

Assignment 4 Relation Algebra

Following are the all RA Expressions of SQL queries ~~is~~ submitted in assignment.

Q.1

$$(\pi_A(W_1 \bowtie_{W_1.A = W_2.A \wedge W_1.B <> W_2.B} W_2))$$

$$= (\pi_A(W) - (\pi_{W_3.A} (W_3 \times (\pi_{W_1.A = W_2.A \wedge W_1.B <> W_2.B} W_2))))$$

Q.2

(a)

$$E_1 = \pi_{sid} (cites \bowtie buys)$$

$$F = \pi_{sid, sname} (Student \bowtie E_1)$$

(b)

$$E_1 = \pi_{sid} (major_1 \bowtie_{m_1.sid = m_2.sid \wedge m_1.major <> m_2.major} major_2)$$

$$F = \pi_{sid, sname} (Student \bowtie E_1)$$

(c)

$$\pi_{sid} (buys) - \pi_{sid} (buys_1 \bowtie_{bs_1.sid = bs_2.sid \wedge bs_1.bookno <> bs_2.bookno} buys_2)$$

(d)

~~$E_1 = \sigma_{B_1.Price < B_2.Price}$~~

$$E_1 = \sigma_{\neg(B_1.Price \leq B_2.Price)} (Book_1 \times Book_2)$$

$$E_2 = \pi_{bookno, title} (E_1)$$

$$E_3 = \sigma_{\neg(E_{11}.Price \leq E_{12}.Price)} (E_{11} \times E_{12})$$

$$E_4 = \pi_{bookno, title} (E_3)$$

$$F = E_2 - E_4$$

(e)

$$E_1 = \pi_{sid} (\sigma_{sid=1001} (Student)) \times \pi_{bookno} (Book)$$

$$E_2 = \pi_{bookno} (Buys - E_1)$$

$$E_3 = \pi_{bookno} (Book) - E_2$$

$$F = \pi_{bookno, title} (E_3 \bowtie Book)$$

(f)

$$E_1 = \pi_{bookno} (\sigma_{Price < 50} (Book))$$

$$E_2 = Buys \bowtie E_1$$

$$E_3 = E_2 \bowtie_{E_{21}.sid = E_{22}.sid \wedge E_{21}.bookno < E_{22}.bookno} E_2$$

$$F = \pi_{sid, sname} (S \bowtie E_3)$$

(g)

$$E_1 = \pi_{sid}(\sigma_{major=cs} (major))$$

$$E_2 = E_1 \times \pi_{bookno} (Book)$$

$$F = \pi_{Bookno} (E_2 - Buys)$$

(h)

$$\pi_{Bookno} (Book) - \pi_{citedbookno} (\sigma_{price > 50} (Cites \bowtie Book))$$

(i)

$$E_1 = \pi_{Bookno} (\sigma_{price < 30} (Book))$$

$$E_2 = \pi_{sid} (Student) \times E_1$$

$$F = \pi_{sid} (Buys - E_2)$$

(j)

$$E_1 = Buys \times \pi_{Bookno} (Cites)$$

$$E_2 = \pi_{bs.sid, bs.bookno, c.citedbookno} (Buys \bowtie_{bs.bookno = c.Bookno} Cites)$$

$$F = \pi_{sid, citedbookno} (E_1 - E_2)$$

(k)

$$E_1 = \Pi_{\text{sid, bookno}} (\text{Buys } \Delta \sigma_{\text{majors}}' (\text{major}))$$

$$\cancel{E_1} = \cancel{\bar{E}_1} \times \cancel{\Pi_{\text{bookno}} (\text{Book})}$$

\bar{E}_1 is

$$\bar{E}_1 = \Pi_{\text{bookno, sid}} (E_1)$$

$$E_2 = \bar{E}_1 \times \Pi_{\text{bookno}} (\text{Book})_{\text{as bookno}}$$

$$E_3 = \cancel{\Pi_{\text{bookno}} \times E_1} \quad \Pi_{\text{bookno}} (\text{Book})_{\text{as bookno}} \times E_1$$

$$E_4 = E_2 - E_3$$

$$E_5 = E_3 - E_2$$

$$E_6 = \Pi_{\text{bookno, bookno}} (E_4 \cup E_5)$$

$$E_7 = \Pi_{B_1.\text{bookno}, B_2.\text{bookno}} (\text{Book}_1 \Delta \text{Book}_2)_{B_1.\text{bookno} < B_2.\text{bookno}}$$

$$F = E_7 - E_6$$

(L)

$$E_1 = \text{Buys} \times \pi_{\text{sid}}(\text{Student})$$

$$\overline{\text{Buys}} = \pi_{\text{bookno, sid}}(\text{Buys})$$

$$E_2 = \pi_{\text{sid}}(\text{Student}) \times \overline{\text{Buys}}$$

$$E_3 = \pi_{\text{sid, sid}}(E_2 - E_1)$$

$$E_4 = \pi_{s_1.sid, s_2.sid}(\text{Student}_1 \bowtie_{s_1.sid < s_2.sid} \text{Student}_2)$$

$$F = E_4 - E_3$$

(M)

$$E_1 = \pi_{\text{citedbookno, bookno}}(\text{Cites} \bowtie_{b.bookno < c.bookno} \pi_{\text{bookno}}(\text{Book}))$$

$$E_2 = \pi_{\text{citedbookno}}(E_1 \bowtie_{E_{11}.citedbookno = E_{12}.citedbookno \wedge E_{11}.bookno < E_{12}.bookno} E_{12})$$

$$F = \pi_{\text{citedbookno}}(\text{Cites}) - E_2$$

Q.3

(a)

$$E_1 = \text{Buys} \times \left(\sigma_{\text{price} \leq 20} (\text{Book}) \right)$$

$\text{Bs.bookno} = \text{B.bookno}$

$$E_2 = \text{major} \times (E_1)$$

$\text{M.sid} = \text{E1.sid}$

$$E_3 = \text{Jl}_{\text{sid, major}} (E_2)$$

(b)

$$E_1 = \text{Jl}_{\text{sid, bookno, price}} (\text{Buys} \times \text{Book})$$

$\text{Bs.bookno} = \text{B.bookno}$

$$E_2 = \text{Buys} \times \text{Book}$$

$\text{Bs.bookno} = \text{B.bookno}$

$$E_3 = \sigma_{(E_{21}.\text{price} \leq E_{22}.\text{price})} (E_{21} \times E_{22})$$

$E_{21}.\text{sid} = E_{22}.\text{sid}$

$$E_4 = \text{Jl}_{\text{sid, bookno, price}} (E_3)$$

$$F = \text{Jl}_{\text{sid, bookno}} (E_1 - E_4)$$

(c)

$$E_1 = \sigma_{20 \leq \text{price} \wedge \text{price} \leq 40} (\text{Book})$$

$$E_2 = E_1 \times \text{Cites}$$

$\text{E1.bookno} = \text{C.cited bookno}$

$$F = \text{Jl}_{\text{bookno, title}} (E_2)$$

(c)

$$E_1 = \sigma_{20 \leq \text{Price} \wedge \text{Price} \leq 40} (\text{Book})$$

$$E_2 = E_1 \bowtie \text{Cites}$$

$E_1.\text{bookno} = C.\text{Citedbookno}$

$$F = \pi_{\text{bookno}, \text{title}} (E_2)$$

(d)

$$E_1 = \sigma_{\text{major} = 'CS'} (\text{major})$$

$$E_2 = \text{Student} \bowtie E_1$$

$S.\text{sid} = E_1.\text{sid}$

$$E_3 = E_2 \bowtie \text{Buys}$$

$E_2.\text{sid} = B.\text{sid}$

$$E_4 = E_3 \bowtie \text{Cites}$$

$E_3.\text{bookno} = C.\text{Citedbookno}$

$$\cancel{E_5} = \cancel{\text{Book}_1} \bowtie \cancel{\text{Book}_2}$$

$B_1.\text{Price} > B_2.\text{Price}$

$$E_5 = E_4 \bowtie (\text{Book}_1 \bowtie \text{Book}_2)$$

$(\text{Citedbookno} = B_1.\text{bookno} \wedge \text{Bookno} = B_2.\text{bookno})$
 $B_1.\text{Price} > B_2.\text{Price}$

$$F = \pi_{\text{sid}, \text{sname}} (E_5)$$

(e)

$$E_1 = \sigma_{\text{major} = 'cs'} (\text{major})$$

$$E_2 = \pi_{\text{Bookno, title, sid}} (\text{Book} \times E_1)$$

$$E_3 = (E_1 \bowtie_{E_1.\text{sid} = B5.\text{sid}} \text{Buys})$$

$$E_4 = \text{Book} \bowtie_{B.\text{Bookno} = E_3.\text{Bookno}} E_3$$

$$E_6 = \pi_{\text{Bookno, title, sid}} (E_4)$$

~~E_5~~ ~~⊗~~

$$F = \pi_{\text{Bookno, title}} (E_2 - E_6)$$

(f)

$$E_1 = \sigma_{\text{major} = 'cs'} (\text{major})$$

$$E_2 = \text{Student} \bowtie_{S.\text{sid} = E_1.\text{sid}} E_1$$

$$E_3 = \sigma_{\text{major} = 'math'} (\text{major})$$

$$E_4 = E_2 \bowtie_{E_4.\text{sid} = E_3.\text{sid}} E_3$$

$$E_5 = \text{Book} \times E_4$$

$$E_6 = \pi_{\text{Bookno, title, Price, sid, name, major}} (E_5)$$

$$E_6 = \pi_{\text{Bookno, title, Price, sid, name, major}} (E_5)$$

$$E_7 = \text{Book } M \quad \text{Boys}$$

$$B \cdot \text{Bookno} = E_6 \cdot \text{Bookno}$$

$$E_8 = E_7 \quad M \quad E_4$$

$$E_7 \cdot \text{sid} = E_4 \cdot \text{sid}$$

$$E_9 = \Pi_{\text{Bookno}, \text{title}, \text{Price}, \text{sid}, \text{Surname}, \text{major}} (E_8)$$

$$E_{10} = \Pi_{\text{Bookno}, \text{title}, \text{Price}} (E_6 - E_9)$$

$$F = \Pi_{\text{Bookno}, \text{title}} (\text{Book} - E_{10})$$