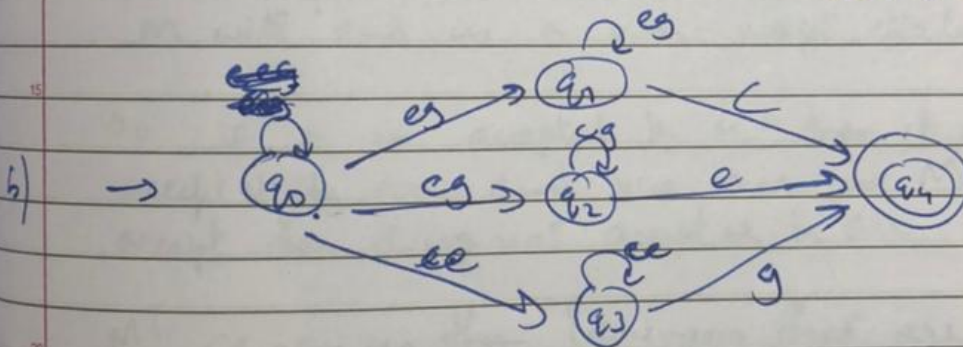


Consider string starting from q_0 and end with e

$T_{eg} = e c g e g e \rightarrow q_0$ goes to q_2 recursively



no last symbol before.

2 M is a DFA that recognizes the regular language B

Let M' be the new DFA that has swapped accept and non-accept states in M

Consider M' accepts a string

Run M' on x so it can enter the accept state

The machines M, M' have swapped accept, non-accept states so if we run M on x then M will end in a non-accept state.

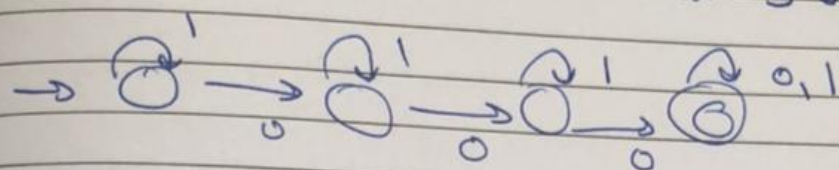
So if x is accepted by M' then it is not accepted by M and vice versa. So M' will accept the strings not accepted by M .

M' recognizes the languages that are complement of B .

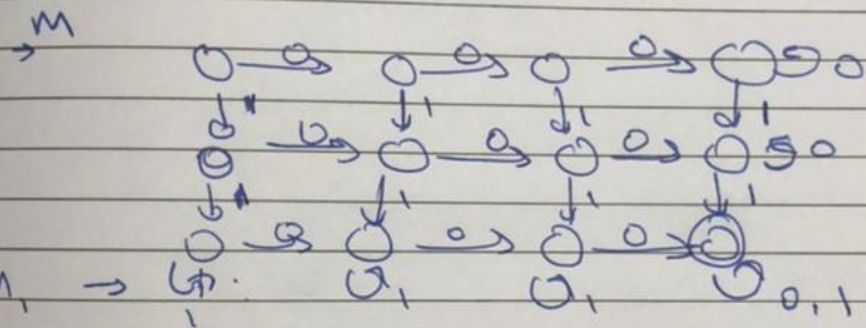
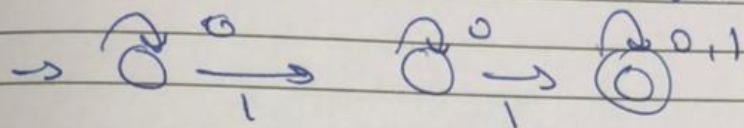
As M recognizes a regular language B , there is m' which recognizes complement of B which is also regular.

3

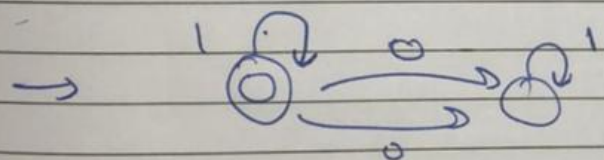
a) $M_1 \rightarrow L_1$ ($\{w \mid w \text{ at least 3 0's}\}$)



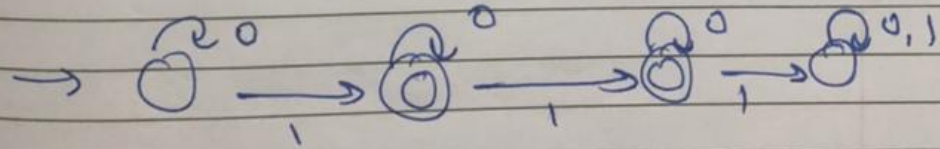
$M_2 \rightarrow L_2$ ($\{w \mid w \text{ at least 2 1's}\}$)



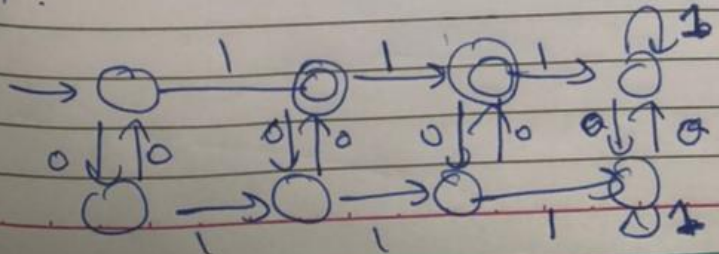
b) $M_1 \rightarrow L_1$



$M_2 \rightarrow L_2$

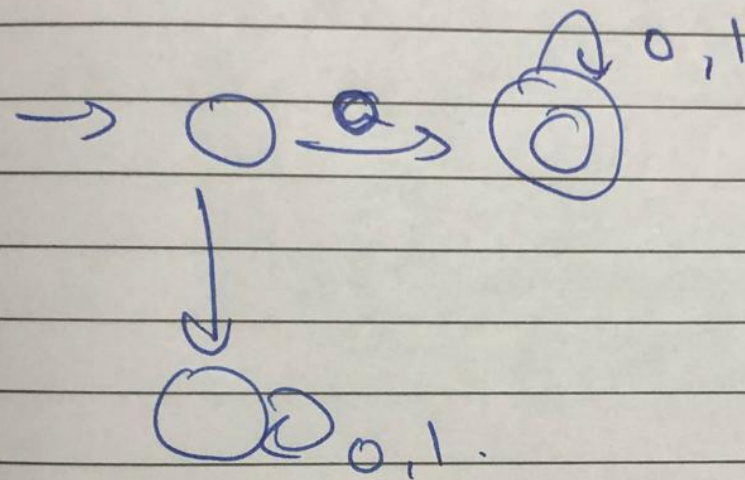


M



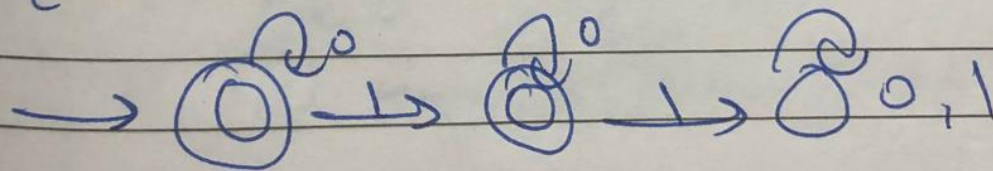
15
a)

$$M_1 \rightarrow L_1$$

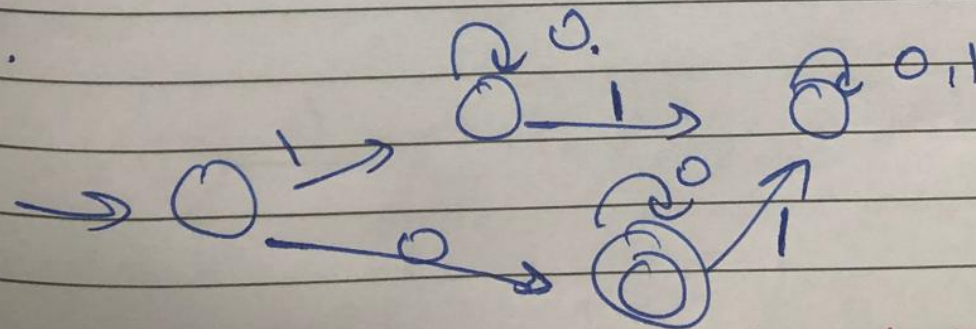


25

$$M_2 \rightarrow L_2$$



M.



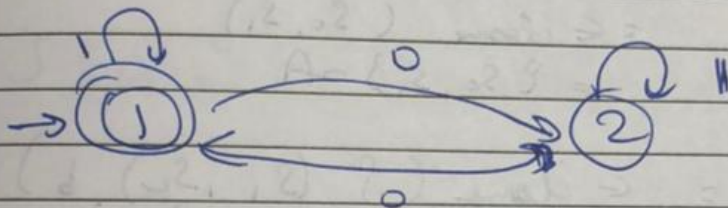
4)

a) Let M_1, M_2 be the NFA's recognized.

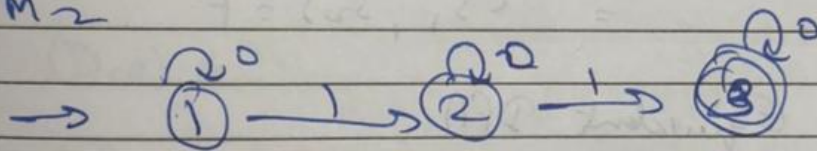
$L_1 = \{w \mid w \text{ contains even number of 0s}\}$

$L_2 = \{w \mid w \text{ contains exactly two 1s}\}$

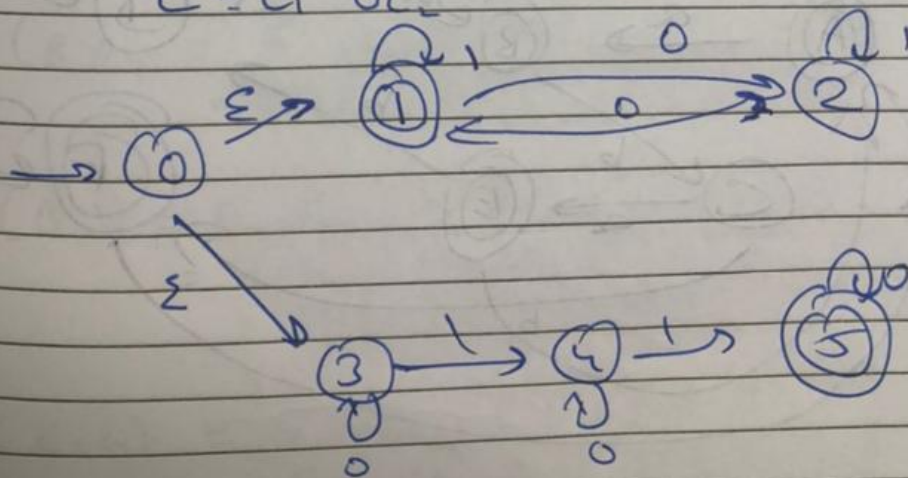
M_1

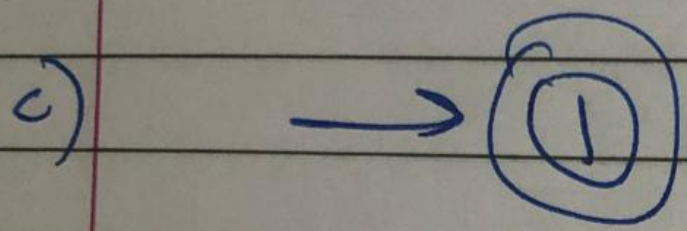
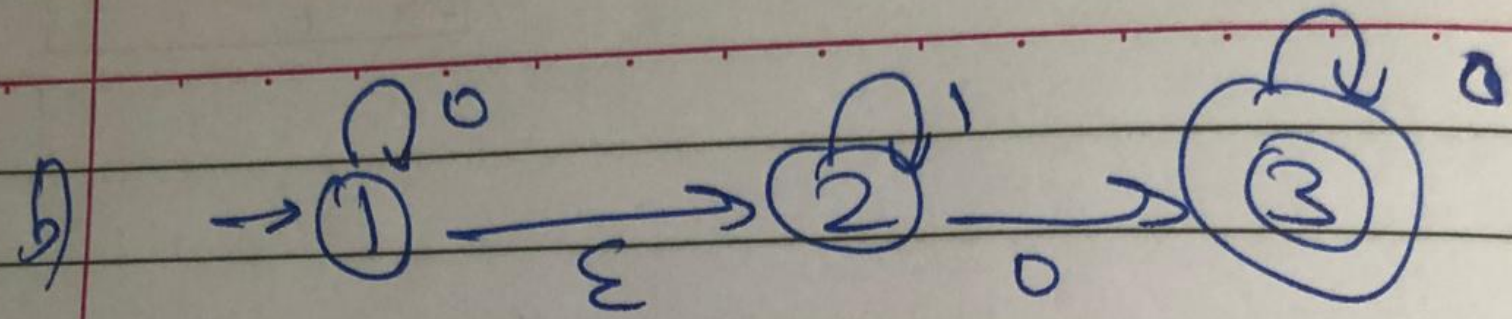


M_2



$L = L_1 \cup L_2$





§ NFA to DFA

$$\Sigma \text{ closure}(s_0) = \{s_0, s_1\} = A$$

$$\delta(A, a) = \Sigma \text{ closure}(\delta(s_0, s_1), a)$$

$$= \Sigma \text{ closure}(s_2, s_0)$$

$$= \{s_0, s_1, s_2\} = B$$

$$\delta(A, b) = \Sigma \text{ closure}(\delta(s_0, s_1), b)$$

$$= \Sigma \text{ closure}(\phi) = D \text{ (Dummy state)}$$

$$\delta(D, a) = D$$

$$\delta(D, b) = D$$

$$\delta(B, a) = \Sigma \text{ closure}(\delta(s_0, s_1, s_2), a)$$
$$= \Sigma \text{ closure}(s_0, s_1, s_2) = B$$

$$\delta(B, b) = \Sigma \text{ closure}(\delta(s_0, s_1, s_2), b)$$
$$= \Sigma \text{ closure}(s_2)$$
$$= \{s_2\} = C$$

$$\delta(C, a) = \Sigma \text{ closure}(\delta(s_2), a)$$
$$= \Sigma \text{ closure}(s_1) = \{s_1\} = E$$

$$\delta(C, b) = \Sigma \text{ closure}(\delta(s_2), b)$$
$$= \Sigma \text{ closure}(s_1, s_2)$$
$$= \{s_1, s_2\} = F$$

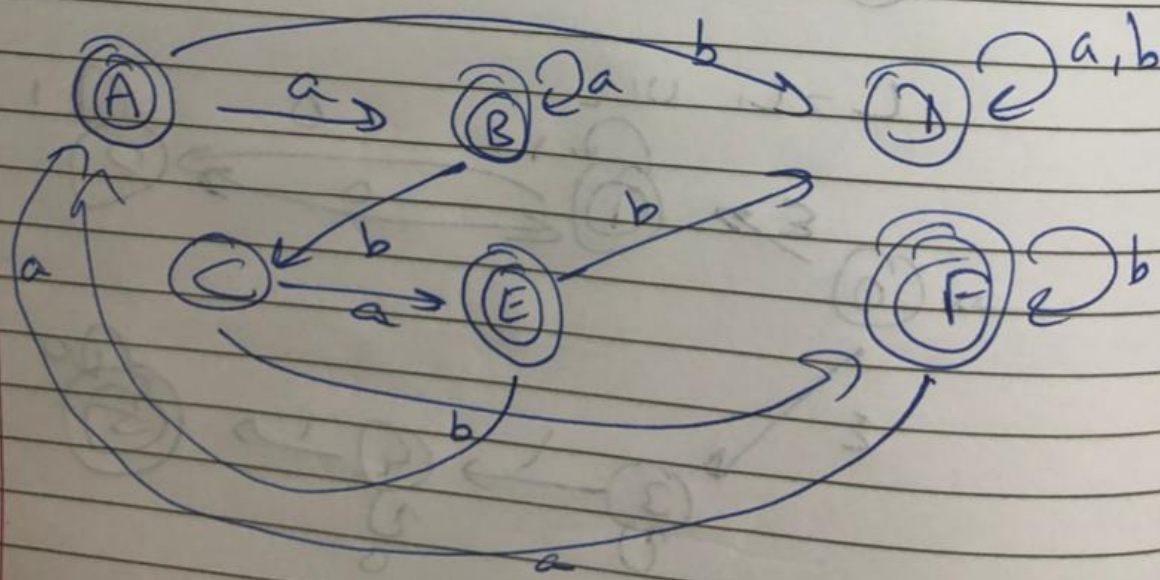
$$\begin{aligned} \delta(E, a) &= \epsilon\text{-closure}(\delta(s_1, a)) \\ &= \epsilon\text{-closure}(s_0) \\ &= \{s_0, s_1\} = A \end{aligned}$$

$$\begin{aligned} \delta(E, b) &= \epsilon\text{-closure}(\delta(s_1, b)) \\ &= \epsilon\text{-closure}(\phi) \\ &= \emptyset \end{aligned}$$

$$\begin{aligned} \delta(F, a) &= \epsilon\text{-closure}(\delta(s_1, s_2), a) \\ &= \epsilon\text{-closure}(s_0, s_1) \\ &= \{s_0, s_1\} = A \end{aligned}$$

$$\begin{aligned} \delta(F, b) &= \epsilon\text{-closure}(\delta(s_1, s_2), b) \\ &= \epsilon\text{-closure}(s_1, s_2) \\ &= \{s_1, s_2\} = F \end{aligned}$$

Equivalent DFA



6)

a) $\{w \mid w \text{ contains at least three 1s}\}$

$$= (0+1)^* 1 (0+1)^* 1 (0+1)^* 1 (0+1)^*$$

b) $\{w \mid w \text{ starts with 0 and has odd length, or starts with 1 and has even length}\}$

$$= 0 ((0+1)(0+1))^* + 1(0+1)((0+1)(0+1))^*$$

c) $\{w \mid \text{the length of } w \text{ is at most 5}\}$

$$= (\Sigma + 0+1) (\Sigma + 0+1) (\Sigma + 0+1) (\Sigma + 0+1) (\Sigma + 0+1)$$

d) $\{w \mid w \text{ is any string except } \epsilon \text{ and } 111\}$

$$(\Sigma + 1) + (0 + 01 + 110 + 1110 + 1111) (0+1)^*$$