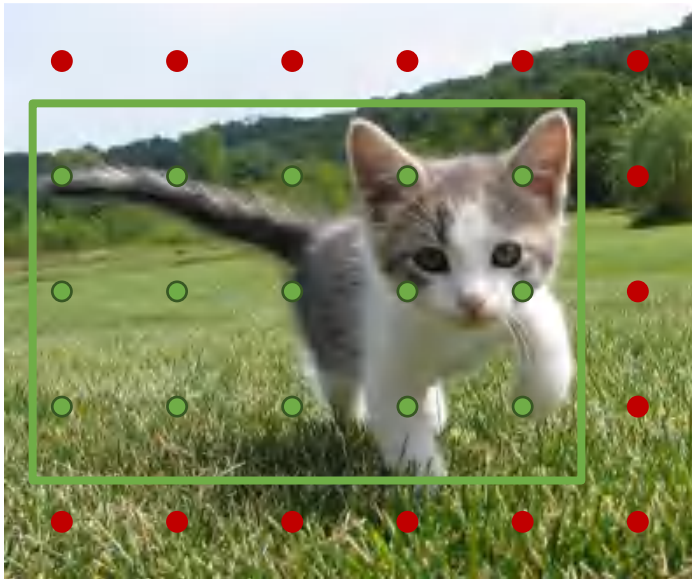


Image features
(e.g. 512 x 5 x 6)

Single-Stage Detectors: FCOS

Run backbone CNN to get features aligned to input image



Input Image
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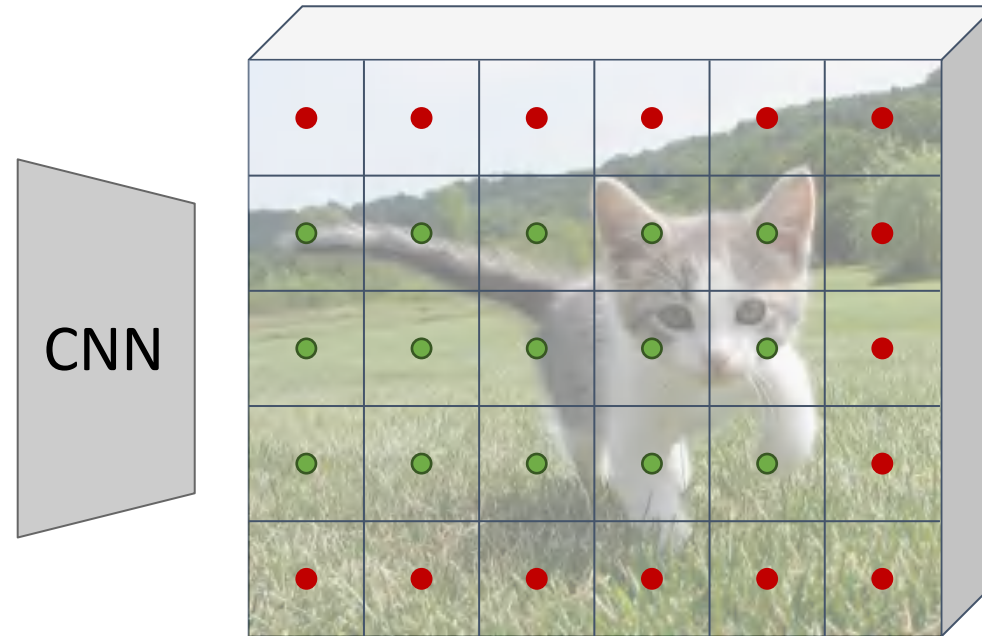


Image features
(e.g. 512 x 5 x 6)

“Anchor-free” detector

Classify points as positive if they fall into a GT box, or negative if they don't

Train independent per-category logistic regressors

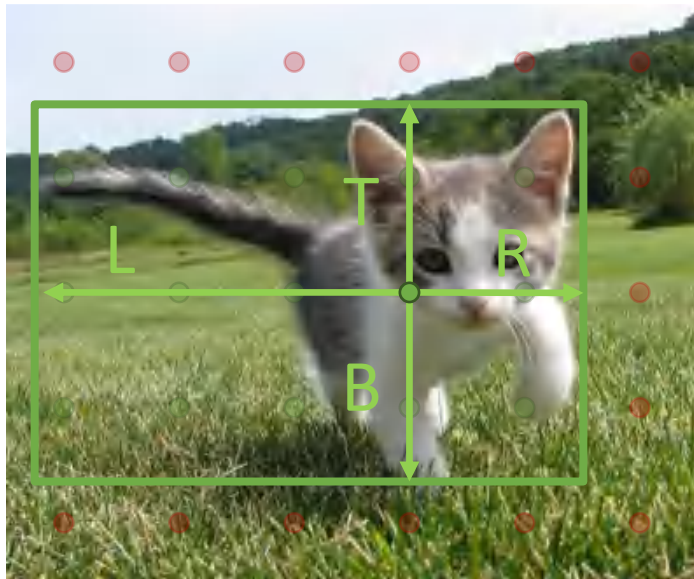
→ Class scores
 $C \times 5 \times 6$



Single-Stage Detectors: FCOS

“Anchor-free” detector

Run backbone CNN to get features aligned to input image



Input Image
(e.g. 3 x 640 x 480)

Each feature corresponds to a point in the input

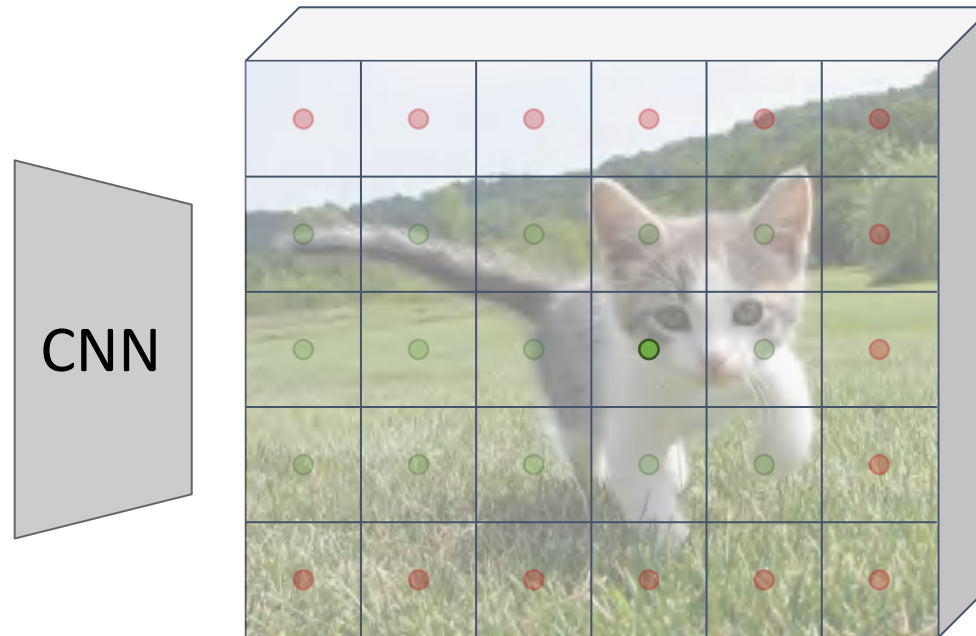


Image features
(e.g. 512 x 5 x 6)

For positive points, also regress distance to left, right, top, and bottom of ground-truth box (with L2 loss)



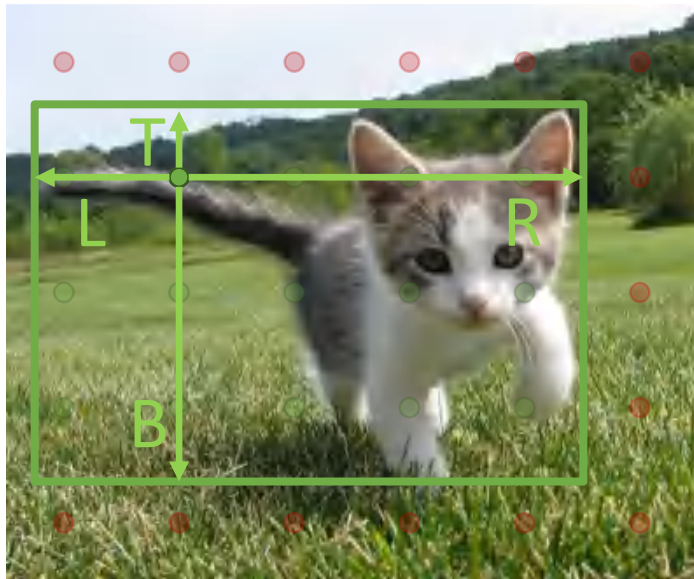
Class scores
 $C \times 5 \times 6$

Box edges
 $4 \times 5 \times 6$

Single-Stage Detectors: FCOS

“Anchor-free” detector

Run backbone CNN to get features aligned to input image



Input Image
(e.g. 3 x 640 x 480)

Each feature corresponds to a point in the input

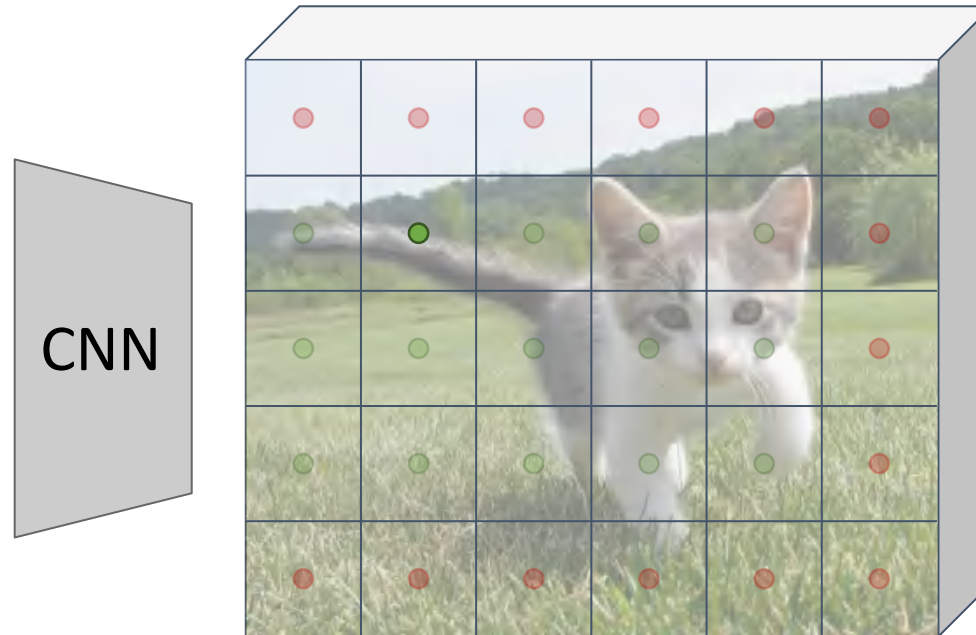


Image features
(e.g. 512 x 5 x 6)

For positive points, also regress distance to left, right, top, and bottom of ground-truth box (with L2 loss)

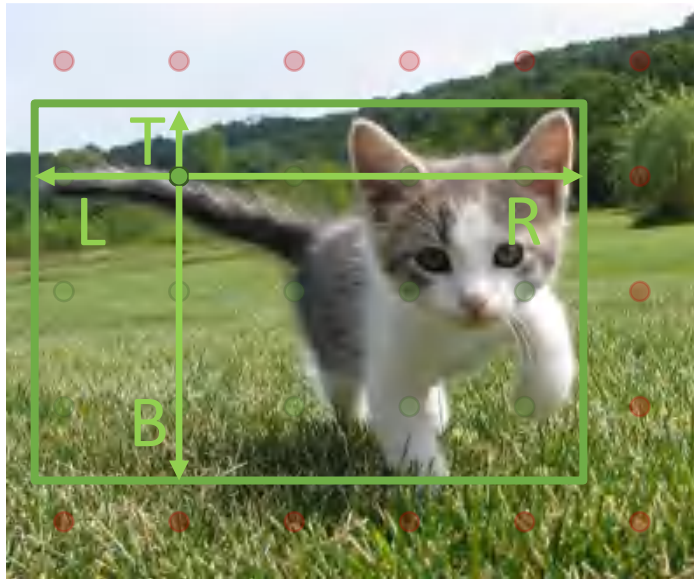


Class scores
 $C \times 5 \times 6$

Box edges
 $4 \times 5 \times 6$

Single-Stage Detectors: FCOS

Run backbone CNN to get features aligned to input image



Input Image
(e.g. 3 x 640 x 480)

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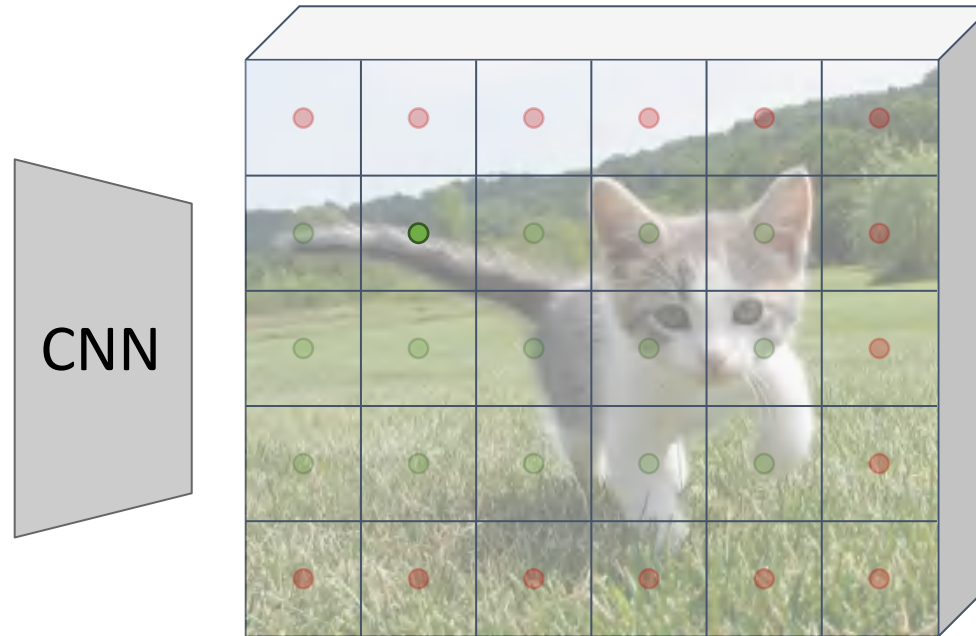


Image features
(e.g. 512 x 5 x 6)

“Anchor-free” detector

Finally, predict “centerness” for all positive points (using logistic regression loss)

Class scores
→ C x 5 x 6

Box edges
→ 4 x 5 x 6

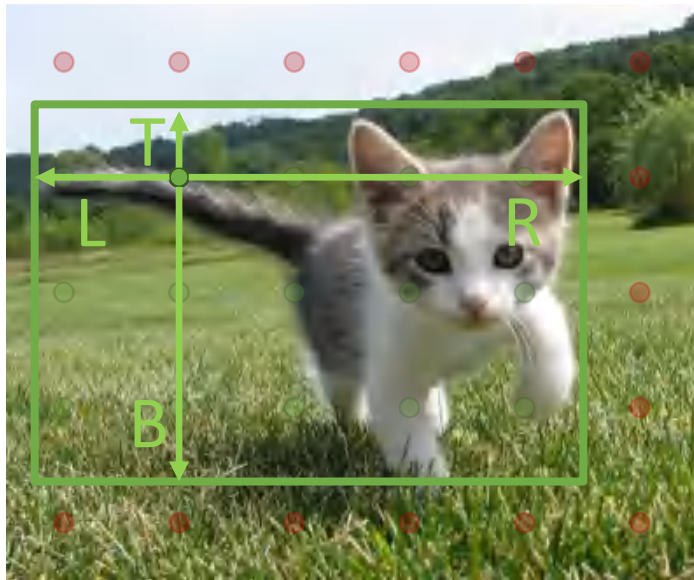
Centerness
→ 1 x 5 x 6

$$centerness = \sqrt{\frac{\min(L, R)}{\max(L, R)} \cdot \frac{\min(T, B)}{\max(T, B)}}$$

Ranges from 1 at box center to 0 at box edge

Single-Stage Detectors: FCOS

Run backbone CNN to get features aligned to input image



Input Image
(e.g. 3 x 640 x 480)

Each feature corresponds to a point in the input

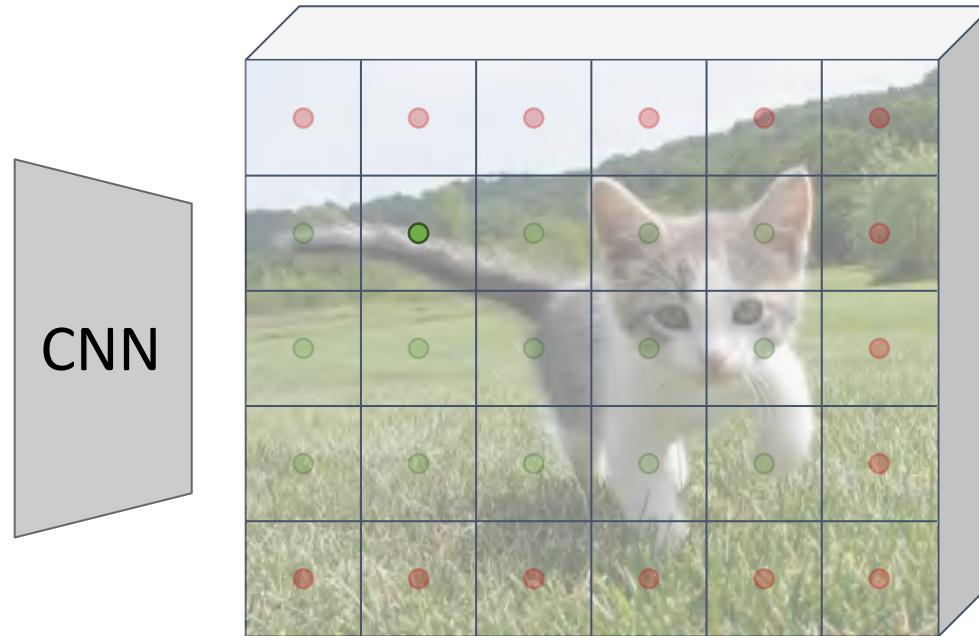


Image features
(e.g. 512 x 5 x 6)

“Anchor-free” detector

Test-time: predicted
“confidence” for the box from
each point is product of its
class score and centerness



- Class scores
 $C \times 5 \times 6$
- Box edges
 $4 \times 5 \times 6$
- Centerness
 $1 \times 5 \times 6$

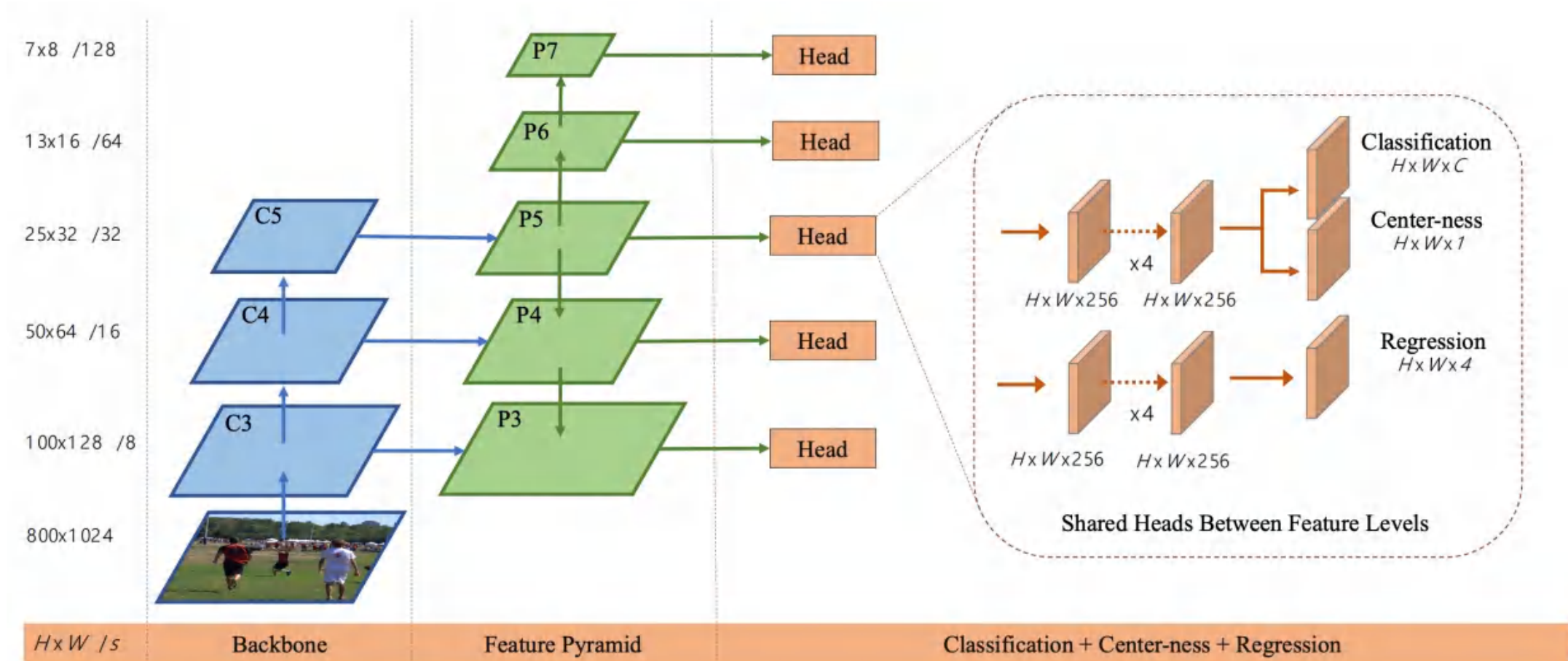
$$centerness = \sqrt{\frac{\min(L, R)}{\max(L, R)} \cdot \frac{\min(T, B)}{\max(T, B)}}$$

Ranges from 1 at box center to 0 at box edge

Single-Stage Detectors: FCOS

“Anchor-free” detector

FCOS also uses a Feature Pyramid Network with heads shared across stages



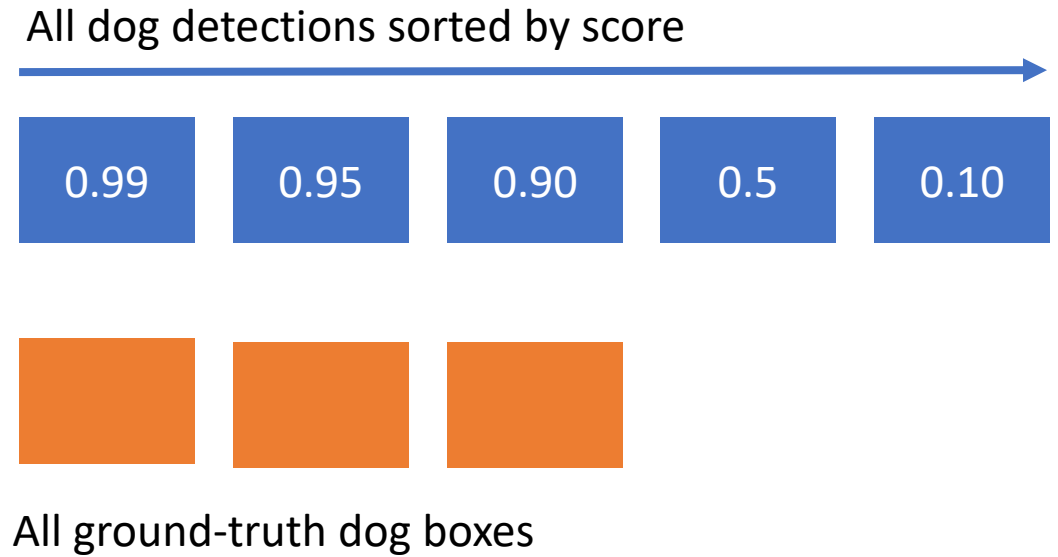
Tian et al, “FCOS: Fully Convolutional One-Stage Object Detection”, ICCV 2019

Evaluating Object Detectors: Mean Average Precision (mAP)

1. Run object detector on all test images (with NMS)
2. For each category, compute Average Precision (AP) =
area under Precision vs Recall Curve

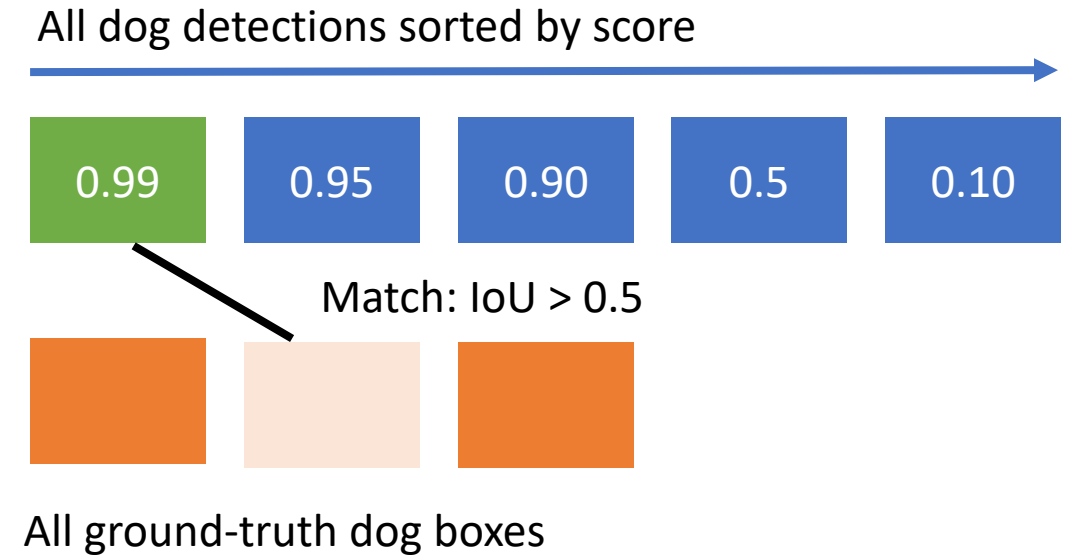
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 1. For each detection (highest score to lowest score)



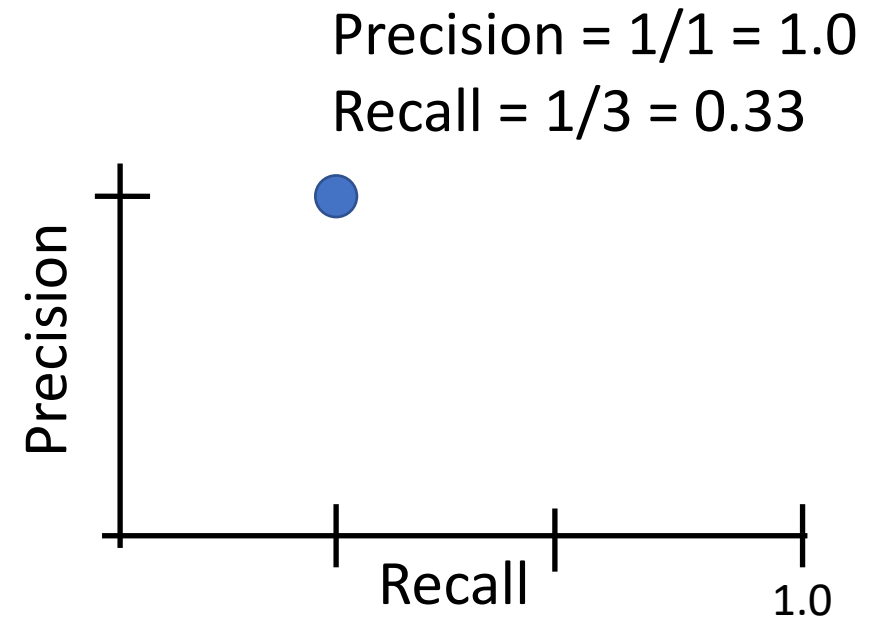
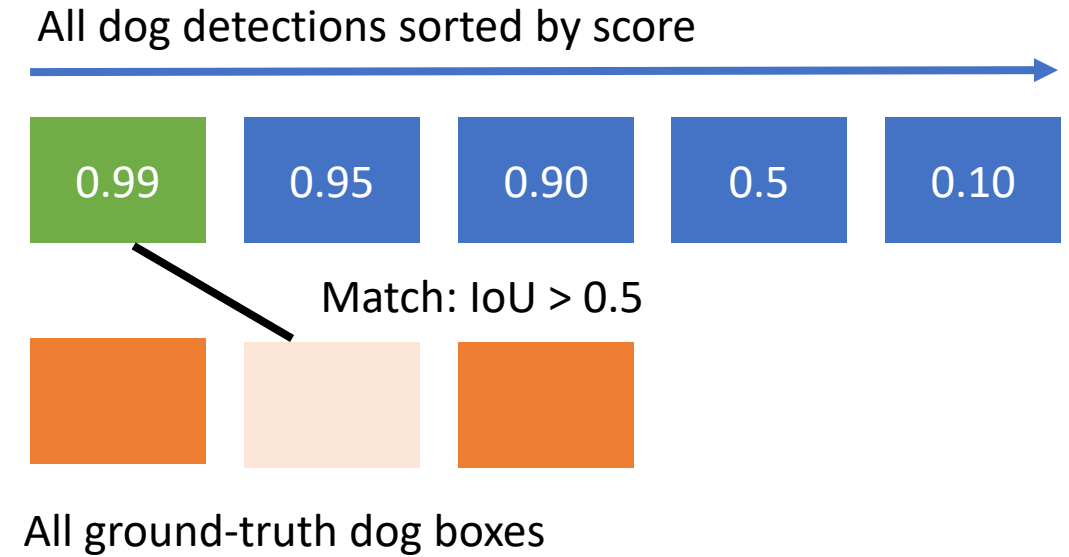
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 2. Otherwise mark it as negative



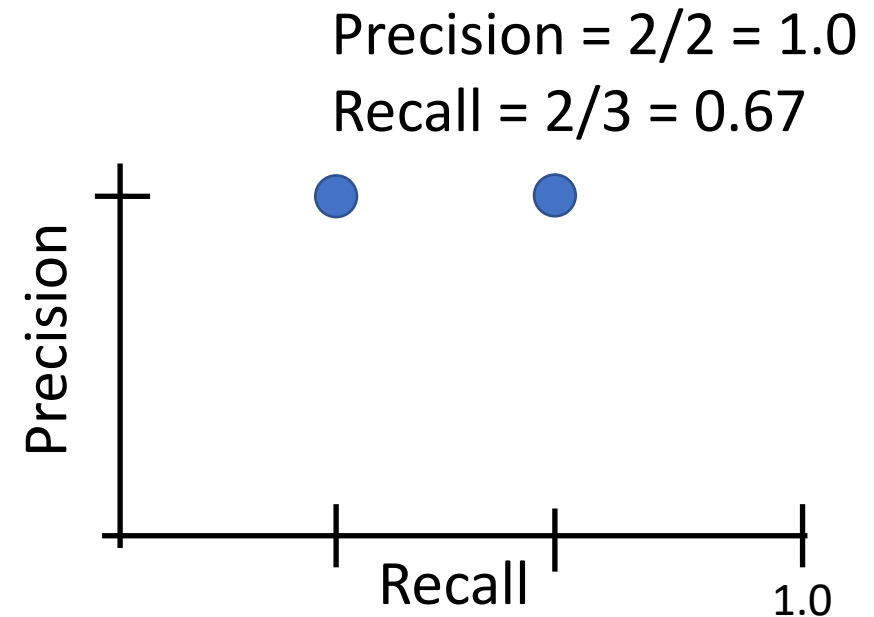
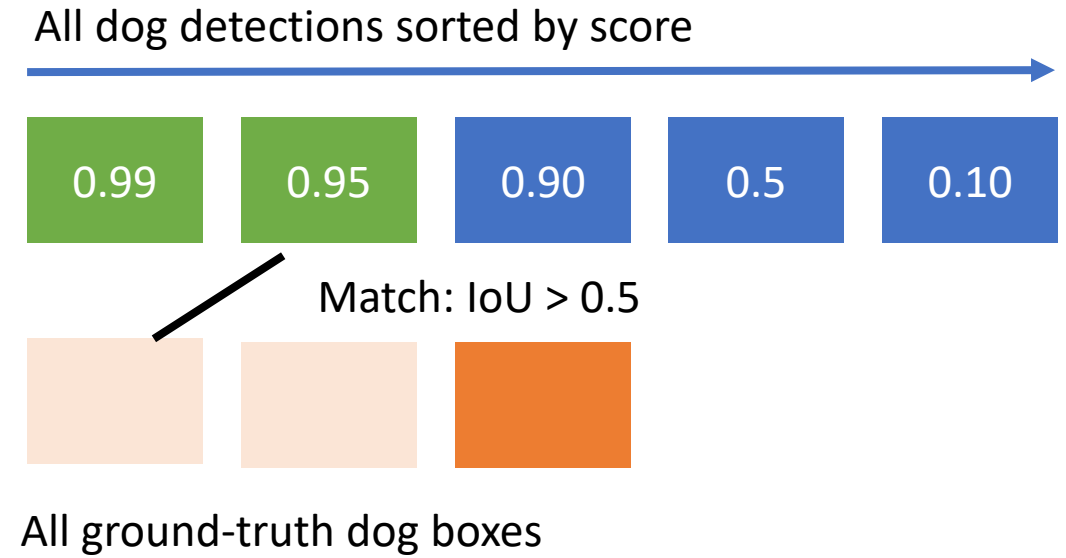
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 2. Otherwise mark it as negative
 3. Plot a point on PR Curve



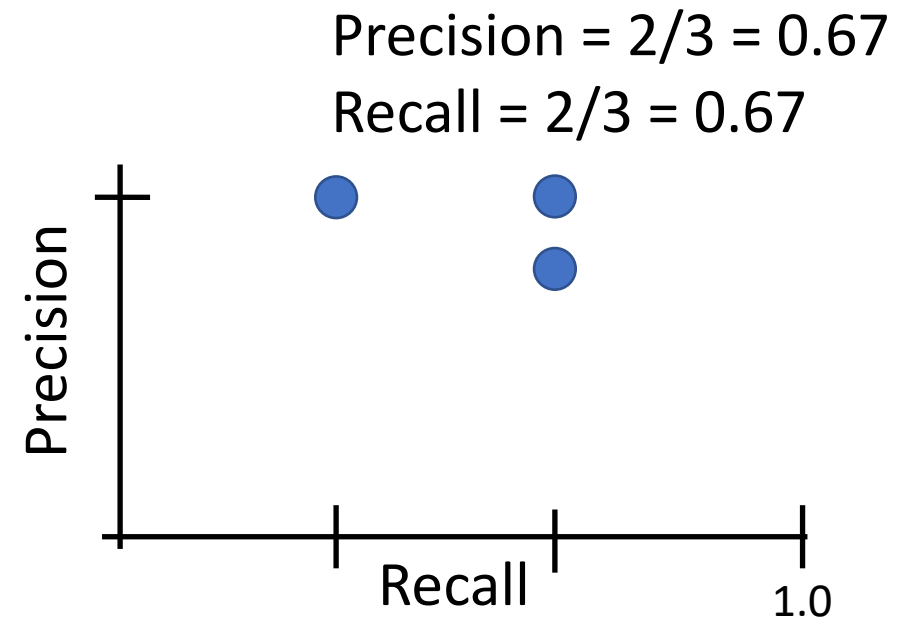
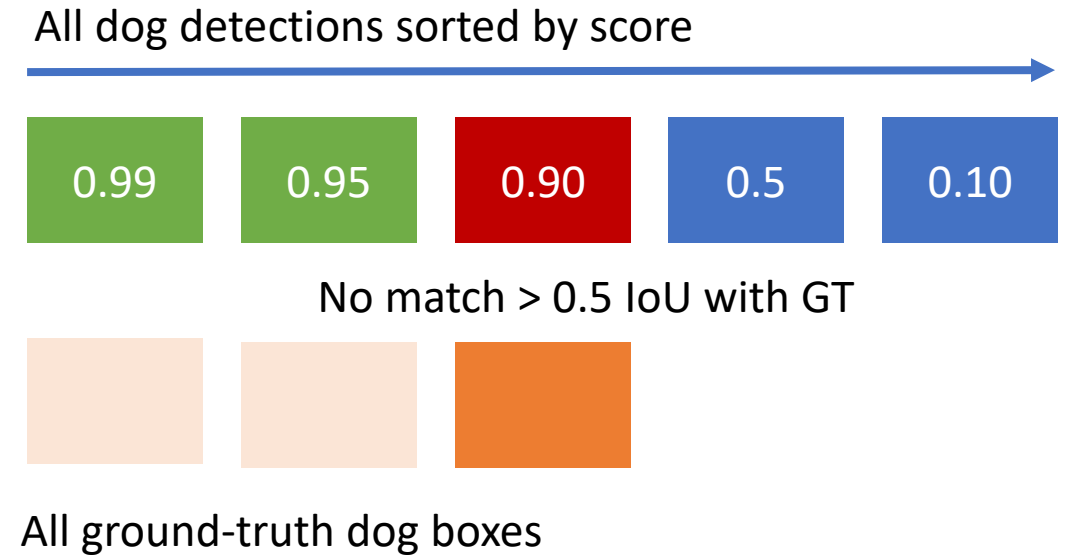
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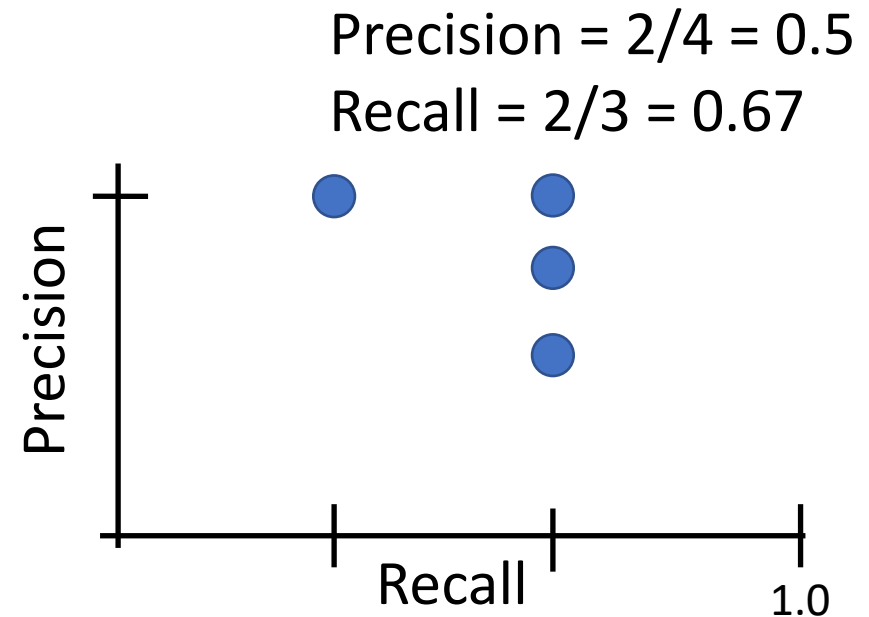
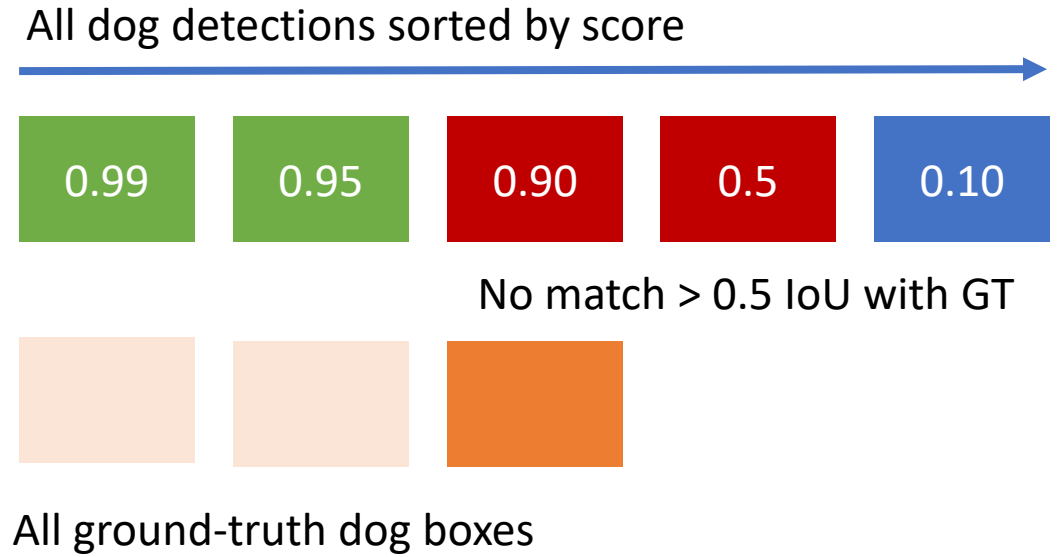
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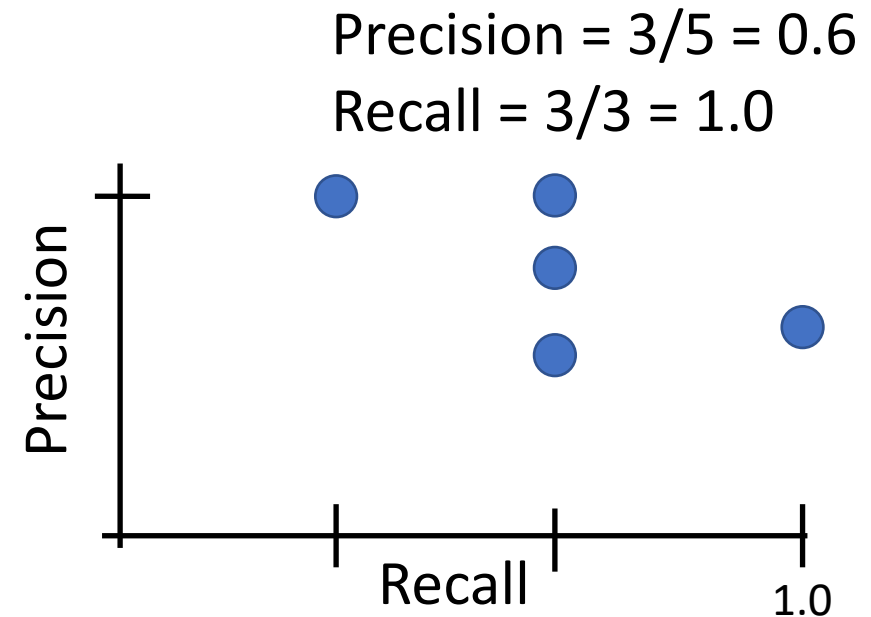
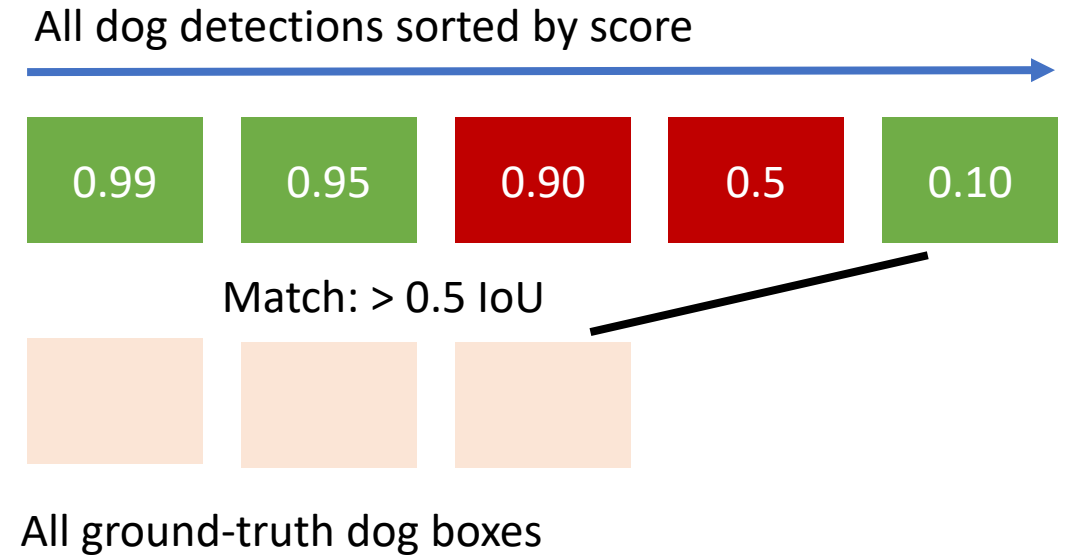
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Evaluating Object Detectors: Mean Average Precision (mAP)

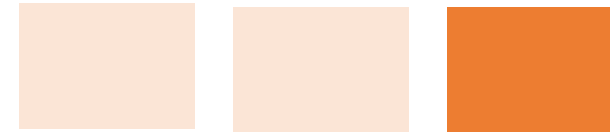
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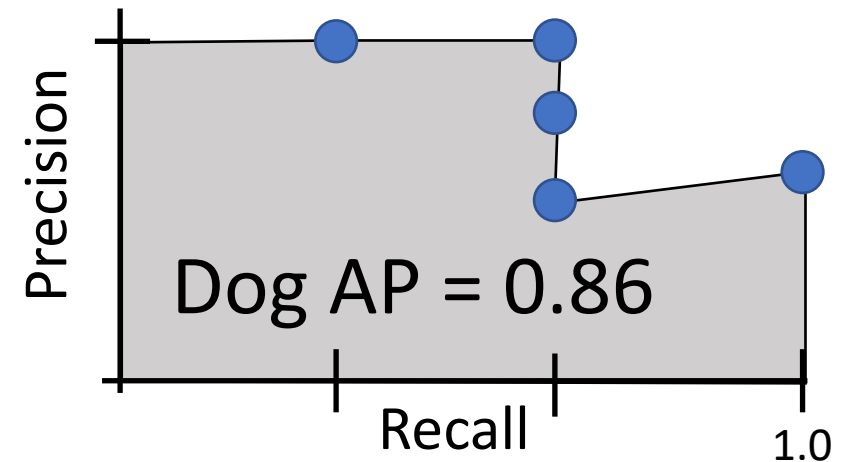
Evaluating Object Detectors: Mean Average Precision (mAP)

1. Run object detector on all test images (with NMS)
2. For each category, compute Average Precision (AP) = area under Precision vs Recall Curve
 1. For each detection (highest score to lowest score)
 1. If it matches some GT box with IoU > 0.5, mark it as positive and eliminate the GT
 2. Otherwise mark it as negative
 3. Plot a point on PR Curve
 2. Average Precision (AP) = area under PR curve

All dog detections sorted by score



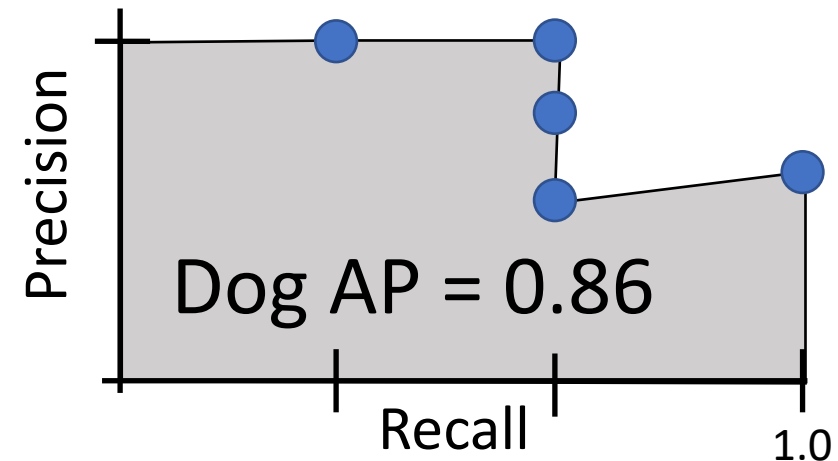
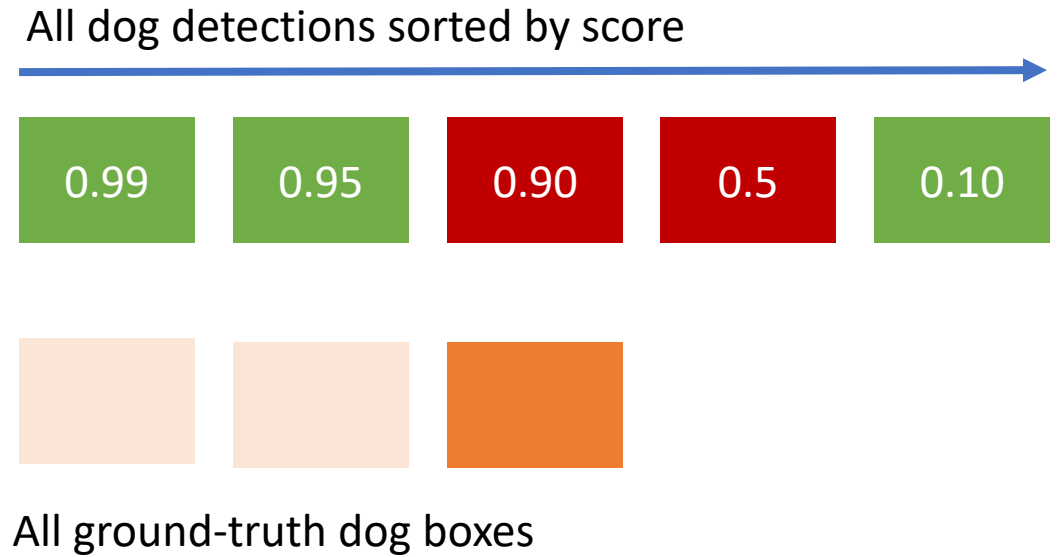
All ground-truth dog boxes



Evaluating Object Detectors: Mean Average Precision (mAP)

1. Run object detector on all test images (with NMS)
2. For each category, compute Average Precision (AP) = area under Precision vs Recall Curve
 1. For each detection (highest score to lowest score)
 1. If it matches some GT box with $\text{IoU} > 0.5$, mark it as positive and eliminate the GT
 2. Otherwise mark it as negative
 3. Plot a point on PR Curve
2. Average Precision (AP) = area under PR curve

How to get AP = 1.0: Hit all GT boxes with $\text{IoU} > 0.5$, and have no “false positive” detections ranked above any “true positives”



Evaluating Object Detectors: Mean Average Precision (mAP)

1. Run object detector on all test images (with NMS)
2. For each category, compute Average Precision (AP) = area under Precision vs Recall Curve
 1. For each detection (highest score to lowest score)
 1. If it matches some GT box with IoU > 0.5, mark it as positive and eliminate the GT
 2. Otherwise mark it as negative
 3. Plot a point on PR Curve
 2. Average Precision (AP) = area under PR curve
3. Mean Average Precision (mAP) = average of AP for each category

Car AP = 0.65

Cat AP = 0.80

Dog AP = 0.86

mAP@0.5 = 0.77

Evaluating Object Detectors: Mean Average Precision (mAP)

1. Run object detector on all test images (with NMS)
2. For each category, compute Average Precision (AP) = area under Precision vs Recall Curve
 1. For each detection (highest score to lowest score)
 1. If it matches some GT box with IoU > 0.5, mark it as positive and eliminate the GT
 2. Otherwise mark it as negative
 3. Plot a point on PR Curve
 2. Average Precision (AP) = area under PR curve
3. Mean Average Precision (mAP) = average of AP for each category
4. For “COCO mAP”: Compute mAP@thresh for each IoU threshold (0.5, 0.55, 0.6, ..., 0.95) and take average

$$\text{mAP}@0.5 = 0.77$$

$$\text{mAP}@0.55 = 0.71$$

$$\text{mAP}@0.60 = 0.65$$

...

$$\text{mAP}@0.95 = 0.2$$

$$\text{COCO mAP} = 0.4$$

Computer Vision Tasks: Object Detection

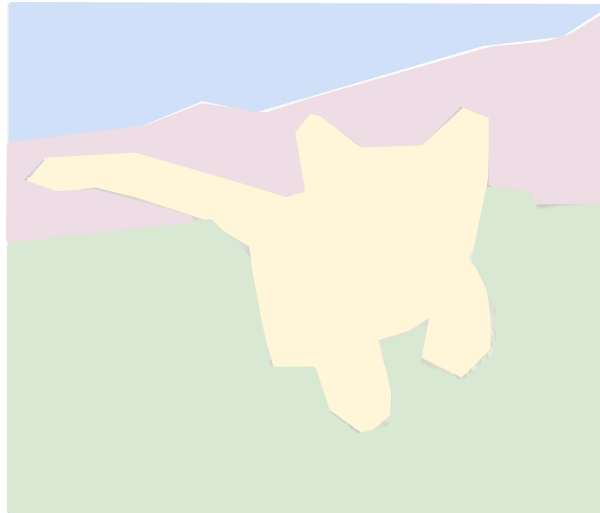
Classification



CAT

No spatial extent

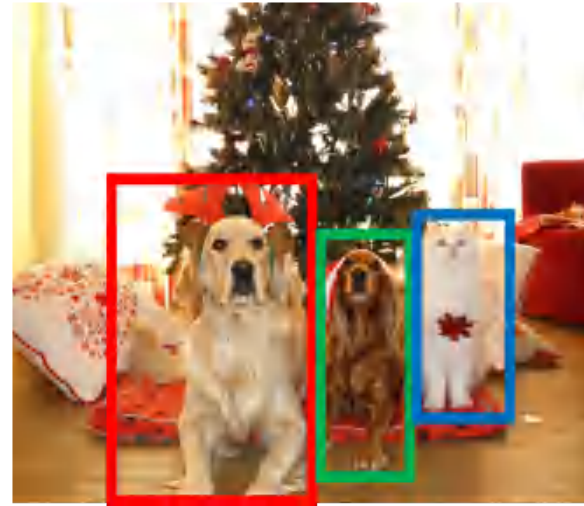
Semantic Segmentation



GRASS, CAT, TREE,
SKY

No objects, just pixels

Object Detection



DOG, DOG, CAT

Multiple Objects

Instance Segmentation



DOG, DOG, CAT

Computer Vision Tasks: Semantic Segmentation

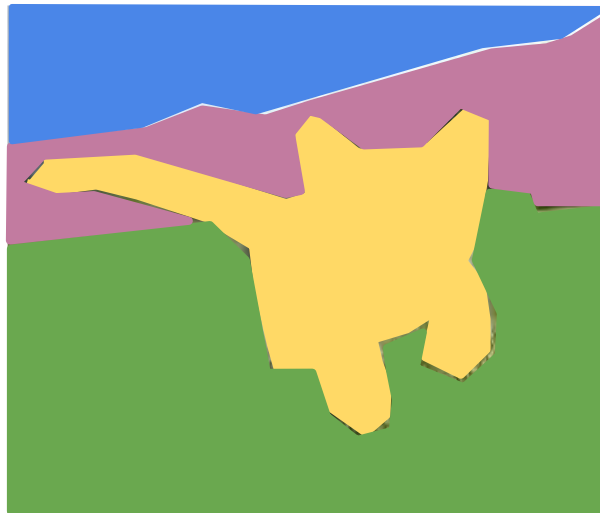
Classification



CAT

No spatial extent

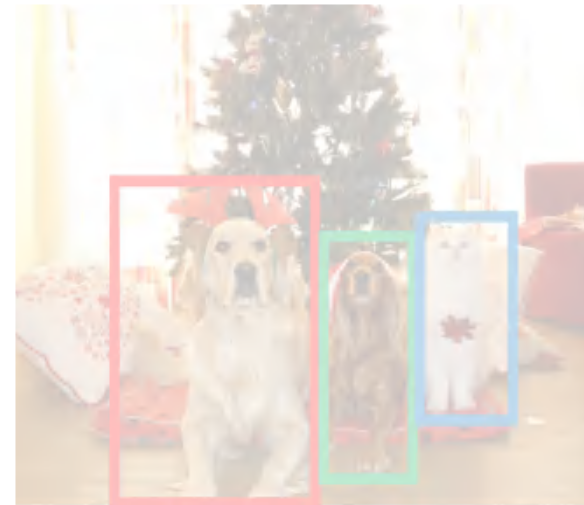
Semantic Segmentation



GRASS, CAT, TREE,
SKY

No objects, just pixels

Object Detection



DOG, DOG, CAT

Multiple Objects

Instance Segmentation

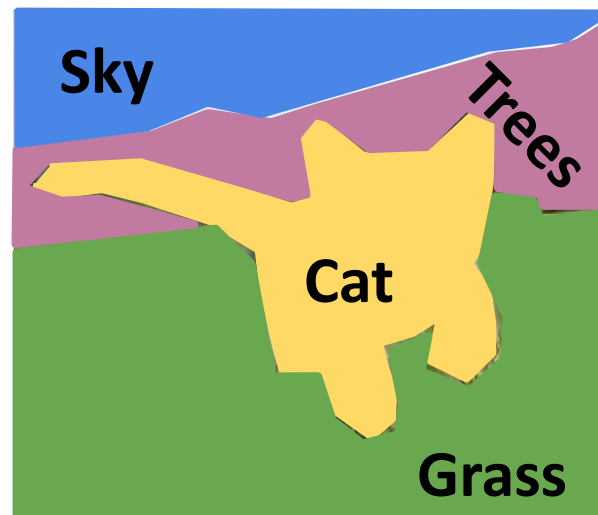


DOG, DOG, CAT

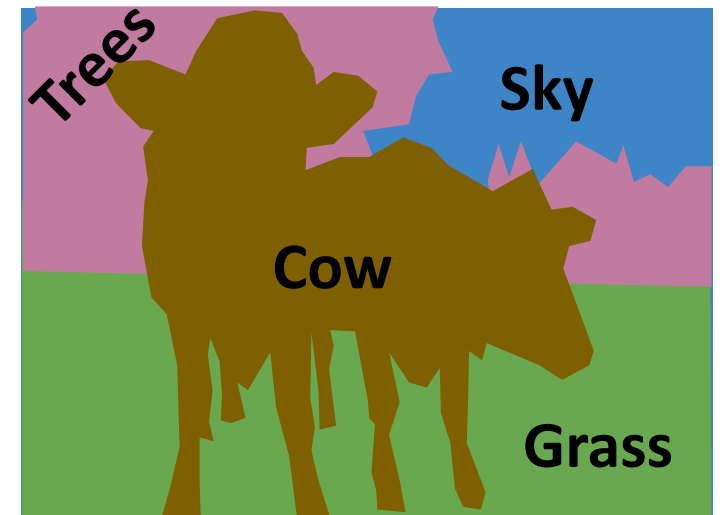
Semantic Segmentation

Label each pixel in the image with a category label

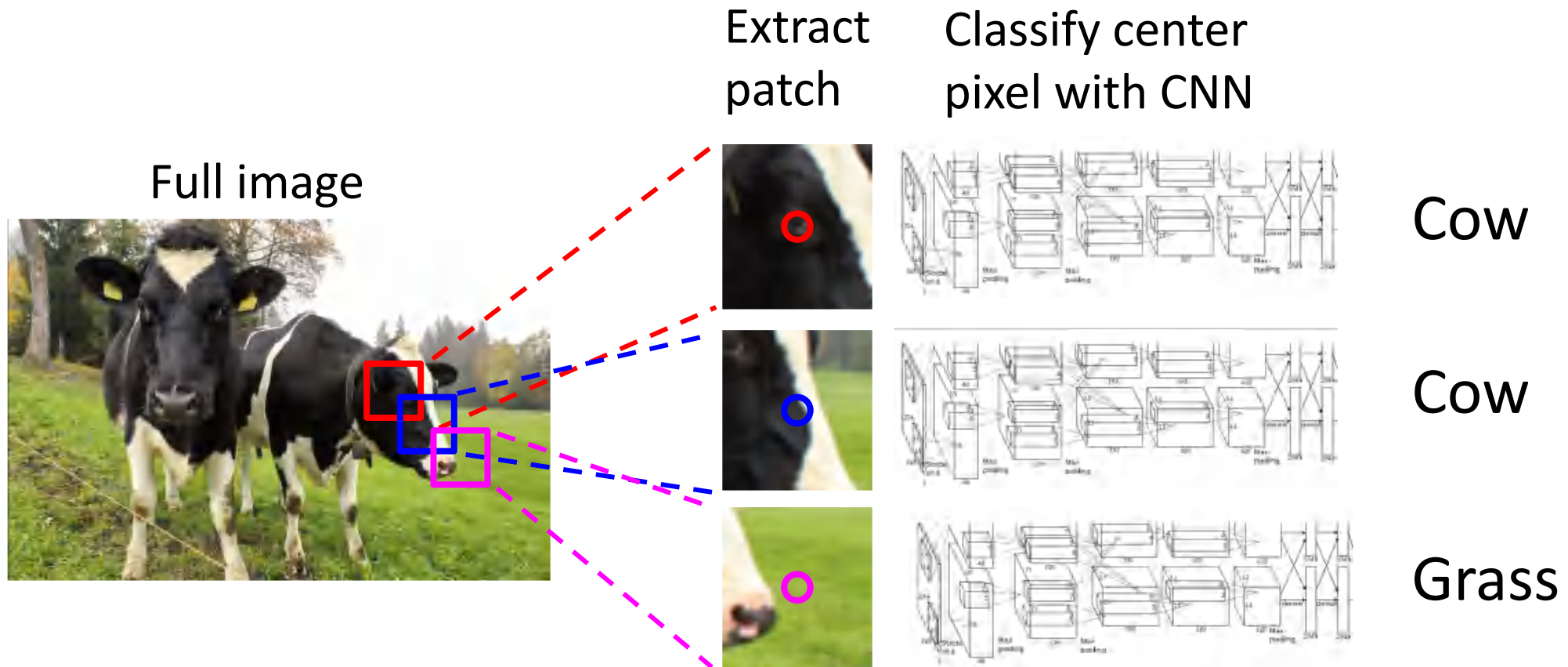
Don't differentiate instances, only care about pixels



[This image](#) is [CC0 public domain](#)



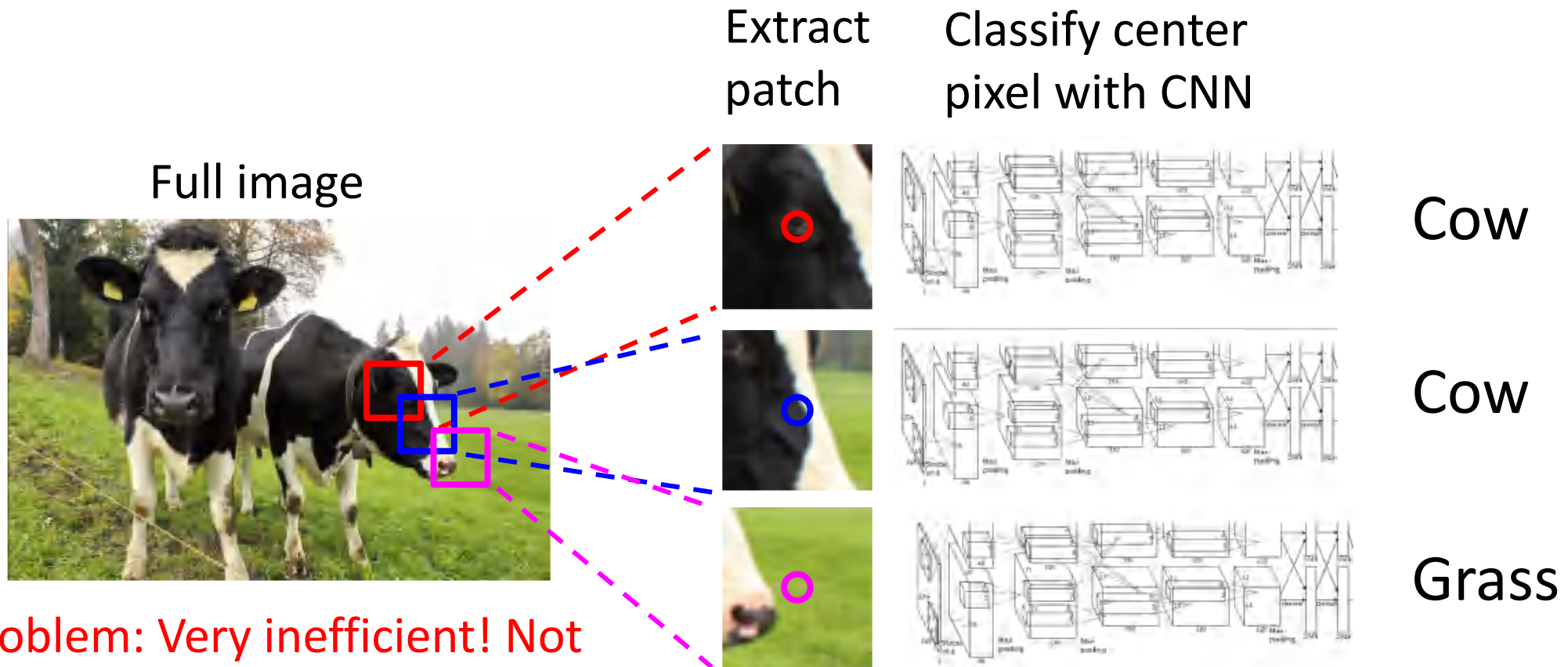
Semantic Segmentation Idea: Sliding Window



Farabet et al, "Learning Hierarchical Features for Scene Labeling," TPAMI 2013

Pinheiro and Collobert, "Recurrent Convolutional Neural Networks for Scene Labeling", ICML 2014

Semantic Segmentation Idea: Sliding Window

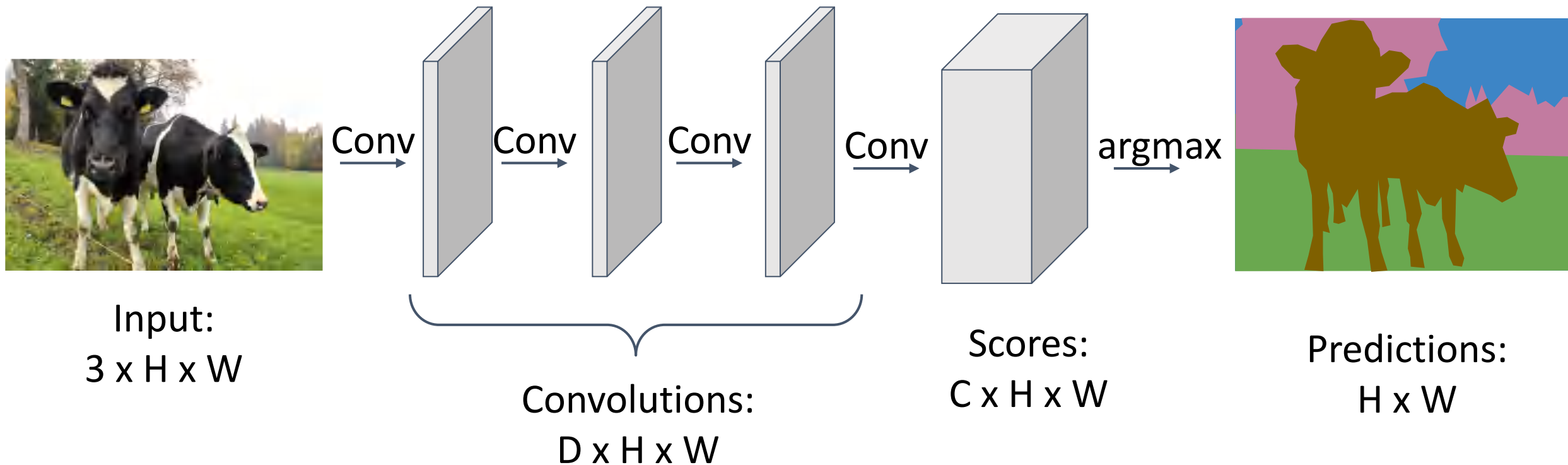


Problem: Very inefficient! Not reusing shared features between overlapping patches

Farabet et al, "Learning Hierarchical Features for Scene Labeling," TPAMI 2013
Pinheiro and Collobert, "Recurrent Convolutional Neural Networks for Scene Labeling", ICML 2014

Semantic Segmentation: Fully Convolutional Network

Design a network as a bunch of convolutional layers to make predictions for pixels all at once!



Loss function: Per-Pixel cross-entropy

Long et al, "Fully convolutional networks for semantic segmentation", CVPR 2015

Summary: Beyond Image Classification

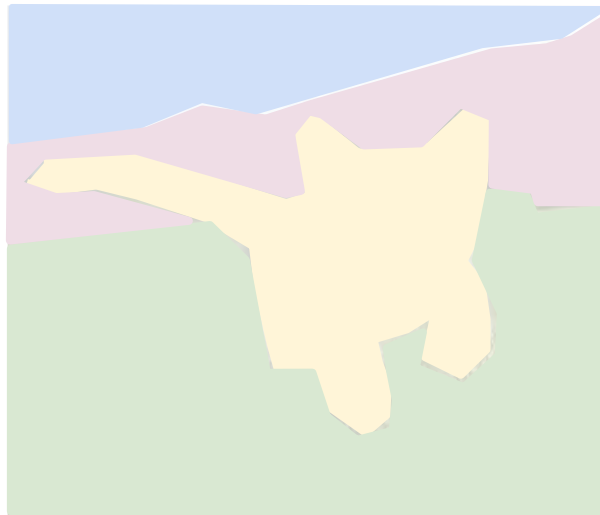
Classification



CAT

No spatial extent

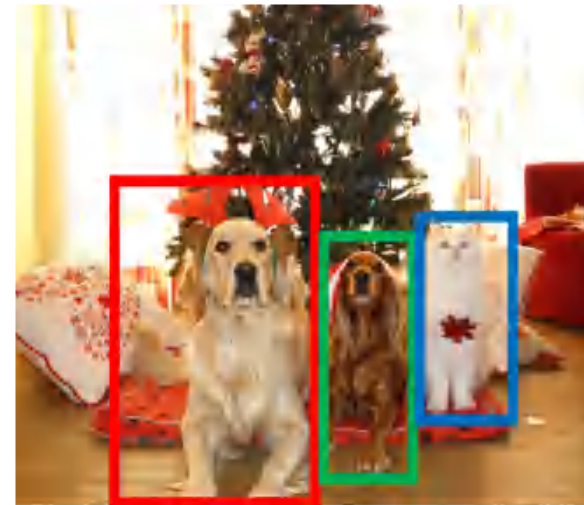
Semantic Segmentation



GRASS, CAT, TREE,
SKY

No objects, just pixels

Object Detection



DOG, DOG, CAT

Multiple Objects

Instance Segmentation

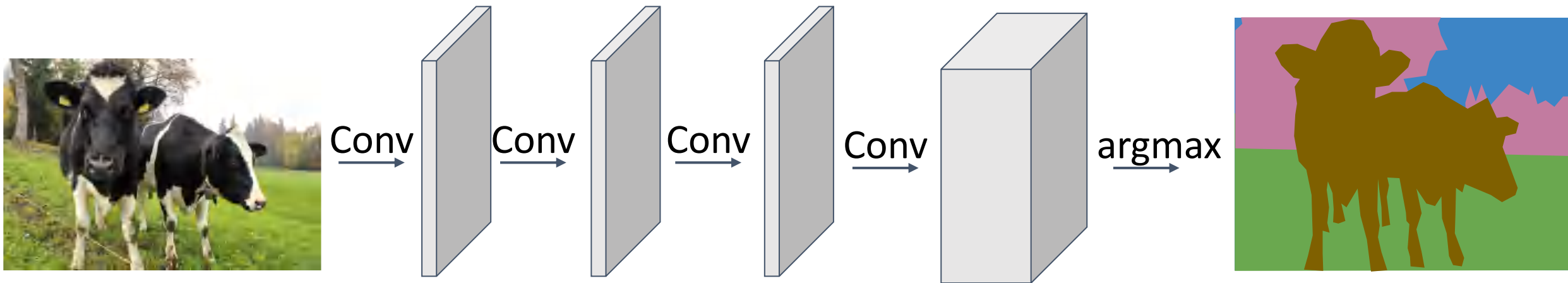


DOG, DOG, CAT

[This image](#) is [CC0 public domain](#)

Semantic Segmentation: Fully Convolutional Network

Design a network as a bunch of convolutional layers to make predictions for pixels all at once!



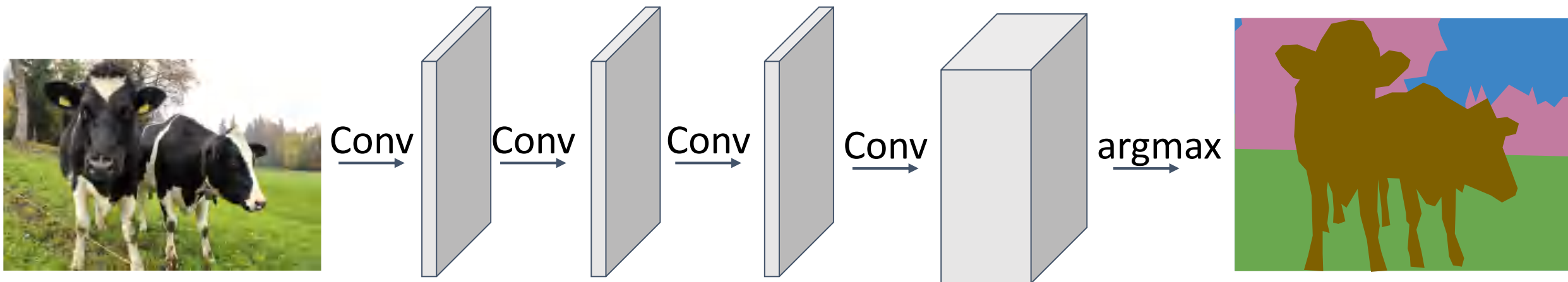
Input: $3 \times H \times W$

Problem #1: Effective receptive field size is linear in number of conv layers: With L 3×3 conv layers, receptive field is $1+2L$

Long et al, "Fully convolutional networks for semantic segmentation", CVPR 2015

Semantic Segmentation: Fully Convolutional Network

Design a network as a bunch of convolutional layers to make predictions for pixels all at once!



Input:
 $3 \times H \times W$

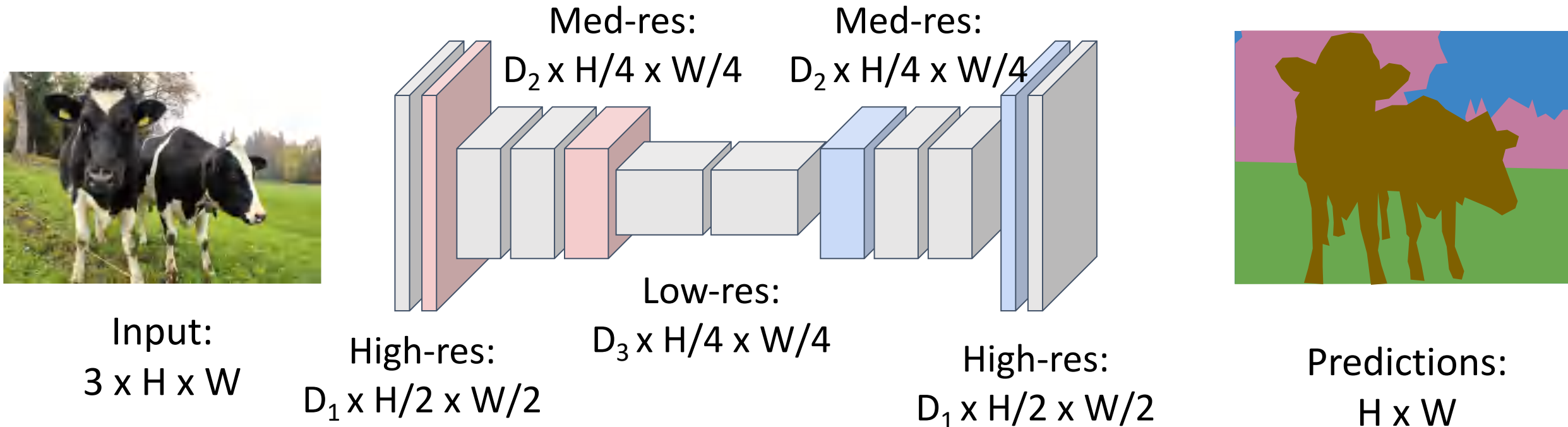
Problem #1: Effective receptive field size is linear in number of conv layers: With L 3×3 conv layers, receptive field is $1+2L$

Problem #2: Convolution on high res images is expensive! Recall ResNet stem aggressively downsamples

Long et al, "Fully convolutional networks for semantic segmentation", CVPR 2015

Semantic Segmentation: Fully Convolutional Network

Design network as a bunch of convolutional layers, with **downsampling** and **upsampling** inside the network!



Semantic Segmentation: Fully Convolutional Network

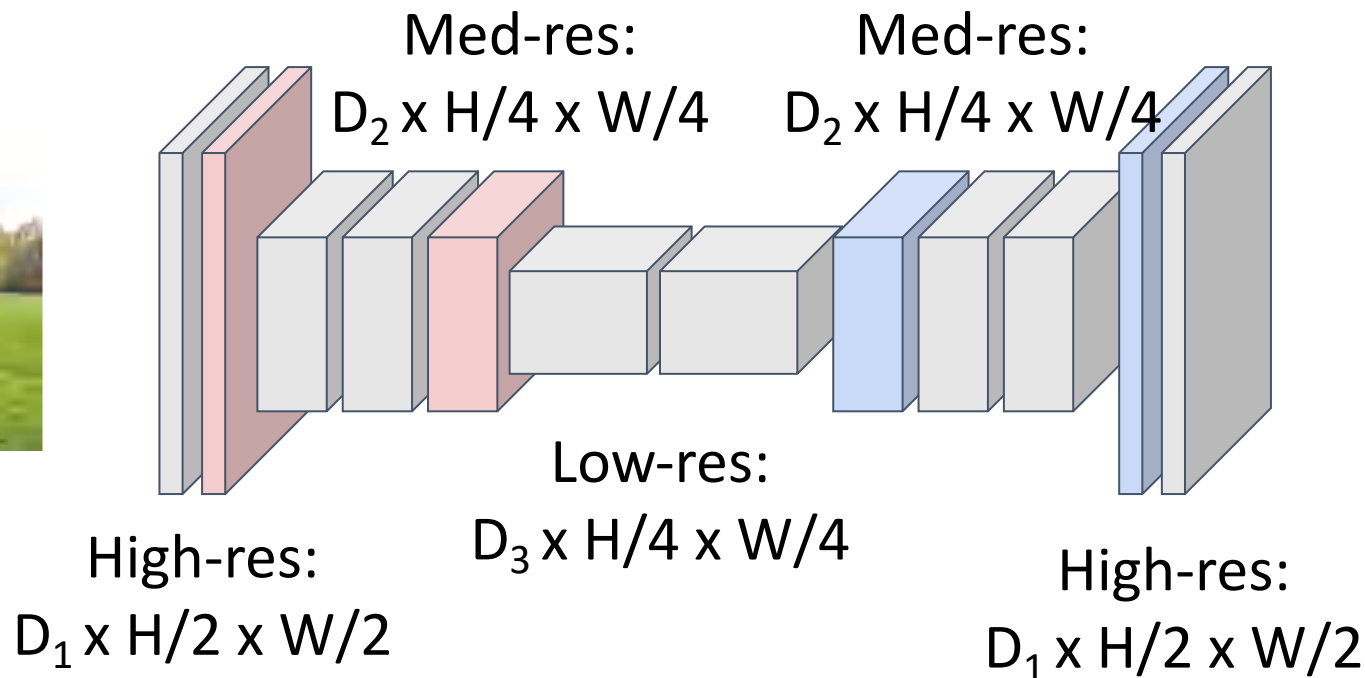
Downsampling:
Pooling, strided
convolution

Design network as a bunch of convolutional layers, with **downsampling** and **upsampling** inside the network!

Upsampling:
???



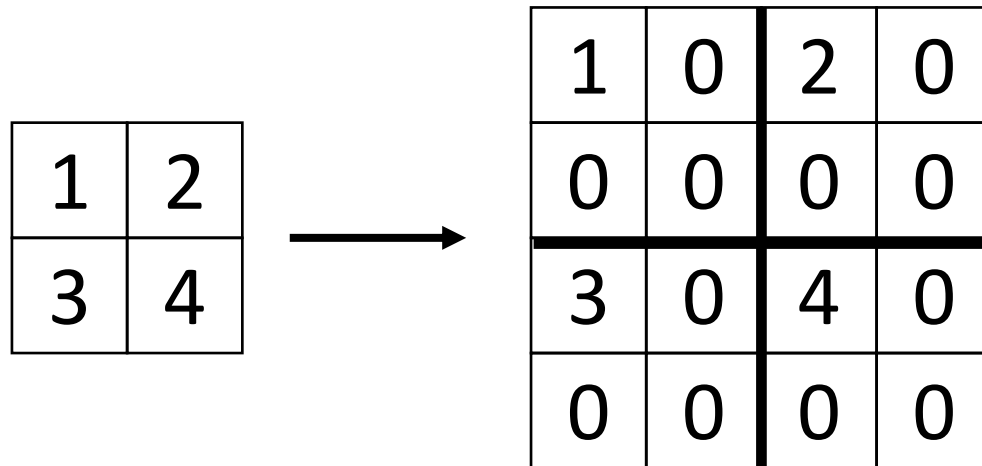
Input:
 $3 \times H \times W$



Predictions:
 $H \times W$

In-Network Upsampling: “Unpooling”

Bed of Nails

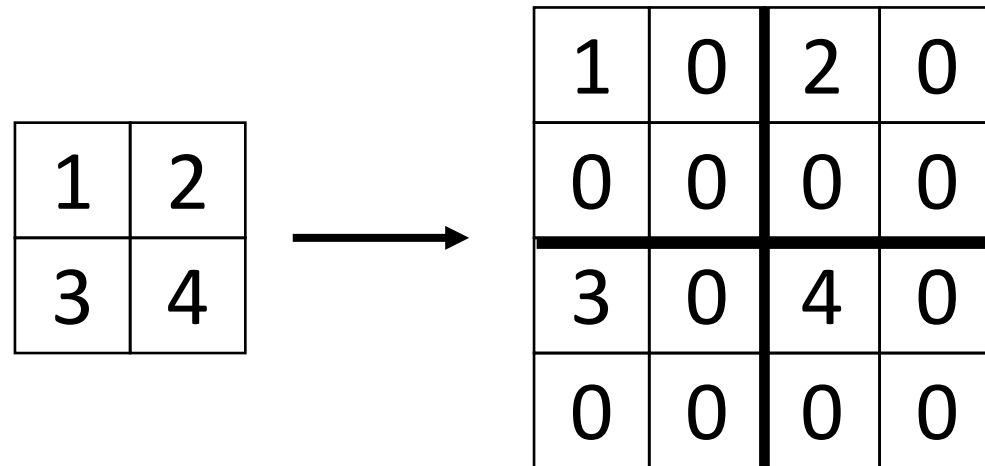


Input
 $C \times 2 \times 2$

Output
 $C \times 4 \times 4$

In-Network Upsampling: “Unpooling”

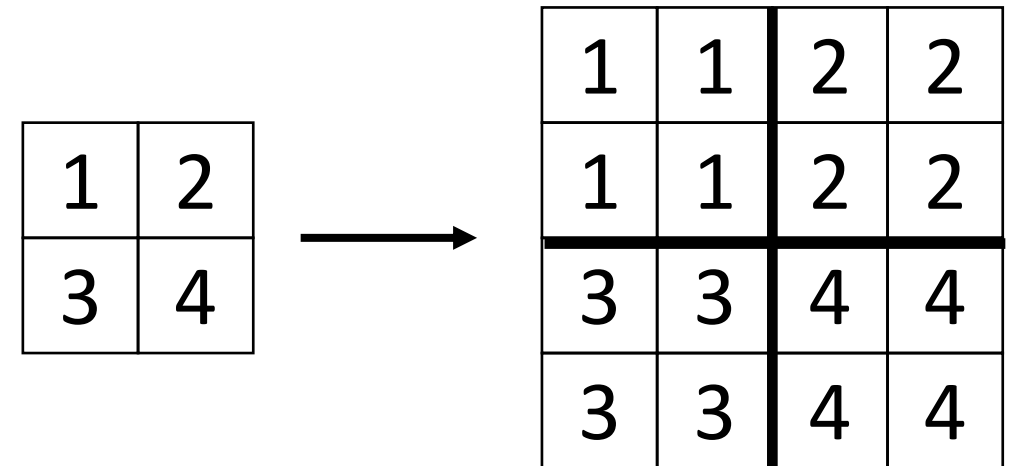
Bed of Nails



Input
 $C \times 2 \times 2$

Output
 $C \times 4 \times 4$

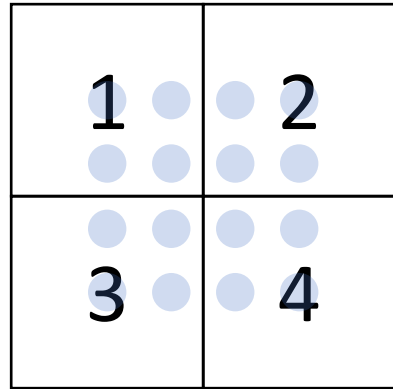
Nearest Neighbor



Input
 $C \times 2 \times 2$

Output
 $C \times 4 \times 4$

In-Network Upsampling: Bilinear Interpolation



Input: C x 2 x 2

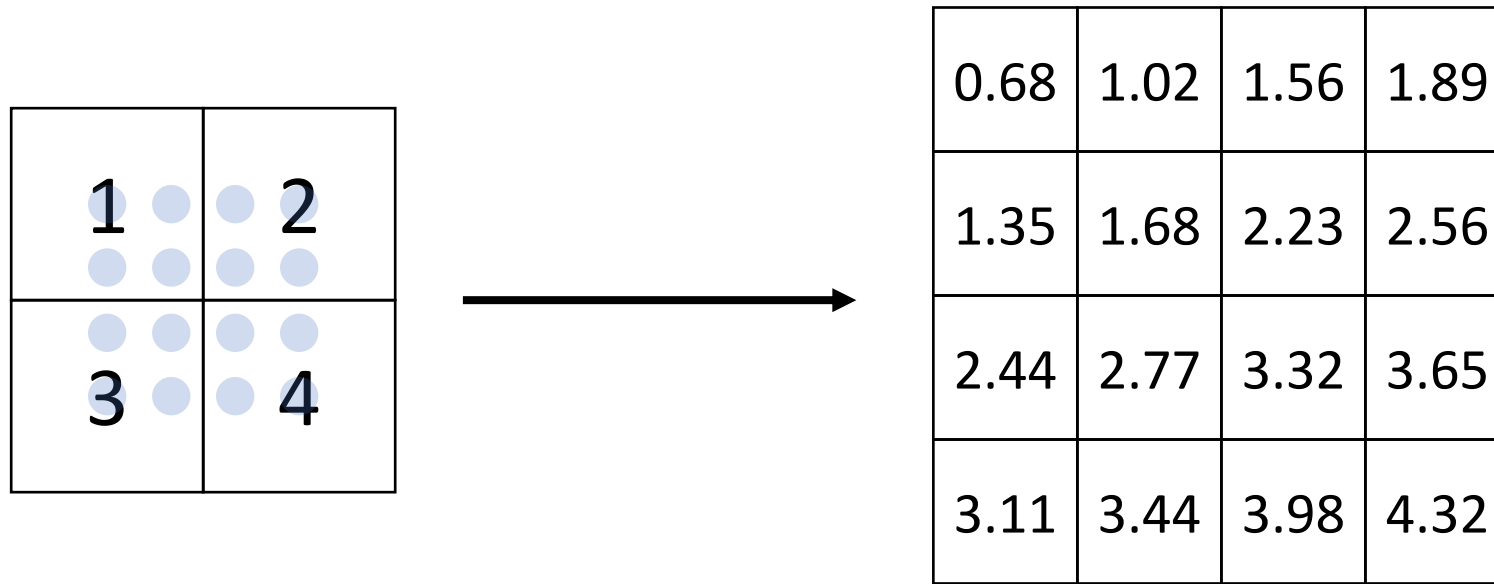
1.00	1.25	1.75	2.00
1.50	1.75	2.25	2.50
2.50	2.75	3.25	3.50
3.00	3.25	3.75	4.00

Output: C x 4 x 4

$$f_{x,y} = \sum_{i,j} f_{i,j} \max(0, 1 - |x - i|) \max(0, 1 - |y - j|) \quad \begin{array}{l} i \in \{\lfloor x \rfloor - 1, \dots, \lceil x \rceil + 1\} \\ j \in \{\lfloor y \rfloor - 1, \dots, \lceil y \rceil + 1\} \end{array}$$

Use two closest neighbors in x and y to construct linear approximations

In-Network Upsampling: Bicubic Interpolation



Input: $C \times 2 \times 2$

Output: $C \times 4 \times 4$

Use **three** closest neighbors in x and y to construct **cubic** approximations
(This is how we normally resize images!)

In-Network Upsampling: “Max Unpooling”

Max Pooling: Remember which position had the max

1	2	6	3
3	5	2	1
1	2	2	1
7	3	4	8



5	6
7	8



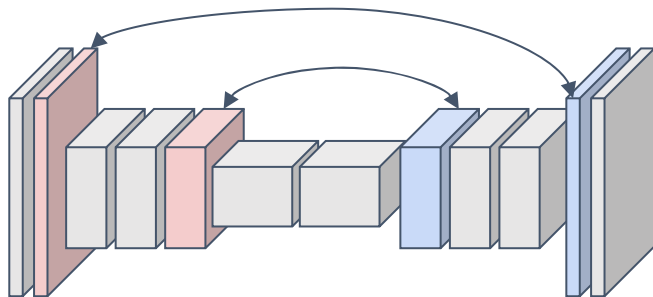
Rest
of
net



1	2
3	4



0	0	2	0
0	1	0	0
0	0	0	0
3	0	0	4

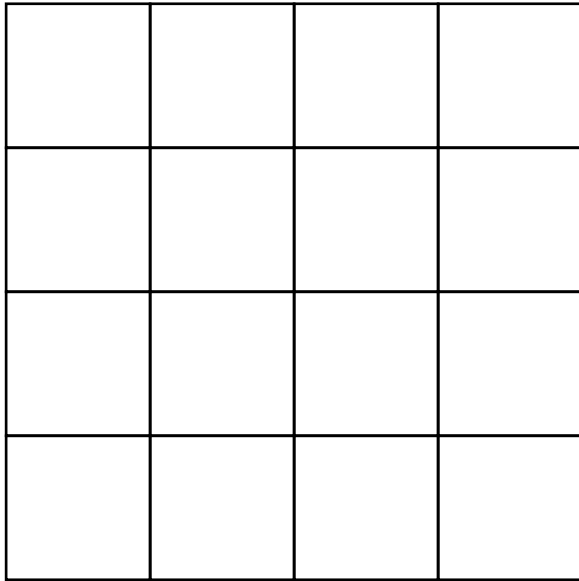


Pair each downsampling layer
with an upsampling layer

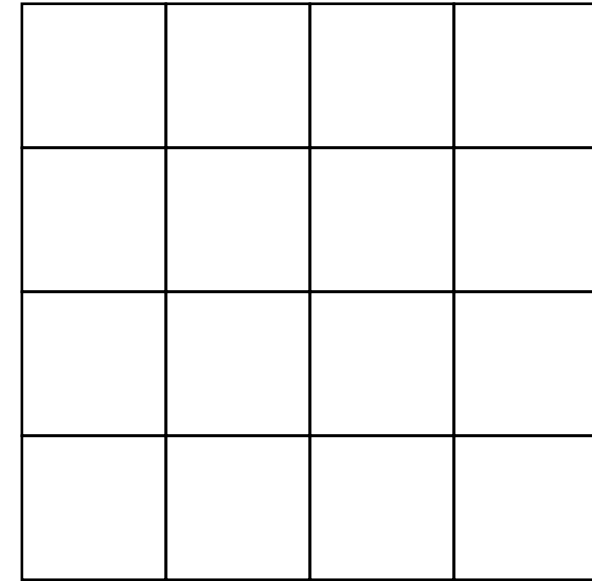
Noh et al, “Learning Deconvolution Network for Semantic Segmentation”, ICCV 2015

Learnable Upsampling: Transposed Convolution

Recall: Normal 3 x 3 convolution, stride 1, pad 1



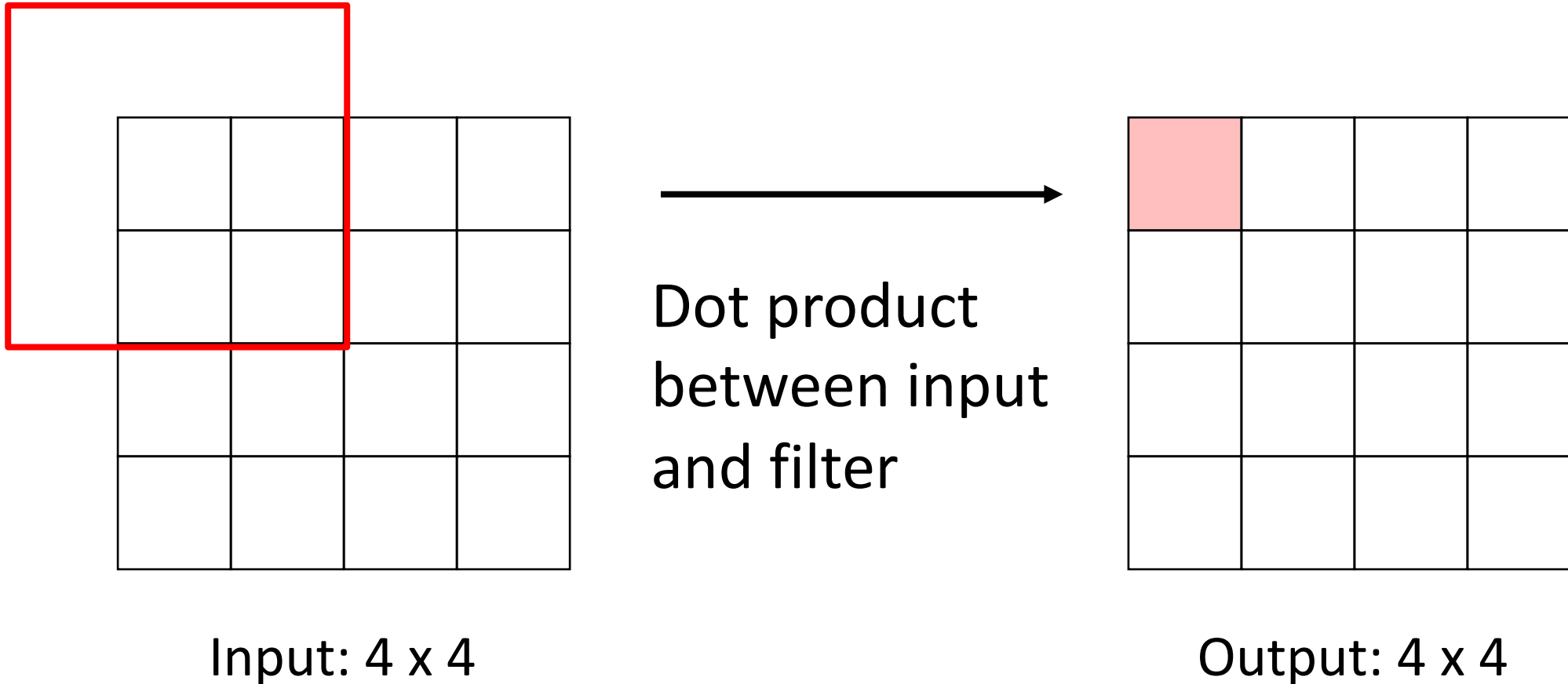
Input: 4 x 4



Output: 4 x 4

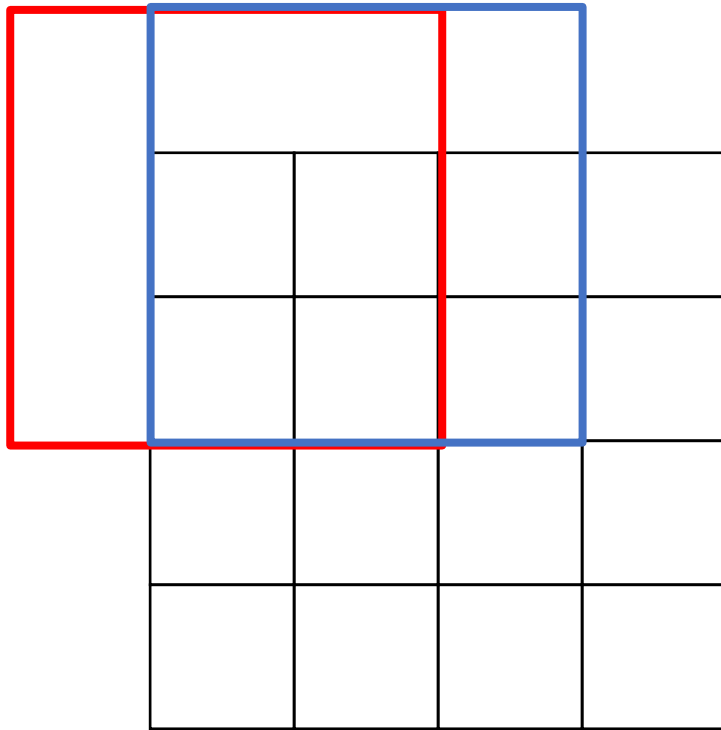
Learnable Upsampling: Transposed Convolution

Recall: Normal 3 x 3 convolution, stride 1, pad 1



Learnable Upsampling: Transposed Convolution

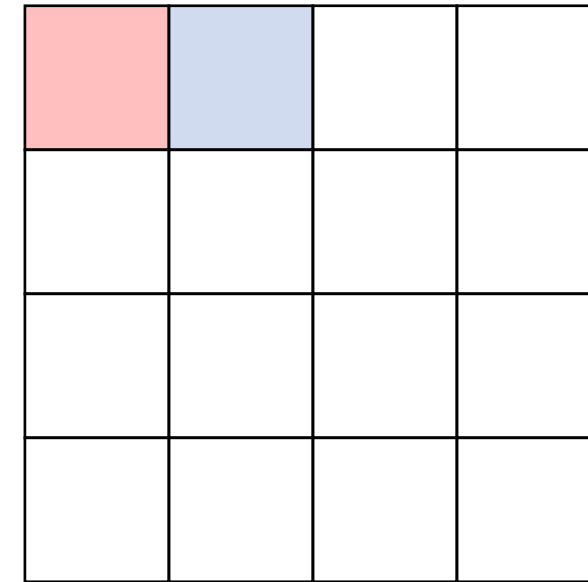
Recall: Normal 3 x 3 convolution, stride 1, pad 1



Input: 4 x 4



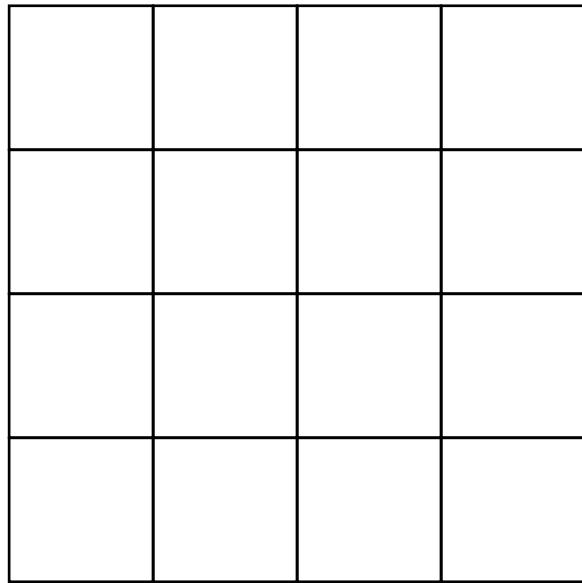
Dot product
between input
and filter



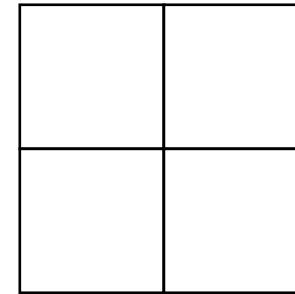
Output: 4 x 4

Learnable Upsampling: Transposed Convolution

Recall: Normal 3 x 3 convolution, stride 2, pad 1



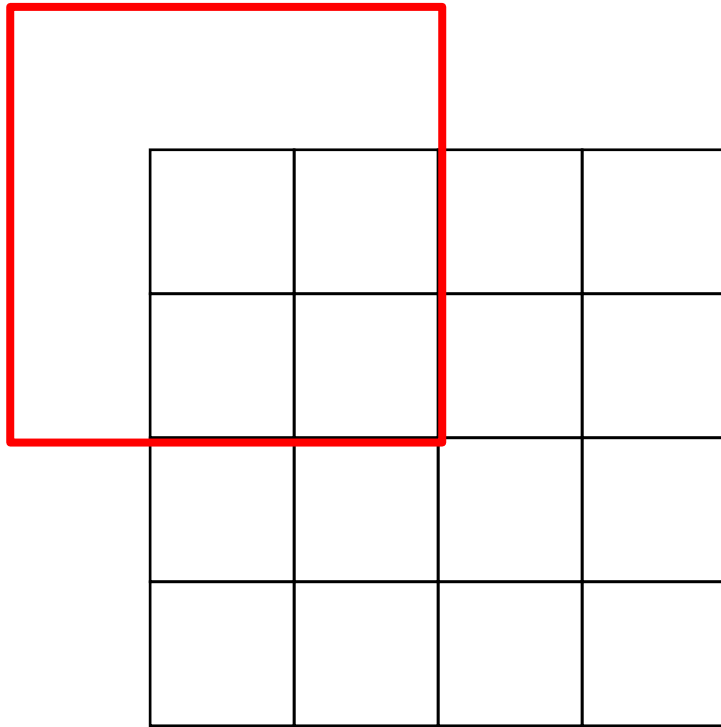
Input: 4 x 4



Output: 2 x 2

Learnable Upsampling: Transposed Convolution

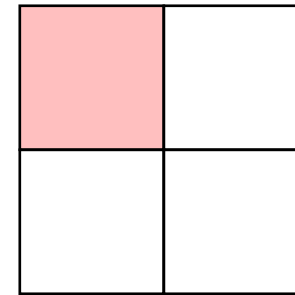
Recall: Normal 3 x 3 convolution, stride 2, pad 1



Input: 4 x 4



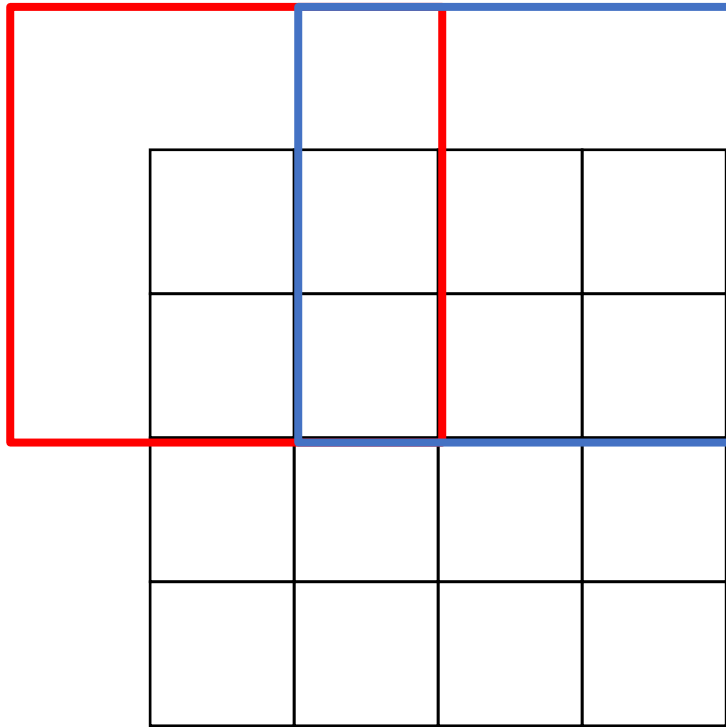
Dot product
between input
and filter



Output: 2 x 2

Learnable Upsampling: Transposed Convolution

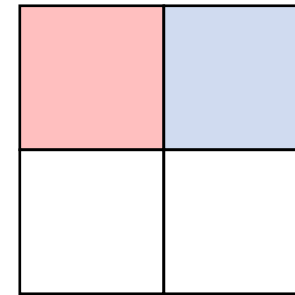
Recall: Normal 3 x 3 convolution, stride 2, pad 1



Input: 4 x 4



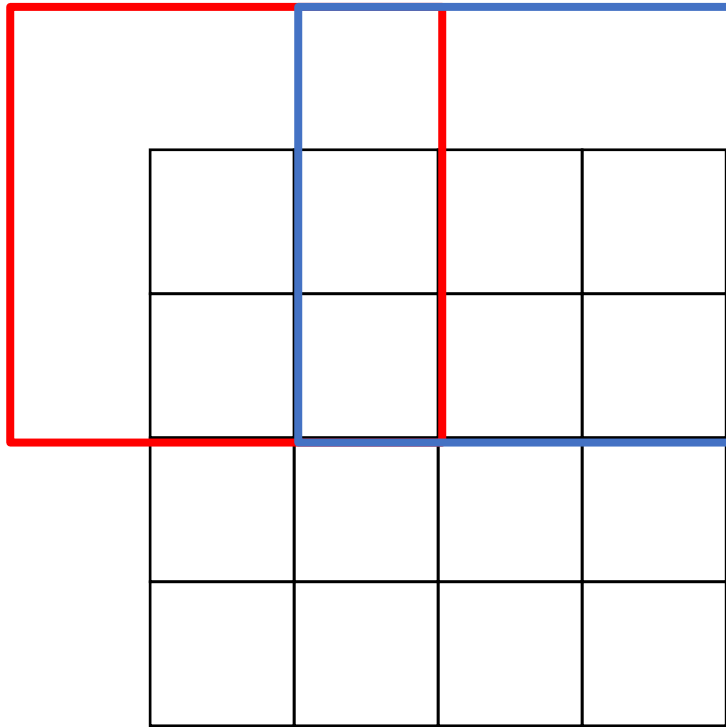
Dot product
between input
and filter



Output: 2 x 2

Learnable Upsampling: Transposed Convolution

Recall: Normal 3 x 3 convolution, stride 2, pad 1

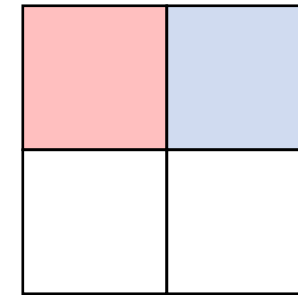


Input: 4 x 4

Convolution with stride > 1 is “Learnable Downsampling”
Can we use stride < 1 for “Learnable Upsampling”?



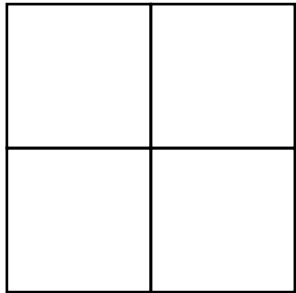
Dot product
between input
and filter



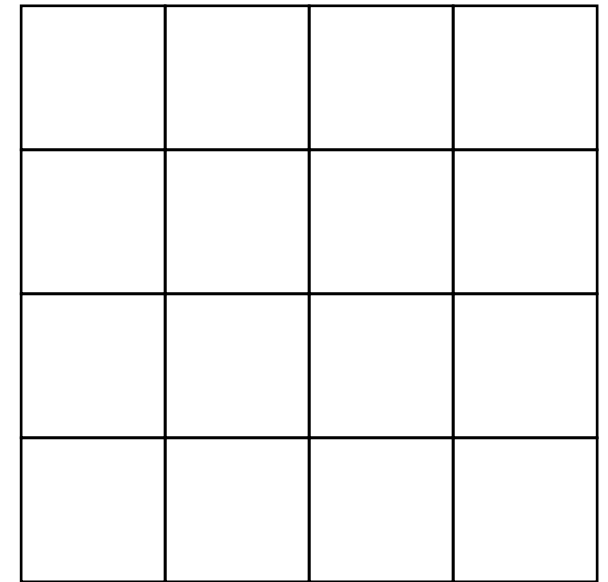
Output: 2 x 2

Learnable Upsampling: Transposed Convolution

3 x 3 convolution transpose, stride 2



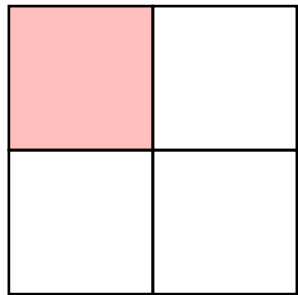
Input: 2 x 2



Output: 4 x 4

Learnable Upsampling: Transposed Convolution

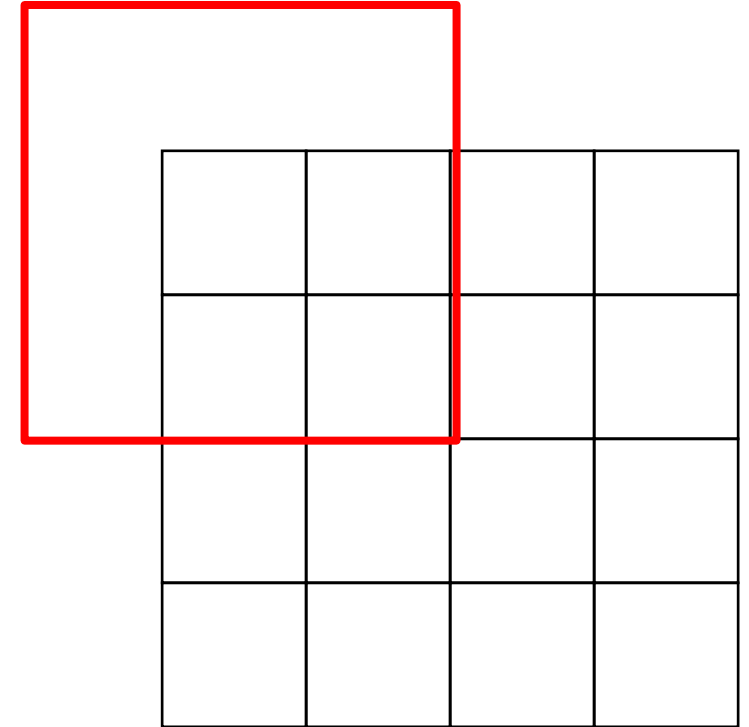
3 x 3 convolution transpose, stride 2



Input: 2 x 2



Weight filter by
input value and
copy to output

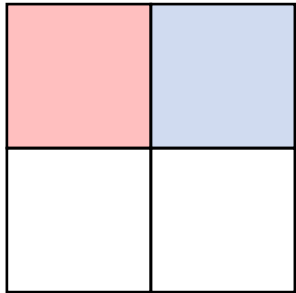


Output: 4 x 4

Learnable Upsampling: Transposed Convolution

3 x 3 **convolution transpose**, stride 2

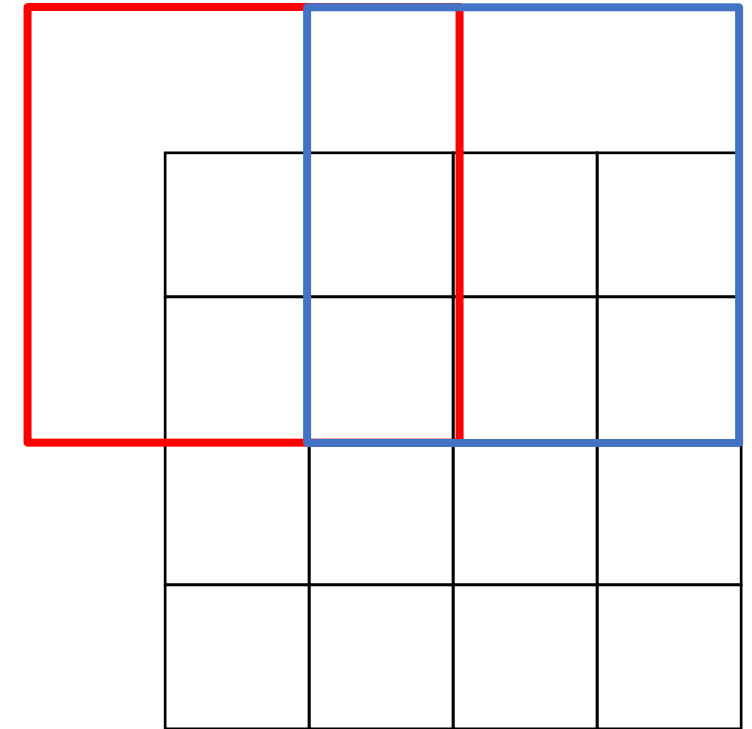
Filter moves 2 pixels in output
for every 1 pixel in input



Input: 2 x 2



Weight filter by
input value and
copy to output

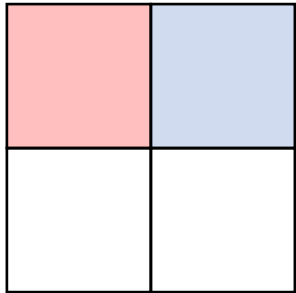


Output: 4 x 4

Learnable Upsampling: Transposed Convolution

3 x 3 **convolution transpose**, stride 2

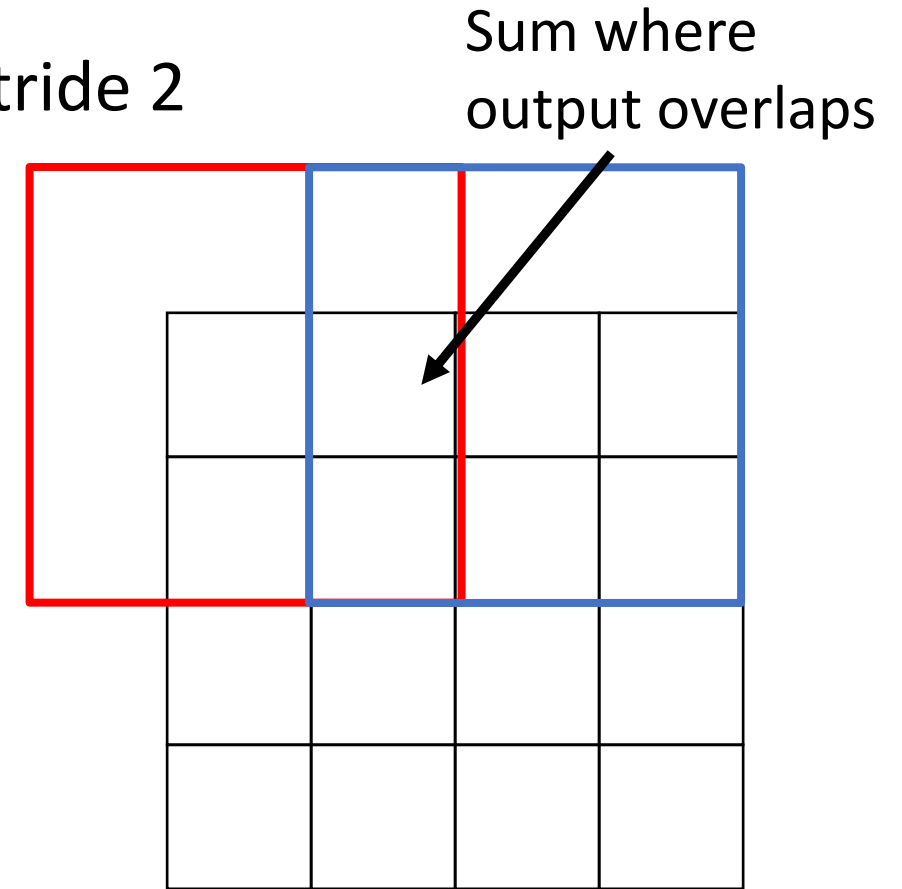
Filter moves 2 pixels in output
for every 1 pixel in input



Input: 2 x 2



Weight filter by
input value and
copy to output

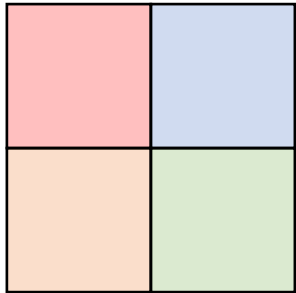


Output: 4 x 4

Learnable Upsampling: Transposed Convolution

3 x 3 **convolution transpose**, stride 2

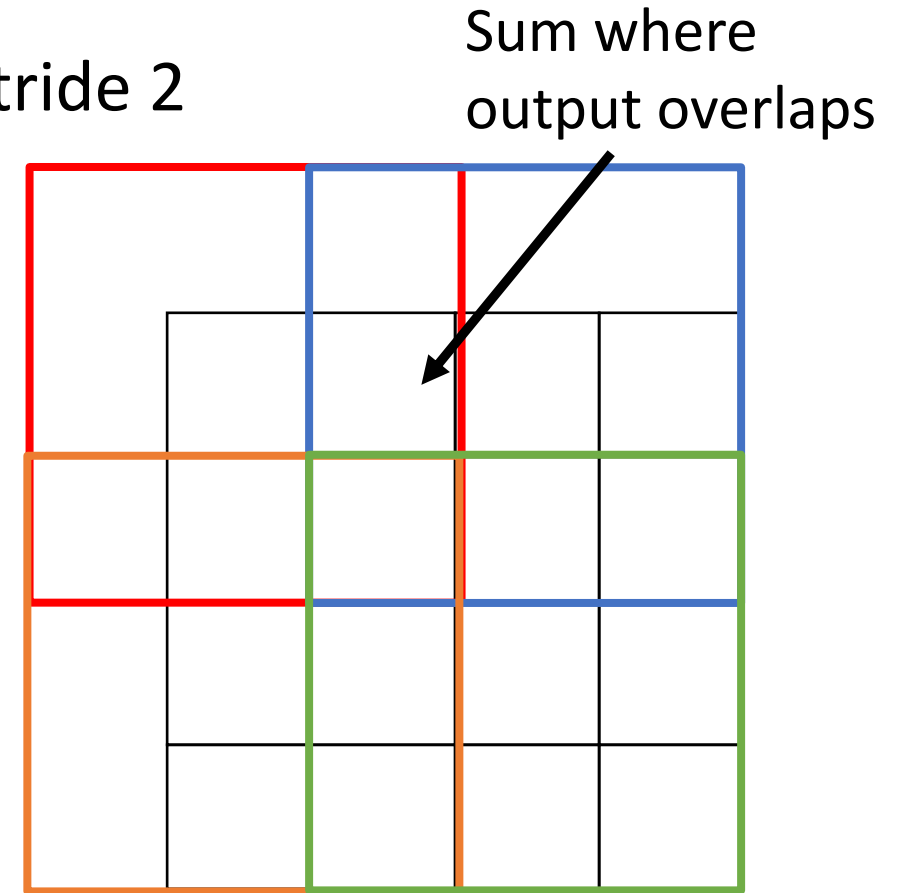
This gives 5x5 output – need to trim one pixel from top and left to give 4x4 output



Input: 2 x 2



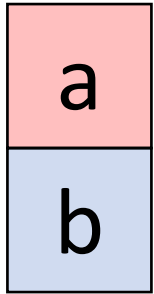
Weight filter by
input value and
copy to output



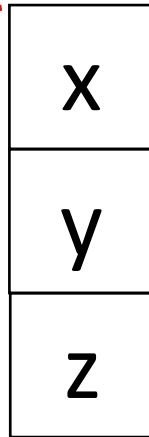
Output: 4 x 4

Transposed Convolution: 1D example

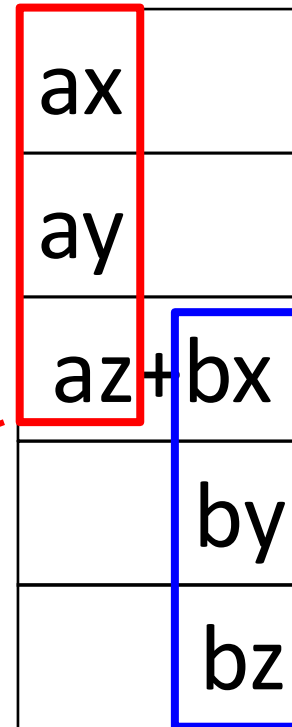
Input



Filter



Output



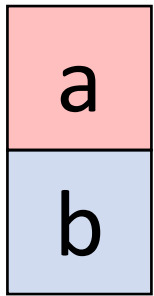
Output has copies of filter weighted by input

Stride 2: Move 2 pixels output for each pixel in input

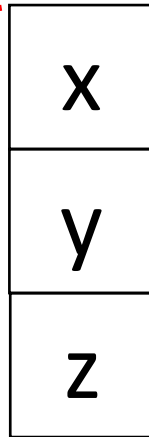
Sum at overlaps

Transposed Convolution: 1D example

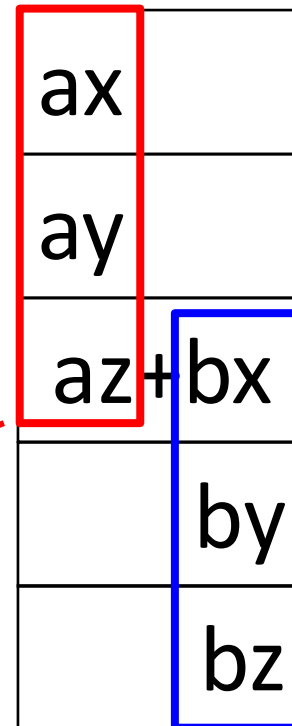
Input



Filter



Output



This has many names:

- Deconvolution (bad)!
- Upconvolution
- Fractionally strided convolution
- Backward strided convolution
- Transposed Convolution (best name)

Convolution as Matrix Multiplication (1D Example)

We can express convolution in terms of a matrix multiplication

$$\vec{x} * \vec{a} = X\vec{a}$$

$$\begin{bmatrix} x & y & z & 0 & 0 & 0 \\ 0 & x & y & z & 0 & 0 \\ 0 & 0 & x & y & z & 0 \\ 0 & 0 & 0 & x & y & z \end{bmatrix} \begin{bmatrix} 0 \\ a \\ b \\ c \\ d \\ 0 \end{bmatrix} = \begin{bmatrix} ay + bz \\ ax + by + cz \\ bx + cy + dz \\ cx + dy \end{bmatrix}$$

Example: 1D conv, kernel
size=3, stride=1, padding=1

Convolution as Matrix Multiplication (1D Example)

We can express convolution in terms of a matrix multiplication

$$\vec{x} * \vec{a} = X\vec{a}$$

$$\begin{bmatrix} x & y & z & 0 & 0 & 0 \\ 0 & x & y & z & 0 & 0 \\ 0 & 0 & x & y & z & 0 \\ 0 & 0 & 0 & x & y & z \end{bmatrix} \begin{bmatrix} 0 \\ a \\ b \\ c \\ d \\ 0 \end{bmatrix} = \begin{bmatrix} ay + bz \\ ax + by + cz \\ bx + cy + dz \\ cx + dy \end{bmatrix}$$

Example: 1D conv, kernel size=3, stride=1, padding=1

Transposed convolution multiplies by the transpose of the same matrix:

$$\vec{x} *^T \vec{a} = X^T \vec{a}$$

$$\begin{bmatrix} x & 0 & 0 & 0 \\ y & x & 0 & 0 \\ z & y & x & 0 \\ 0 & z & y & x \\ 0 & 0 & z & y \\ 0 & 0 & 0 & z \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = \begin{bmatrix} ax \\ ay + bx \\ az + by + cx \\ bz + cy + dx \\ cz + dy \\ dz \end{bmatrix}$$

When stride=1, transposed conv is just a regular conv (with different padding rules)

Convolution as Matrix Multiplication (1D Example)

We can express convolution in terms of a matrix multiplication

$$\vec{x} * \vec{a} = X \vec{a}$$

$$\begin{bmatrix} x & y & z & 0 & 0 & 0 \\ 0 & 0 & x & y & z & 0 \end{bmatrix} \begin{bmatrix} 0 \\ a \\ b \\ c \\ d \\ 0 \end{bmatrix} = \begin{bmatrix} ay + bz \\ bx + cy + dz \end{bmatrix}$$

Example: 1D conv, kernel
size=3, stride=2, padding=1

Transposed convolution multiplies by the transpose of the same matrix:

$$\vec{x} *^T \vec{a} = X^T \vec{a}$$

Convolution as Matrix Multiplication (1D Example)

We can express convolution in terms of a matrix multiplication

$$\vec{x} * \vec{a} = X \vec{a}$$

$$\begin{bmatrix} x & y & z & 0 & 0 & 0 \\ 0 & 0 & x & y & z & 0 \end{bmatrix} \begin{bmatrix} 0 \\ a \\ b \\ c \\ d \\ 0 \end{bmatrix} = \begin{bmatrix} ay + bz \\ bx + cy + dz \end{bmatrix}$$

Example: 1D conv, kernel size=3, stride=2, padding=1

Transposed convolution multiplies by the transpose of the same matrix:

$$\vec{x} *^T \vec{a} = X^T \vec{a}$$

$$\begin{bmatrix} x & 0 \\ y & 0 \\ z & x \\ 0 & y \\ 0 & z \\ 0 & 0 \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} ax \\ ay \\ az + bx \\ by \\ bz \\ 0 \end{bmatrix}$$

When stride>1, transposed convolution cannot be expressed as normal conv

Semantic Segmentation: Fully Convolutional Network

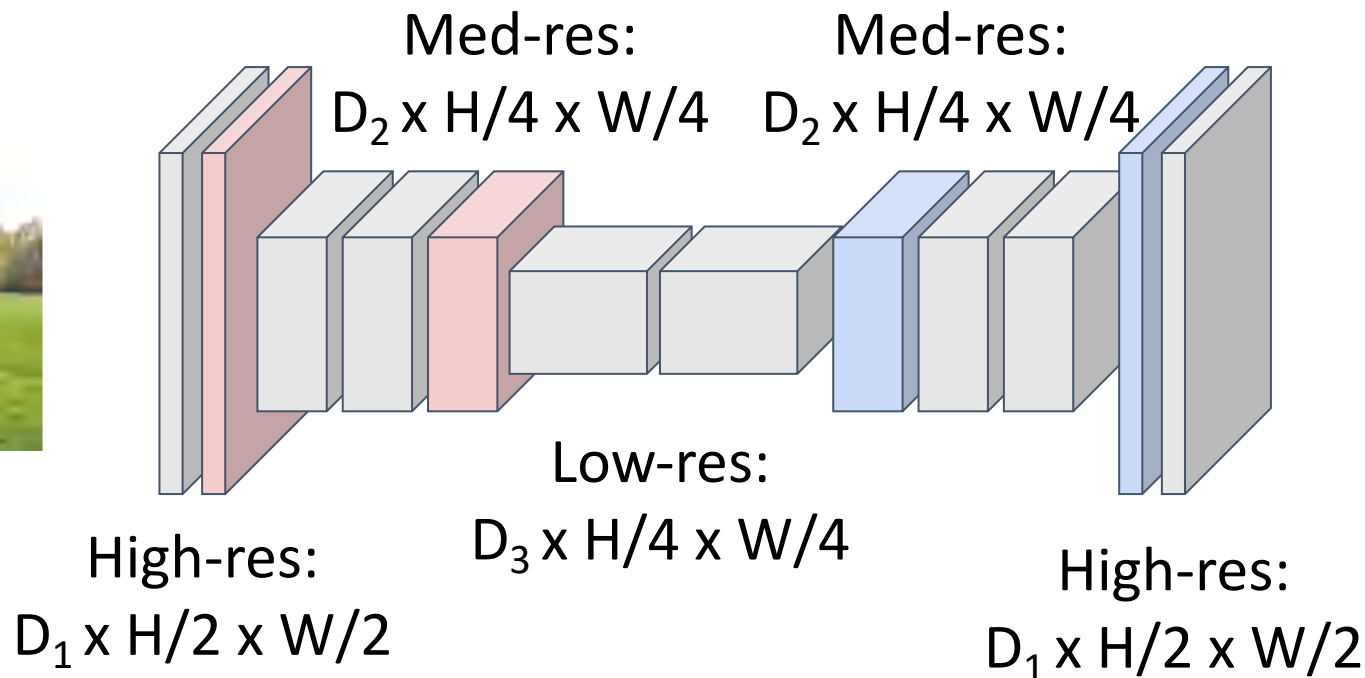
Downsampling:
Pooling, strided
convolution

Design network as a bunch of convolutional layers, with **downsampling** and **upsampling** inside the network!

Upsampling:
Interpolation,
transposed conv



Input:
 $3 \times H \times W$



Predictions:
 $H \times W$

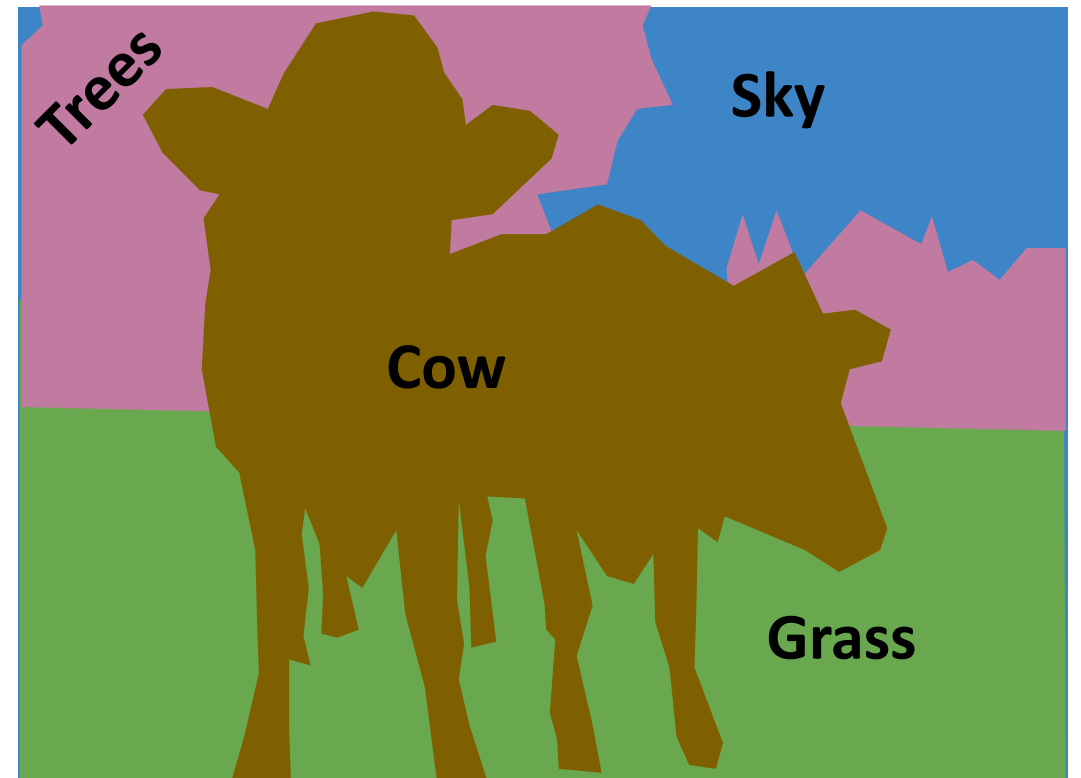
Loss function: Per-Pixel cross-entropy

Computer Vision Tasks

Object Detection: Detects individual object instances, but only gives box

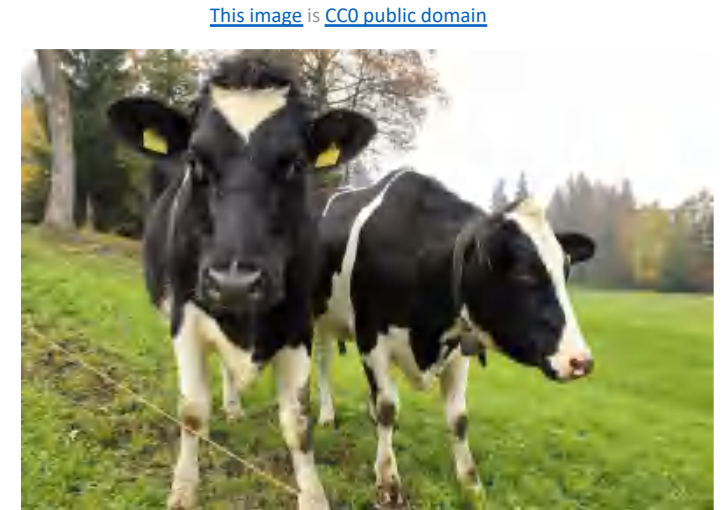


Semantic Segmentation: Gives per-pixel labels, but merges instances

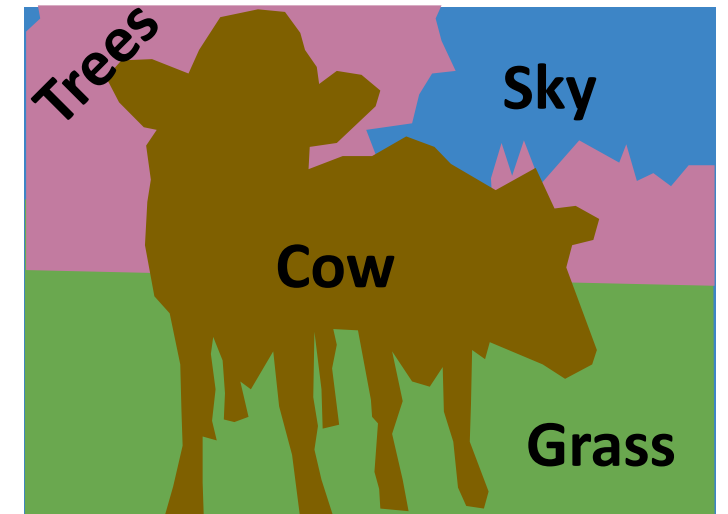
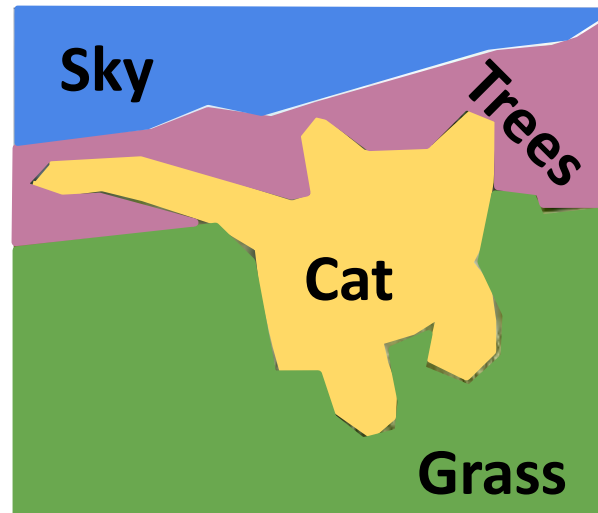


Things and Stuff

Things: Object categories that can be separated into object instances (e.g. cats, cars, person)



Stuff: Object categories that cannot be separated into instances (e.g. sky, grass, water, trees)

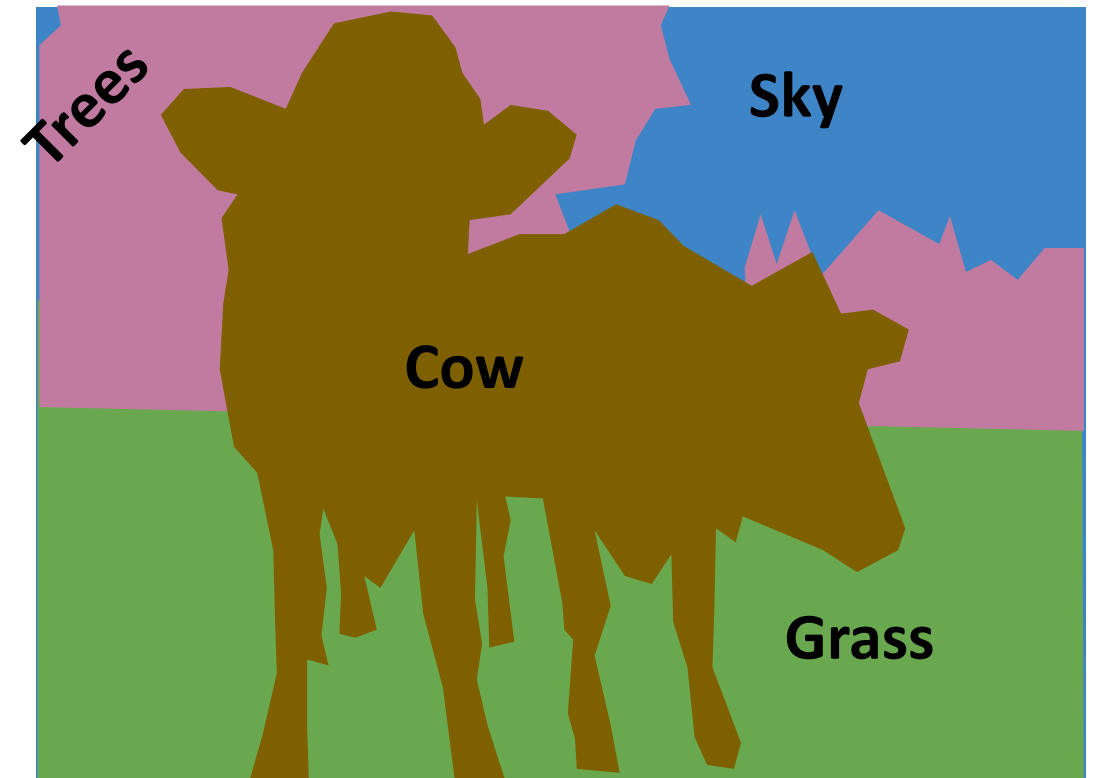


Computer Vision Tasks

Object Detection: Detects individual object instances, but only gives box (Only things!)



Semantic Segmentation: Gives per-pixel labels, but merges instances (Both things and stuff)



Computer Vision Tasks: Instance Segmentation

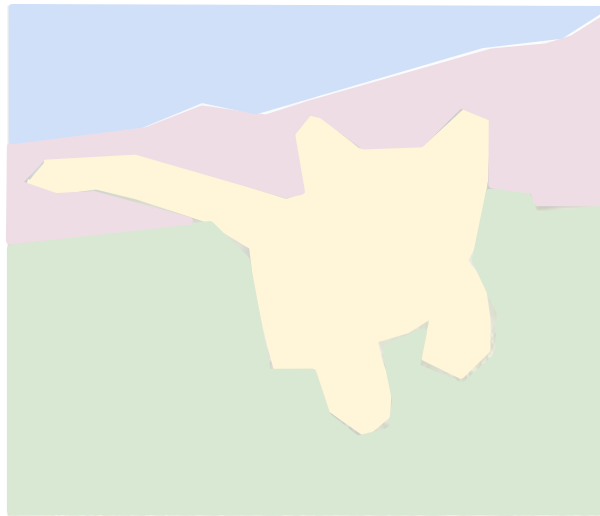
Classification



CAT

No spatial extent

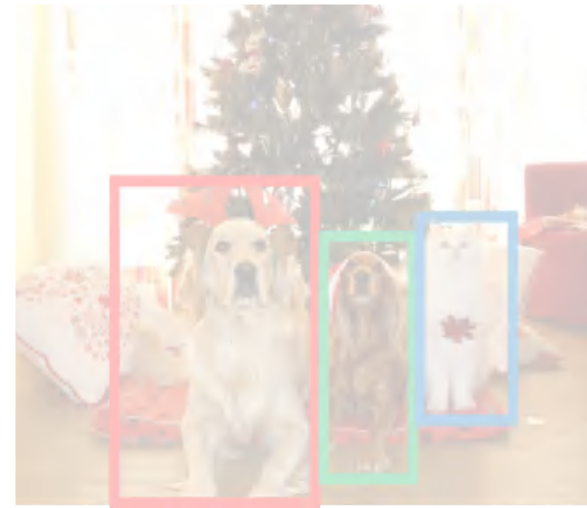
Semantic
Segmentation



GRASS, CAT, TREE,
SKY

No objects, just pixels

Object
Detection



DOG, DOG, CAT

Multiple Objects

Instance
Segmentation

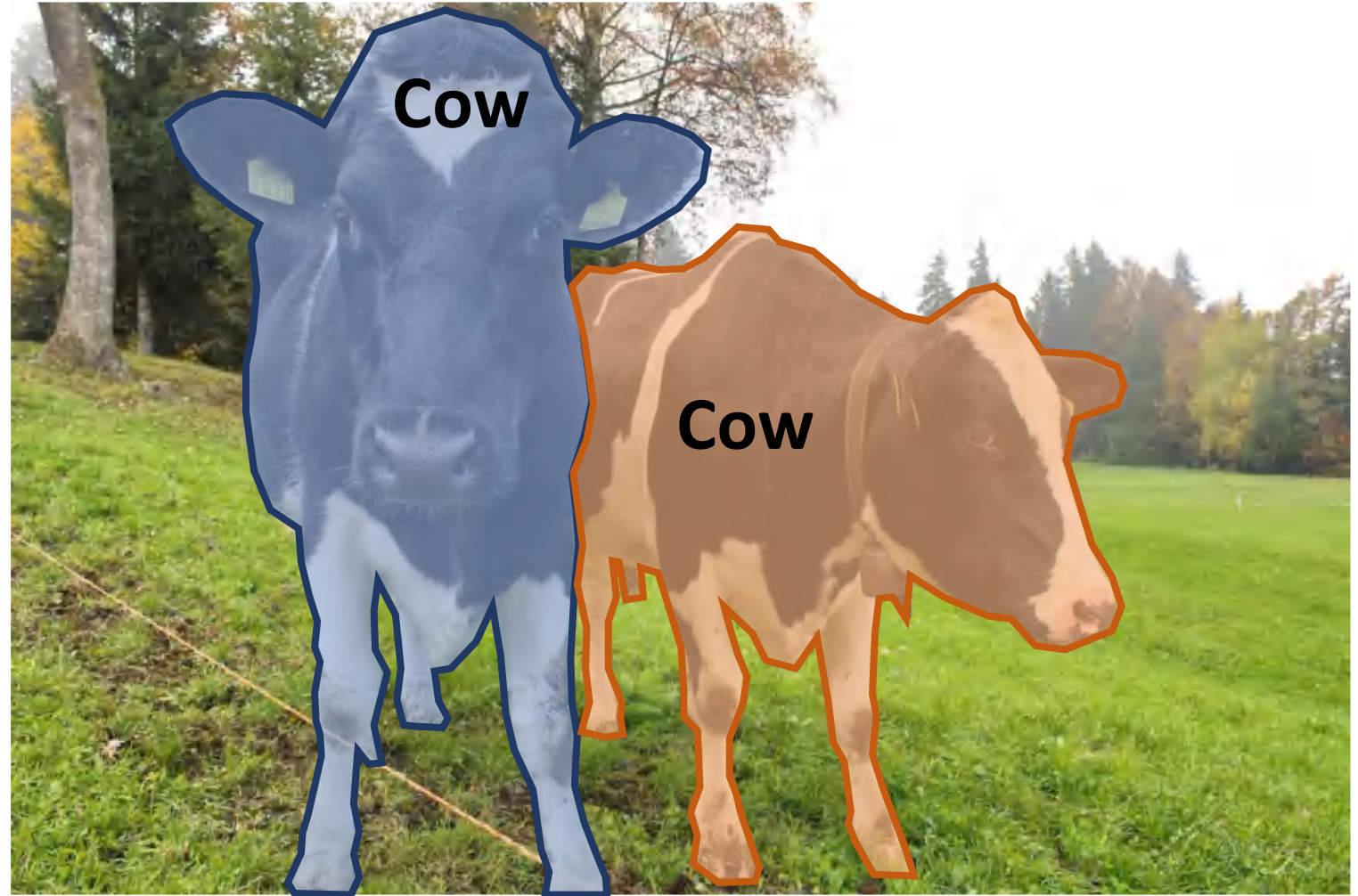


DOG, DOG, CAT

Computer Vision Tasks: Instance Segmentation

Instance Segmentation:

Detect all objects in the image, and identify the pixels that belong to each object (Only things!)



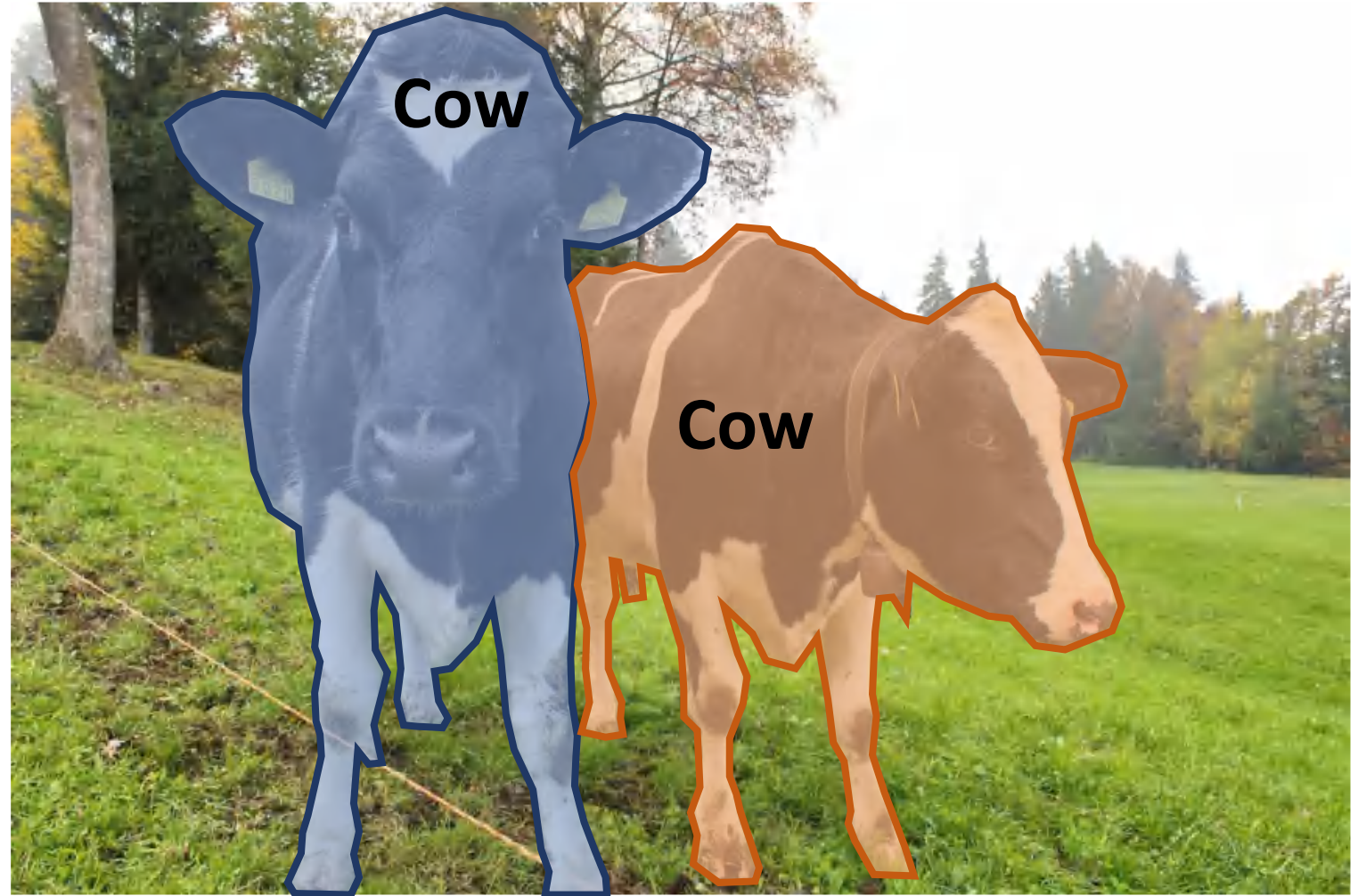
[This image](#) is [CC0 public domain](#)

Computer Vision Tasks: Instance Segmentation

Instance Segmentation:

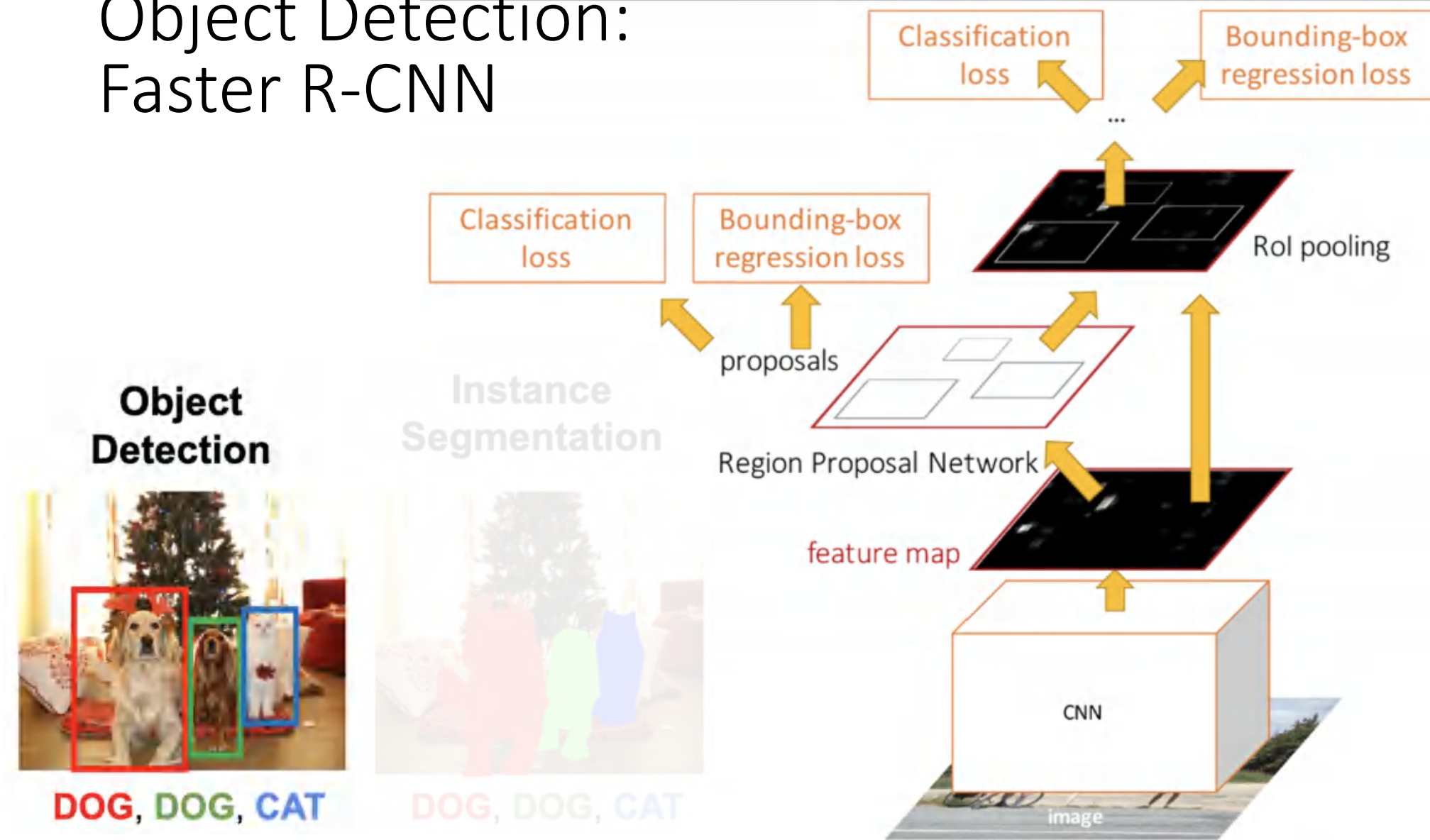
Detect all objects in the image, and identify the pixels that belong to each object (Only things!)

Approach: Perform object detection, then predict a segmentation mask for each object!



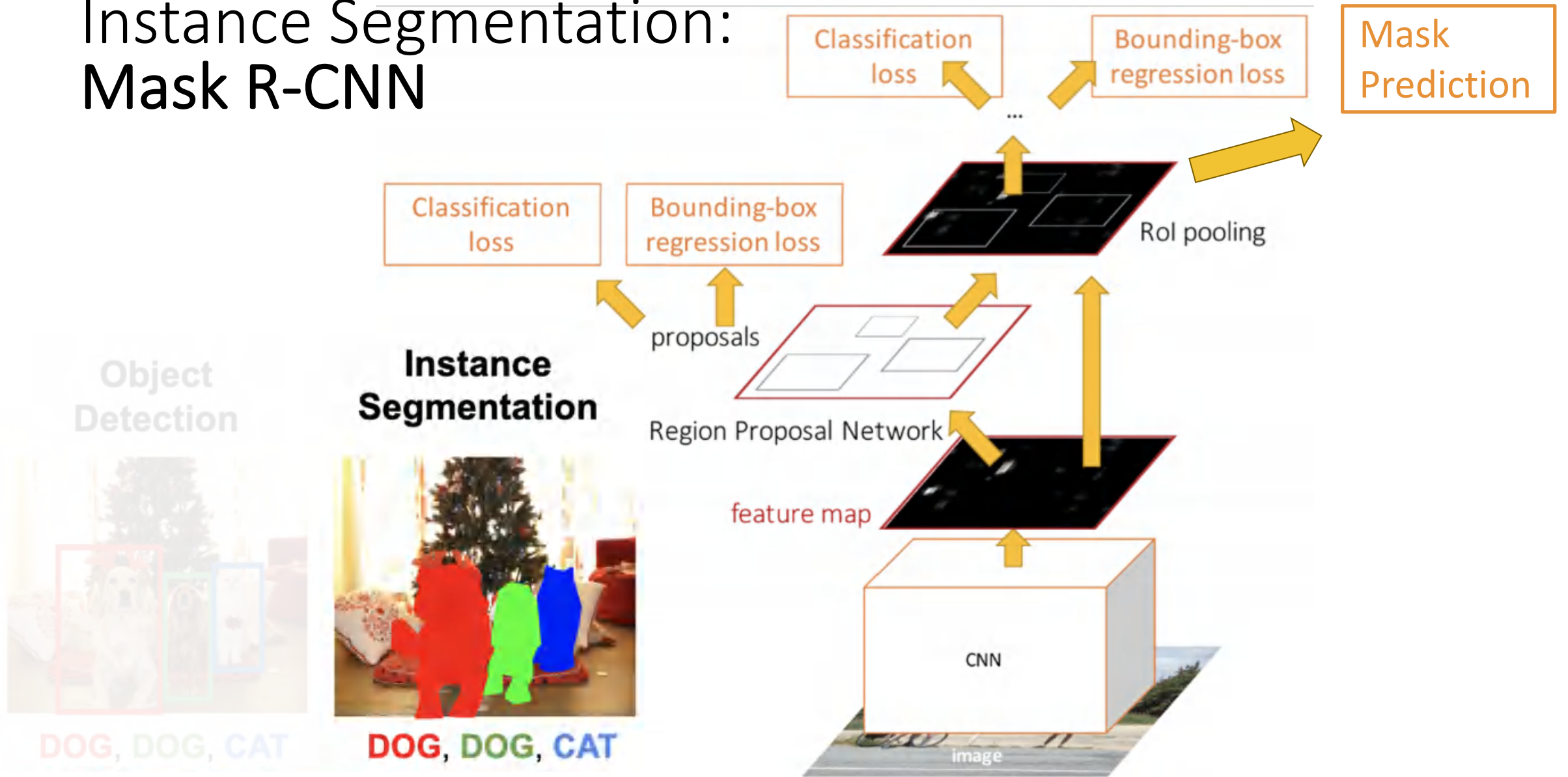
[This image](#) is [CC0 public domain](#)

Object Detection: Faster R-CNN



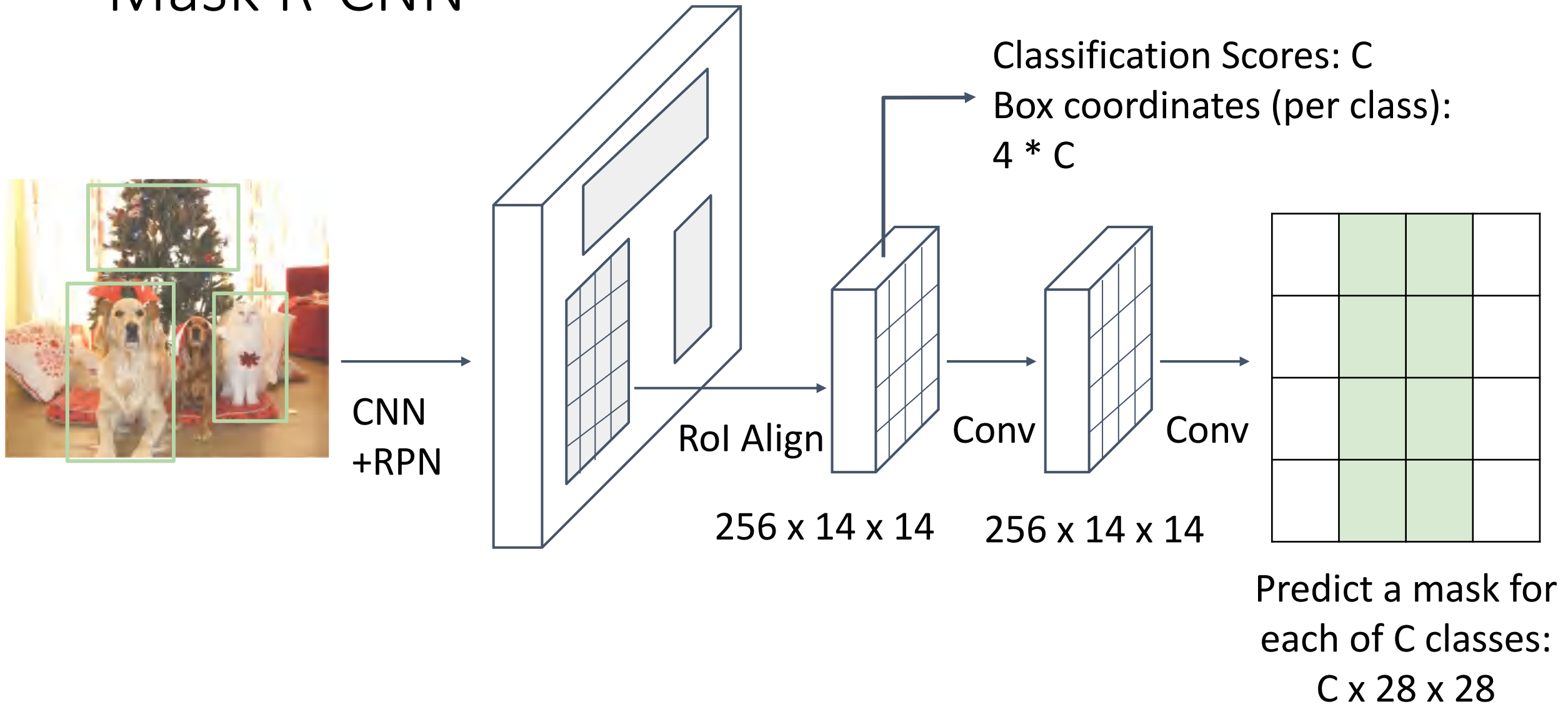
Ren et al, "Faster R-CNN: Towards Real-Time Object Detection with Region Proposal Networks", NeurIPS 2015

Instance Segmentation: Mask R-CNN



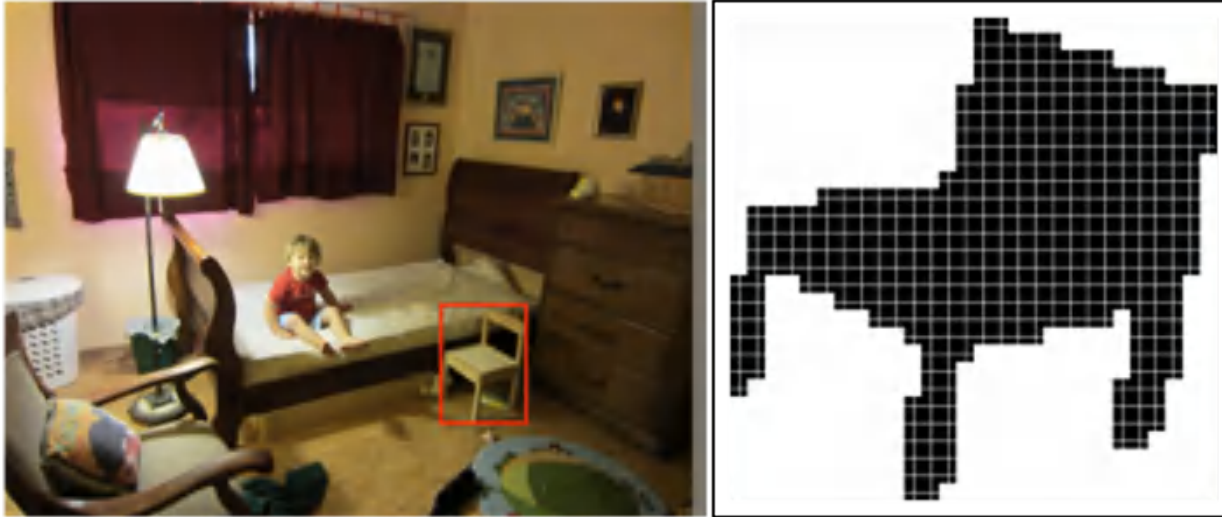
He et al, "Mask R-CNN", ICCV 2017

Mask R-CNN

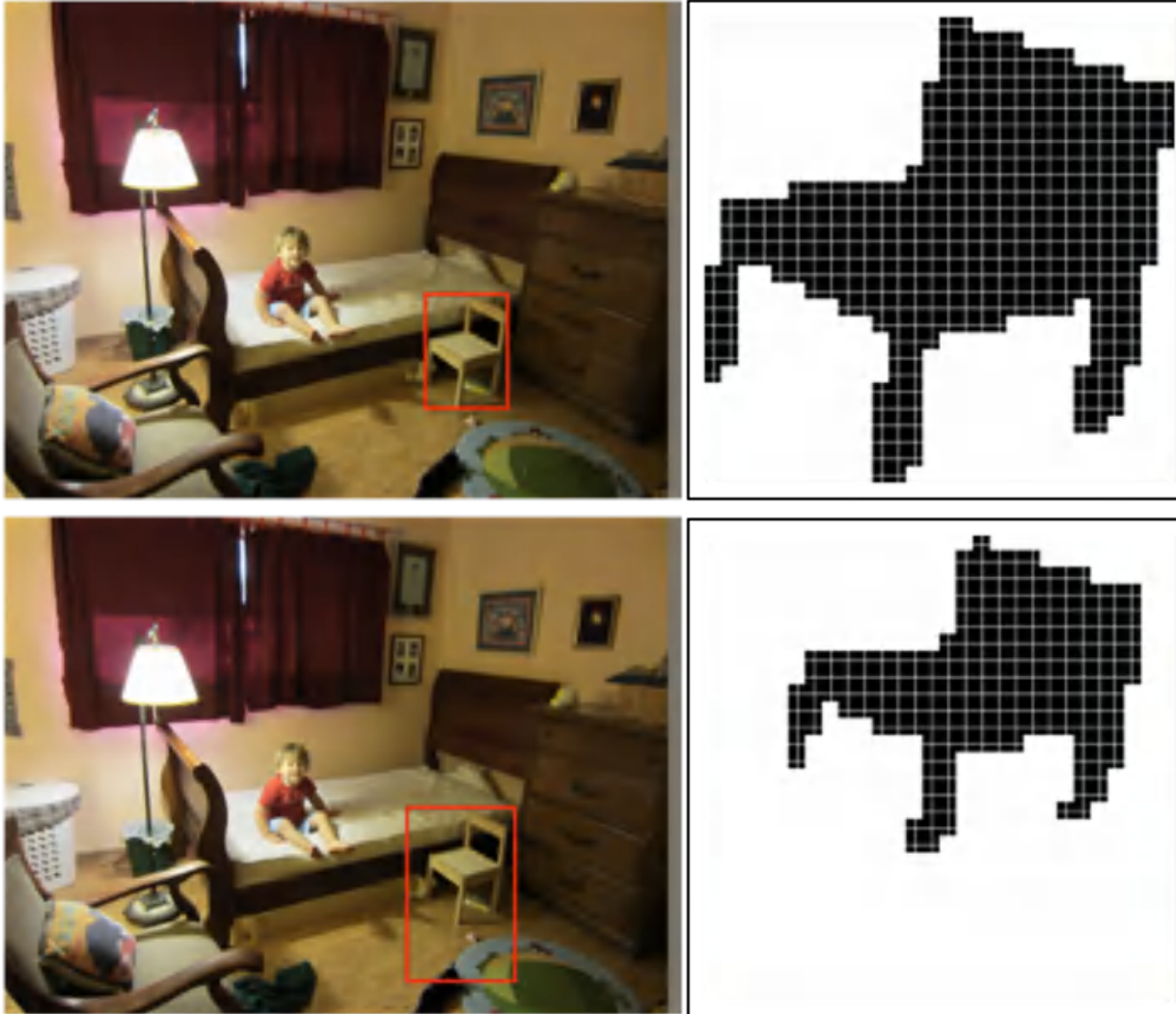


He et al, "Mask R-CNN", ICCV 2017

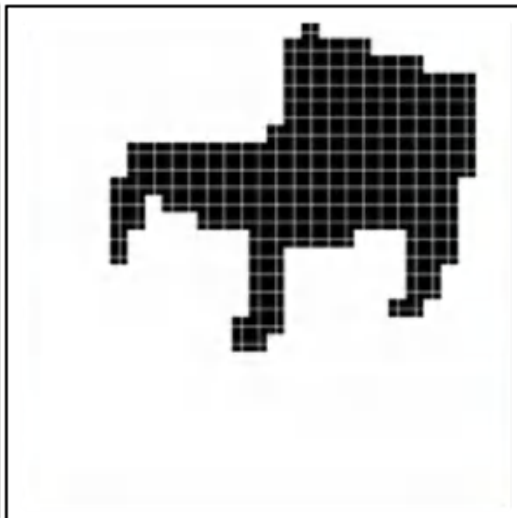
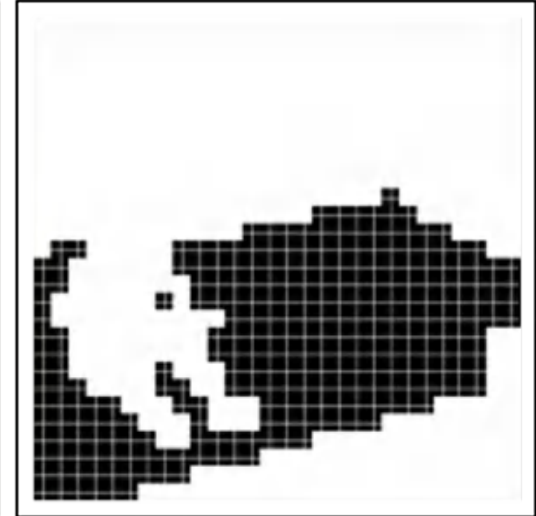
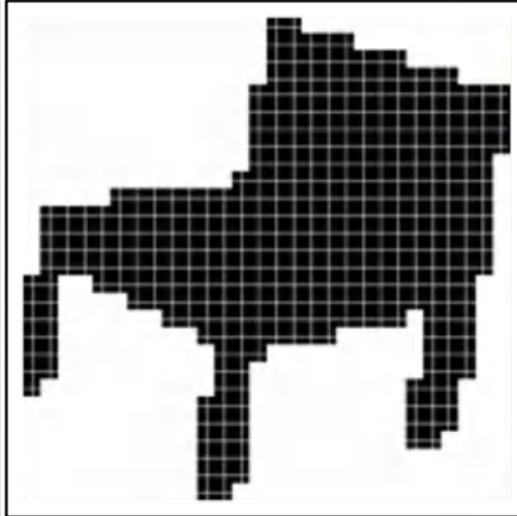
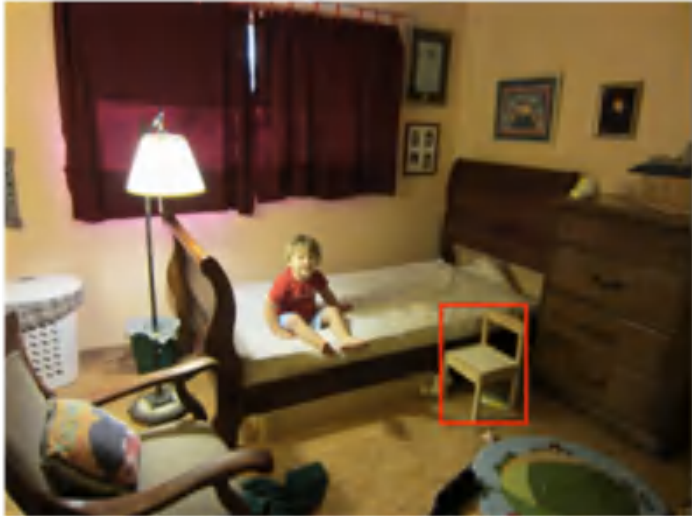
Mask R-CNN: Example Training Targets



Mask R-CNN: Example Training Targets



Mask R-CNN: Example Training Targets



Mask R-CNN: Example Training Targets

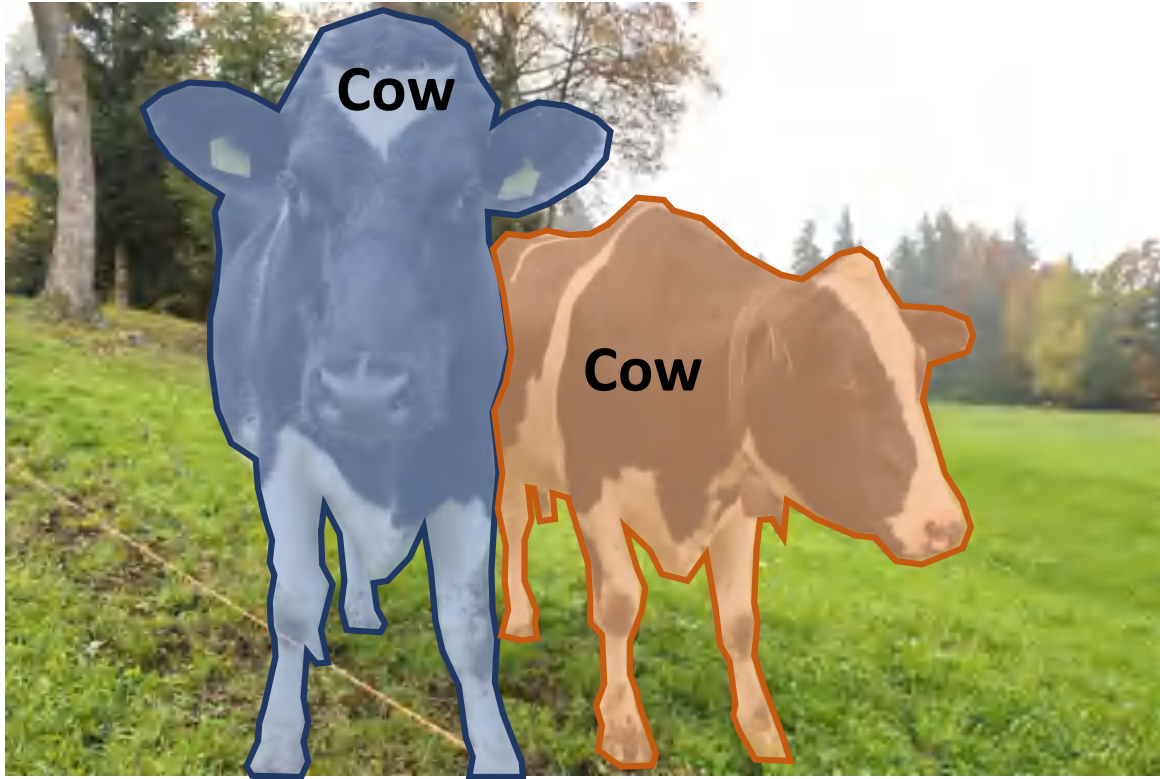


Mask R-CNN: Very Good Results!

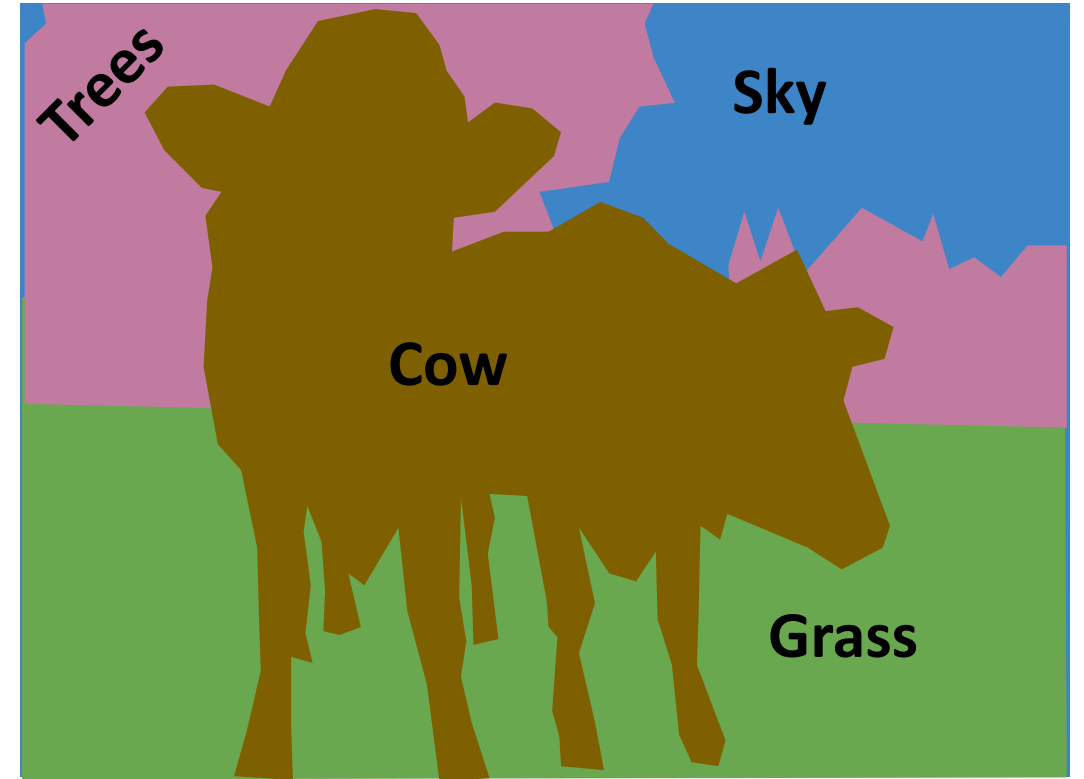


Beyond Instance Segmentation

Instance Segmentation: Separate object instances, but only things



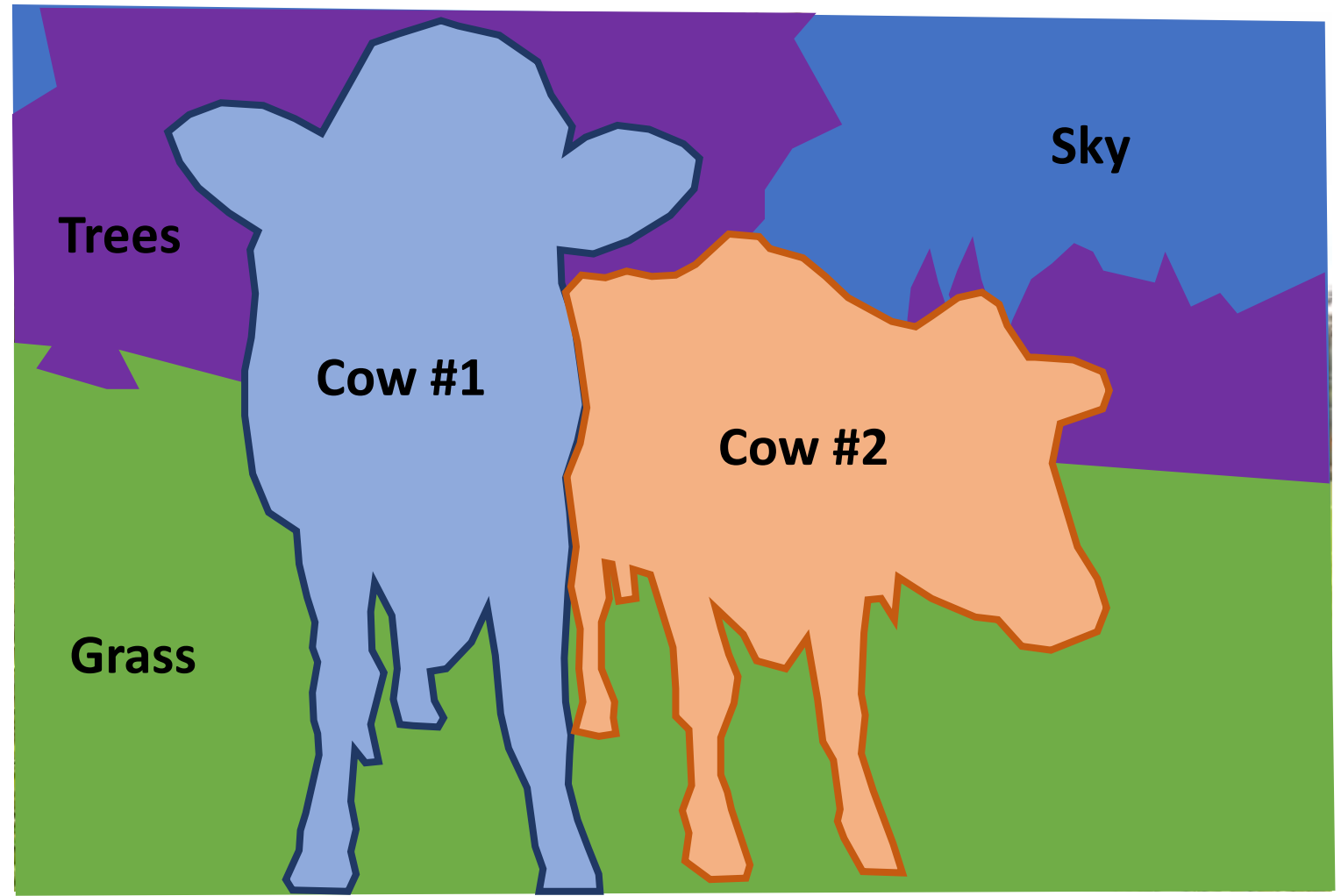
Semantic Segmentation: Identify both things and stuff, but doesn't separate instances



Beyond Instance Segmentation: Panoptic Segmentation

Label all pixels in the image (both things and stuff)

For “thing” categories also separate into instances



Kirillov et al, “Panoptic Segmentation”, CVPR 2019

Kirillov et al, “Panoptic Feature Pyramid Networks”, CVPR 2019

Beyond Instance Segmentation: Panoptic Segmentation



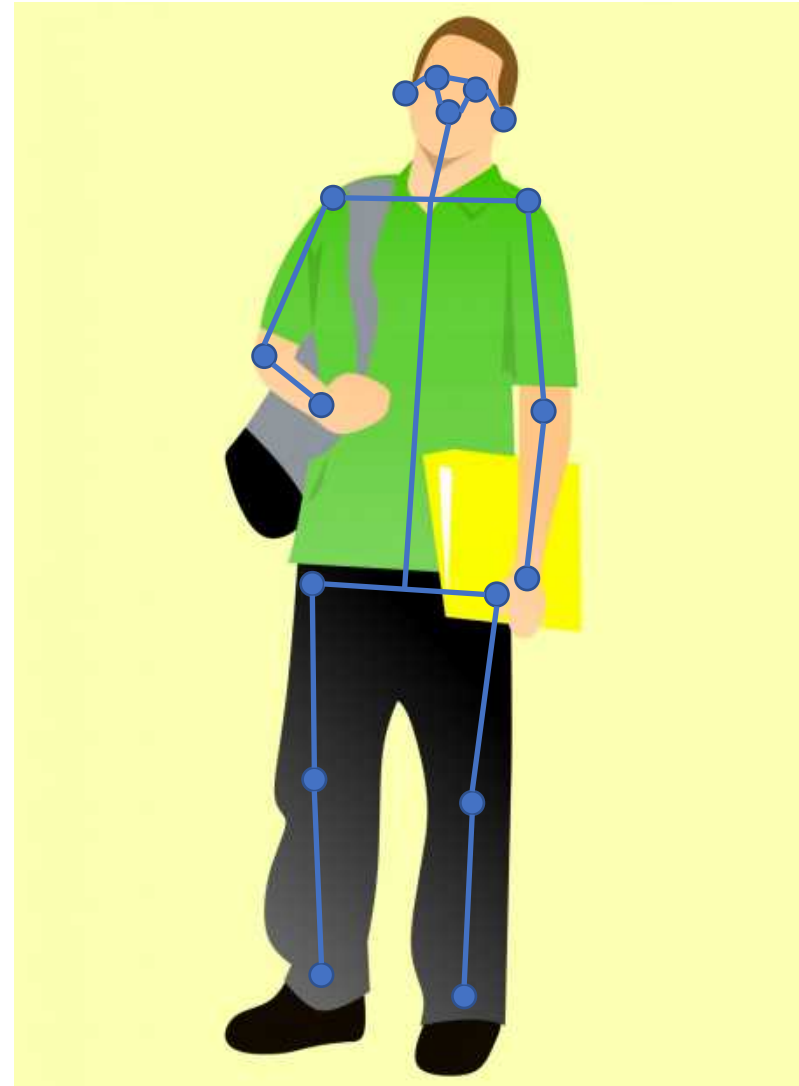
Kirillov et al, "Panoptic Feature Pyramid Networks", CVPR 2019

Beyond Instance Segmentation: Human Keypoints

Represent the pose of a human by locating a set of **keypoints**

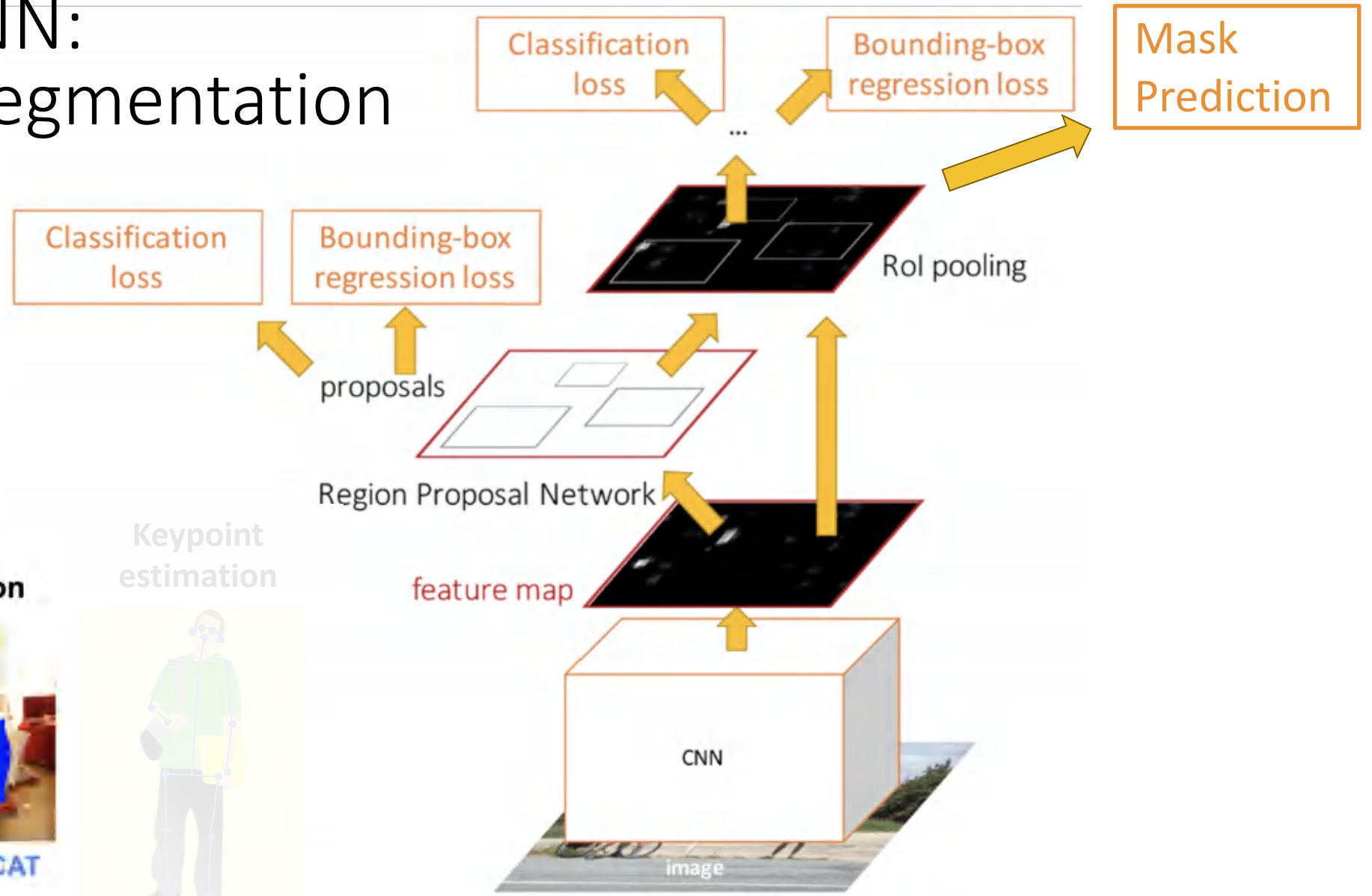
e.g. 17 keypoints:

- Nose
- Left / Right eye
- Left / Right ear
- Left / Right shoulder
- Left / Right elbow
- Left / Right wrist
- Left / Right hip
- Left / Right knee
- Left / Right ankle



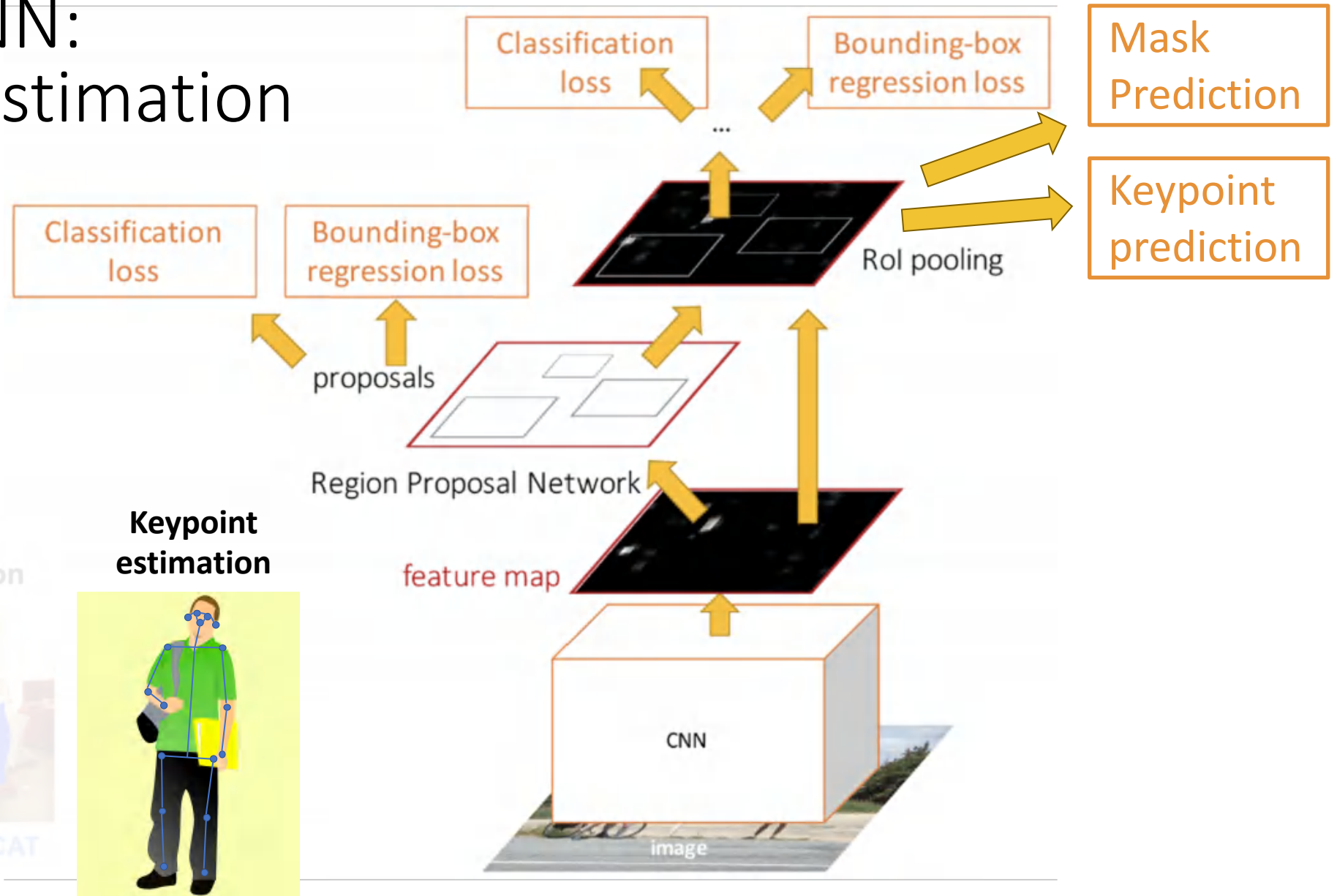
[Person image](#) is [CC0 public domain](#)

Mask R-CNN: Instance Segmentation



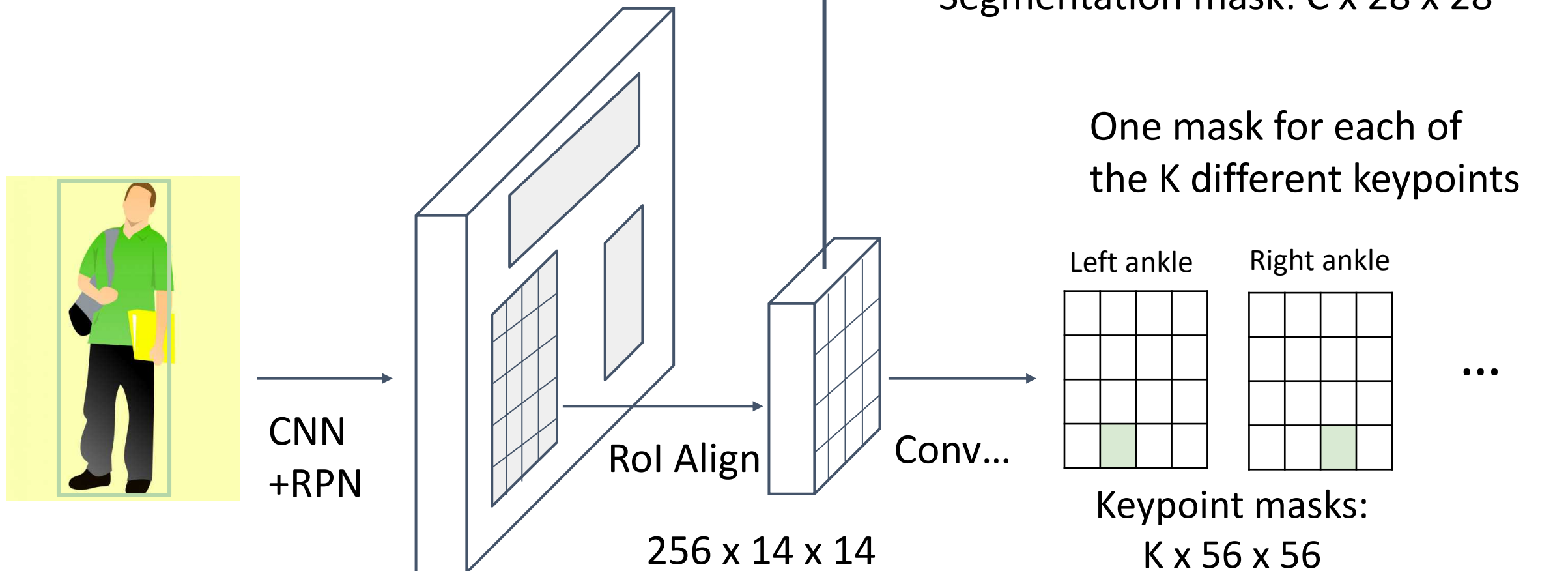
He et al, "Mask R-CNN", ICCV 2017

Mask R-CNN: Keypoint Estimation

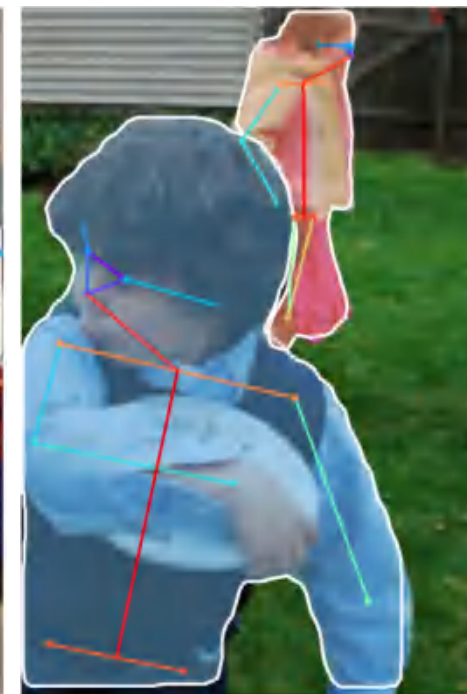


He et al, "Mask R-CNN", ICCV 2017

Mask R-CNN: Keypoints

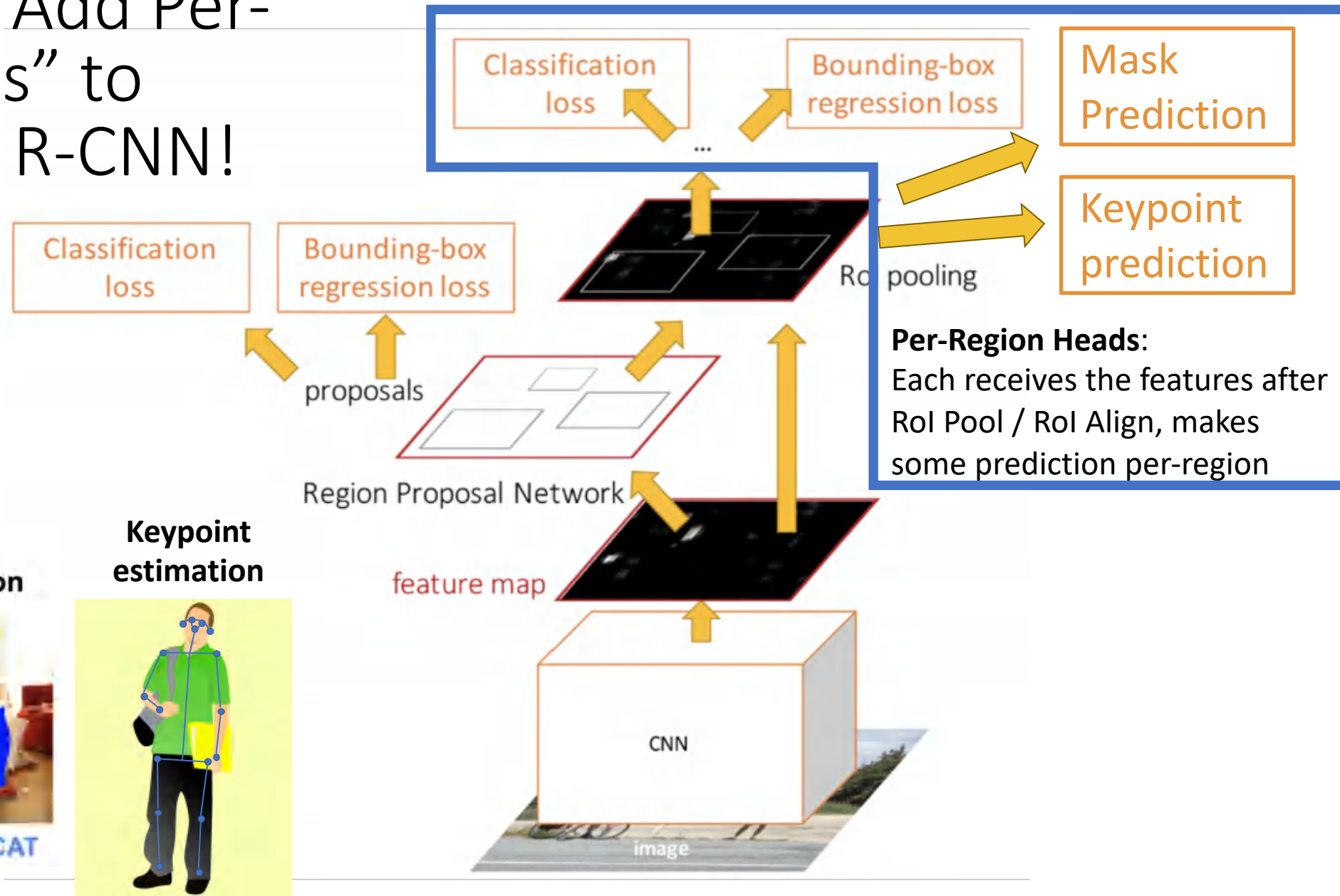


Joint Instance Segmentation and Pose Estimation



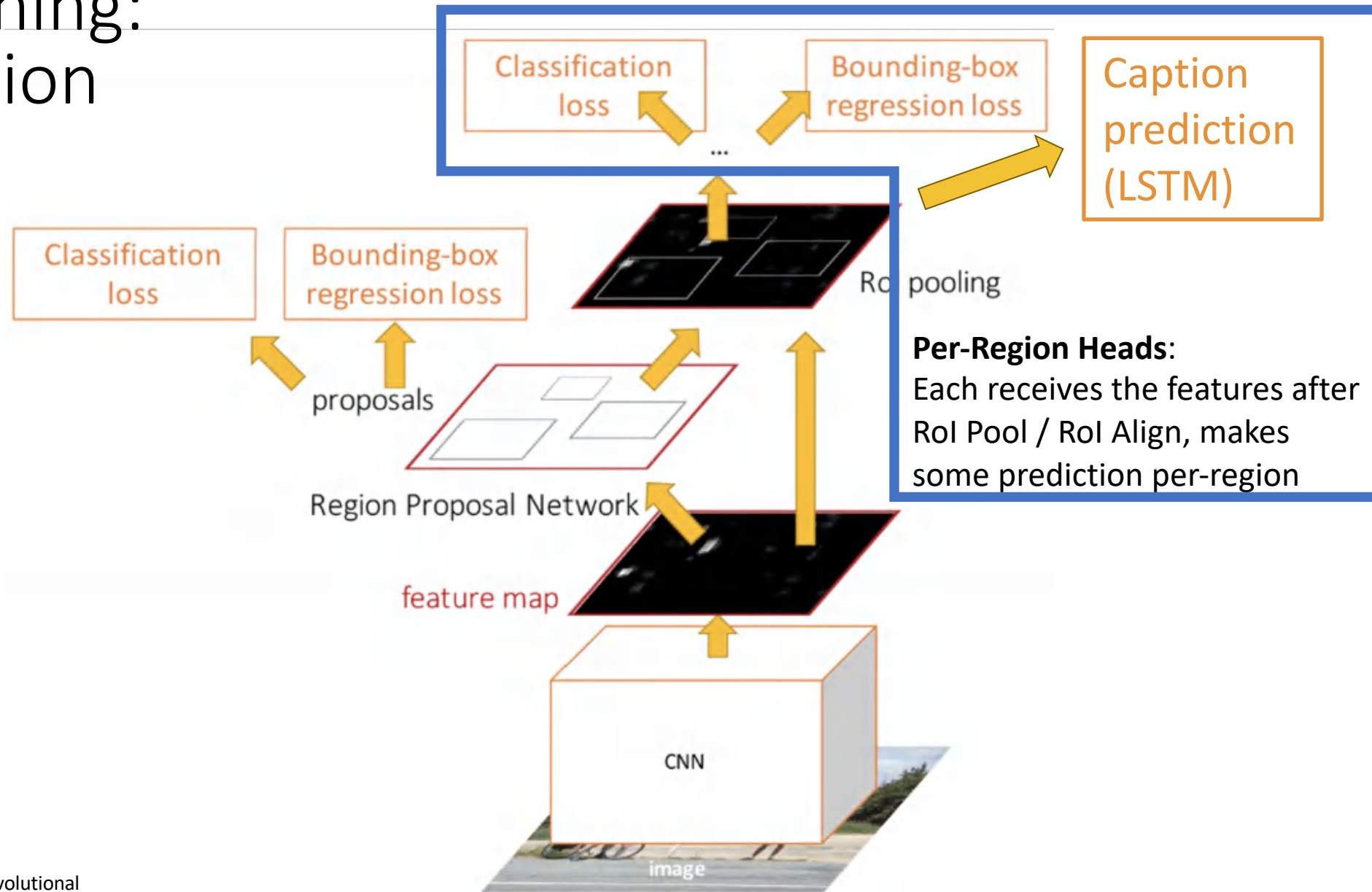
He et al, "Mask R-CNN", ICCV 2017

General Idea: Add Per-Region “Heads” to Faster / Mask R-CNN!



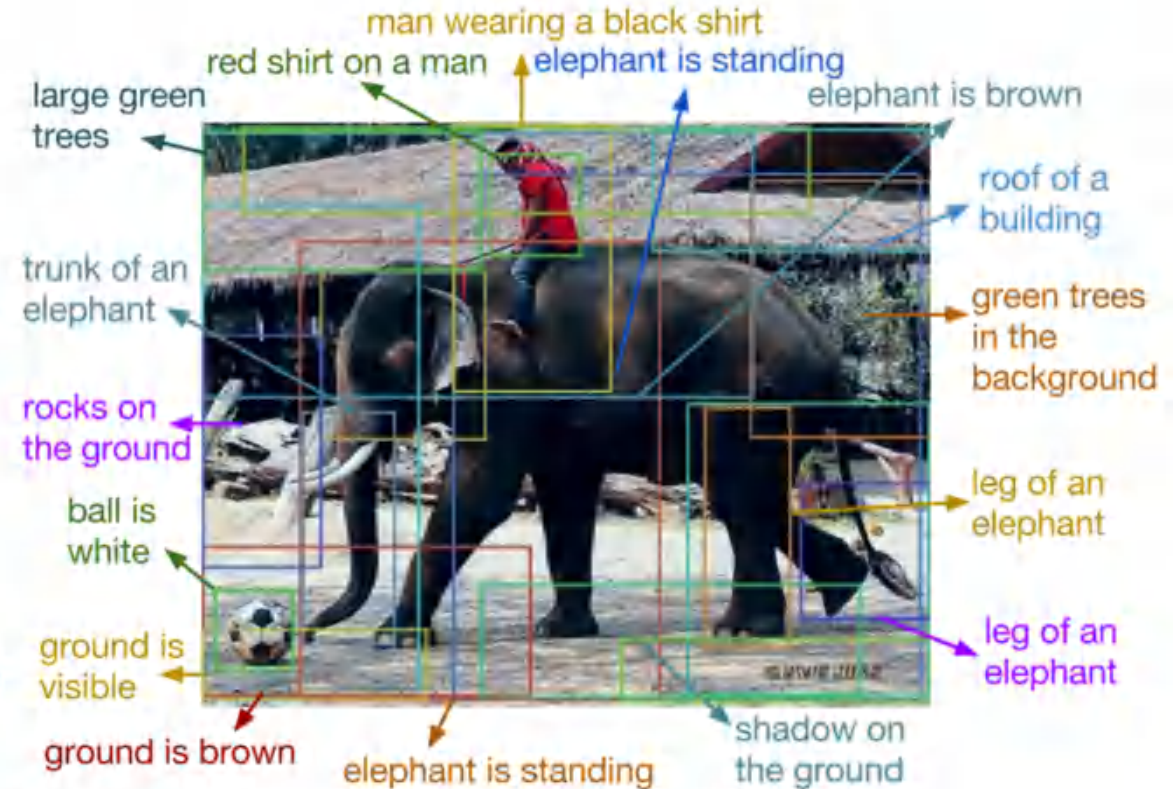
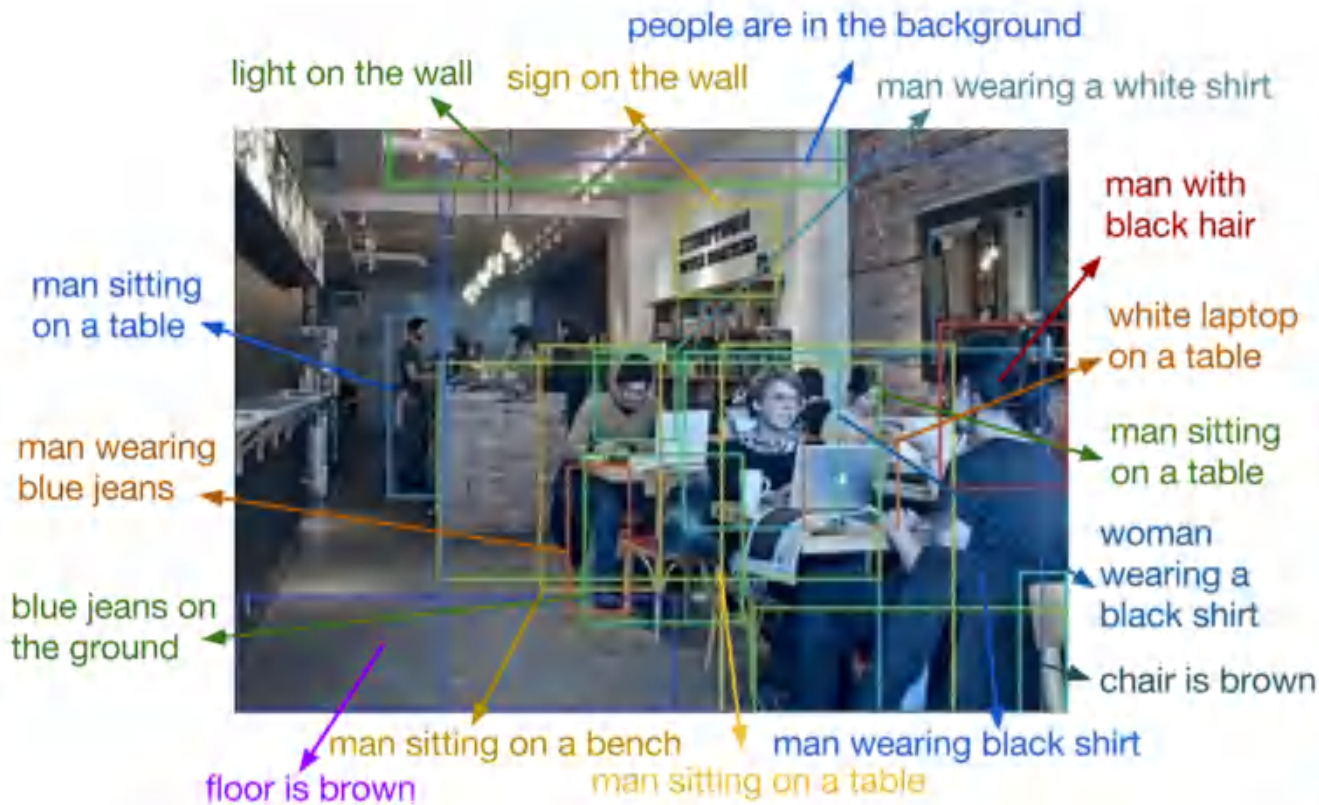
He et al, "Mask R-CNN", ICCV 2017

Dense Captioning: Predict a caption per region!

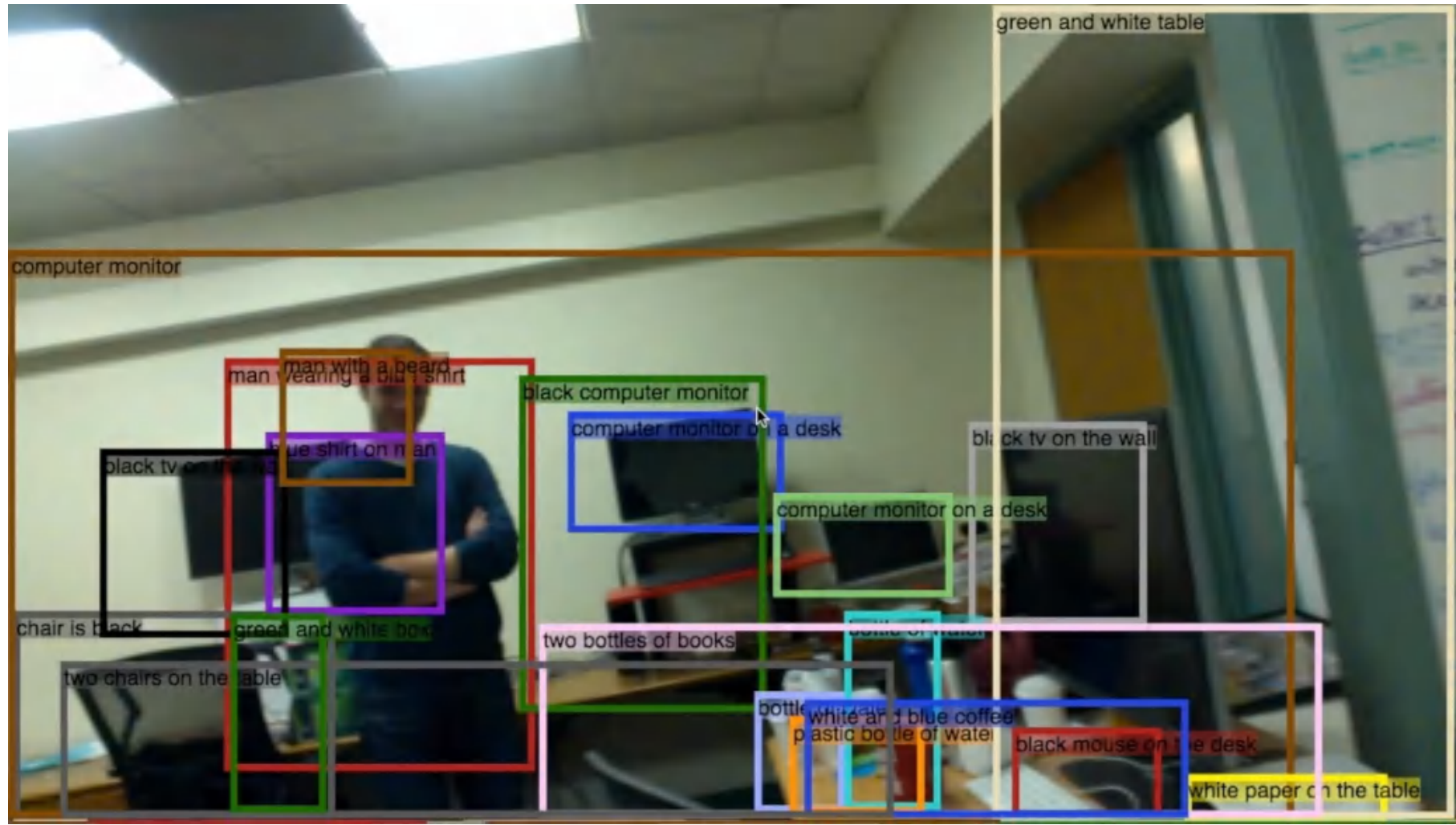


Johnson, Karpathy, and Fei-Fei, "DenseCap: Fully Convolutional Localization Networks for Dense Captioning", CVPR 2016

Dense Captioning

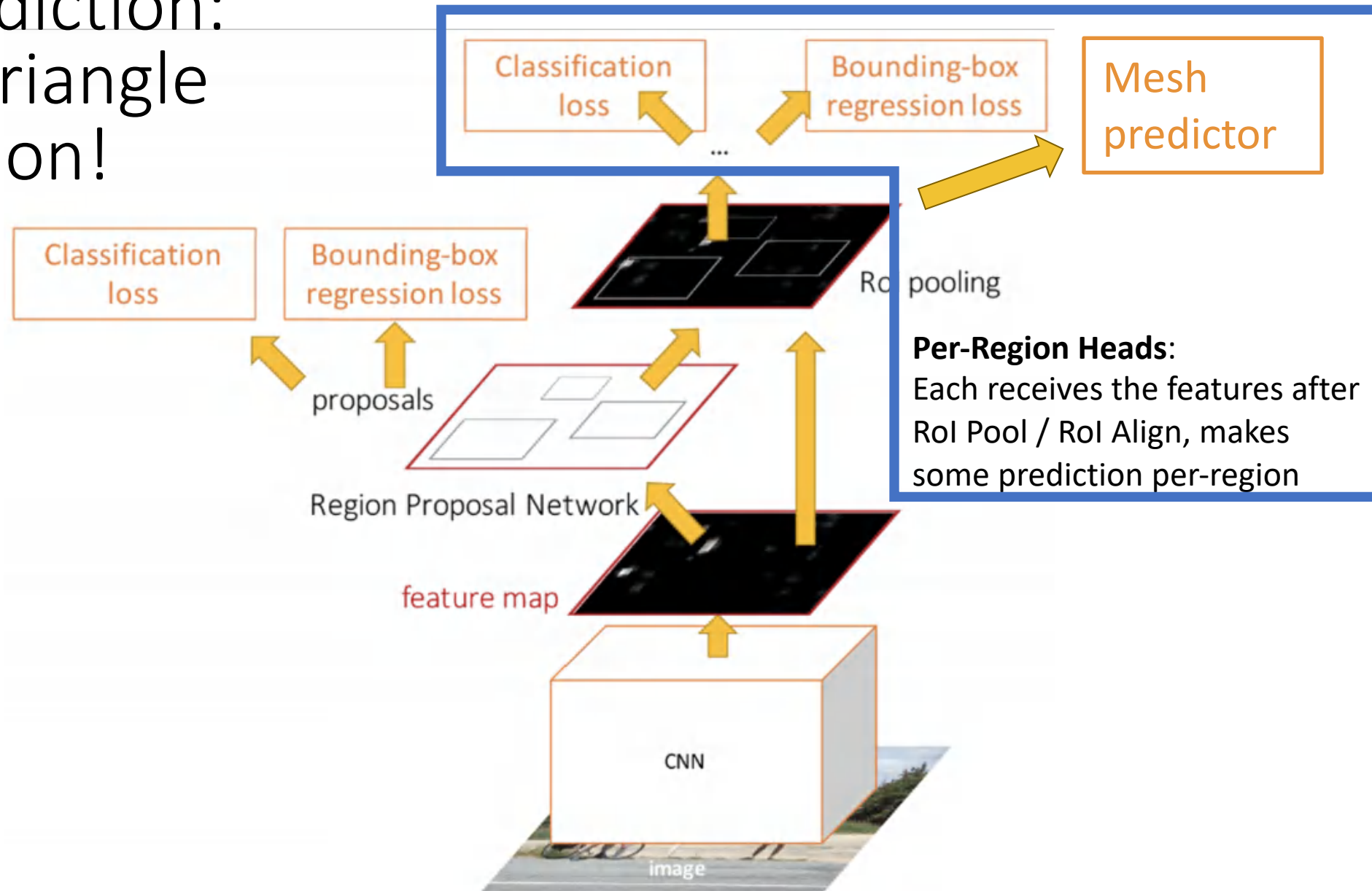


Dense Captioning



Johnson, Karpathy, and Fei-Fei, "DenseCap: Fully Convolutional Localization Networks for Dense Captioning", CVPR 2016

3D Shape Prediction: Predict a 3D triangle mesh per region!

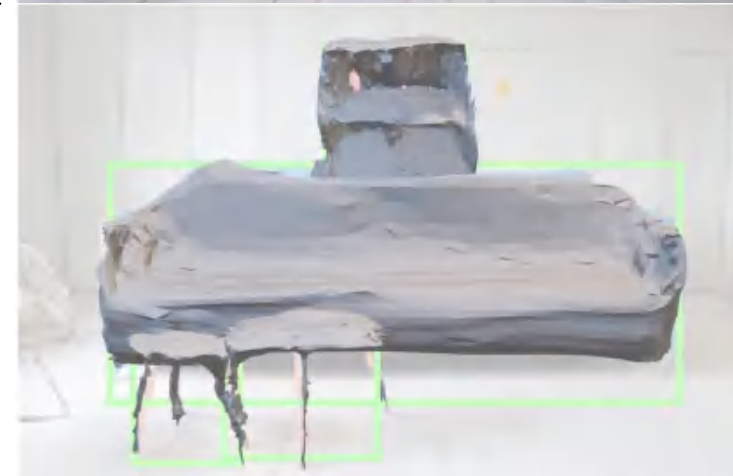
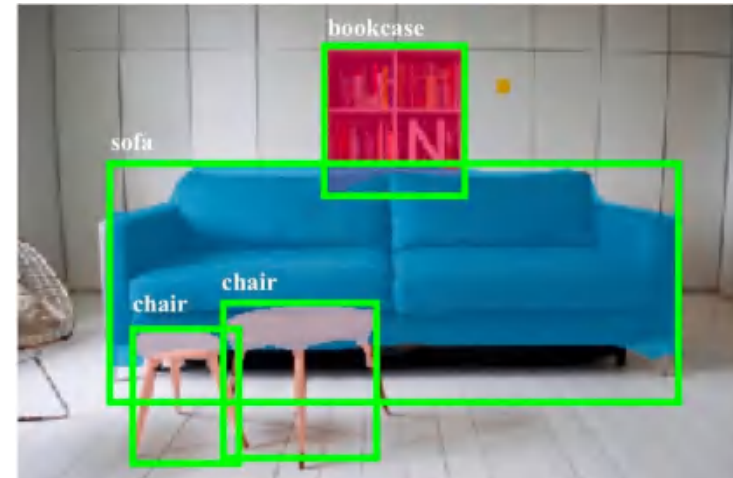


3D Shape Prediction: Mask R-CNN + Mesh Head

Mask R-CNN:
2D Image -> 2D shapes



Mesh R-CNN:
2D Image -> **3D** shapes



More details
next time!

He, Gkioxari, Dollár, and Girshick, "Mask R-CNN", ICCV 2017

Gkioxari, Malik, and Johnson, "Mesh R-CNN", ICCV 2019

Summary: Many Computer Vision Tasks!

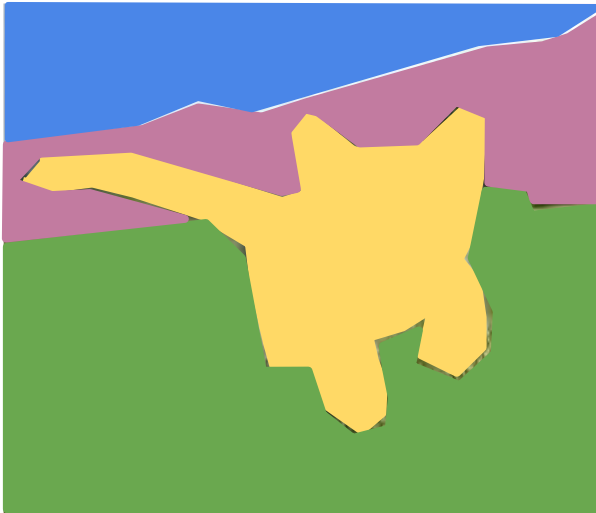
Classification



CAT

No spatial extent

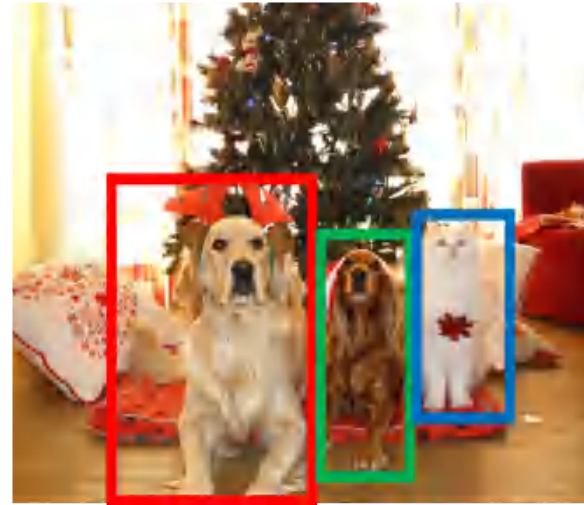
Semantic Segmentation



GRASS, CAT, TREE, SKY

No objects, just pixels

Object Detection



DOG, DOG, CAT

Multiple Objects

Instance Segmentation



DOG, DOG, CAT

[This image](#) is [CC0 public domain](#)

Next Time:
Recurrent Neural Networks