Gauss Jordan

In[80]:=

$$A = \{\{1, 0, 1, 2\}, \{0, -2, 3, 3\}, \{2, 2, -1, 1\}\}$$

Out[80]=

$$\{\{1, 0, 1, 2\}, \{0, -2, 3, 3\}, \{2, 2, -1, 1\}\}$$

In[81]:=

MatrixForm[A]

Out[81]//MatrixForm=

$$\begin{pmatrix} 1 & 0 & 1 & 2 \\ 0 & -2 & 3 & 3 \\ 2 & 2 & -1 & 1 \end{pmatrix}$$

In[82]:=

RowReduce[A]

Out[82]=

$$\left\{ \{1, 0, 1, 2\}, \left\{0, 1, -\frac{3}{2}, -\frac{3}{2}\right\}, \{0, 0, 0, 0\} \right\}$$

In[83]:=

MatrixForm[RowReduce[A]]

Out[83]//MatrixForm=

$$\begin{pmatrix} 1 & 0 & 1 & 2 \\ 0 & 1 & -\frac{3}{2} & -\frac{3}{2} \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

In[84]:=

Solve
$$\left[\left\{x+z=2, y-\frac{3}{2}z=\frac{-3}{2}, z=0\right\}, \{x, y, z\}\right]$$

Out[84]=

$$\left\{\left\{x
ightarrow 2, \ y
ightarrow - rac{3}{2}, \ z
ightarrow 0
ight\}
ight\}$$

In[85]:=

Solve[RowReduce[A]]

••• Solve: $\{1, 0, 1, 2\}$ && $\{0, 1, -\frac{3}{2}, -\frac{3}{2}\}$ && $\{0, 0, 0, 0, 0\}$ is not a quantified system of equations and inequalities.

Out[85]=

Solve
$$\left[\left\{\{1, 0, 1, 2\}, \left\{0, 1, -\frac{3}{2}, -\frac{3}{2}\right\}, \{0, 0, 0, 0\}\right\}\right]$$

In[86]:=

Solve
$$\left[\left\{\{1, 0, 1, 2\}, \left\{0, 1, -\frac{3}{2}, -\frac{3}{2}\right\}, \{0, 0, 0, 0\}\right\}\right]$$

••• Solve: $\{1, 0, 1, 2\} \&\& \{0, 1, -\frac{3}{2}, -\frac{3}{2}\} \&\& \{0, 0, 0, 0, 0\}$ is not a quantified system of equations and inequalities.

Out[86]=

Solve
$$\left[\left\{\{1, 0, 1, 2\}, \left\{0, 1, -\frac{3}{2}, -\frac{3}{2}\right\}, \{0, 0, 0, 0\}\right\}\right]$$

Question 6x-y+z==13, x+y+z==9,10x+y-z==19

```
A = \{\{6, -1, 1, 13\}, \{1, 1, 1, 9\}, \{10, 1, -1, 19\}\}
 In[87]:=
               \{\,\{6\,,\,\, ^-1,\,\, 1,\,\, 13\,\}\,,\,\,\{1,\,\, 1,\,\, 1,\,\, 9\,\}\,,\,\,\{10,\,\, 1,\,\, ^-1,\,\, 19\,\}\,\}
Out[87]=
```

In[88]:= MatrixForm[A]

Out[88]//MatrixForms

-1 1 13 1 1 1 9 1 10 -1 19

In[89]:= MatrixForm[RowReduce[A]]

Out[89]//MatrixForm=

1 0 0 2 0 1 0 3 0 0 1 4

Solve[RowReduce[A]] In[90]:=

... Solve: {1, 0, 0, 2} && {0, 1, 0, 3} && {0, 0, 1, 4} is not a quantified system of equations and inequalities.

Solve[{{1, 0, 0, 2}, {0, 1, 0, 3}, {0, 0, 1, 4}}] Out[90]=

Solve [$\{6x - y + z = 13, x + y + z = 9, 10x + y - z = 19\}, \{x, y, z\}$] In[91]:=

Out[91]= $\{\,\{\,x\rightarrow 2\text{, }y\rightarrow 3\text{, }z\rightarrow 4\}\,\}\,$

 $\{ \{x \rightarrow 2, y \rightarrow 3, z \rightarrow 4\} \}$ In[92]:=

 $\{\,\{\,x\rightarrow 2\text{, }y\rightarrow 3\text{, }z\rightarrow 4\}\,\}\,$ Out[92]=

Ques-1. x+y+z=4, 2x-3y+z=2, -x+2y-z=-1

 $Q1 = \{\{1, 1, 1, 4\}, \{2, -3, 1, 2\}, \{-1, 2, -1, -1\}\}$ In[94]:= Out[94]= $\{\{1, 1, 1, 4\}, \{2, -3, 1, 2\}, \{-1, 2, -1, -1\}\}$

MatrixForm[Q1] In[95]:=

Out[95]//MatrixForm=

In[93]:=

2 -3 1 2 2 -1 -1

```
MatrixForm[RowReduce[Q1]]
In[96]:=
```

Out[96]//Matrix

1 0 0 2 0 1 0 1 0 0 1 1

Solve[$\{x + y + z == 4, 2x - 3y + z == 2, -x + 2y - z == -1\}, \{x, y, z\}$] In[97]:=

Out[97]= $\{\,\{\,x\rightarrow 2\text{, }y\rightarrow \text{1, }z\rightarrow \text{1}\}\,\}$

Ques-2. x+3y+z=10, x-2y-z=-6, 2x+y+2z=10

 $Q2 = \{\{1, 3, 1, 10\}, \{1, -2, -1, -6\}, \{2, 1, 2, 10\}\}$ In[98]:=

 $\{\{1, 3, 1, 10\}, \{1, -2, -1, -6\}, \{2, 1, 2, 10\}\}$ Out[98]=

MatrixForm[Q2] In[99]:=

Out[99]//Matrix

1 3 1 10 1 - 2 - 1 - 62 1 2 10

MatrixForm[RowReduce[Q2]] In[100]:=

Out[100]//MatrixForm=

1 0 0 1 0 1 0 2 0 0 1 3

Solve[$\{x + 3 y + z == 10, x - 2 y - z == -6, 2 x + y + 2 z == 10\}, \{x, y, z\}$] In[101]:= Out[101]= $\{\,\{\,x\rightarrow \textbf{1,}\ y\rightarrow \textbf{2,}\ z\rightarrow \textbf{3}\,\}\,\}$

Ques-3. x+y+2z=-1, x+3y-6z=7, 2x-y+2z=0

 $Q3 = \{\{1, 1, 2, -1\}, \{1, 3, -6, 7\}, \{2, -1, 2, 0\}\}$ In[102]:=

 $\{\{1, 1, 2, -1\}, \{1, 3, -6, 7\}, \{2, -1, 2, 0\}\}$ Out[102]=

MatrixForm[Q3] In[103]:=

Out[103]//MatrixForm=

2 -1 1 1 1 3 -6 7 2 -1 2

In[104]:=

MatrixForm[RowReduce[Q3]]

Out[104]//MatrixForm=

$$\left(\begin{array}{cccc}
1 & 0 & 0 & 1 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & -1
\end{array}\right)$$

In[105]:=

Solve [
$$\{x + y + 2z = -1, x + 3y - 6z = 7, 2x - y + 2z = 0\}, \{x, y, z\}$$
]

Out[105]=

$$\{\,\{\,x\,\rightarrow\,\textbf{1,}\,\,y\,\rightarrow\,\textbf{0,}\,\,z\,\rightarrow\,-\,\textbf{1}\,\}\,\}$$

Ques-4. 2x+3y+z=-1, 5x+y+z=9, 3x+2y+4z=11

In[106]:=

$$Q4 = \{\{2, 3, 1, -1\}, \{5, 1, 1, 9\}, \{3, 2, 4, 11\}\}$$

Out[106]=

$$\{\{2, 3, 1, -1\}, \{5, 1, 1, 9\}, \{3, 2, 4, 11\}\}$$

In[107]:=

MatrixForm[Q4]

Out[107]//MatrixForm=

$$\begin{pmatrix}
2 & 3 & 1 & -1 \\
5 & 1 & 1 & 9 \\
3 & 2 & 4 & 11
\end{pmatrix}$$

In[108]:=

MatrixForm[RowReduce[Q4]]

Out[108]//MatrixForm=

$$\begin{pmatrix} 1 & 0 & 0 & \frac{7}{4} \\ 0 & 1 & 0 & -\frac{19}{8} \\ 0 & 0 & 1 & \frac{21}{8} \end{pmatrix}$$

In[109]:=

Solve[
$$\{2x+3y+z=-1, 5x+y+z=9, 3x+2y+4z=11\}, \{x, y, z\}$$
]

Out[109]=

$$\left\{\left\{x\rightarrow\frac{7}{4}\text{, }y\rightarrow-\frac{19}{8}\text{, }z\rightarrow\frac{21}{8}\right\}\right\}$$