Lecture 2: Image Classification

Waitlisted Students

- We'll continue sending overrides in waitlist order as seats open
- If you get one, enroll right now override will expire in 24h
- If you received an override and it expires, you will not get another

Office Hours

Office hours start this week; check Google Calendar for details

Fill out the following form about your office hour time preferences: https://forms.gle/Qh41oXuzjrTxFEVk9

Piazza

Reminder: Piazza is our main source of communication this semester

Right now (enrolled students) < (enrolled students on Piazza)

Go enroll on Piazza if you haven't already

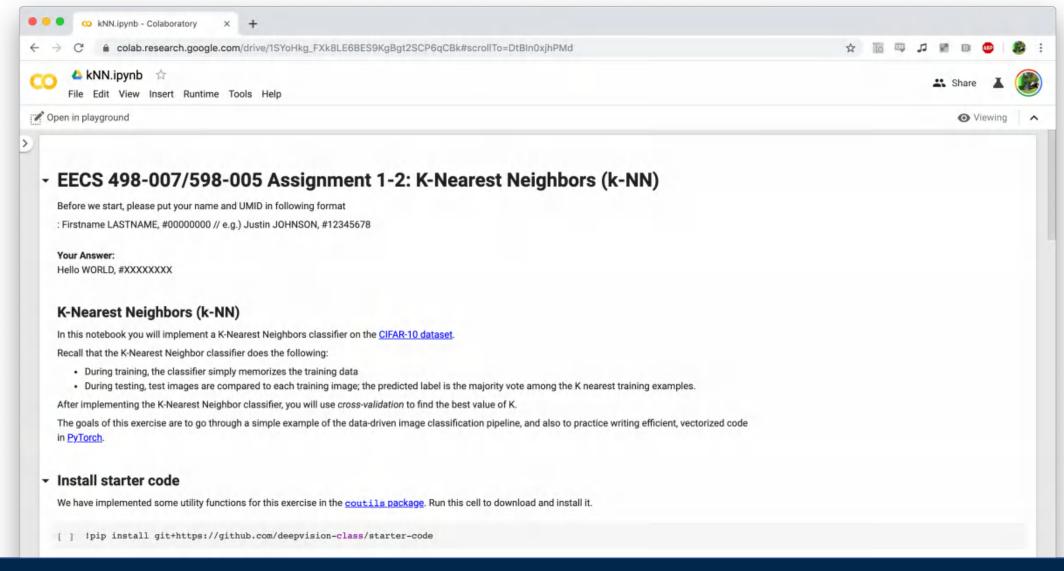
Assignment 1 Released

- https://web.eecs.umich.edu/~justincj/teaching/eecs498/WI2022/assignment1.html
- Uses Python, PyTorch, and Google Colab
- Introduction to PyTorch Tensors
- K-Nearest Neighbor classification
- Two challenge questions worth 2% each
- Due Friday January 14, 11:59pm ET

Assignment 1 Released

- https://web.eecs.umich.edu/~justincj/teaching/eecs498/WI2022/assignment1.html
- Make sure you download the WI2022 version of the assignment!
- We released a slightly updated assignment today with minor bugfixes;
 see Piazza: https://piazza.com/class/kxtai72amx34p0?cid=46
- Only enrolled students can submit the assignment, but if you enroll late we will give you extra days to submit A1

Google Colab: Cloud Computing in the Browser



Google Colab: Cloud Computing in the Browser

EECS 498-007 / 598-005
Deep Learning for Computer Vision
Fall 2020

Colab Tutorial

What is Colab?

- Colaboratory is a Google research project created to help disseminate machine learning education and research. It's a Jupyter notebook environment that requires no setup to use and runs entirely in the cloud. (from Google Colab Notebooks page)
- It allows you to use virtual machines with a GPU (or TPU) to accelerate machinelearning workloads for up to 12 hours at a time.
- It is free to use! There is a paid option called Colab Pro which gives access to faster GPUs, more RAM, more CPU cores, more disk space, and longer runtimes, those won't be necessary for this course.

Steps to use Colab

We've written a Colab tutorial: https://web.eecs.umich.edu/~j ustincj/teaching/eecs498/WI2 022/colab.html

Lecture 2: Image Classification

Image Classification: A core computer vision task

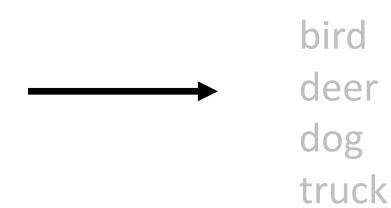
Input: image



This image by Nikita is licensed under CC-BY 2.0

Output: Assign image to one of a fixed set of categories

cat

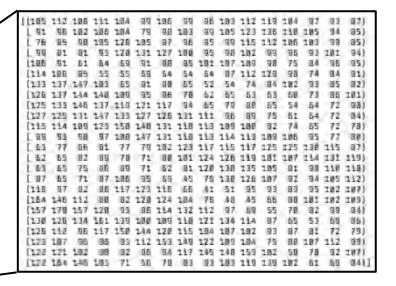


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Problem: Semantic Gap



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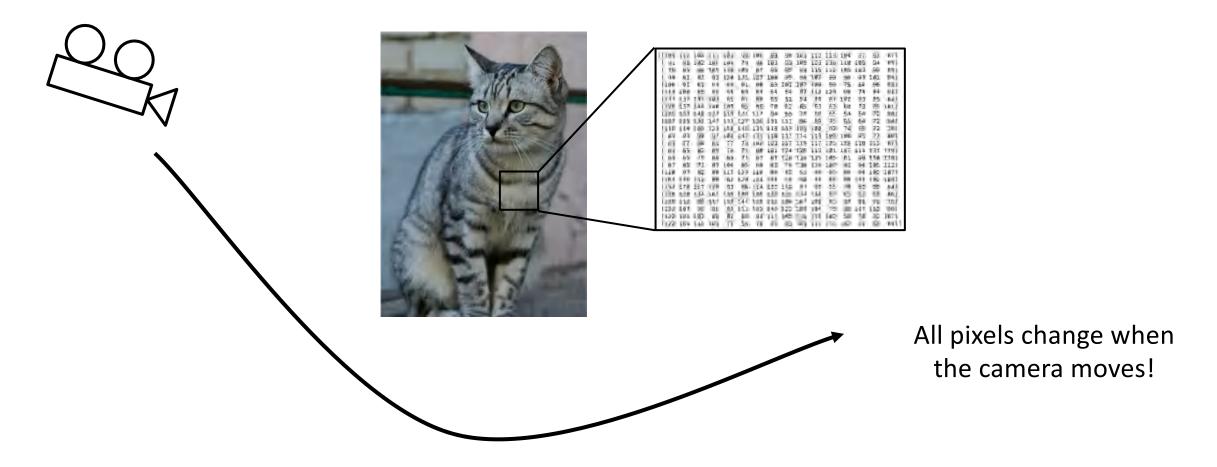


What the computer sees

An image is just a big grid of numbers between [0, 255]:

e.g. 800 x 600 x 3 (3 channels RGB)

Challenges: Viewpoint Variation



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Challenges: Intraclass Variation



This image is CCO 1.0 public domain

Challenges: Fine-Grained Categories

Maine Coon



This image is free for for use under the Pixabay License

Ragdoll



This image is CCO public domain

American Shorthair



This image is CCO public domain

Challenges: Background Clutter





This image is CC0 1.0 public domain

This image is CC0 1.0 public domain

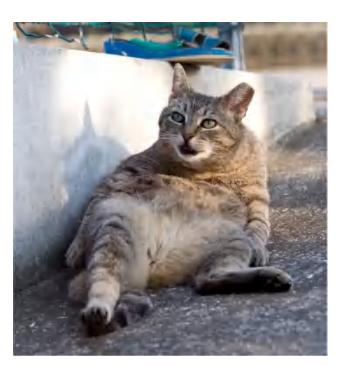
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Challenges: Illumination Changes



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Challenges: Deformation



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This image by Umberto Salvagnin is licensed under CC-BY 2.0



This image by sare bear is licensed under CC-BY 2.0



This image by Tom Thai is licensed under CC-BY 2.0

Challenges: Occlusion







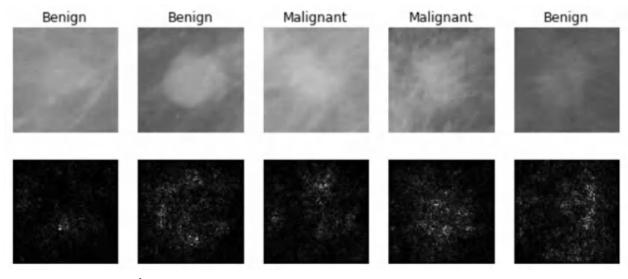
This image is CCO 1.0 public domain

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<u>This image</u> by <u>ionsson</u> is licensed under <u>CC-BY 2.0</u>

Image Classification: Very Useful!

Medical Imaging



Levy et al, 2016 Figure reproduced with permission

Galaxy Classification



Dieleman et al, 2014

From left to right: <u>public domain by NASA</u>, usage <u>permitted</u> by ESA/Hubble, <u>public domain by NASA</u>, and <u>public domain</u>.

Whale recognition

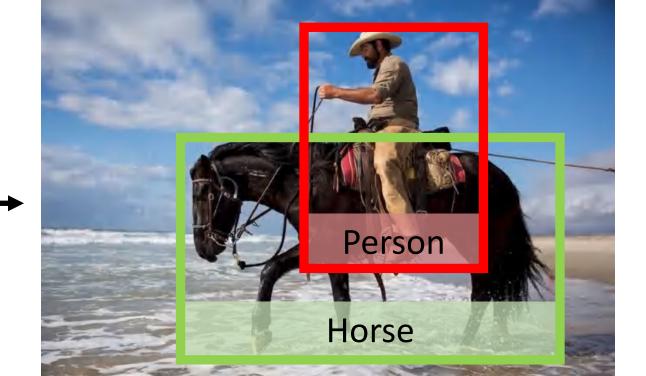


Kaggle Challenge

This image by Christin Khan is in the public domain and originally came from the U.S. NOAA

Example: Object Detection





<u>This image</u> is free to use under the <u>Pexels license</u>

Example: Object Detection



Background

Horse

Person

Car

Truck

This image is free to use under the Pexels license

Example: Object Detection



Background

Horse

Person

Car

Truck

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Example: Image Captioning



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Example: Image Captioning



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Example: Image Captioning



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Example: Image Captioning

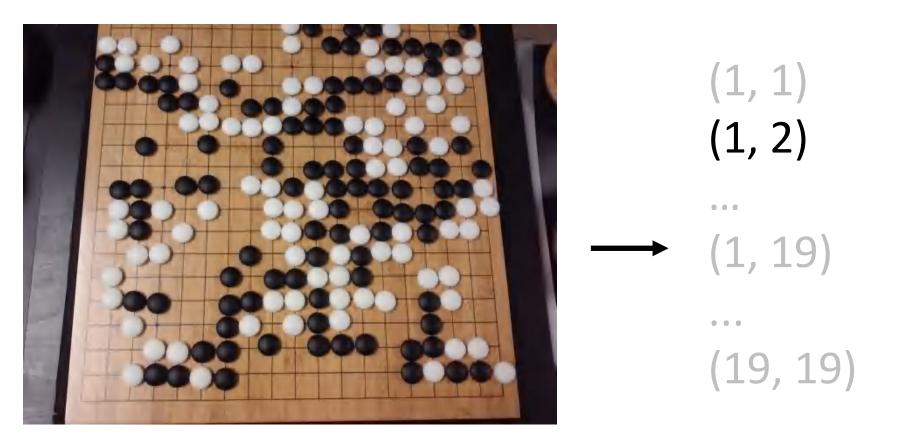


This image is free to use under the Pexels license

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Example: Playing Go



Where to play next?

This image is CCO public domain

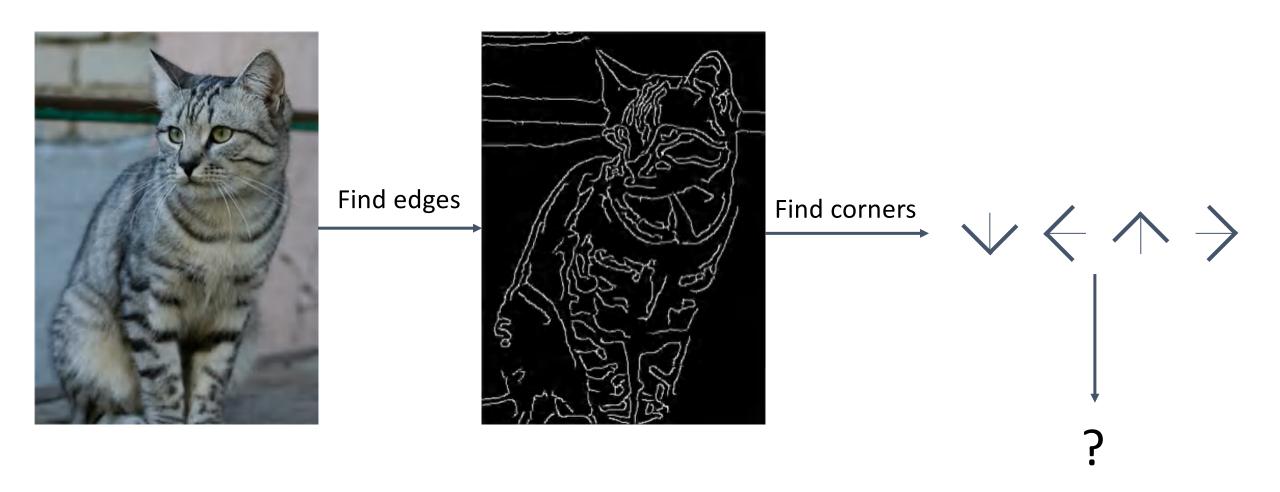
An Image Classifier

```
def classify_image(image):
    # Some magic here?
    return class_label
```

Unlike e.g. sorting a list of numbers,

no obvious way to hard-code the algorithm for recognizing a cat, or other classes.

You could try ...



John Canny, "A Computational Approach to Edge Detection", IEEE TPAMI 1986

Machine Learning: Data-Driven Approach

- 1. Collect a dataset of images and labels
- 2. Use Machine Learning to train a classifier
- 3. Evaluate the classifier on new images

def train(images, labels): # Machine learning! return model def predict(model, test_images): # Use model to predict labels return test_labels

Example training set

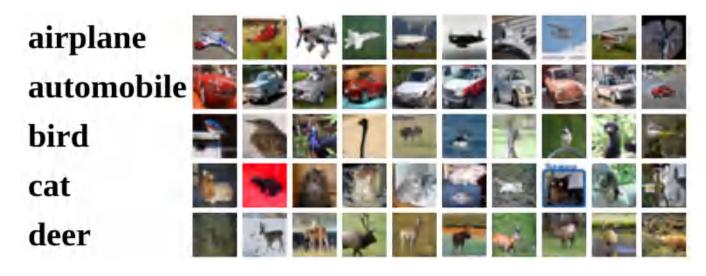
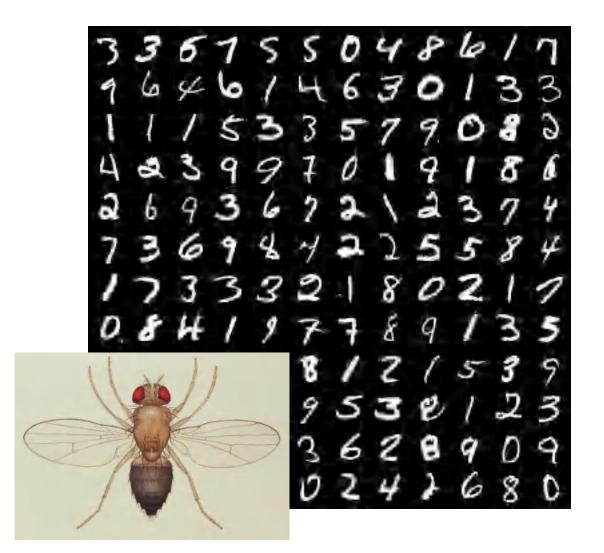


Image Classification Datasets: MNIST



10 classes: Digits 0 to 928x28 grayscale images50k training images10k test images

Image Classification Datasets: MNIST

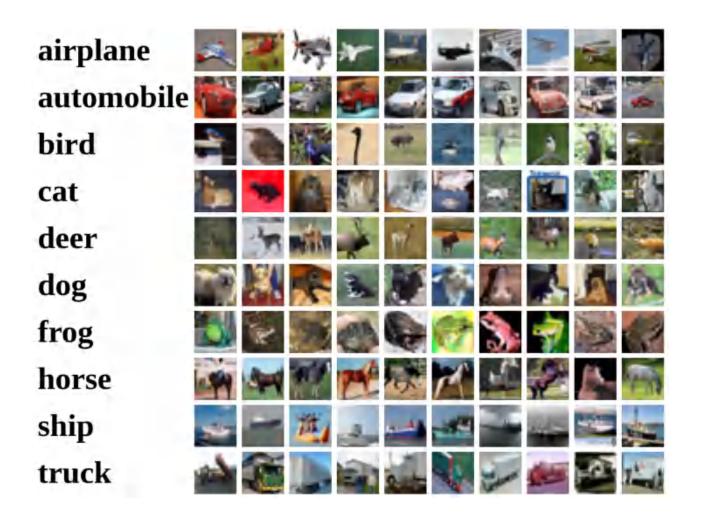


10 classes: Digits 0 to 928x28 grayscale images50k training images10k test images

"Drosophila of computer vision"

Results from MNIST often do not hold on more complex datasets!

Image Classification Datasets: CIFAR10



10 classes50k training images (5k per class)10k testing images (1k per class)32x32 RGB images

We will use this dataset for homework assignments

Alex Krizhevsky, "Learning Multiple Layers of Features from Tiny Images", Technical Report, 2009.

Image Classification Datasets: CIFAR100



100 classes50k training images (500 per class)10k testing images (100 per class)32x32 RGB images

20 superclasses with 5 classes each:

Aquatic mammals: beaver, dolphin, otter, seal, whale

Trees: Maple, oak, palm, pine, willow

Alex Krizhevsky, "Learning Multiple Layers of Features from Tiny Images", Technical Report, 2009.

Image Classification Datasets: ImageNet

flamingo cock ruffed grouse quail partridge Persian cat Siamese cat tabby Egyptian cat dalmatian keeshond miniature schnauzer standard schnauzer giant schnauzer

1000 classes

~1.3M training images (~1.3K per class) **50K** validation images (50 per class) **100K** test images (100 per class)

Performance metric: **Top 5 accuracy** Algorithm predicts 5 labels for each image; one of them needs to be right

Deng et al, "ImageNet: A Large-Scale Hierarchical Image Database", CVPR 2009 Russakovsky et al, "ImageNet Large Scale Visual Recognition Challenge", IJCV 2015

Image Classification Datasets: ImageNet



Deng et al, "ImageNet: A Large-Scale Hierarchical Image Database", CVPR 2009 Russakovsky et al, "ImageNet Large Scale Visual Recognition Challenge", IJCV 2015 **1000** classes

~1.3M training images (~1.3K per class)50K validation images (50 per class)100K test images (100 per class)test labels are secret!

Images have variable size, but often resized to **256x256** for training

There is also a 22k category version of ImageNet, but less commonly used

Image Classification Datasets: MIT Places



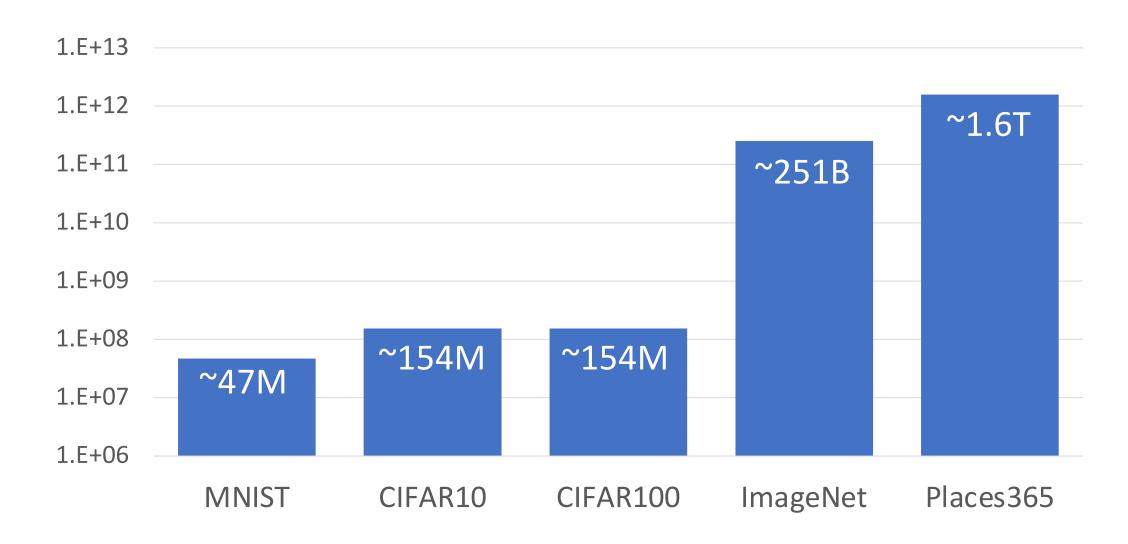
365 classes of different scene types

~8M training images 18.25K val images (50 per class) 328.5K test images (900 per class)

Images have variable size, often resize to **256x256** for training

Zhou et al, "Places: A 10 million Image Database for Scene Recognition", TPAMI 2017

Classification Datasets: Number of Training Pixels



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Image Classification Datasets: Omniglot



1623 categories: characters from 50 different alphabets

20 images per category

Meant to test few shot learning

Lake et al, "Human-level concept learning through probabilistic program induction", Science, 2015

First classifier: Nearest Neighbor

```
def train(images, labels):
                                              Memorize all data
  # Machine learning!
                                              and labels
  return model
                                             Predict the label of
def predict(model, test_images):
  # Use model to predict labels
                                             the most similar
  return test_labels
                                             training image
```

Distance Metric to compare images

L1 distance:

$$d_1(I_1,I_2) = \sum_p |I_1^p - I_2^p|$$

	•
toot	image
	IIIIaue
LOOL	IIIIIAAO

56	32	10	18
90	23	128	133
24	26	178	200
2	0	255	220

training image

10	20	24	17
8	10	89	100
12	16	178	170
4	32	233	112

pixel-wise absolute value differences

=	46	12	14	1	
	82	13	39	33	add
	12	10	0	30	→ 456
	2	32	22	108	

```
import numpy as np
class NearestNeighbor:
 def init (self):
   pass
 def train(self, X, y):
    """ X is N x D where each row is an example. Y is 1-dimension of size N """
   # the nearest neighbor classifier simply remembers all the training data
    self.Xtr = X
   self.ytr = y
 def predict(self, X):
    """ X is N x D where each row is an example we wish to predict label for """
    num test = X.shape[0]
    # lets make sure that the output type matches the input type
    Ypred = np.zeros(num test, dtype = self.ytr.dtype)
    # loop over all test rows
    for i in xrange(num test):
      # find the nearest training image to the i'th test image
      # using the L1 distance (sum of absolute value differences)
      distances = np.sum(np.abs(self.Xtr - X[i,:]), axis = 1)
      min index = np.argmin(distances) # get the index with smallest distance
      Ypred[i] = self.ytr[min index] # predict the label of the nearest example
    return Ypred
```

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```
import numpy as np
class NearestNeighbor:
 def init (self):
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 def train(self, X, y):
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    return Ypred
```

Memorize training data

```
import numpy as np
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 def init (self):
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 def train(self, X, y):
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      min index = np.argmin(distances) # get the index with smallest distance
      Ypred[i] = self.ytr[min index] # predict the label of the nearest example
```

return Ypred

Nearest Neighbor Classifier

For each test image:
Find nearest training image
Return label of nearest image

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```
import numpy as np
class NearestNeighbor:
 def init (self):
   pass
 def train(self, X, y):
    """ X is N x D where each row is an example. Y is 1-dimension of size N """
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```

Q: With N examples, how fast is training?

```
import numpy as np
class NearestNeighbor:
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      Ypred[i] = self.ytr[min index] # predict the label of the nearest example
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```

Q: With N examples, how fast is training?

A: O(1)

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```
import numpy as np
class NearestNeighbor:
 def init (self):
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```

Q: With N examples, how fast is training?A: O(1)

Q: With N examples, how fast is testing?

```
import numpy as np
class NearestNeighbor:
 def init (self):
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    return Ypred
```

Q: With N examples, how fast is training?

A: O(1)

Q: With N examples, how fast is testing?

A: O(N)

```
import numpy as np
class NearestNeighbor:
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    return Ypred
```

Q: With N examples, how fast is training?

A: O(1)

Q: With N examples, how fast is testing?

A: O(N)

This is **bad**: We can afford slow training, but we need fast testing!

```
import numpy as np
class NearestNeighbor:
 def init (self):
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 def train(self, X, y):
    """ X is N x D where each row is an example. Y is 1-dimension of size N """
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      min index = np.argmin(distances) # get the index with smallest distance
      Ypred[i] = self.ytr[min index] # predict the label of the nearest example
    return Ypred
```

There are many methods for fast / approximate nearest neighbors; e.g. see

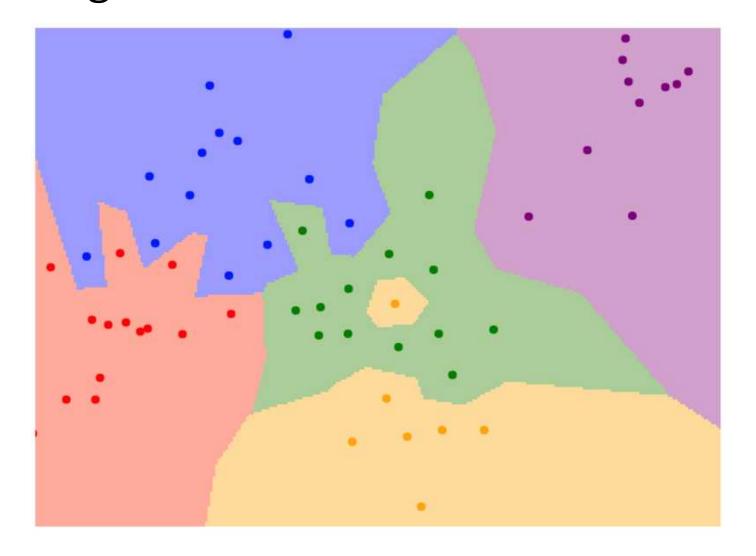
https://github.com/facebookresearch/faiss

What does this look like?



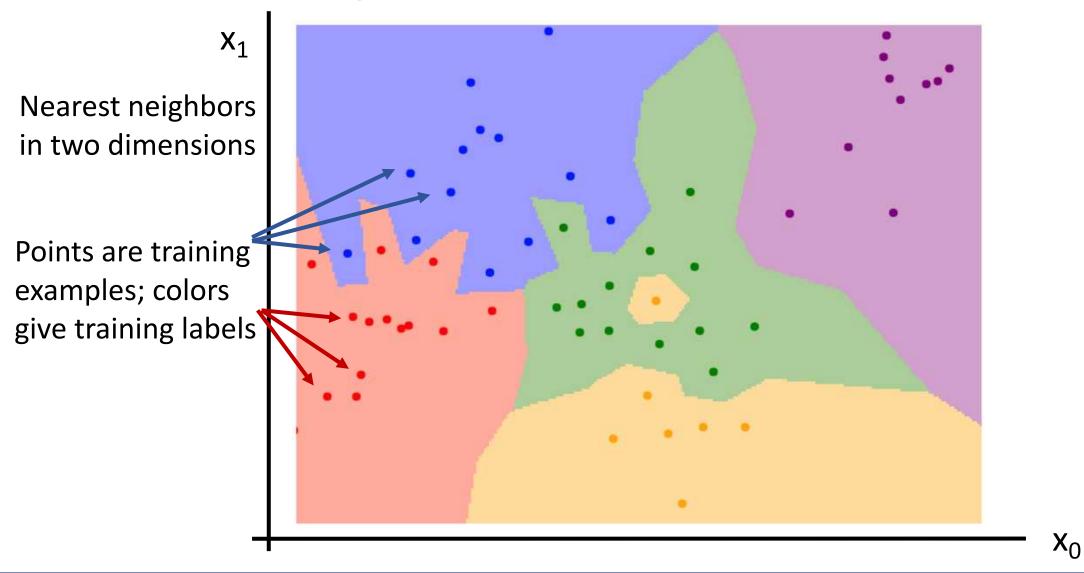
What does this look like?



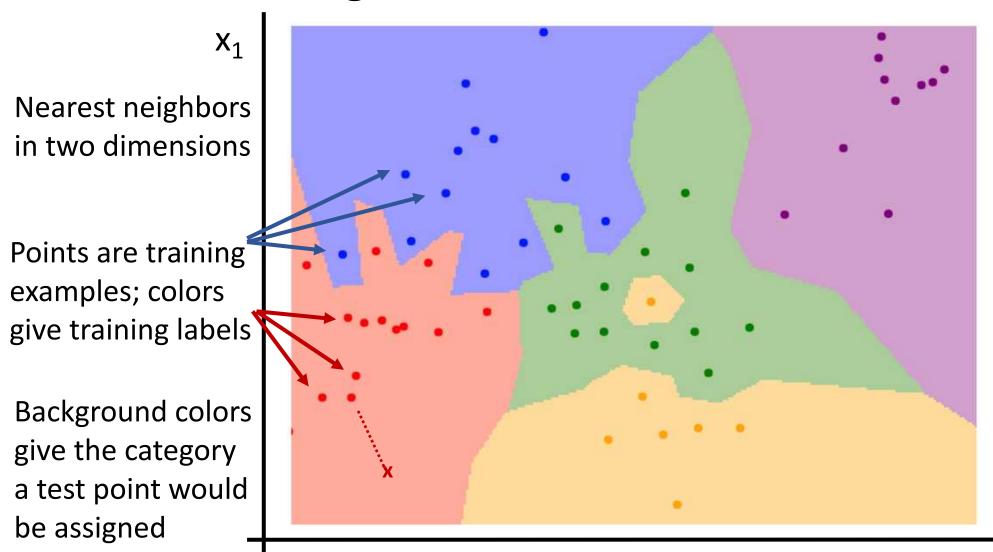


 \mathbf{X}_1 Nearest neighbors in two dimensions X_0

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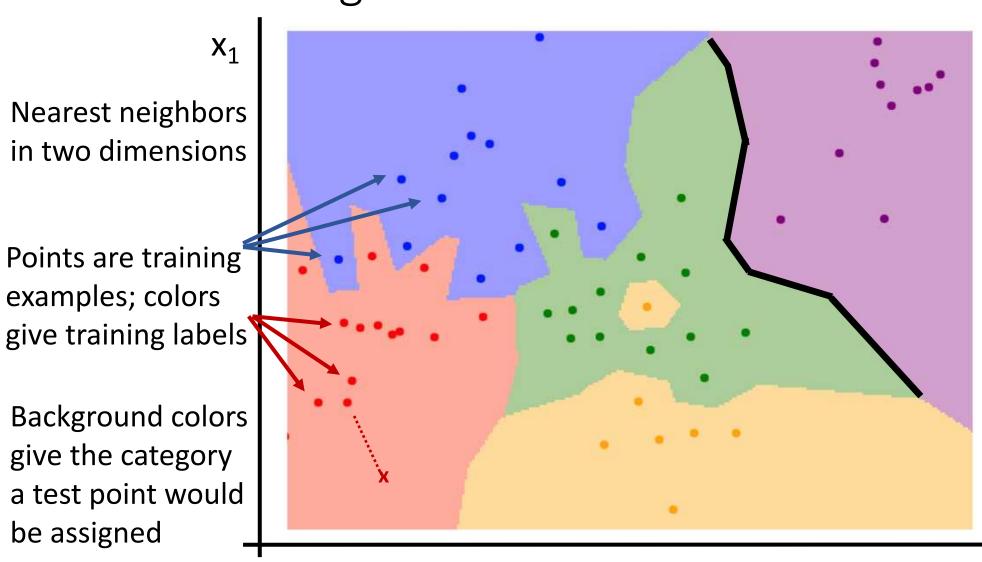


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 X_0



Decision boundary
is the boundary
between two
classification regions

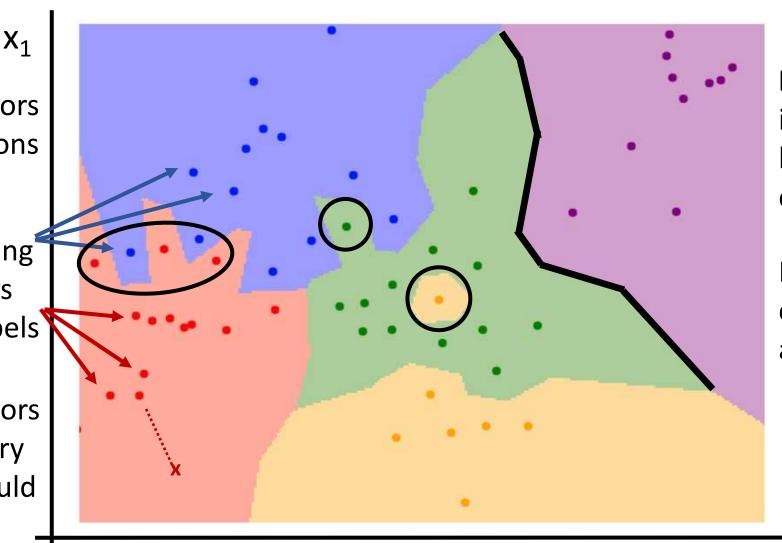
 X_0

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Nearest neighbors in two dimensions

Points are training examples; colors give training labels

Background colors give the category a test point would be assigned



Decision boundary

is the boundary between two classification regions

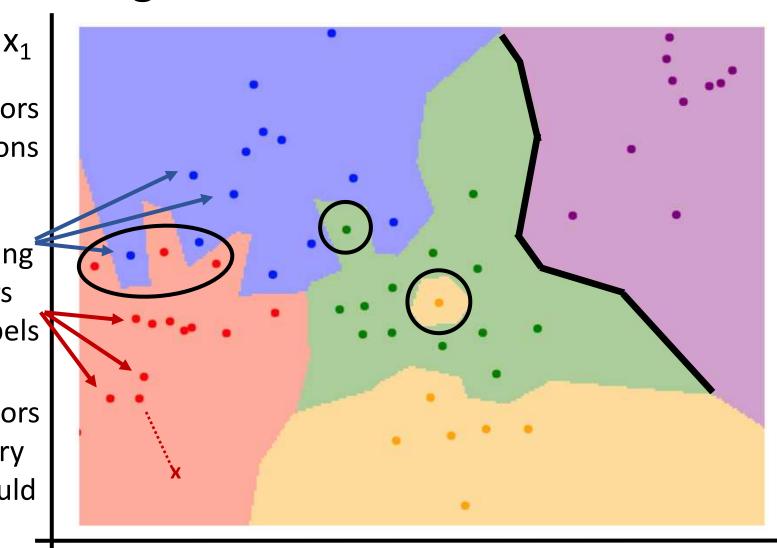
Decision boundaries can be noisy; affected by outliers

 X_0

Nearest neighbors in two dimensions

Points are training examples; colors give training labels

Background colors give the category a test point would be assigned



Decision boundary

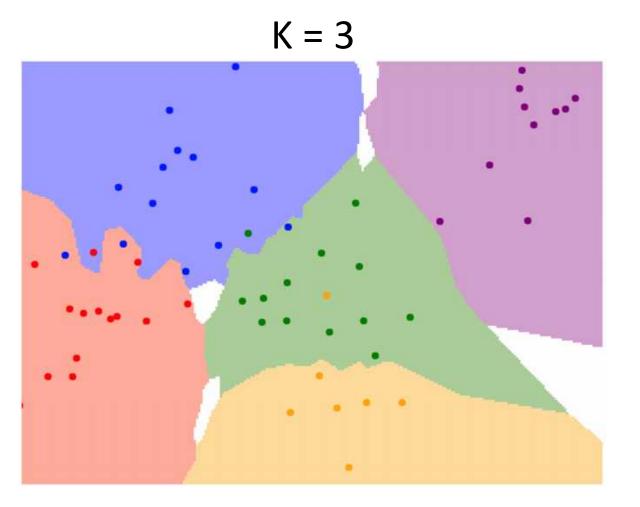
is the boundary between two classification regions

Decision boundaries can be noisy; affected by outliers

How to smooth out decision boundaries? Use more neighbors!

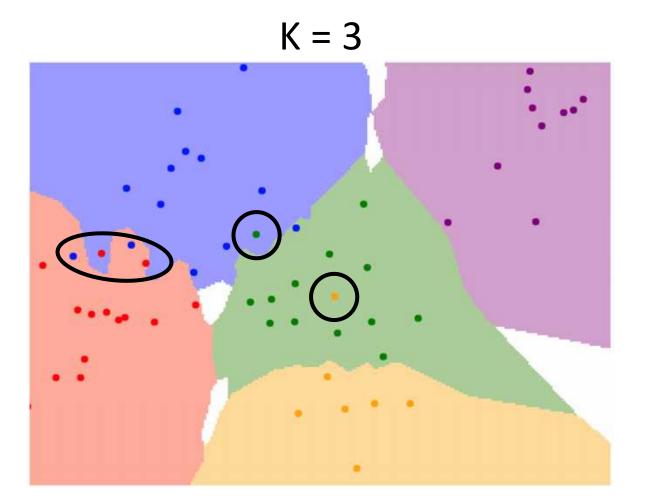
 $\mathbf{X}_{\mathbf{0}}$

Instead of copying label from nearest neighbor, take **majority vote** from K closest points

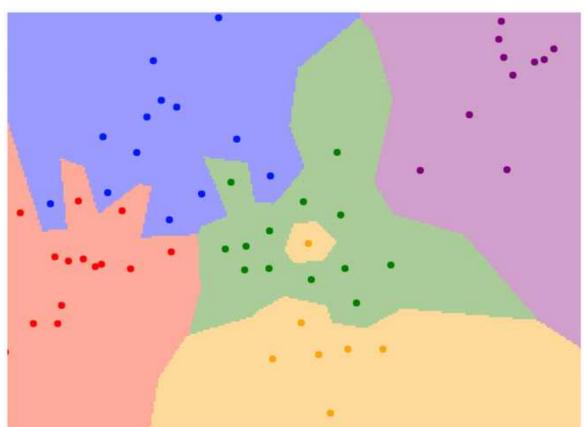


Using more neighbors helps smooth out rough decision boundaries

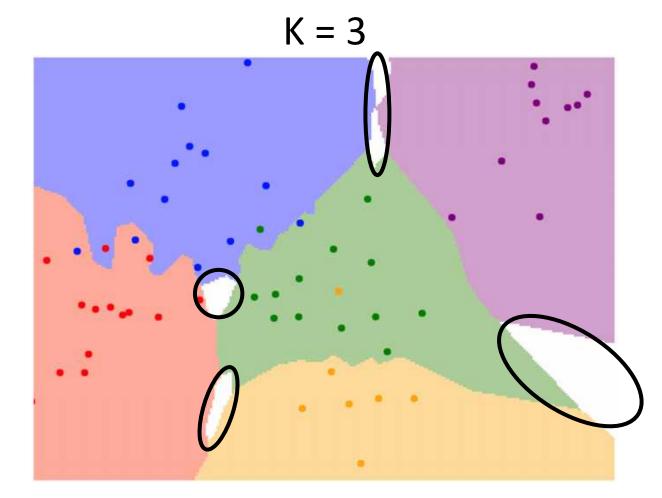
Using more neighbors helps reduce the effect of outliers



K = 1

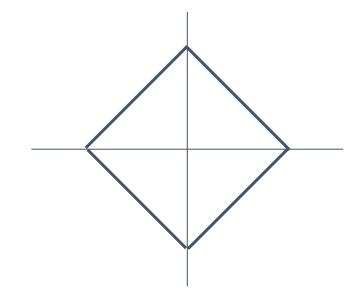


When K > 1 there can be ties between classes.
Need to break somehow!



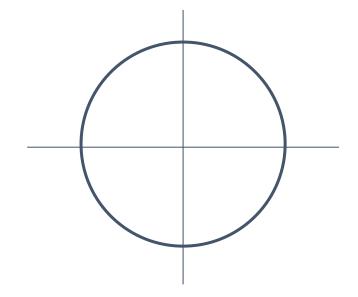
L1 (Manhattan) distance

$$d_1(I_1, I_2) = \sum_p |I_1^p - I_2^p|$$



L2 (Euclidean) distance

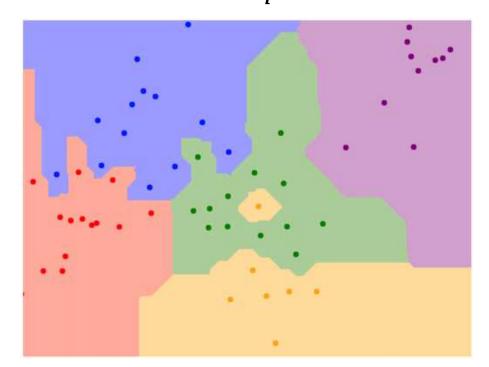
$$d_1(I_1, I_2) = \left(\sum_p (I_1^p - I_2^p)^2\right)^{\frac{1}{2}}$$



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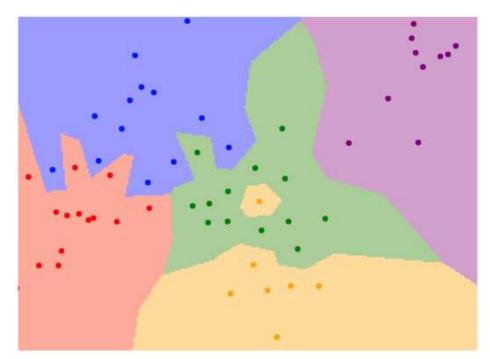
L1 (Manhattan) distance

$$d_1(I_1, I_2) = \sum_{p} |I_1^p - I_2^p|$$



L2 (Euclidean) distance

$$d_1(I_1, I_2) = \left(\sum_{p} (I_1^p - I_2^p)^2\right)^{\frac{1}{2}}$$

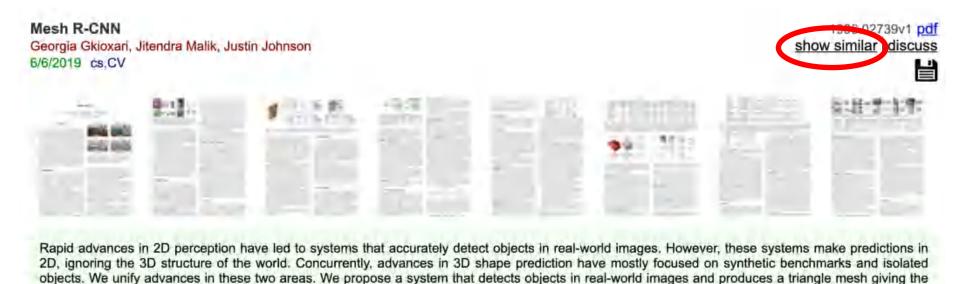


K = 1

With the right choice of distance metric, we can apply K-Nearest Neighbor to any type of data!

With the right choice of distance metric, we can apply K-Nearest Neighbor to any type of data!

Example:
Compare
research
papers using
tf-idf similarity



http://www.arxiv-sanity.com/search?q=mesh+r-cnn

full 3D shape of each detected object. Our system, called Mesh R-CNN, augments Mask R-CNN with a mesh prediction branch that outputs meshes with varying topological structure by first predicting coarse voxel representations which are converted to meshes and refined with a graph convolution network operating over the mesh's vertices and edges. We validate our mesh prediction branch on ShapeNet, where we outperform prior work on single-image

shape prediction. We then deploy our full Mesh R-CNN system on Pix3D, where we jointly detect objects and predict their 3D shapes.





Mesh models are a promising approach for encoding the structure of 3D objects. Current mesh reconstruction systems predict uniformly distributed vertex locations of a predetermined graph through a series of graph convolutions, leading to compromises with respect to performance or resolution. In this paper, we argue that the graph representation of geometric objects allows for additional structure, which should be leveraged for enhanced reconstruction. Thus, we propose a system which properly benefits from the advantages of the geometric structure of graph encoded objects by introducing (1) a graph convolutional update preserving vertex information, (2) an adaptive splitting heuristic allowing detail to emerge; and (3) a training objective operating both on the local surfaces defined by vertices as well as the global structure defined by the mesh. Our proposed method is evaluated on the task of 3D object reconstruction from images with the ShapeNet dataset, where we demonstrate state of the art performance, both visually and numerically, while having far smaller space requirements by generaling adaptive meshes.

http://www.arxiv-sanity.com/1906.02739v1

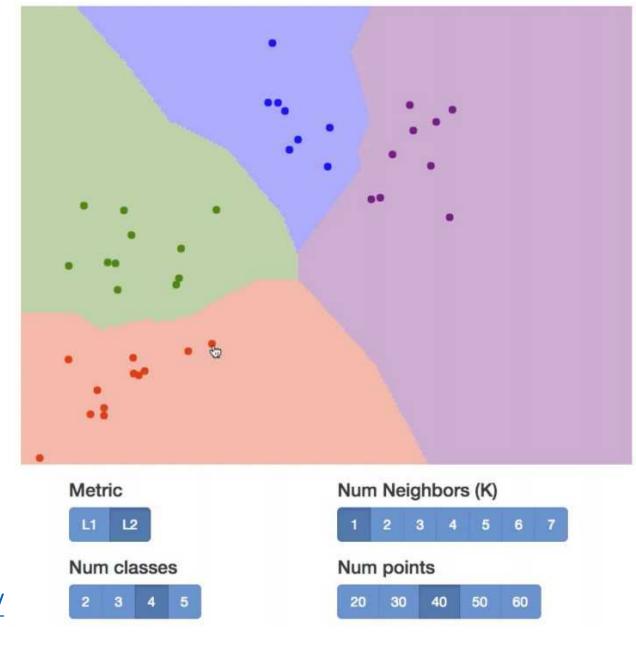
K-Nearest Neighbors: Web Demo

Interactively move points around and see decision boundaries change

Play with L1 vs L2 metrics

Play with changing number of training points, value of K

http://vision.stanford.edu/teaching/cs231n-demos/knn/



Hyperparameters

What is the best value of **K** to use? What is the best **distance metric** to use?

These are examples of **hyperparameters**: choices about our learning algorithm that we don't learn from the training data; instead we set them at the start of the learning process

Hyperparameters

What is the best value of **K** to use? What is the best **distance metric** to use?

These are examples of **hyperparameters**: choices about our learning algorithm that we don't learn from the training data; instead we set them at the start of the learning process

Very problem-dependent. In general need to try them all and see what works best for our data / task.

Setting Hyperparameters

Idea #1: Choose hyperparameters that work best on the data

Your Dataset

Idea #1: Choose hyperparameters that work best on the data

BAD: K = 1 always works perfectly on training data

Your Dataset

Idea #1: Choose hyperparameters that work best on the data

BAD: K = 1 always works perfectly on training data

Your Dataset

Idea #2: Split data into train and test, choose hyperparameters that work best on test data

train test

Idea #1: Choose hyperparameters that work best on the data

BAD: K = 1 always works perfectly on training data

Your Dataset

Idea #2: Split data into train and test, choose hyperparameters that work best on test data

BAD: No idea how algorithm will perform on new data

train

test

Idea #1: Choose hyperparameters that work best on the data

BAD: K = 1 always works perfectly on training data

Your Dataset

Idea #2: Split data into train and test, choose hyperparameters that work best on test data

BAD: No idea how algorithm will perform on new data

train

test

Idea #3: Split data into train, val, and test; choose hyperparameters on val and evaluate on test

Better!

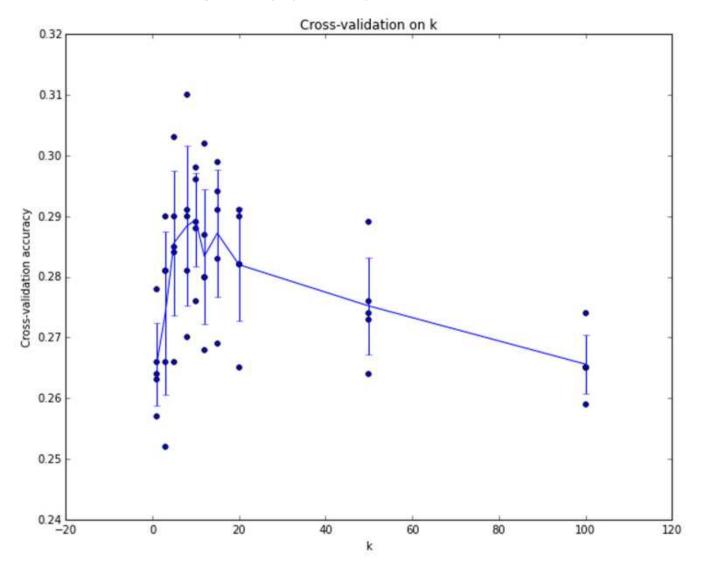
train validation test

Your Dataset

Idea #4: **Cross-Validation**: Split data into **folds**, try each fold as validation and average the results

fold 1	fold 2	fold 3	fold 4	fold 5	test
fold 1	fold 2	fold 3	fold 4	fold 5	test
fold 1	fold 2	fold 3	fold 4	fold 5	test

Useful for small datasets, but (unfortunately) not used too frequently in deep learning



Example of 5-fold cross-validation for the value of **k**.

Each point: single outcome.

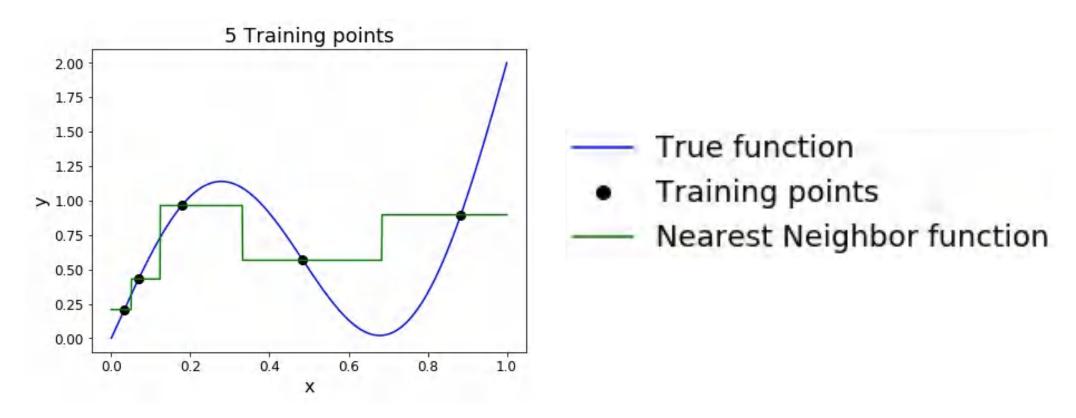
The line goes through the mean, bars indicated standard deviation

(Seems that $k \sim 7$ works best for this data)

As the number of training samples goes to infinity, nearest neighbor can represent any^(*) function!

^(*) Subject to many technical conditions. Only continuous functions on a compact domain; need to make assumptions about spacing of training points; etc.

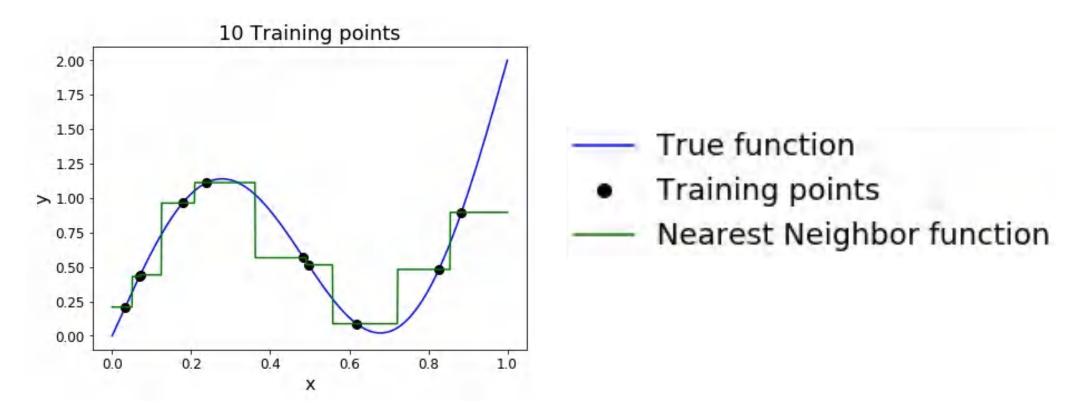
As the number of training samples goes to infinity, nearest neighbor can represent any^(*) function!



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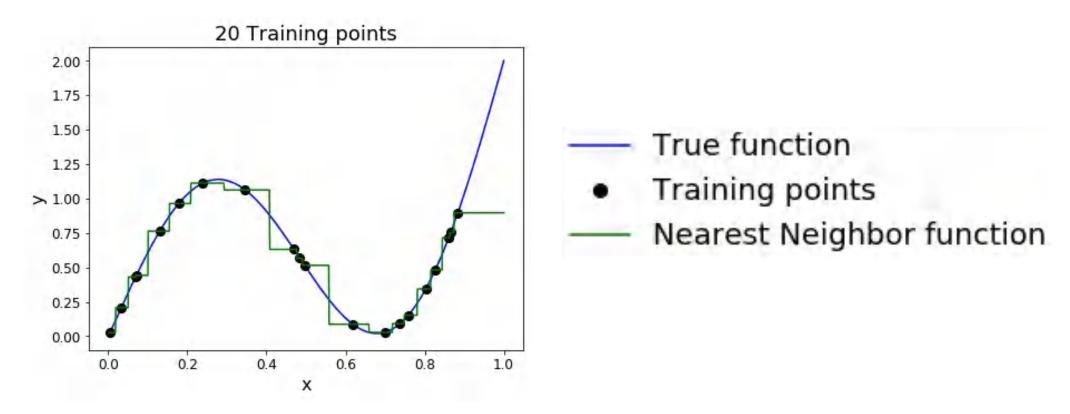
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As the number of training samples goes to infinity, nearest neighbor can represent any^(*) function!



^(*) Subject to many technical conditions. Only continuous functions on a compact domain; need to make assumptions about spacing of training points; etc.

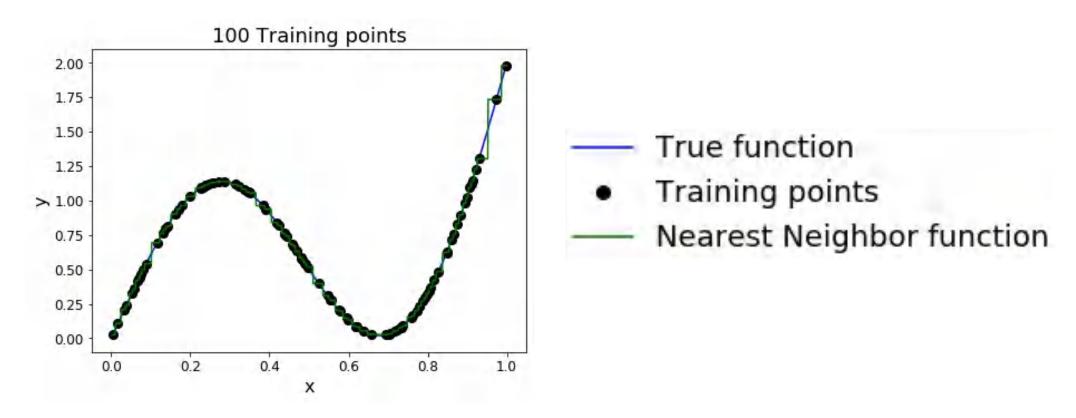
As the number of training samples goes to infinity, nearest neighbor can represent any^(*) function!



^(*) Subject to many technical conditions. Only continuous functions on a compact domain; need to make assumptions about spacing of training points; etc.

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As the number of training samples goes to infinity, nearest neighbor can represent any^(*) function!



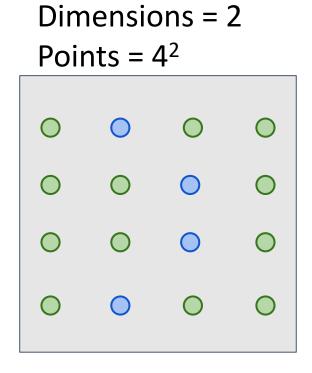
^(*) Subject to many technical conditions. Only continuous functions on a compact domain; need to make assumptions about spacing of training points; etc.

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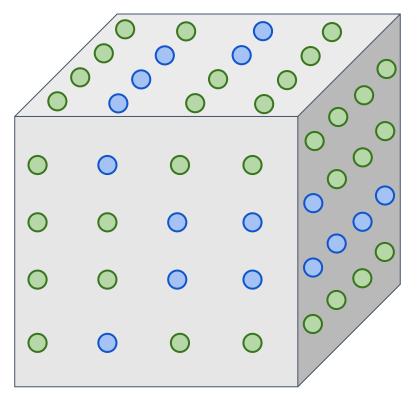
Problem: Curse of Dimensionality

Curse of dimensionality: For uniform coverage of space, number of training points needed grows exponentially with dimension

Dimensions = 1 Points = 4



Dimensions = 3Points = 4^3



Problem: Curse of Dimensionality

Curse of dimensionality: For uniform coverage of space, number of training points needed grows exponentially with dimension

Number of possible 32x32 binary images:

 $2^{32\times32} \approx 10^{308}$

Problem: Curse of Dimensionality

Curse of dimensionality: For uniform coverage of space, number of training points needed grows exponentially with dimension

Number of possible 32x32 binary images:

Number of elementary particles in the visible universe: (source)

$$2^{32\times32} \approx 10^{308}$$

$$\approx 10^{97}$$

K-Nearest Neighbor on raw pixels is seldom used

- Very slow at test time
- Distance metrics on pixels are not informative

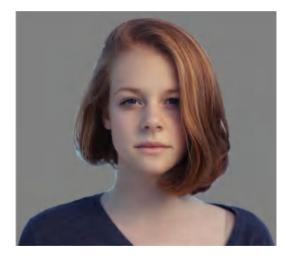
Original



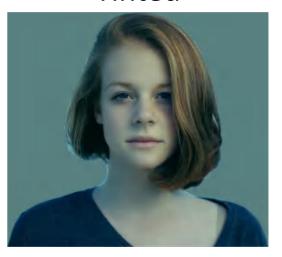
Boxed



Shifted



Tinted



(all 3 images have same L2 distance to the one on the left)

Nearest Neighbor with ConvNet features works well!



Devlin et al, "Exploring Nearest Neighbor Approaches for Image Captioning", 2015

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Nearest Neighbor with ConvNet features works well!

Example: Image Captioning with Nearest Neighbor



A bedroom with a bed and a couch.



A cat sitting in a bathroom sink.



A train is stopped at a train station.



A wooden bench in front of a building.

Devlin et al, "Exploring Nearest Neighbor Approaches for Image Captioning", 2015

Summary

In Image classification we start with a training set of images and labels, and must predict labels on the test set

Image classification is challenging due to the semantic gap: we need invariance to occlusion, deformation, lighting, intraclass variation, etc

Image classification is a **building block** for other vision tasks

The **K-Nearest Neighbors** classifier predicts labels based on nearest training examples

Distance metric and K are hyperparameters

Choose hyperparameters using the **validation set**; only run on the test set once at the very end!

Next time: Linear Classifiers

