AlgoLab AS 2014

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1 ACM

1.1 Even Pairs

Keywords: Scanline

```
#include <iostream>
#include <vector>
using namespace std;
int main(void)
      int n;
      cin >> n;
      vector < int > elems(n);
for(int i = 0; i < n; i++) {
   cin >> elems.at(i);
      int even = 0;
     for(int start = 0; start < n; start++) {
    for(int end = start; end < n; end++) {
        int sum = 0;
        for(int i = start; i <= end; i++) {</pre>
                          sum += elems.at(i);
                   if(sum % 2 == 0) {
                         even++;
                   }
            }
      cout << even << endl;</pre>
      return 0:
```

```
#include <iostream>
using namespace std;
int main () {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int n;
  cin >> n;
  int nr_odd_input = 0;
  int even = 1;
  int odd = 0;
  int total_pairs = 0;
  short next_number;
for (int i = 0; i < n; i++) {
  cin >> next_number;
    if (next_number == 1) {
       nr_odd_input++;
    if ((nr_odd_input & 0x1) == 0) {
   //cout << "even: " << even << endl;
   total_pairs += even++;</pre>
    } else {
       //cout << "odd: " << odd << endl;
       total_pairs += odd++;
    }
  cout << total_pairs << endl;</pre>
  return 0;
```

1.2 Build The Sum

Keywords:

```
#include <iostream>
#include <vector>
using namespace std;
int main(void)
{
   int n;
    cin >> n; // ignore this

while(cin >> n) {
    float sum = 0.0;
```

```
for(int i=0; i < n; i++) {
    float v = 0.0;
    cin >> v;
    sum += v;
}
cout << sum << endl;
}
return 0;
}</pre>
```

```
#include <iostream>
using namespace std;
int main () {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int m;
    double sum = 0, c = 0, summand;
for (int i = 0; i < m; i++) {</pre>
       cin >> summand;
       double y = summand - c;
       double t = sum + y;
       c = (t - sum) - y;
      sum = t;
    cout << sum << endl;</pre>
  return 0;
}
```

1.3 Shelves

Keywords:

```
#include <iostream>
#include <vector>
#include <cmath>
using namespace std;
int main(void)
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int N;
    cin >> N;
    for(int i = 0; i < N; i++) {</pre>
         int length, large_shelve_length, small_shelve_length;
         cin >> length;
         cin >> small_shelve_length;
         cin >> large_shelve_length;
         int opt_small_shelves = 0;
         int opt_large_shelves = 0;
int opt_wall_left = length;
         int sqrt_len = (int)sqrt(length);
         if(large_shelve_length > sqrt_len) {
              for(int large_shelves = min(sqrt_len, (int)(length / large_shelve_length)); large_shelves >= 0; large_shelves
                   int wall_left_for_small = (length - (large_shelves * large_shelve_length));
int wall_left = wall_left_for_small % small_shelve_length;
                   if(wall_left < opt_wall_left) {</pre>
                        opt_wall_left = wall_left;
                        opt_small_shelves = (int)(wall_left_for_small / small_shelve_length);
opt_large_shelves = large_shelves;
                   if(opt_wall_left == 0) {
                        break;
                   }
              }
         } else {
              int max_small = min(sqrt_len, (int)(length / small_shelve_length));
              for(int small_shelves = 0; small_shelves <= max_small; small_shelves++) {
  int wall_left_for_large = (length - (small_shelves * small_shelve_length));</pre>
                   int wall_left = wall_left_for_large % large_shelve_length;
                   if(wall_left < opt_wall_left) {</pre>
```

```
#include <limits>
using namespace std;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    unsigned int total_length, small_length, large_length;
    cin >> total_length >> small_length >> large_length;
    unsigned int best_nr_small_shelves = 0, best_nr_large_shelves = 0, best_uncovered_wall = total_length;
    int min_large_shelves = 0;
    if (((long long)small_length)*((long long)large_length) < (long long)numeric_limits<int>::max() && small_length*
         large_length <= total_length) {</pre>
       min_large_shelves = total_length / large_length - small_length;
    for (int nr_large_shelves = total_length / large_length; nr_large_shelves >= min_large_shelves; nr_large_shelves--) {
   unsigned int uncovered_wall_large = total_length - (large_length*nr_large_shelves);
       unsigned int nr_small_shelves = uncovered_wall_large / small_length;
       unsigned int uncovered_wall = uncovered_wall_large - (small_length*nr_small_shelves);
       if (uncovered_wall < best_uncovered_wall) {</pre>
         best_uncovered_wall = uncovered_wall;
         best_nr_large_shelves = nr_large_shelves;
best_nr_small_shelves = nr_small_shelves;
if (best_uncovered_wall == 0) {
           break;
         }
    cout << best_nr_small_shelves << " " << best_nr_large_shelves << " " << best_uncovered_wall << endl;</pre>
  return 0;
```

1.4 Checking Change

Keywords: Dynamic Programming

```
#include <iostream>
#include <vector>
#include <cmath>
#include <climits>
using namespace std;
int main(void)
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int n;
    cin >> n:
    for(int i = 0; i < n; i++) {</pre>
         int c, m;
cin >> c;
         cin >> m;
         vector < int > coins(c);
         for(int j = 0; j < c; j++) {
    cin >> coins.at(j);
         vector<int> ret(m);
         int max_ret = 0;
```

```
for(int j = 0; j < m; j++) {</pre>
              int ret_val;
              cin >> ret_val;
              ret.at(j) = ret_val;
              if(ret_val > max_ret) {
                  max_ret = ret_val;
         7
         vector<int> table(max_ret + 1);
         table.at(0) = 0;
         for(int v = 1; v <= max_ret; v++) {
   table.at(v) = INT_MAX;</pre>
              for(auto coin : coins) {
   if(v - coin >= 0 && coin <= v) {</pre>
                       if(table.at(v-coin) != INT_MAX) {
                            table.at(v) = min(table.at(v), table.at(v-coin) + 1);
                  }
              }
         }
         for(auto r : ret) {
              if(table.at(r) == INT_MAX) {
                   cout << "not possible" << endl;</pre>
              } else {
                  cout << table.at(r) << endl;</pre>
    }
    return 0;
}
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
using namespace std;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_coins, nr_test_values;
    cin >> nr_coins >> nr_test_values;
    vector<int> coins(nr_coins);
for (int i = 0; i < nr_coins; i++) {
  cin >> coins[i];
    int max_test_value = 0;
    vector <int > test_values(nr_test_values);
    for (int test_value_id = 0; test_value_id < nr_test_values; test_value_id++) {</pre>
       cin >> test_values[test_value_id];
       if (test_values[test_value_id] > max_test_value) {
         max_test_value = test_values[test_value_id];
      }
    vector < int > nr_coins_for_values(max_test_value + 1, -1);
    nr_coins_for_values[0] = 0;
    for (int value = 0; value <= max_test_value; value++) {
  int nr_coins_for_value = nr_coins_for_values[value];
  if (nr_coins_for_value != -1) {</pre>
         for (int coin_id = 0; coin_id < nr_coins; coin_id++) {</pre>
           int new_value = value + coins[coin_id];
           if (new_value <= max_test_value) {</pre>
              if (nr_coins_for_values[new_value] == -1) {
               nr_coins_for_values[new_value] = nr_coins_for_value + 1;
              else {
               nr_coins_for_values[new_value] = min(nr_coins_for_values[new_value], nr_coins_for_value + 1);
             }
          }
        }
      }
    for (int test_value_id = 0; test_value_id < nr_test_values; test_value_id++) {</pre>
       int nr_coins_for_value = nr_coins_for_values[test_values[test_value_id]];
if (nr_coins_for_value == -1) {
         cout << "not possible" << endl;</pre>
         cout << nr_coins_for_value << endl;</pre>
```

```
}
}
return 0;
}
```

1.5 Even Matrices

Keywords:

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
using namespace std;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int n;
cin >> n;
    vector < vector < bool > > matrix(n, vector < bool > (n, 0));
    for (int i = 0; i < n; i++) {</pre>
      vector < bool > & row = matrix[i];
      for (int j = 0; j < n; j++) {</pre>
        short input;
cin >> input;
row[j] = (input == 1);
    int even = 0;
for (int row_i = 0; row_i < n; row_i++) {</pre>
      //cout << matrix[row_j][i] << " ";
        //cout << endl;
         int nr_odd_input = 0;
        int e = 1;
         int o = 0;
        for (int i = 0; i < n; i++) {
  if (previous[i] == 1) {</pre>
            nr_odd_input++;
          if ((nr_odd_input & 0x1) == 0) {
            //cout << "even: " << even << endl;
even += e++;
          }
          else {
             //cout << "odd: " << odd << endl;
             even += o++;
          }
        }
      }
    }
    cout << even << endl;
 }
  return 0;
```

1.6 Race Tracks

Keywords: BFS (Graph)

```
#include <iostream>
#include <vector>
#include <queue>
#include <cmath>
#include <climits>

using namespace std;
int main(void)
{
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test_cases;
```

```
cin >> test_cases;
for(int i = 0; i < test_cases; i++) {</pre>
           int width_x, height_y;
           cin >> width_x;
           cin >> height_y;
           int start_x, start_y;
           cin >> start_x;
           cin >> start_y;
           int end_x, end_y;
           cin >> end_x;
           cin >> end_y;
           int obstacle_count;
           cin >> obstacle count:
           vector < vector < bool >> obstacles(width_x, vector < bool > (height_y, false));
           for(int j = 0; j < obstacle_count; j++) {</pre>
                       int x1, x2, y1, y2;
                       cin >> x1;
                      cin >> y1;
cin >> x2;
                       cin >> y2;
                       for(int k = x1; k <= x2; k++) {</pre>
                                for(int 1 = y1; 1 <= y2; 1++) {
                                              obstacles.at(k).at(l) = true;
                      }
           }
           // cout << "width: " << width_x << " & height: " << height_y << endl; cout << "start: x=" << start_x << ", y=" << start_y << endl; cout << "end: x=" << end_x << ", y=" << end_y << endl;
           cout << "obstacles:" << endl;</pre>
           for(int y = 0; y < height_y; y++) {
   for(int x = 0; x < width_x; x++) {</pre>
                                  if(obstacles.at(x).at(y)) {
                                              cout << "X";
                                  } else if(start_x == x && start_y == y) {
                                              cout << "S";
                                   } else if(end_x == x && end_y == y) {
                                             cout << "E";
                                  } else {
                                            cout << "0";
                                  }
                      cout << endl;</pre>
           cout << "----" << endl << endl; */
           // algo start
           // x , y , v_x, v_y, depth
queue<tuple<int, int, int, int, int>> next_tiles;
           next_tiles.push(make_tuple(start_x, start_y, 0, 0, 0));
           bool found = false;
           \label{lem:vector} \textbf{vector} < \textbf{vector}
           >>(7, vector <bool>(7, false)))); while(!next_tiles.empty()) {
                       auto tile = next_tiles.front();
                       next_tiles.pop();
                      int x = get<0>(tile);
int y = get<1>(tile);
int v_x = get<2>(tile);
int v_y = get<3>(tile);
int depth = get<4>(tile);
                       if(x < 0 \mid \mid x >= width_x \mid \mid
                                 y < 0 || y >= height_y ||

v_x < -3 || v_x > 3 ||

v_y < -3 || v_y > 3 ||

obstacles.at(x).at(y) ||
                                   << end1;
                                   continue;
                       }
                       /*for(int i_y = 0; i_y < height_y; i_y++) {
                                   for(int i_x = 0; i_x < width_x; i_x++) {
                                             if(x == i_x && y == i_y) {
   cout << "P";</pre>
                                              } else if(obstacles.at(i_x).at(i_y)) {
                                                         cout << "X":
                                              } else if(start_x == i_x && start_y == i_y) {
                                                          cout << "S";
                                              } else if(end_x == i_x && end_y == i_y) {
                                                         cout << "E";
                                             } else {
                                                        cout << "0";
                                   cout << endl;</pre>
```

```
cout << endl << endl;*/</pre>
                                    \label{eq:continuous} $$ ''\cos x < x < y < y < y < y < y < x_x < y_x < y_y < y
                                    if(x == end_x && y == end_y) {
                                                                      "Optimal solution takes " << depth << " hops." << endl;
                                                found = true;
                                                break:
                                    7
                                    visited.at(x).at(y).at(v_x + 3).at(v_y + 3) = true;
                                    next_tiles.push(make_tuple(x + v_x - 1, y + v_y - 1,
                                                                                                                                                                                                        v_x - 1, v_y - 1,
                                                                                                                                                                                                                                                                     depth + 1));
                                    next_tiles.push(make_tuple(x + v_x - 1, y + v_y,
                                                                                                                                                                                                         v_x - 1, v_y,
                                                                                                                                                                                                                                                                     depth + 1));
                                    next_tiles.push(make_tuple(x + v_x - 1, y + v_y + 1,
                                                                                                                                                                                                         v_x - 1, v_y + 1,
                                                                                                                                                                                                                                                                    depth + 1));
                                    next\_tiles.push(make\_tuple(x + v\_x, y + v\_y - 1,
                                                                                                                                                                                                                     v_y - 1,
                                                                                                                                                                                                                                                     depth + 1));
                                                                                                                                                                                            v_x,
                                    next_tiles.push(make_tuple(x + v_x, y + v_y,
                                                                                                                                                                                                                                                       depth + 1));
                                                                                                                                                                                             v_x,
                                                                                                                                                                                                                     v_{-}y ,
                                    next_tiles.push(make_tuple(x + v_x, y + v_y + 1,
                                                                                                                                                                                                                     v_y + 1,
                                                                                                                                                                                                                                                  depth + 1));
                                                                                                                                                                                             v_x,
                                   next_tiles.push(make_tuple(x + v_x + 1, y + v_y - 1, next_tiles.push(make_tuple(x + v_x + 1, y + v_y,
                                                                                                                                                                                                        v_x + 1, v_y - 1,
                                                                                                                                                                                                                                                                     depth + 1));
                                                                                                                                                                                                         v_x + 1, v_y,
                                                                                                                                                                                                                                                                     depth + 1));
                                    next_tiles.push(make_tuple(x + v_x + 1, y + v_y + 1, v_x + 1, v_y + 1,
                                                                                                                                                                                                                                                                depth + 1));
                        }
                        if(!found) {
                                    cout << "No solution." << endl;</pre>
            return 0;
}
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
using namespace std;
class State {
public:
  short x, y, speed_x, speed_y;
  int hops;
  State(short x, short y, short speed_x, short speed_y, int hops)
    :x(x), y(y), speed_x(speed_x), speed_y(speed_y), hops(hops) {}
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int width, height, start_x, start_y, end_x, end_y, nr_obstacles;
cin >> width >> height >> start_x >> start_y >> end_x >> end_y >> nr_obstacles;
    vector<vector<vector<bool> > > race_track(width, vector<vector<bool> > >(height, vector<vector<bool>
          >(7, vector <bool > (7, false))));
    for (int obstacle_id = 0; obstacle_id < nr_obstacles; obstacle_id++) {</pre>
       int obstacle_x_start, obstacle_y_start, obstacle_x_end, obstacle_y_end;
       cin >> obstacle_x_start >> obstacle_y_start >> obstacle_x_end >> obstacle_y_end;
       vector<vector<bool> > obstacle_indicator(7, vector<bool>(7, true));
       for (int x = obstacle_x_start; x <= obstacle_x_end; x++) {
  for (int y = obstacle_y_start; y <= obstacle_y_end; y++) {</pre>
           race_track[x][y] = obstacle_indicator;
         }
      }
    int min_hops = -1;
    if (start_x == end_x && start_y == end_y) {
      min_hops = 0;
    else {
       queue < State > states;
       race_track[start_x][start_y][3][3] = true;

//cout << "start: " << start_x << " " << start_y << " " << end_x << " " << end_y << end];
       //cout << "start: " << start_x << " " << start_y << " " << end //cout << "width: " << width << " height: " << height << end];
       while (!states.empty()) {
         State current_state = states.front();
         states.pop();
         //cout << current_state.x << " " << current_state.y << " " << current_state.speed_x << " " << current_state.
                              " << current_state.hops << endl;
              speed_y << "
         for (int new_speed_x = max(current_state.speed_x - 1, 0); new_speed_x <= min(current_state.speed_x + 1, 6);
              new_speed_x++) {
```

```
for (int new_speed_y = max(current_state.speed_y - 1, 0); new_speed_y <= min(current_state.speed_y + 1, 6);</pre>
                new_speed_y++) {
             int new_x = current_state.x + new_speed_x - 3;
            int new_x = current_state.x : new_speed_x = 3;
int new_y = current_state.y + new_speed_y = 3;
//cout << "Checking " << new_x << " " << new_y << " " << new_speed_x << " " << new_speed_y << " " <<</pre>
                  current_state.hops+1 << endl;
ut << " " << (new_x >= 0) << " " << (new_y < height) <<
                  endl;
            if (new_x >= 0 && new_x < width && new_y >= 0 && new_y < height) {
               if (!race_track[new_x][new_y][new_speed_x][new_speed_y]) {
  if (new_x == end_x && new_y == end_y) {
                    min_hops = current_state.hops + 1;
                   goto solution_found;
                 }
                 else {
                   race_track[new_x][new_y][new_speed_x][new_speed_y] = true;
//cout << "Adding " << new_x << " " << new_y << " " << new_speed_x << " " << new_speed_y << " " <<</pre>
                    //cout << "Adding " << new_x << "
current_state.hops+1 << endl;</pre>
                                                                << new_y <<
                    states.push(State(new_x, new_y, new_speed_x, new_speed_y, current_state.hops + 1));
                 }
      } }
              }
solution_found:
  if (min_hops == -1) {
    cout << "No solution." << endl;
  else {
     cout << "Optimal solution takes " << min_hops << " hops." << endl;</pre>
}
return 0:
```

1.7 Boats

Keywords: Custom compare, Class with compare, Uses class, Greedy

```
#include <iostream>
#include <vector>
#include <queue>
#include <tuple>
#include <cmath>
#include <climits>
#include <algorithm>
using namespace std;
class Data {
public:
    int length, ring_pos, min_pos;
    Data(int length, int ring_pos) : length(length), ring_pos(ring_pos), min_pos(ring_pos) {}
    bool operator< (const Data& other) const {</pre>
        if(min_pos == other.min_pos) {
            return ring_pos > other.ring_pos;
        return min_pos > other.min_pos;
};
int main(void)
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test_cases;
    cin >> test_cases;
    for(int i = 0; i < test_cases; i++) {</pre>
        int N;
        cin >> N;
        priority_queue < Data > boats;
        for(int j = 0; j < N; j++) {
   int 1, p;</pre>
             cin >> 1;
             cin >> p;
             boats.push(Data(1, p));
        int last_end = boats.top().ring_pos;
        boats.pop();
        int counter = 1;
        while(!boats.empty()) {
             auto boat = boats.top();
             boats.pop();
```

```
if(boat.min_pos - boat.length >= last_end) {
    counter++;
    last_end = boat.min_pos;
} else if(last_end <= boat.ring_pos) {
    // boat overlaps with a previous boat, we have to move it
    boat.min_pos = last_end + boat.length;
    if(boat.min_pos >= boat.ring_pos) {
        boats.push(boat);
    }
}
cout << counter << endl;
}
return 0;
}</pre>
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
using namespace std;
class Boat {
public:
  int length, ring_position, min_end_position;
  Boat(int length, int ring_position)
  :length(length), ring_position(ring_position) {
    this->min_end_position = ring_position;
 }
};
class CompareBoat {
public:
  bool operator()(const Boat& lhs, const Boat& rhs) {
    if (lhs.min_end_position == rhs.min_end_position) {
      return lhs.ring_position > rhs.ring_position;
    return lhs.min_end_position > rhs.min_end_position;
 }
};
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_wizard_boats;
    cin >> nr_wizard_boats;
    priority_queue <Boat, vector <Boat>, CompareBoat> boats;
    for (int wizard_boat_id = 0; wizard_boat_id < nr_wizard_boats; wizard_boat_id++) {</pre>
      int boat_length, ring_position;
      cin >> boat_length >> ring_position;
      boats.push(Boat(boat_length, ring_position));
    int current_end = numeric_limits < int > :: min();
    int max_boats = 0;
    while (!boats.empty()) {
  Boat b = boats.top();
      boats.pop();
      if (b.min_end_position - b.length >= current_end) {
        current_end = b.min_end_position;
        max_boats++;
      else {
        if (current_end <= b.ring_position) {</pre>
          b.min_end_position = current_end + b.length;
          boats.push(b);
        }
     }
    cout << max_boats << endl;</pre>
  return 0;
```

1.8 Aliens

Keywords: Custom compare, Compare function, Compare struct, Uses class, Scanline

```
#include <iostream>
#include <vector>
```

```
#include <queue>
#include <tuple>
#include <cmath>
#include <climits>
#include <algorithm>
using namespace std;
class Alien {
public:
    int from;
    int to;
    Alien(int from, int to) : from(from), to(to), dominated(false) {}
};
bool cmp(Alien left, Alien right) {
    if(left.from == right.from) {
        return left.to > right.to;
        return left.from < right.from;</pre>
    }
}
int main(void)
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test_cases;
    cin >> test_cases;
    for(int i = 0; i < test_cases; i++) {</pre>
         int alien_count, human_count;
         cin >> alien_count >> human_count;
         vector < Alien > aliens;
         for(int j = 0; j < alien_count; j++) {</pre>
             int p, q;
             cin \Rightarrow p \Rightarrow q;
             aliens.push_back(Alien(p, q));
         sort(aliens.begin(), aliens.end(), cmp);
        /*for(auto a : aliens) {
    cout << "alien: [" << a.from << ", " << a.to << "]" << endl;
         cout << endl << endl;</pre>
         int last_human_attacked = 0;
         int last_alien_end = 0;
         int count = 0;
         bool not_all_humans = false;
         bool id = false;
         Alien last = Alien(0, 0);
         for(int cur = 0; cur < alien_count; cur++) {</pre>
             Alien &cur_alien = aliens.at(cur);
             if(cur_alien.from > last_human_attacked + 1) {
                 not_all_humans = true;
                 break;
             } else {
                 last_human_attacked = max(cur_alien.to, last_human_attacked);
             if(!id && last.from == cur_alien.from && last.to == cur_alien.to && cur_alien.to != 0) {
             count --;
id = true;
} else if(cur_alien.to > last_alien_end) {
                 count++;
                 last = cur_alien;
                 last_alien_end = cur_alien.to;
                 id = false;
             }
         if(not_all_humans || last_human_attacked != human_count) {
             //cout << "!0" << " last = " << last_human_attacked << endl; cout << "0" << endl;
        } else {
             cout << count << endl;</pre>
    return 0;
}
```

```
#include <iostream>
#include <vector>
#include #include #include #include
```

```
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
using namespace std;
struct RangeComparator {
  bool operator() (const pair<int, int>& lhs, const pair<int, int>& rhs) {
    return (lhs.first == rhs.first) ? lhs.second > rhs.second : lhs.first < rhs.first;</pre>
};
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
     int nr_aliens, nr_humans;
     cin >> nr_aliens >> nr_humans;
    multiset<pair<int, int>, RangeComparator> ranges;
for (int alien_id = 0; alien_id < nr_aliens; alien_id++) {</pre>
        int first_wounded, last_wounded;
       cin >> first_wounded >> last_wounded;
if (first_wounded != 0) {
          ranges.insert(make_pair(first_wounded, last_wounded));
     pair < int , int > last_pair = make_pair(0, 0);
     int nr_superior = 0;
bool gap_found = false;
bool found_ident = false;
     //cout << endl;</pre>
     for (multiset < pair < int, int > >::iterator it = ranges.begin(); it != ranges.end(); ++it) {
   //cout << (*it).first << " " << (*it).second << endl;
   if ((*it).second > last_pair.second) {
          if ((*it).first > last_pair.second + 1) {
    //gap in ranges found no superior alien
            gap_found = true;
            break;
          last_pair = (*it);
          found_ident = false;
          nr_superior++;
        else if ((*it).second == last_pair.second && (*it).first == last_pair.first && !found_ident) {
          nr_superior --
          found_ident = true;
     if (!gap_found && last_pair.second == nr_humans) {
       cout << nr_superior << endl;</pre>
     else {
       cout << 0 << endl;
  }
  return 0;
}
```

1.9 Next Path

Keywords: Custom compare, Compare struct, BFS (Graph)

```
#include <iostream>
#include <algorithm>
#include <vector>
#include <queue>

using namespace std;
int main() {
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test_cases;
    cin >> test_cases;
    cin >> test_cases;
    for(int test = 0; test < test_cases; test++) {
        // clean up
        best_distance.clear();

        // get graph properties
        int vertex_count, edge_count;
        cin >> vertex_count >> edge_count;
```

```
// get start and target vertices
          start_vertex, target_vertex;
      cin >> start_vertex >> target_vertex;
start_vertex -= 1; // input starts at 1
target_vertex -= 1; // input starts at 1
       // read in edges
       vector<vector<int > > edges(vertex_count, vector<int>());
       for(int edge_index = 0; edge_index < edge_count; edge_index++) {</pre>
           int from, to;
           cin >> from >> to;
           from -= 1; // input starts at 1
to -= 1; // input starts at 1
           // create edge
           edges.at(from).push_back(to);
       // keeps track of the second best solution
       int second_best = -1;
       // queue for vertices to visit
      // pair.first: lenth so far
// pair.second: next vertex
       next_moves.push(make_pair(0, start_vertex));
       // keep track how many times a vertex was reached
      vector<int> visited_counters(vertex_count, 0);
visited_counters.at(start_vertex) = 1;
       // "The Algorithm" TM
       while(!next_moves.empty()) {
           pair < int , int > cur_move = next_moves.top();
           next_moves.pop();
           // extract information from current vertex we sit on
           int vertex = cur_move.second;
           int length = cur_move.first;
           // iterate over all neighbors
           for(int neighbor_index = 0; neighbor_index < edges.at(vertex).size(); neighbor_index++) {</pre>
               int neighbor_vertex = edges.at(vertex).at(neighbor_index);
                if(visited_counters.at(neighbor_vertex) < 2) {</pre>
                    // ^- only visit neighbor if it wasn't visited already twice // v- update visited counter
                    visited_counters.at(neighbor_vertex)++;
                    if(neighbor_vertex == target_vertex && visited_counters.at(neighbor_vertex) == 2) {
                        // ok, so we found our target vertex and it was already visited twice (i.e. we visit it right now
                              for the second time)
                        // we can abort early :-D
second_best = length + 1;
                    goto _solution; // haha
} else {
                        // visit neighbor
                        next_moves.push(make_pair(length + 1, neighbor_vertex));
                   }
               }
          }
  _solution:
      if(second_best == -1) {
          cout << "no" << endl;
      } else {
          cout << second_best << endl;</pre>
  }
return 0:
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
using namespace std;
struct PairComparator {
 bool operator() (const pair < int, int > & lhs, const pair < int, int > & rhs) {
   return lhs.first > rhs.first;
 }
};
int main() {
 cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
```

```
int nr_test_cases;
cin >> nr_test_cases;
for (int test_case = 0; test_case < nr_test_cases; test_case++) {
  int nr_vertices, nr_edges;</pre>
   cin >> nr_vertices >> nr_edges;
   int start_v, end_v;
   cin >> start_v >> end_v;
   start_v--;
   end_v --;
   vector < vector < int > > graph(nr_vertices, vector < int > ());
  for (int edge_id = 0; edge_id < nr_edges; edge_id++) {
  int edge_source, edge_target;
  cin >> edge_source >> edge_target;
  graph[edge_source - 1].push_back(edge_target - 1);
   //cout << endl;</pre>
   int solution = -1;
   priority_queue<pair<int, int>, vector<pair<int, int> >, PairComparator> moves;
moves.push(make_pair(0, start_v));
   vector < int > reachable(nr_vertices, 0);
   reachable[start_v] = 1;
   while (!moves.empty()) {
  pair<int, int> move = moves.top();
  //cout << move.first << " " << move.second << endl;</pre>
      moves.pop();
int v = move.second;
      int length = move.first;
      for (unsigned int edge_id = 0; edge_id < graph[v].size(); edge_id++) {
  int reachable_v = graph[v][edge_id];</pre>
        if (reachable[reachable_v] < 2) {
  reachable[reachable_v]++;</pre>
           if (reachable_v == end_v && reachable[reachable_v] == 2) {
              solution = length + 1;
              goto solution_found;
           }
           else {
             moves.push(make_pair(length + 1, reachable_v));
        }
     }
solution found:
  if (solution == -1) {
    cout << "no" << endl;
  else {
     cout << solution << endl;</pre>
  }
}
return 0;
```

2 Dynamic Programming

2.1 Longest Path

Keywords: BFS (Graph)

```
#include <iostream>
#include <vector>
#include <stack>
using namespace std;
int main(void) {
    int testcases;
    cin >> testcases;
    for(int t = 0; t < testcases; t++) {</pre>
         int vertices;
         cin >> vertices;
         vector<vector<int>> graph(vertices, vector<int>());
         for(int i = 0; i < vertices - 1; i++) {</pre>
             int from, to;
              cin >> from >> to;
              graph.at(from).push_back(to);
              graph.at(to).push_back(from);
         int longest = 0;
         int longest_v = -1;
         int i = 0; // random start
stack<int> tovisit;
         vector < bool > visited(vertices, false);
         int longest_from_i = 0;
         tovisit.push(i);
         int prev = -1;
while(!tovisit.empty()) {
              int next = tovisit.top();
              tovisit.pop();
              if(next == -1) {
                   if(longest < longest_from_i) {</pre>
                       longest = longest_from_i;
longest_v = prev;
                       //cout << "longest_v: " << longest_v << endl;</pre>
                  longest_from_i --;
//cout << " ... " << endl;</pre>
                   continue;
              if(!visited.at(next)) {
                  prev = next;
                  longest_from_i++;
//cout << "visiting: " << next << ", depth: " << longest_from_i << endl;</pre>
                  visited.at(next) = true;
                   tovisit.push(-1);
                  for(auto add_v : graph.at(next)) {
                       tovisit.push(add_v);
             }
         // -----
         stack<int> tovisit2:
         vector < bool > visited2(vertices, false);
         int longest_from_i2 = 0;
         tovisit2.push(longest_v);
         while(!tovisit2.empty()) {
              int next = tovisit2.top();
              tovisit2.pop();
              if(next == -1) {
                  longest = max(longest, longest_from_i2);
                  longest_from_i2--;
//cout << " ... " << endl;</pre>
                   continue;
              if(!visited2.at(next)) {
                  longest_from_i2++;
//cout << "visiting: " << next << ", depth: " << longest_from_i2 << endl;
visited2.at(next) = true;</pre>
                   tovisit2.push(-1);
                   for(auto add_v : graph.at(next)) {
                       tovisit2.push(add_v);
```

```
}
         cout << longest << endl;</pre>
         /*int longest = 0;
for(int i = 0; i < vertices; i++) {</pre>
             if(graph.at(i).size() != 1) {
                  continue;
              stack<int> tovisit;
              vector < bool > visited(vertices, false);
              int longest_from_i = 0;
              tovisit.push(i);
              while(!tovisit.empty()) {
                  int next = tovisit.top();
                  tovisit.pop();
                  if(next == -1) {
                       longest = max(longest, longest_from_i);
                       longest_from_i --;
//cout << " ... " << endl;
                       continue;
                  7
                  if(!visited.at(next)) {
                       longest_from_i++;
                       //cout << "visiting: " << next << ", depth: " << longest_from_i << endl;</pre>
                       visited.at(next) = true;
                       tovisit.push(-1);
                       for(auto add_v : graph.at(next)) {
   tovisit.push(add_v);
                 }
            }
         cout << longest << endl;*/</pre>
    }
}
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
using namespace std;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_vertices;
    cin >> nr_vertices;
    vector<set<int> > vertices(nr_vertices, set<int>());
    for (int i = 0; i < nr_vertices - 1; i++) {</pre>
      int v1, v2;
       cin >> v1 >> v2;
       vertices[v1].insert(v2);
      vertices[v2].insert(v1);
    int longest_path = -1;
    queue <int > leafs;
for (int i = 0; i < nr_vertices; i++) {</pre>
      if (vertices[i].size() == 1) {
         leafs.push(i);
      }
    7
    vector < int > path_length(nr_vertices, 0);
    while (!leafs.empty()) {
       int leaf = leafs.front();
       leafs.pop();
       if (vertices[leaf].size() == 1) {
         int parent = *(vertices[leaf].begin());
//cout << leaf << " " << parent << " " << path_length[leaf] << endl;</pre>
         vertices[parent].erase(leaf);
         if (vertices[parent].size() == 1) {
          leafs.push(parent);
         longest_path = max(longest_path, path_length[parent] + path_length[leaf] + 1);
path_length[parent] = max(path_length[parent], path_length[leaf] + 1);
```

```
cout << (longest_path + 1) << endl;
}
return 0;
}</pre>
```

2.2 Light Pattern

Keywords: Scanline

```
#include <iostream>
#include <vector>
#include <queue>
#include <tuple>
#include <cmath>
#include <climits>
#include <algorithm>
using namespace std;
void debug_state(vector<bool> state) {
    for(int i = 0; i < state.size(); i++) {
    if(state.at(i)) {</pre>
              cout << "[X]";
          } else {
              cout << "[ ]";
    cout << endl << endl:
int main(void)
     cin.sync_with_stdio(false);
     cout.sync_with_stdio(false);
     int test_cases;
     cin >> test_cases;
     for(int i = 0; i < test_cases; i++) {</pre>
          int bulb_count, bulbs_in_lightpattern, pattern;
cin >> bulb_count >> bulbs_in_lightpattern >> pattern;
          // read initial state
          vector < bool > state(bulb_count);
          for(int j = 0; j < bulb_count; j++) {</pre>
              int v:
               cin >> v:
               state.at(j) = v == 1;
          //debug_state(state);
//cout << "TO" << endl;</pre>
          // calc target state
          vector < bool > target_state(bulbs_in_lightpattern);
          for(int j = bulbs_in_lightpattern - 1; j >= 0; j--) {
  target_state.at(j) = pattern & 0x1;
              pattern = pattern >> 1;
          //debug_state(target_state);
          int group_count = (int)bulb_count / bulbs_in_lightpattern;
int swapping_all = 1;
int single_switching = 0;
          for(int group = group_count; group > 0; group--) {
   int from = group * bulbs_in_lightpattern - bulbs_in_lightpattern;
   //cout << "working on group: " << group << " from: " << from << " to: " << from + bulbs_in_lightpattern - 1</pre>
                    << endl;
               int local_swapping_all = 0;
               int local_single_switching = 0;
               for(int pos = 0; pos < bulbs_in_lightpattern; pos++) {</pre>
                    if(state.at(from + pos) != target_state.at(pos)) {
                         local_single_switching++;
                    } else {
                         local_swapping_all++;
                    }
               /
//cout << "\t current all: " << local_swapping_all << ", current single: " << local_single_switching << endl;
               int tmp_swapped = min(
                       already swapped till at least previously visited block
                    min(
                         swapping_all + local_swapping_all, // how much do we need to changes in case we are already swapped
                         swapping_all + 2 + local_single_switching // we swap again, but only till current block and do normal
                               changes
                         ),
                    // not swapped yet
                    min(
                         single_switching + 1 + local_swapping_all, // we swap till current block and do swapping changes single_switching + 1 + local_single_switching // we swap till the next block and do normal changes in
                                current block
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
using namespace std;
int main() {
  cin.svnc with stdio(false):
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_lights, nr_lights_for_pattern, pattern;
cin >> nr_lights >> nr_lights_for_pattern >> pattern;
     int nr_patterns = nr_lights / nr_lights_for_pattern;
     vector<int> pattern_changes(nr_patterns);
for (int i = 0; i < nr_patterns; i++) {</pre>
       int tmp_pattern = 0;
for (int j = 0; j < nr_lights_for_pattern; j++) {</pre>
          int light;
          cin >> light;
          tmp_pattern <<= 1;
tmp_pattern |= light;
       int pattern_xor = tmp_pattern ^ pattern;
        int changes = 0;
for (int j = 0; j < nr_lights_for_pattern; j++) {</pre>
          if ((pattern_xor & (0x1 << j)) != 0) {</pre>
             changes++;
          }
       pattern_changes[i] = changes;
     int seconds_swapped = 1;
     int seconds_not_swapped = 0;
for (int i = nr_patterns - 1; i >= 0; i--) {
  int changes = pattern_changes[i];
        int swapped_changes = nr_lights_for_pattern - changes;
        int tmp_seconds_not_swapped = min(
          min(seconds_not_swapped + changes, seconds_not_swapped + 2 + swapped_changes),
min(seconds_swapped + 1 + changes, seconds_swapped + 1 + swapped_changes));
        seconds_swapped = min(
          min(seconds_swapped + swapped_changes, seconds_swapped + 2 + changes),
min(seconds_not_swapped + 1 + changes, seconds_not_swapped + 1 + swapped_changes));
        seconds_not_swapped = tmp_seconds_not_swapped;
        //cout << seconds_not_swapped << "</pre>
                                                      " << seconds_swapped << endl;
     cout << min(seconds_not_swapped, seconds_swapped) << endl;</pre>
  }
  return 0;
```

2.3 Burning Coins

Keywords: Dynamic Programming

```
#include <iostream>
#include <vector:
#include <queue>
#include <tuple>
#include <cmath>
#include <climits>
#include <algorithm>
int at_least(vector<vector<int> >& table, vector<int>& values, int left, int right)
        check first if we know the value already
    if(left == right) {
         // only one coin on the table, we can choose so it's ours
         return values[left];
    if(table[left][right] > 0) {
         // already calculated value, reuse
         return table[left][right];
    // calculate easy cases, fast paths
int delta = right - left;
    if(delta == 1) {
         // case: left_coin, right_coin
         int best_of_both = max(values[left], values[right]);
table[left][right] = best_of_both;
         return best_of_both;
    } else if(delta == 2) {
    // case: left_coin, middle_coin, right_coin
    // we have to take middle coin into account and resolve all three coins
         int left_coin = values[left];
         int middle_coin = values[left+1];
int right_coin = values[right];
         int resulting_value = -2;
         if(left_coin > right_coin) {
              // we take the left coin, now we have to take into account that opposite
// side will take the best of middle/right coin
              resulting_value = left_coin;
              if(middle_coin > right_coin) {
    resulting_value += right_coin;
              } else {
                 resulting_value += middle_coin;
              }
         } else {
    // we take right coin, again take middle coin into account
              resulting_value = right_coin;
if(middle_coin > left_coin) {
                   resulting_value += left_coin;
              } else {
                   resulting_value += middle_coin;
              }
         table[left][right] = resulting_value;
         return resulting_value;
    }
     * now decide what happens in general
     // assume we took the left coin
    int we_left_other_left = at_least(table, values, left+2, right); // opposite side takes also the next left one int we_left_other_right = at_least(table, values, left+1, right-1); // opposite side takes the right one
    // assume we took the right coin
    int we_right_other_left = we_left_other_right; //at_least(table, values, left+1, right-1);
    int we_right_other_right = at_least(table, values, left, right-2); // opposite side takes the right one too
    \ensuremath{//} find the minimum value we're guaranteed to get
    int we_get_at_least = max(
         values[left] + min(we_left_other_left, we_left_other_right),
         values[right] + min(we_right_other_left, we_right_other_right)
    table[left][right] = we_get_at_least;
    return we_get_at_least;
}
int main(void)
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test cases:
    cin >> test_cases;
    for(int i = 0; i < test_cases; i++) {</pre>
         int coin_amount;
```

```
cin >> coin_amount;
vector <int > coins;
for(int j = 0; j < coin_amount; j++) {
        int value;
        cin >> value;
        coins.push_back(value);
}

vector < vector < int > table (coin_amount + 1, vector < int > (coin_amount + 1, -1));
cout << at_least(table, coins, 0, coin_amount - 1) << endl;
}

return 0;
}</pre>
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
using namespace std:
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_coins;
     cin >> nr_coins;
    vector < int > coins(nr_coins);
for (int i = 0; i < nr_coins; i++) {</pre>
      cin >> coins[i];
    vector<vector<int> > ta(nr_coins + 1, vector<int>(nr_coins + 1, 0));
vector<vector<int> > tb(nr_coins + 1, vector<int>(nr_coins + 1, 0));
    for (int 1 = 1; 1 <= nr_coins; 1++) {</pre>
       for (int i = 0; i < nr_coins; i++) {
  ta[i][1] = max(coins[i] + tb[i + 1][1 - 1], coins[i + 1 - 1] + tb[i][1 - 1]);</pre>
          tb[i][1] = min(ta[i + 1][1 - 1], ta[i][1 - 1]);
    cout << ta[0][nr_coins] << endl;</pre>
  return 0;
}
```

2.4 Poker Chips

Keywords: Dynamic Programming

```
#include <iostream>
#include <vector>
#include <queue>
#include <tuple>
#include <cmath>
#include <climits>
#include <algorithm>
#define EMPTY_CELL -1
using namespace std;
if(table[conf.at(0)][conf.at(1)][conf.at(2)][conf.at(3)][conf.at(4)] == EMPTY_CELL) {
   int max_value = EMPTY_CELL;
   // go over possible sets of poker chip stacks
   for(int set_index = 1; set_index < 32; set_index++) {</pre>
     int color = EMPTY_CELL;
bool valid = true;
int removed = 0;
     vector < int > new_conf(5);
     // go over all stacks and decide if it is part of the set, if so do calculation
     for(int stack_index = 0; stack_index < 5; stack_index++) {</pre>
       if((set_index >> stack_index) & 1) { // stack is in the current set
         if(conf.at(stack_index) == 0) {
           // can't remove a chip from current stack
```

```
valid = false;
             break;
           if(color == EMPTY_CELL) {
             // set current color
             color = chips.at(stack_index).at(conf.at(stack_index) - 1);
           } else if(color != chips.at(stack_index).at(conf.at(stack_index) - 1)) {
             \ensuremath{//} color top of current stack not the same as we selected
             valid = false:
             break;
           new_conf.at(stack_index) = conf.at(stack_index) - 1;
         } else {
           new conf.at(stack index) = conf.at(stack index):
       if(valid) {
         int points = 0;
         if(removed > 1) {
         points = pow(2, removed - 2);
}
         int val = points + round(stack_count, stack_sizes, chips, table, new_conf);
max_value = max(max_value, val);
    table[conf.at(0)][conf.at(1)][conf.at(2)][conf.at(3)][conf.at(4)] = max_value;
  return table[conf.at(0)][conf.at(1)][conf.at(2)][conf.at(3)][conf.at(4)];
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int test count:
  cin >> test_count;
  for(int test_index = 0; test_index < test_count; test_index++) {</pre>
    int stack_count;
    cin >> stack_count;
    // read in size of each stack
    vector < int > stack_sizes(5, 0);
     vector<int> conf(5, 0);
    for(int stack_index = 0; stack_index < stack_count; stack_index++) {</pre>
       int chip_amount;
       cin >> chip_amount;
       stack_sizes.at(stack_index) = chip_amount;
       conf.at(stack_index) = chip_amount;
    // contains the chips of each stack at the start
vector<vector<int > > chips;
    chips.reserve(stack_count);
    for(int stack_index = 0; stack_index < stack_count; stack_index++) {
   chips.push_back(vector<int>(stack_sizes[stack_index], -1));
       for(int chip_index = 0; chip_index < stack_sizes[stack_index]; chip_index++) {
  cin >> chips.at(stack_index).at(chip_index);
    // create DP table, initial value is EMPTY_CELL
vector<vector<vector<vector<int > > > > table(stack_sizes[0] + 1,
       vector<vector<vector<int > > >(stack_sizes[1] + 1,
         vector<vector<int > > (stack_sizes[2] + 1,
           vector < vector < int > >(stack_sizes[3] + 1;
             vector < int > (stack_sizes[4] + 1, EMPTY_CELL)))));
    // initialise table
    table[0][0][0][0][0] = 0;
    // play the game
    cout << round(stack_count, stack_sizes, chips, table, conf) << endl;</pre>
 }
}
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <vector</pre>
#include <queue>
#include <set>
#include <vector</pre>
#include <vector</p>
#include
```

```
int max_stacks = 5;
vector <int> stack size:
vector < vector < int > > stacks;
vector < vector < vector < vector < int > > > > maximum;
int getMaximum(int first, int second, int third, int fourth, int fifth) {
   //cout << first << " " << second << " " << third << " " << fourth << " " << fifth << endl;
   if (maximum[first][second][third][fourth][fifth] == -1) {</pre>
     for (int i = 0; i < 2; i++) {
  if (first - i < 0) continue;</pre>
        for (int j = 0; j < 2; j++) {
   if (second - j < 0) continue;
   for (int k = 0; k < 2; k++) {
      if (third - k < 0) continue;
}</pre>
             for (int 1 = 0; 1 < 2; 1++) {
                for (int m = 0; m < 2; m++) {
   if (foirth - 1 < 0) continue;
   if (fifth - m < 0) continue;</pre>
                  int chips_to_remove = i + j + k + 1 + m;
if (chips_to_remove == 0) continue;
                  int chip = -1;
if (i == 1) {
    //cout << "Setting chip to " << stacks[0][first-1] << endl;
    chip = stacks[0][first - 1];</pre>
                   if (j == 1) {
                     if (chip == -1) {
   chip = stacks[1][second - 1];
                      else {
                        // cout << "Compare to " << stacks[1][second-1] << endl;
if (chip != stacks[1][second - 1]) continue;</pre>
                     }
                   if (k == 1) {
                     if (chip == -1) {
                        chip = stacks[2][third - 1];
                      else {
                        if (chip != stacks[2][third - 1]) continue;
                     }
                  }
                   if (1 == 1) {
                     if (chip == -1) {
  chip = stacks[3][fourth - 1];
                        if (chip != stacks[3][fourth - 1]) continue;
                     }
                  }
                   if (m == 1) {
                     if (chip == -1) {
                       chip = stacks[4][fifth - 1];
                      else {
                        if (chip != stacks[4][fifth - 1]) continue;
                     }
                   //cout << "Maximum for: " << first-i << " " << second-j << " " << third-k << " " << fourth-l << " " <
                         fifth-m << endl;
                   int newMax = getMaximum(first - i, second - j, third - k, fourth - 1, fifth - m);
                   if (chips_to_remove > 1) {
                     //cout << "Updataing for: " << first << " " << second << " " << third << " " << fourth << " " << fifth <<
                            endl;
                      //cout << "By: " << (1 << (chips_to_remove-2)) << endl;
                     newMax += 1 << (chips_to_remove - 2);</pre>
                   maximum[first][second][third][fourth][fifth] = max(maximum[first][second][third][fourth][fifth], newMax);
            }
          }
       }
    }
  }
  return maximum[first][second][third][fourth][fifth];
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
     int nr_stacks;
     cin >> nr_stacks;
     stack_size = vector < int > (max_stacks);
for (int i = 0; i < nr_stacks; i++) {</pre>
       cin >> stack_size[i];
     for (int i = nr_stacks; i < max_stacks; i++) {</pre>
```

```
stack_size[i] = 0;
}
stacks = vector<vector<int>>(max_stacks);
for (int i = 0; i < nr_stacks; i++) {
    stacks[i] = vector<int>>(stack_size[i]);
    for (int j = 0; j < stack_size[i]; j++) {
        cin >> stacks[i][j];
    }
}
for (int i = nr_stacks; i < max_stacks; i++) {
    stacks[i] = vector<int>>();
}

maximum = vector<vector<vector<vector<vector<vector<int>>>>(
    stack_size[0] + 1,
    vector<vector<vector<int>>>>(
    stack_size[1] + 1,
    vector<vector<vector<int>>>(
    stack_size[2] + 1,
    vector<vector<int>>(
    stack_size[3] + 1,
    vector<vector<int>>(
    stack_size[3] + 1,
    vector<int>>(
    stack_size[3] + 1,
    vector<int>>(stack_size[4] + 1, -1))));
    maximum[0][0][0][0][0] = 0;
    cout << getMaximum(stack_size[0], stack_size[1], stack_size[2], stack_size[3], stack_size[4]) << endl;
}
return 0;
}</pre>
```

3 BGL Introduction

3.1 Building a Graph

Keywords: Shortest path, Spanning tree, Graph with edge weight map

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/dijkstra_shortest_paths.hpp>
#include <boost/graph/kruskal_min_spanning_tree.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, undirectedS, no_property, property<edge_weight_t, int> > Graph;
typedef graph_traits<Graph>::vertex_descriptor Vertex;
typedef graph_traits < Graph > :: edge_descriptor Edge;
int main() {
  cin.svnc with stdio(false):
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
     //read graph
     int nr_vertices, nr_edges;
     cin >> nr_vertices >> nr_edges;
     Graph g(nr_vertices);
     property_map < Graph , edge_weight_t >:: type weight_map = get(edge_weight , g);
for (int i = 0; i < nr_edges; i++) {</pre>
       int v1, v2, weight;
cin >> v1 >> v2 >> weight;
       bool success;
       Edge e;
       tie(e, success) = add_edge(v1, v2, g);
weight_map[e] = weight;
     vector < Edge > spanning_tree;
     kruskal_minimum_spanning_tree(g, back_inserter(spanning_tree));
     int total_spanning_tree_edge_weight = 0;
     for (vector < Edge > :: iterator it = spanning_tree.begin(); it != spanning_tree.end(); ++it) {
       total_spanning_tree_edge_weight += get(weight_map, *it);
     vector<int> distances(num_vertices(g));
    dijkstra_shortest_paths(g, 0, distance_map(&distances[0]));
int max_distance = 0;
for (int i = 0; i < distances.size(); i++) {</pre>
       max_distance = max(max_distance, distances[i]);
     \verb|cout| << total_spanning_tree_edge_weight| << \verb|""| << max_distance| << endl; \\
  return 0;
}
```

3.2 Ant Challenge

Keywords: Spanning tree, Shortest path, Graph with edge index map

```
#include <iostream>
#include <vector>
#include <queue>
#include <tuple>
#include <cmath>
#include <climits>
#include <algorithm>
#include <climits>
#include <climits>

#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/kruskal_min_spanning_tree.hpp>
#include <boost/graph/dijkstra_shortest_paths.hpp>
using namespace std;
using namespace boost;

typedef adjacency_list<vecS, vecS, undirectedS, no_property, property<edge_index_t, int> > Graph;
```

```
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits < Graph > :: vertex_descriptor Vertex;
int main(void)
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test_cases;
    cin >> test_cases;
    for(int i = 0; i < test_cases; i++) {</pre>
         int vertices, edges, species, start, end;
         cin >> vertices;
         cin >> edges;
         cin >> species;
         cin >> start;
         cin >> end;
         Graph graph(vertices);
         property_map < Graph , edge_index_t >:: type indices = get(edge_index , graph);
         vector<vector<int > > weights(species, vector<int>(edges, -1));
         for(int j = 0; j < edges; j++) {</pre>
             int from, to;
             cin >> from;
             cin >> to:
             // add edge
             bool success;
             Edge edge;
             tie(edge, success) = add_edge(from, to, graph);
             indices[edge] = j;
             for(int k = 0: k < species: k++) {
                  int species_weight;
                  cin >> species_weight;
                  // set weight
                  weights[k][j] = species_weight;
             }
         // no reason to know where the hives are...
         int ignore;
for(int k = 0; k < species; k++) {</pre>
             cin >> ignore;
         // find minimum spanning for each species
         vector<int> spanning_tree_weights(edges, numeric_limits<int>::max());
for(int k = 0; k < species; k++) {</pre>
             vector < Edge > spanning_tree;
             kruskal_minimum_spanning_tree(graph, back_inserter(spanning_tree), weight_map(make_iterator_property_map(
                  weights[k].begin(), indices)));
             for(vector<Edge>::iterator spanning_tree_edge = spanning_tree.begin(); spanning_tree_edge != spanning_tree.
                  end(); ++spanning_tree_edge) {
                 if(weights[k][indices[*spanning_tree_edge]] < spanning_tree_weights[indices[*spanning_tree_edge]]) {
    spanning_tree_weights[indices[*spanning_tree_edge]] = weights[k][indices[*spanning_tree_edge]];</pre>
             }
         // now we have a minimal spanning tree we can use to find the shortest path from start to end
         vector < Vertex > predecessors(num_vertices(graph));
         vector<int> distances(num_vertices(graph));
         dijkstra_shortest_paths(graph, start, predecessor_map(&predecessors[0]).distance_map(&distances[0]).weight_map(
              make_iterator_property_map(&spanning_tree_weights[0], indices)));
         // ok, now we can read out the path length
cout << distances[end] << endl;</pre>
    return 0;
}
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <set>
#include <map>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/dijkstra_shortest_paths.hpp>
#include <boost/graph/dijkstra_shortest_paths.hpp>
#include <boost/graph/kruskal_min_spanning_tree.hpp>
#include <boost/property_map/transform_value_property_map.hpp>

using namespace std;
using namespace boost;
```

```
typedef adjacency_list<vecS, vecS, undirectedS, no_property, property<edge_index_t, int> > Graph;
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits < Graph > :: vertex_descriptor Vertex;
typedef adjacency_list<vecS, vecS, undirectedS, no_property, property<edge_weight_t, vector<int> > > Graph;
typedef graph_traits<Graph>::vertex_descriptor Vertex;
typedef graph_traits<Graph>::edge_descriptor Edge;
struct get_weight {
 int species_id;
  get_weight(int species_id) : species_id(species_id) {}
  typedef int result_type;
 int operator()(vector<int> x) const {return x[0];}
class record_edges : public dijkstra_visitor<>
  public:
  record_edges(map<int, Edge>& edges)
  : edges(edges) { }
  template <class Edge, class Graph>
 void edge_relaxed(Edge e, Graph& g) {
  cout << "bla" << endl;</pre>
   edges[target(e, g)] = e;
 protected:
 map<int, Edge>& edges;
struct VertexInformation
 typedef boost::vertex_property_type type;
record_edges use_edges_visitor(use_edges);
dijkstra_shortest_paths(g, hives[i], weight_map(make_transform_value_property_map(get_weight(i), get(edge_weight, g))).
     visitor(use_edges_visitor));
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_vertices, nr_edges, nr_species, start_edge, end_edge;
    cin >> nr_vertices >> nr_edges >> nr_species >> start_edge >> end_edge;
    Graph g(nr_vertices);
    property_map < Graph, edge_index_t >:: type ind = get(edge_index, g);
vector < vector < int > graph_species_weights(nr_species, vector < int > (nr_edges));
    for (int i = 0; i < nr_edges; i++) {</pre>
      int v1, v2;
vector<int> weights(nr_species);
       cin >> v1 >> v2;
for (int j = 0; j < nr_species; j++) {
        cin >> graph_species_weights[j][i];
       bool success;
       Edge e;
      tie(e, success) = add_edge(v1, v2, g);
ind[e] = i;
    vector < int > hives(nr_species);
for (int i = 0; i < nr_species; i++) {</pre>
      cin >> hives[i];
    vector<int> edge_weights(nr_edges, numeric_limits<int>::max());
for (int i = 0; i < nr_species; i++) {</pre>
       vector < Edge > spanning_tree;
       kruskal_minimum_spanning_tree(g, back_inserter(spanning_tree), weight_map(make_iterator_property_map(
            graph_species_weights[i].begin(), ind)));
       for (vector < Edge >:: iterator ei = spanning_tree.begin(); ei != spanning_tree.end(); ++ei) {
         edge_weights[ind[*ei]] = min(edge_weights[ind[*ei]], graph_species_weights[i][ind[*ei]]);
      }
    vector<int> distances(num_vertices(g), numeric_limits<int>::max());
dijkstra_shortest_paths(g, start_edge, distance_map(&distances[0]).weight_map(make_iterator_property_map(&
         edge_weights[0], ind)));
    cout << distances[end_edge] << endl;</pre>
  return 0;
```

3.3 Important Bridges

Keywords: Articulation points, Biconnected components

```
#include <iostream>
#include <vector>
#include <queue>
#include <tuple>
#include <cmath>
#include <climits>
#include <algorithm>
#include <climits>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/biconnected_components.hpp>
#define ISLAND 1
#define BRIDGE 2
using namespace std;
using namespace boost;
typedef adjacency_list < vecS, vecS, undirectedS, no_property, no_property > Graph;
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
int main(void)
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test_cases;
    cin >> test_cases;
    for(int i = 0; i < test_cases; i++) {</pre>
           read test case
         int islands, bridges;
         cin >> islands;
         cin >> bridges;
         // create graph for test case
         Graph graph(islands + bridges);
         // keep track which vertex is what
         vector<int> vertex_type(islands + bridges, -1);
         // keep track of bridges trough island pairs
         vector<pair<int, int> > bridge_to_island(bridges, make_pair(-1, -1));
         // set vertex properties
         for(int bridge_vertex = 0; bridge_vertex < bridges; bridge_vertex++) {
   assert(vertex_type.at(bridge_vertex) == -1);</pre>
             vertex_type.at(bridge_vertex) = BRIDGE;
         for(int island_vertex = bridges + 1; island_vertex < bridges+islands; island_vertex++) {</pre>
             assert(vertex_type.at(island_vertex) == -1);
             vertex_type.at(island_vertex) = ISLAND;
         // read in bridges
         for(int k = 0; k < bridges; k++) {</pre>
             int from_island, to_island;
             cin >> from_island;
             cin >> to_island;
             // each bridge is also a vertices and connects both islands (also vertices) through edges
             // calculate vertices indexes first
             int from_island_index = bridges + from_island - 1; // input starts at 1, we start at 0
             int to_island_index = bridges + to_island - 1; // input starts at 1, we start at 0
             int bridge_index = k;
             // add edges:
                         bridge
              // from island to island
             bool success;
             Edge edge;
             tie(edge, success) = add_edge(from_island_index, bridge_index, graph);
tie(edge, success) = add_edge(to_island_index, bridge_index, graph);
              // keep track of islands the bridge connects
             bridge_to_island.at(bridge_index) = make_pair(from_island, to_island);
         // find the important bridges
         vector < Vertex > vertices;
         articulation_points(graph, back_inserter(vertices));
         set < pair < int , int >> out_bridges;
         for(vector < Vertex >:: iterator v2 = vertices.begin(); v2 != vertices.end(); ++v2) {
    //cout << "type: " << vertex_type[*v2] << " edge nr: " << *v2 << endl;
    // only if articulation point is a bridge, we're interested because it's an important bridge!</pre>
             if(vertex_type[*v2] == BRIDGE) {
                  pair < int , int > islands_connected_by_important_bridge = bridge_to_island.at(*v2);
```

```
\verb"out_bridges.insert(make_pair(min(islands_connected_by_important_bridge.first)", and the pair(min(islands_connected_by_important_bridge.first), and the pair(min(islands_connected_by_important_bridge.first)), and the pair(min(islands_connected_by_important_bridge_bridge_bridge_bridge_bridge_bridge_bridge_bridge_bri
                                                                                                                                       is lands\_connected\_by\_important\_bridge.second), \ max(is lands\_connected\_by\_important\_bridge.first, and the substitution of 
                                                                                                                                       islands_connected_by_important_bridge.second)));
                                                                            }
                                                     /*// print out the edges, sorted order
                                                     set<pair<int, int>> out_bridges;
                                                     for(vector < Vertex >:: iterator v2 = vertices.begin(); v2 != vertices.end(); ++v2) {
                                                                              //cout << "city: " << *v2 << endl;
                                                                              //sort(island_to_bridge[*v2].begin(), island_to_bridge[*v2].end());
for(vector<pair<int, int> >::iterator bridge_islands = island_to_bridge[*v2].begin(); bridge_islands !=
                                                                                                         island_to_bridge[*v2].end(); ++bridge_islands) {
//cout << (*bridge_islands).first << " " << (*bridge_islands).second << endl;
out_bridges.insert(make_pair(min((*bridge_islands).first, (*bridge_islands).second), max((*bridge_islands).second)</pre>
                                                                                                                                    ).first, (*bridge_islands).second)));
                                                                           }
                                                     cout << out_bridges.size() << endl;</pre>
                                                     for(pair<int, int> bout : out_bridges) {
   cout << bout.first << " " << bout.second << endl;</pre>
                         return 0;
}
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <map>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/dijkstra_shortest_paths.hpp>
#include <boost/graph/kruskal_min_spanning_tree.hpp>
#include <boost/property_map/transform_value_property_map.hpp>
#include <boost/graph/boyer_myrvold_planar_test.hpp>
#include <boost/graph/biconnected_components.hpp>
using namespace std;
using namespace boost;
struct edge_component_t {
  enum
    num = 555
  }:
  typedef edge_property_tag kind;
} edge_component;
typedef adjacency_list<vecS, vecS, undirectedS, no_property, property<edge_component_t, size_t> > Graph;
typedef graph_traits < Graph > :: edge_descriptor Edge;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
typedef property_map < Graph , vertex_index_t > :: type IndexMap;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_vertices, nr_edges;
    cin >> nr_vertices >> nr_edges;
    Graph g(nr_vertices + 1);
    for (int i = 0; i < nr_edges; i++) {</pre>
      int v1, v2;
       cin >> v1 >> v2;
      bool success;
      Edge e;
      tie(e, success) = add_edge(v1, v2, g);
    property_map < Graph , edge_component_t > :: type component = get(edge_component , g);
    size_t nr_components = biconnected_components(g, component);
    vector<int> component_edges(nr_components, -1);
    graph_traits < Graph >:: edge_iterator ei, ei_end;
for (tie(ei, ei_end) = edges(g); ei != ei_end; ++ei) {
       size_t edge_component_id = component[*ei];
      if (component_edges[edge_component_id] == -1) {
        component_edges[edge_component_id] = 1;
      else {
         component_edges[edge_component_id] = -2;
```

```
vector<pair<int, int> > bridges = vector<pair<int, int> >();
IndexMap index = get(vertex_index, g);
for (tie(ei, ei_end) = edges(g); ei != ei_end; ++ei) {
    size_t edge_component_id = component[*ei];
    if (component_edges[edge_component_id] == 1) {
        int source_ind = index[source(*ei, g)];
        int target_ind = index[target(*ei, g)];
        bridges.push_back(make_pair(min(source_ind, target_ind), max(source_ind, target_ind)));
    }
} sort(bridges.begin(), bridges.end());
cout << bridges.size() << endl;
for (vector<pair<int, int> >::iterator b_it = bridges.begin(); b_it != bridges.end(); ++b_it) {
        cout << b_it->first << " " << b_it->second << endl;
}

return 0;
}
</pre>
```

3.4 Shy Programmers

Keywords: Planarity

```
#include <iostream>
#include <vector>
#include <queue>
#include <tuple>
#include <cmath>
#include <climits>
#include <algorithm>
#include <climits>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/boyer_myrvold_planar_test.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, undirectedS, no_property, no_property> Graph;
typedef graph_traits < Graph >:: edge_descriptor Edge;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
int main(void)
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test_cases;
    cin >> test_cases;
    for(int i = 0; i < test_cases; i++) {</pre>
        // read test case
        int employee_count, friendship_count;
        cin >> employee_count;
        cin >> friendship_count;
        // create graph for test case
        Graph graph(employee_count + 1);
        // add personal door edge
        for(int k = 0; k < employee_count; k++) {</pre>
             bool success;
             Edge edge;
             tie(edge, success) = add_edge(k, employee_count + 1, graph);
        // add friendship connections
for(int k = 0; k < friendship_count; k++) {
   int friend_A, friend_B;</pre>
             cin >> friend_A;
             cin >> friend_B;
             bool success;
             Edge edge;
             tie(edge, success) = add_edge(friend_A, friend_B, graph);
        if(boyer_myrvold_planarity_test(graph)) {
             cout << "yes" << endl;</pre>
        } else {
             cout << "no" << endl;
    return 0;
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <map>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/dijkstra_shortest_paths.hpp>
#include <boost/graph/kruskal_min_spanning_tree.hpp>
#include <boost/property_map/transform_value_property_map.hpp>
#include <boost/graph/boyer_myrvold_planar_test.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, undirectedS, no_property, no_property> Graph;
typedef graph_traits < Graph > :: edge_descriptor Edge;
typedef graph_traits<Graph>::vertex_descriptor Vertex;
int main() {
 cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
 int nr_test_cases;
 cin >> nr_test_cases;
 for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_vertices, nr_edges;
    cin >> nr_vertices >> nr_edges;
    Graph g(nr_vertices + 1);
    for (int i = 0; i < nr_edges; i++) {</pre>
      int v1, v2;
cin >> v1 >> v2;
      bool success;
      Edge e;
      tie(e, success) = add_edge(v1, v2, g);
   for (int i = 0; i < nr_vertices; i++) {</pre>
      bool success;
      Edge e;
      tie(e, success) = add_edge(i, nr_vertices, g);
   if (boyer_myrvold_planarity_test(g)) {
      cout << "yes" << endl;</pre>
    else {
      cout << "no" << endl;
  return 0;
```

3.5 Fluid Borders

Keywords: Planarity

```
#include <iostream>
#include <vector>
#include <queue>
#include <tuple>
#include <cmath>
#include <climits>
#include <algorithm>
#include <climits>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/boyer_myrvold_planar_test.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, undirectedS, no_property, no_property> Graph;
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
int main(void)
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test_cases;
    cin >> test_cases;
    for(int i = 0; i < test_cases; i++) {</pre>
```

```
int meta_blob_count;
       cin >> meta_blob_count;
       // create graph
       Graph graph(meta_blob_count);
       // read in election results
       vector<vector<int> > election_results(meta_blob_count, vector<int>(meta_blob_count - 1, -1));
       voting_meta_blob '
               cin >> election_results.at(voting_meta_blob).at(vote_place_index);
           }
       }
       int t = 0; // needed as result later
for(; t < meta_blob_count - 1; t++) {</pre>
           for(int voting_meta_blob = 0; voting_meta_blob < meta_blob_count; voting_meta_blob++) {
               // add edge for current place under check 't'
               Edge edge;
               tie(edge, tuples::ignore) = add_edge(voting_meta_blob, election_results.at(voting_meta_blob).at(t), graph
                  ):
           }
           // check if it's possible
           if(!boyer_myrvold_planarity_test(graph)) {
               break:
           }
       }
       cout << t << endl;
   return 0;
}
```

```
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <map>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/dijkstra_shortest_paths.hpp>
#include <boost/graph/kruskal_min_spanning_tree.hpp>
#include <boost/property_map/transform_value_property_map.hpp>
#include <boost/graph/boyer_myrvold_planar_test.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, undirectedS, no_property, no_property> Graph;
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits<Graph>::vertex_descriptor Vertex;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_vertices;
    cin >> nr_vertices;
    vector<vector<int> > election_outcomes(nr_vertices, vector<int>(nr_vertices - 1));
    for (int j = 0; j < nr_vertices; i++) {
for (int j = 0; j < nr_vertices - 1; j++) {
         cin >> election_outcomes[i][j];
      }
    7
    int t = 0;
    Graph g(nr_vertices);
for (int i = 0; i < nr_vertices - 1; i++) {
  for (int j = 0; j < nr_vertices; j++) {</pre>
         bool success;
         Edge e;
         tie(e, success) = add_edge(j, election_outcomes[j][i], g);
       if (boyer_myrvold_planarity_test(g)) {
         t++;
       }
       else {
         break;
    cout << t << endl;</pre>
  }
```

return 0;

4 Flows and Matchings

4.1 Buddies Selection

Keywords: Matching, Match size

```
#include <iostream>
#include <vector>
#include <queue>
#include <tuple>
#include <cmath>
#include <climits>
#include <algorithm>
#include <climits>
#include <string>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/max_cardinality_matching.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, undirectedS> Graph;
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
int main(void)
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test cases:
    cin >> test_cases;
    for(int i = 0; i < test_cases; i++) {</pre>
         // read test case
         int student_count, characteristic_count, min_solution;
         cin >> student_count >> characteristic_count >> min_solution;
         // create graph for test case
         Graph graph(student_count);
         // create a set of characteristics for each student from input
         map<int, set<string> > student_to_characs;
         for(int student_i = 0; student_i < student_count; student_i++) {
    set<string> charac_set;
              for(int j = 0; j < characteristic_count; j++) {</pre>
                   string charac_value;
                  cin >> charac_value;
                  //cout << "\tbla: " << charac_value << endl;</pre>
                  charac_set.insert(charac_value);
              }
              student_to_characs[student_i] = charac_set;
         for(int k = 0; k < student_count; k++) {</pre>
              for(int p = k + 1; p < student_count; p++) {
    vector < string > intersec;
                  back_inserter(intersec));
                  //cout << "size A: " << student_to_characs.at(k).size() << endl;
//cout << "size B: " << student_to_characs.at(p).size() << endl;
//cout << "intersec size: " << intersec.size() << endl;</pre>
                  if(intersec.size() > min_solution) {
                       //cout << "added" << endl;
                       // more in common than minimum given, add edge between students
                       bool success;
                       Edge edge;
                       tie(edge, success) = add_edge(k, p, graph);
             }
         }
         // find matching
         vector < Vertex > mate(student_count);
         \tt checked\_edmonds\_maximum\_cardinality\_matching(graph\,,\,\,\&mate[0])\,;
         //cout << "size: " << matching_size(graph, &mate[0]) << endl; //cout << "half: " << (int)(student_count / 2) << endl;
         if(matching_size(graph, &mate[0]) == (int)(student_count / 2)) {
    cout << "not optimal" << endl;</pre>
         } else {
             cout << "optimal" << endl;</pre>
    }
```

```
return 0;
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <map>
#include <string>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/dijkstra_shortest_paths.hpp>
#include <boost/graph/kruskal_min_spanning_tree.hpp>
#include <boost/property_map/transform_value_property_map.hpp>
#include <boost/graph/boyer_myrvold_planar_test.hpp>
#include <boost/graph/max_cardinality_matching.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, undirectedS, no_property, no_property> Graph;
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_students, nr_char, min_common_char;
    cin >> nr_students >> nr_char >> min_common_char;
    map<string, int> char_map = map<string, int>();
    vector<vector<int> > student_chars(nr_students, vector<int>(nr_char));
    int next_char_id = 0;
    for (int i = 0; i < nr_students; i++) {</pre>
      for (int j = 0; j < nr_char; j++) {</pre>
         string charact;
         cin >> charact;
         map<string, int>::iterator it = char_map.find(charact);
         int char_id;
if (it == char_map.end()) {
   char_id = next_char_id;
           char_map[charact] = next_char_id++;
         else {
          char_id = it->second;
         student_chars[i][j] = char_id;
    for (int i = 0; i < nr_students; i++) {</pre>
      sort(student_chars[i].begin(), student_chars[i].end());
    Graph g(nr_students);
    for (int i = 0; i < nr_students; i++) {</pre>
      vector<int>& char_a = student_chars[i];
for (int j = i + 1; j < nr_students; j++) {
  vector<int>& char_b = student_chars[j];
         int common = 0;
         vector<int>::iterator a_it = char_a.begin();
         vector<int>::iterator b_it = char_b.begin();
         while (a_it != char_a.end() && b_it != char_b.end()) {
  if (*a_it == *b_it) {
             common++;
             ++a_it;
             ++b_it;
           else if (*a_it < *b_it) {</pre>
             ++a_it;
           else {
             ++b_it;
           }
         if (common > min_common_char) {
           bool success;
           Edge e;
           tie(e, success) = add_edge(i, j, g);
         }
      }
    vector < Vertex > mate(nr_students);
    edmonds_maximum_cardinality_matching(g, &mate[0]);
    bool success = true;
```

```
for (vector<Vertex>::iterator v_it = mate.begin(); v_it != mate.end(); ++v_it) {
    if (*v_it == graph_traits<Graph>::null_vertex()) {
        success = false;
        break;
    }
    if (success) {
        cout << "not optimal" << endl;
    }
    else {
        cout << "optimal" << endl;
    }
}

return 0;
}</pre>
```

4.2 Satellites

Keywords: Matching, DFS (Graph), Matching with DFS

```
#include <iostream>
#include <vector>
#include <queue>
#include <tuple>
#include <cmath>
#include <climits>
#include <algorithm>
#include <climits>
#include <string>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/max_cardinality_matching.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, undirectedS> Graph;
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
// code given
typedef graph_traits < Graph >:: out_edge_iterator OutEdgeIt;
void DFS(int u, Graph &G, vector<bool> &visited, vector<Vertex> &mate) {
    OutEdgeIt ebeg, eend;
    visited[u] = true:
    for (tie(ebeg, eend) = out_edges(u, G); ebeg != eend; ++ebeg) {
   const int v = target(*ebeg, G);
   // v not vis. && left to right with Non-Matching edges
         // right to left with Matching edges if (!visited[v] && (((v == mate[u]) != (u < v)))) {
             DFS(v, G, visited, mate);
    }
// END code given
int main(void)
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test_cases;
    cin >> test_cases;
    for(int i = 0; i < test_cases; i++) {</pre>
         // read test case
         int ground_count, satellite_count, link_count;
         cin >> ground_count >> satellite_count >> link_count;
         // create bipartit graph
Graph graph(ground_count + satellite_count);
         // read links and create edges for them
         for(int li = 0; li < link_count; li++) {</pre>
             int ground_index, satellite_index;
             cin >> ground_index >> satellite_index;
             bool success;
             Edge edge;
             tie(edge, success) = add_edge(ground_index, satellite_index + ground_count, graph);
         // find maximum matching
         vector < Vertex > mate(ground_count + satellite_count);
         checked_edmonds_maximum_cardinality_matching(graph, &mate[0]);
         // keep track of visited vertices
         vector <bool> visited(ground_count + satellite_count);
```

```
vector<int> startpoints;
//cout << "Matching:" << endl;
for (int i = 0; i < ground_count + satellite_count; ++i) {</pre>
               // output the matching
               if (mate[i] == graph_traits < Graph >:: null_vertex() && i < ground_count) {
                    startpoints.push_back(i);
               }
          7
          // run depth first visit
for (int i = 0; i < startpoints.size(); ++i) {</pre>
               DFS(startpoints[i], graph, visited, mate);
// END code given
          // collect unmarked
          vector<int> out_ground_ids;
vector<int> out_satellite_ids;
          for(int index = 0; index < ground_count + satellite_count; index++) {</pre>
               if(index < ground_count && !visited[index]) {
    //cout << "ground ID: " << index << endl;</pre>
                    out_ground_ids.push_back(index);
               } else if(index >= ground_count && visited[index]) {
   //cout << "satellite ID: " << index - ground_count << endl;</pre>
                    out_satellite_ids.push_back(index - ground_count);
               }
          }
          // NOTE: abstand am ende kein Problem! So kompliziertes spaces einfügen nicht noetig :)
          cout << out_ground_ids.size() << " " << out_satellite_ids.size() << endl;</pre>
          bool first = true;
for(int og : out_ground_ids) {
               if(!first) {
    cout << " ";</pre>
               } else {
                    first = false;
               cout << og;</pre>
          if(!first) {
          first = true;
for(int os : out_satellite_ids) {
               if(!first) {
                     cout << " ";
               } else {
                    first = false;
               cout << os;
          cout << endl;
     return 0;
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <map>
#include <string>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/dijkstra_shortest_paths.hpp>
#include <boost/graph/kruskal_min_spanning_tree.hpp>
#include <boost/property_map/transform_value_property_map.hpp>
#include <boost/graph/boyer_myrvold_planar_test.hpp>
#include <boost/graph/max_cardinality_matching.hpp>
#include <boost/graph/push_relabel_max_flow.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, undirectedS> Graph;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
typedef graph_traits < Graph > :: out_edge_iterator OutEdgeIt;
const Vertex NULL_VERTEX = graph_traits<Graph>::null_vertex();
void DFS(int u, Graph &G, vector<bool> &visited, vector<Vertex> &mate) {
 OutEdgeIt ebeg, eend;
visited[u] = true;
  for (tie(ebeg, eend) = out_edges(u, G); ebeg != eend; ++ebeg) {
```

```
const int v = target(*ebeg, G);
    // v not vis. & left to right with Non-Matching edges
// right to left with Matching edges
if (!visited[v] & (((v == mate[u]) != (u < v)))) {
      DFS(v, G, visited, mate);
 }
}
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_ground, nr_sat, nr_links;
    cin >> nr_ground >> nr_sat >> nr_links;
    int nr_vertices = nr_ground + nr_sat;
    Graph g(nr_vertices);
    for (int i = 0; i < nr_links; i++) {</pre>
       int ground_id, sat_id;
cin >> ground_id >> sat_id;
       add_edge(ground_id, nr_ground + sat_id, g);
    // maximum matching
    vector < Vertex > mate(nr_vertices);
    edmonds_maximum_cardinality_matching(g, &mate[0]);
    // starting points for VC
    vector < int > startpoints;
    //cout << "Matching:" << endl;
for (int i = 0; i < nr_vertices; ++i) {</pre>
       // output the matching
       if (mate[i] != NULL_VERTEX && i < nr_ground){</pre>
         //cout << i << " - " << mate[i] << endl;
// make unmatched L vertices the root vertices of DFS,</pre>
         // i.e. "mark as visited"
       else if (mate[i] == NULL_VERTEX && i < nr_ground) {</pre>
         startpoints.push_back(i);
    7
    // run depth first visit
    vector < bool > visited(nr_vertices + 1);
         (int i = 0; i < startpoints.size(); ++i) {
      DFS(startpoints[i], g, visited, mate);
    // output Minimum vertex cover
//cout << "Minimum Vertex Cover:" << endl;</pre>
    vector < int > monitored_ground;
    vector < int > monitored_station;
    for (int i = 0; i < nr_vertices; ++i) {
   if (visited[i] == 0 && i < nr_ground) {</pre>
         monitored_ground.push_back(i);
       else if (visited[i] > 0 && i >= nr_ground) {
         monitored_station.push_back(i - nr_ground);
    cout << monitored_ground.size() << " " << monitored_station.size() << endl;</pre>
    for (vector<int>::iterator it = monitored_ground.begin(); it != monitored_ground.end(); ++it) {
      cout << *it << "
    for (vector<int>::iterator it = monitored_station.begin(); it != monitored_station.end(); ++it) {
       cout << *it << " ";
    cout << endl;
  }
  return 0;
}
```

4.3 Coin Tossing

Keywords: Graph with edge capacity, Graph with residual capacity, Graph with reverse edges, Custom add edge function, Max-flow

```
#include <iostream>
#include <algorithm>
#include <vector>

#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/push_relabel_max_flow.hpp>
#include <boost/graph/edmonds_karp_max_flow.hpp>
#include <boost/tuple/tuple.hpp>

using namespace std;
```

```
using namespace boost;
typedef adjacency_list_traits<vecS, vecS, directedS> Traits;
typedef adjacency_list<vecS, vecS, directedS, no_property,
    property<edge_capacity_t, long,</pre>
    property < edge_residual_capacity_t , long ,</pre>
      property < edge_reverse_t, Traits::edge_descriptor> > > Graph;
typedef property_map < Graph , edge_capacity_t >: : type
                                                          EdgeCapacityMap;
typedef property_map <Graph, edge_residual_capacity_t>::type ResidualCapacityMap;
typedef graph_traits < Graph > :: edge_descriptor
                                                        Edge;
// Custom add_edge, also creates reverse edges with corresponding capacities.
void addEdge(int u, int v, long c, EdgeCapacityMap &capacity, ReverseEdgeMap &rev_edge, Graph &G) {
  Edge e, reverseE;
  tie(e, tuples::ignore) = add_edge(u, v, G);
  tie(reverseE, tuples::ignore) = add_edge(v, u, G);
capacity[e] = c;
  capacity[reverseE] = 0;
  rev_edge[e] = reverseE;
  rev_edge[reverseE] = e;
int main() {
  cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test_cases;
    cin >> test_cases;
    for(int i = 0; i < test_cases; i++) {</pre>
      int players, rounds;
       cin >> players >> rounds;
       // create graph and additional stuff
       Graph graph(players + rounds + 2);
    EdgeCapacityMap capacity = get(edge_capacity, graph);
ReverseEdgeMap rev_edge = get(edge_reverse, graph);
    ResidualCapacityMap res_capacity = get(edge_residual_capacity, graph);
    // source ans target vertex
    int source = players + rounds;
int target = players + rounds + 1;
       for(int roundIndex = 0; roundIndex < rounds; roundIndex++) {
  int playerA, playerB, outcome;</pre>
         cin >> playerA >> playerB >> outcome;
         int roundVertex = players + roundIndex;
            source -> round vertex
         addEdge(source, roundVertex, 1, capacity, rev_edge, graph);
         // round vertex -> player vertex representing possible wins
         if(outcome == 0) {
           // both might have won
         addEdge(roundVertex, playerA, 1, capacity, rev_edge, graph);
addEdge(roundVertex, playerB, 1, capacity, rev_edge, graph);
} else if(outcome == 1) {
           // player A won
           addEdge(roundVertex,
                                  playerA, 1, capacity, rev_edge, graph);
         } else if(outcome == 2) {
           // player B won
           addEdge(roundVertex, playerB, 1, capacity, rev_edge, graph);
       int totalPoints = 0;
       for(int playerIndex = 0; playerIndex < players; playerIndex++) {</pre>
         int points;
         cin >> points;
         totalPoints += points;
         // player vertex -> target
         addEdge(playerIndex, target, points, capacity, rev_edge, graph);
       long flowValue = push_relabel_max_flow(graph, source, target);
       if(flowValue == totalPoints && totalPoints == rounds) {
  cout << "yes" << endl;</pre>
      } else {
         cout << "no" << endl;
      }
    }
  return 0;
}
```

```
#include <iostream>
#include <vector>
```

```
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <map>
#include <string>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/dijkstra_shortest_paths.hpp>
#include <boost/graph/kruskal_min_spanning_tree.hpp>
#include <boost/property_map/transform_value_property_map.hpp>
#include <boost/graph/boyer_myrvold_planar_test.hpp>
#include <boost/graph/max_cardinality_matching.hpp>
#include <boost/graph/push_relabel_max_flow.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, directedS> Traits;
typedef adjacency_list<vecS, vecS, directedS, no_property, property<edge_capacity_t, long, property<
    edge_residual_capacity_t, long, property<edge_reverse_t, Traits::edge_descriptor> >> > Graph;
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
typedef property_map < Graph , edge_capacity_t >: : type EdgeCapacityMap;
typedef property_map < Graph , edge_reverse_t >:: type ReverseEdgeMap;;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr test cases:
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
     int nr_players, nr_rounds;
     cin >> nr_players >> nr_rounds;
     vector < int > winners:
     vector <pair <int, int > undecided;
for (int i = 0; i < nr_rounds; i++) {</pre>
       int player_a, player_b, c;
       cin >> player_a >> player_b >> c;
if (c == 0) {
         undecided.push_back(make_pair(player_a, player_b));
       else if (c == 1) {
         winners.push_back(player_a);
       else if (c == 2) {
         winners.push_back(player_b);
    vector < int > points(nr_players);
for (int i = 0; i < nr_players; i++) {</pre>
      cin >> points[i];
     //Remove certain results
     for (vector<int>::iterator it = winners.begin(); it != winners.end(); ++it) {
      points[*it]--;
     int total_points_needed = 0;
     bool possible = true;
     for (int i = 0; i < nr_players; i++) {</pre>
       if (points[i] < 0) {</pre>
         possible = false;
          break:
       total_points_needed += points[i];
     if (total_points_needed != undecided.size()) {
       possible = false;
     if (possible) {
       int nr_vertices = nr_players + undecided.size() + 2;
       int source = nr_vertices - 2;
       int sink = nr_vertices - 1;
       Graph g(nr_vertices);
       EdgeCapacityMap capacity = get(edge_capacity, g);
ReverseEdgeMap rev_edge = get(edge_reverse, g);
       for (int i = 0; i < undecided.size(); i++) {</pre>
          int edge_id = nr_players + i;
         Edge e, rev_e;
bool success;
          //add middle edges
          tie(e, success) = add_edge(edge_id, undecided[i].first, g);
          tie(rev_e, success) = add_edge(undecided[i].first, edge_id, g);
```

```
capacity[e] = 1;
         capacity[rev_e] = 0;
         rev_edge[e] = rev_e;
         rev_edge[rev_e] = e;
         tie(e, success) = add_edge(edge_id, undecided[i].second, g);
         tie(rev_e, success) = add_edge(undecided[i].second, edge_id, g);
         capacity[e] = 1;
         capacity[rev_e] = 0;
         rev_edge[e] = rev_e;
         rev_edge[rev_e] = e;
         tie(e, success) = add_edge(source, edge_id, g);
         tie(rev_e, success) = add_edge(edge_id, source, g);
         capacity[e] = 1;
        capacity[rev_e] = 0;
        rev_edge[e] = rev_e;
        rev_edge[rev_e] = e;
      int total_need = 0;
for (int i = 0; i < nr_players; i++) {
  if (points[i] <= 0) {</pre>
          continue;
        Edge e, rev_e;
         bool success;
        tie(e, success) = add_edge(i, sink, g);
        tie(rev_e, success) = add_edge(sink, i, g);
capacity[e] = points[i];
         capacity[rev_e] = 0;
         rev_edge[e] = rev_e;
        rev_edge[rev_e] = e;
      possible = (total_points_needed == push_relabel_max_flow(g, source, sink));
    if (possible) {
      cout << "yes" << endl;</pre>
    else {
      cout << "no" << endl;
 }
  return 0:
}
```

4.4 Kingdom Defence

Keywords: Graph with edge capacity, Graph with residual capacity, Graph with reverse edges, Max-flow, Custom add edge function inlined by hand

```
#include <iostream>
#include <vector>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/push_relabel_max_flow.hpp>
#include <algorithm>
#include <boost/tuple/tuple.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, directedS> Traits;
typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
                               property<edge_capacity_t, long,
property<edge_residual_capacity_t, long,</pre>
                               property < edge_reverse_t, Traits::edge_descriptor> > > Craph;
typedef property_map < Graph , edge_capacity_t > :: type EdgeCapacityMap;
typedef property_map < Graph, edge_reverse_t >:: type ReverseEdgeMap;
typedef property_map < Graph , edge_residual_capacity_t>::type ResidualCapacityMap;
typedef graph_traits<Graph>::edge_descriptor Edge;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
 int test_count;
  cin >> test_count;
 for(int test = 0; test < test_count; test++) {</pre>
    int location_count, path_count;
    cin >> location_count >> path_count;
    // create graph
Graph graph(location_count + 2); // don't forget source and sink
    EdgeCapacityMap capacity = get(edge_capacity, graph);
ReverseEdgeMap rev_edge = get(edge_reverse, graph);
    ResidualCapacityMap res_capacity = get(edge_residual_capacity, graph);
```

```
// define source and sink vertex
    int source = location_count;
    int sink = location_count + 1;
    // holds locations, first element of pair is the amount of soldier it has and
    // the seond the amount it needs
    vector < pair < int , int > > locations (location_count);
    for(int location_index = 0; location_index < location_count; location_index++) {</pre>
      int has_soldiers, needs_soliders;
      cin >> has_soldiers >> needs_soliders;
      locations.at(location_index) = make_pair(has_soldiers, needs_soliders);
    // read in paths for soldiers
for(int path_index = 0; path_index < path_count; path_index++) {</pre>
      int from, to, min_soldiers, max_soldiers;
       cin >> from >> to >> min_soldiers >> max_soldiers;
      // modify how many soldiers a location needs
       // it needs more soldiers as some of them must move on to the next city
      locations.at(from).second += min_soldiers;
       // needs less soldiers, as it will for sure get some from the current path!
      locations.at(to).second -= min_soldiers;
       // add edge
      Edge edge, r_edge;
      tie(edge, tuples::ignore) = add_edge(from, to, graph);
      tie(r_edge, tuples::ignore) = add_edge(to, from, graph);
// we already basically moved the minimum amount of soldiers above by modifieng the locations
       // we therefore are interested in the rest that might move over the path and can compare the resulting
       // flow with the expected sum of soldiers
      capacity[edge] = max_soldiers - min_soldiers;
capacity[r_edge] = 0;
      rev_edge[edge] = r_edge;
      rev_edge[r_edge] = edge;
    // add edges from the source to the city, with its "have soldiers" weights
for(int location_index = 0; location_index < location_count; location_index++) {</pre>
      Edge edge, r_edge;
      tie(edge, tuples::ignore) = add_edge(source, location_index, graph);
      tie(r_edge, tuples::ignore) = add_edge(location_index, source, graph);
       capacity[edge] = locations.at(location_index).first;
      capacity[r_edge] = 0;
      rev_edge[edge] = r_edge;
      rev_edge[r_edge] = edge;
    // add edges from the city to the sink with the city's "needs soldiers" weights
    // also keep track how much we need in total
    int need total = 0:
    for(int location_index = 0; location_index < location_count; location_index++) {</pre>
      int needs = locations.at(location_index).second;
      if(needs <= 0) {
        continue;
      Edge edge, r_edge;
tie(edge, tuples::ignore) = add_edge(location_index, sink, graph);
      tie(r_edge, tuples::ignore) = add_edge(sink, location_index, graph);
      capacity[edge] = needs;
      capacity[r_edge] = 0;
      rev_edge[edge] = r_edge;
      rev_edge[r_edge] = edge;
      need_total += needs;
    }
    // do max flow
    int max = push_relabel_max_flow(graph, source, sink);
    // check if it corresponds to the expected amount (at least)
    if(max >= need_total) {
  cout << "yes" << endl;</pre>
    } else {
      cout << "no" << endl;
 }
  return 0;
}
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <set>
#include <set>
#include <string>
```

```
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/dijkstra_shortest_paths.hpp>
#include <boost/graph/kruskal_min_spanning_tree.hpp>
#include <boost/property_map/transform_value_property_map.hpp>
#include <boost/graph/boyer_myrvold_planar_test.hpp>
#include <boost/graph/max_cardinality_matching.hpp>
#include <boost/graph/push_relabel_max_flow.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, directedS> Traits;
typedef adjacency_list<vecS, vecS, directedS, no_property, property<edge_capacity_t, long, property<
    edge_residual_capacity_t, long, property<edge_reverse_t, Traits::edge_descriptor> >> > Graph;
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
typedef property_map < Graph , edge_capacity_t >:: type EdgeCapacityMap;
typedef property_map < Graph , edge_reverse_t >: : type ReverseEdgeMap;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_locations, nr_paths;
     cin >> nr_locations >> nr_paths;
     Graph g(nr_locations + 2);
     int source = nr locations:
     int sink = nr_locations + 1;
     EdgeCapacityMap capacity = get(edge_capacity, g);
     ReverseEdgeMap rev_edge = get(edge_reverse, g)
    //first -> nr_stationed, second -> nr_needed
vector<pair<int, int> > locations(nr_locations);
for (int i = 0; i < nr_locations; i++) {</pre>
       int nr_stationed, nr_needed;
       cin >> nr_stationed >> nr_needed;
       locations[i] = make_pair(nr_stationed, nr_needed);
     for (int i = 0; i < nr_paths; i++) {</pre>
       int from, to, min, max; //from, to can be equal!
       cin >> from >> to >> min >> max;
       locations[from].second += min;
       locations[to].second -= min;
       Edge e, rev_e;
       bool success;
       tie(e, success) = add_edge(from, to, g);
       tie(rev_e, success) = add_edge(to, from, g);
       capacity[e] = max - min;
       capacity[rev_e] = 0;
rev_edge[e] = rev_e;
       rev_edge[rev_e] = e;
    for (int i = 0; i < nr_locations; i++) {</pre>
       Edge e, rev_e;
       bool success;
       tie(e, success) = add_edge(source, i, g);
       tie(rev_e, success) = add_edge(i, source, g);
       capacity[e] = locations[i].first;
capacity[rev_e] = 0;
rev_edge[e] = rev_e;
       rev_edge[rev_e] = e;
     int total_need = 0;
    for (int i = 0; i < nr_locations; i++) {
  if (locations[i].second < 0) {</pre>
         locations[i].second = 0;
       Edge e, rev_e;
       bool success;
       tie(e, success) = add_edge(i, sink, g);
       tie(rev_e, success) = add_edge(sink, i, g);
       capacity[e] = locations[i].second;
       capacity[rev_e] = 0;
       rev_edge[e] = rev_e;
       rev_edge[rev_e] = e;
total_need += locations[i].second;
    int max = push_relabel_max_flow(g, source, sink);
```

```
if (max >= total_need) {
    cout << "yes" << endl;
}
else {
    cout << "no" << endl;
}

return 0;
}</pre>
```

4.5 The Great Game

Keywords: Dynamic Programming

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <map>
#include <string>
using namespace std;
int get_min_moves(int start, vector<vector<int> >&trans, vector<int>& min_fields, vector<int>& max_fields, int
     field count):
int get_max_moves(int start, vector<vector<int> %trans, vector<int> % min_fields, vector<int> % max_fields, int
     field_count) {
    // if we reached the end, nothing can be doen
    if(start == field_count - 1) {
        return 0;
    // only calculate if value unknown
    if(max_fields.at(start) == -1) {
         // keeps track of the maximum amount of steps needed to reach the end from the given starting point
         int cur_max_found = -1;
        // iterate over all edges one can follow at the 'start' p
for(vector<int>::iterator iter = trans.at(start).begin();
                                                                      position
             iter != trans.at(start).end();
             ++iter) {
             // now we search for the largest minimum amount of steps needed to reach the end
             int possible_max = get_min_moves(*iter, trans, min_fields, max_fields, field_count);
if(possible_max > cur_max_found) {
                 cur_max_found = possible_max;
        // update value
        max_fields.at(start) = cur_max_found + 1; // we still have to take the edge we followed
     // return solution
    return max_fields.at(start);
}
int get min moves(int start, vector<vector<int> %trans, vector<int>% min fields, vector<int>% max fields, int
     field_count) {
       if we reached the end, no more moves needed
    if(start == field_count - 1) {
        return 0;
    // only calculate if we don't know the solution yet
    if (min_fields.at(start) == -1) {
        // search for the minimum amount of moves to win from the current starting point
         int cur_min_found = numeric_limits <int>::max();
         // iterate over all possible next moves, i.e. the edges leaving the starting position
         for(vector<int>::iterator iter = trans.at(start).begin();
             iter != trans.at(start).end();
             ++iter) {
             // 'iter' refers now to the edge we can follow, i.e. the next position we reach
             // now we have to assume that our opponent will be in our way and make our life complicated. // search for the maximum of moves from the next point we can reach to the finish line.
             int possible_min = get_max_moves(*iter, trans, min_fields, max_fields, field_count);
             if(possible_min < cur_min_found) {</pre>
                 cur_min_found = possible_min;
        min_fields.at(start) = cur_min_found + 1; // we still have to use the edge, so add one
    // return solution
    return min_fields.at(start);
}
```

```
int main() {
 cin.svnc with stdio(false):
    cout.sync_with_stdio(false);
    int test_cases;
   cin >> test_cases;
    for(int i = 0: i < test cases: i++) {</pre>
        // read in basic information
        int position_count, transition_count;
        cin >> position_count >> transition_count;
        int start_red, start_black;
        cin >> start_red >> start_black;
        start_red -= 1; start_black -= 1; // let it start with 0, not 1
        // read in the possible transitions
        vector < vector < int > > trans(position_count, vector < int >());
        for(int transition_index = 0; transition_index < transition_count; transition_index++) {</pre>
            int from, to;
cin >> from >> to;
            from -= 1; to -= 1; // let it start at 0
            // create transition, it's directed!
            trans.at(from).push_back(to);
        vector < int > min_fields (position_count, -1);
        vector < int > max_fields (position_count, -1);
        int red_min = get_min_moves(start_red, trans, min_fields, max_fields, position_count);
        int black_min = get_min_moves(start_black, trans, min_fields, max_fields, position_count);
        // now we calculate the minimum amount of games each of the players does
        int min_sherlock = -1;
        int min_moriarty = -1;
        // check if the steps needed to win with the red meeple is even \dots
        if(red_min % 2 == 0) {
            // ... ok it is even. Now we have to find out how many game steps were needed to
            // move the red meeple to the target position, as every second move sherlock moves the
            // black and not the red meeple
            min_sherlock = ((red_min - 2) / 2) * 4 + 4;
        } else {
           min_sherlock = ((red_min - 1) / 2) * 4 + 1;
        if(black_min % 2 == 0) {
            min_moriarty = ((black_min - 2) / 2) * 4 + 3;
        } else {
            min_moriarty = ((black_min - 1) / 2) * 4 + 2;
        if(min_sherlock < min_moriarty) {</pre>
            cout << 0 << end1;
        } else {
            cout << 1 << endl;
 return 0;
}
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <map>
#include <string>
using namespace std;
int last_position;
vector < vector < int > > field;
vector < int > min_field;
vector < int > max_field;
int getMax(int pos);
int getMin(int pos) {
 if (pos == last_position) {
   return 0;
  if (min_field[pos] == -1) {
    int cur_min = numeric_limits < int >:: max();
    for (vector<int>::iterator it = field[pos].begin(); it != field[pos].end(); ++it) {
      int new_min = getMax(*it);
      if (new_min < cur_min) {</pre>
        cur_min = new_min;
```

```
min_field[pos] = cur_min + 1;
  return min_field[pos];
int getMax(int pos) {
 if (pos == last_position) {
   return 0;
 if (max_field[pos] == -1) {
    int cur_max = -1;
    for (vector<int>::iterator it = field[pos].begin(); it != field[pos].end(); ++it) {
      int new_max = getMin(*it);
if (new_max > cur_max) {
        cur_max = new_max;
    max_field[pos] = cur_max + 1;
 1
  return max_field[pos];
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_positions, nr_transitions;
    cin >> nr_positions >> nr_transitions;
    last_position = nr_positions - 1;
    int r_start, b_start;
    cin >> r_start >> b_start;
    //adjust starting position
    r_start--;
    b_start--;
    field = vector<vector<int> >(nr_positions, vector<int>());
    for (int i = 0; i < nr_transitions; i++) {
  int from, to;
      cin >> from >> to;
      from --:
      to--:
      field[from].push_back(to);
    min_field = vector<int>(nr_positions, -1);
    max_field = vector < int > (nr_positions, -1);
    int r_min = getMin(r_start);
int b_min = getMin(b_start);
    if (r_min % 2 == 1) {
     r_min = ((r_min - 1) / 2) * 4 + 1;
    else {
     r_min = ((r_min - 2) / 2) * 4 + 4;
    if (b_min % 2 == 1) {
      b_min = ((b_min - 1) / 2) * 4 + 2;
     b_min = ((b_min - 2) / 2) * 4 + 3;
    if (r_min < b_min) {</pre>
     cout << 0 << endl;
    else {
      cout << 1 << endl;
    }
 }
 return 0:
```

4.6 Surveillance Photographs

Keywords: Graph with edge capacity, Graph with residual capacity, Graph with reverse edges, Custom add edge function, Max-flow

```
#include <iostream>
#include <algorithm>
#include <vector>

#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/push_relabel_max_flow.hpp>
```

```
#include <boost/graph/edmonds_karp_max_flow.hpp>
#include <boost/tuple/tuple.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list_traits<vecS, vecS, directedS> Traits;
typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
 property < edge_capacity_t , long ,</pre>
    property < edge_residual_capacity_t, long,
    property < edge_reverse_t, Traits::edge_descriptor> > > > Graph;
typedef property_map <Graph, edge_capacity_t>::type EdgeCapacityMap;
typedef property_map <Graph, edge_residual_capacity_t>::type ResidualCapacityMap;
typedef property_map <Graph, edge_reverse_t>::type ReverseEdgeMap;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
typedef graph_traits < Graph > :: edge_descriptor Edge;
// Custom add_edge, also creates reverse edges with corresponding capacities.
void addEdge(int u, int v, long c, EdgeCapacityMap &capacity, ReverseEdgeMap &rev_edge, Graph &G) {
 Edge e, reverseE;
  tie(e, tuples::ignore) = add_edge(u, v, G);
  tie(reverseE, tuples::ignore) = add_edge(v, u, G);
  capacity[e] = c;
  capacity[reverseE] = 0;
  rev_edge[e] = reverseE;
  rev_edge[reverseE] = e;
int main() {
  cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test cases:
    cin >> test_cases;
    for(int test = 0; test < test_cases; test++) {</pre>
        int intersection_count, street_count, station_count, photograph_count;
        cin >> intersection_count >> street_count >> station_count >> photograph_count;
        // create graph and additional stuff
        // we need a graph that can hold a sink, a source ant twice the citie's map
        Graph graph(2 * intersection_count + 2);
        EdgeCapacityMap capacity = get(edge_capacity, graph);
ReverseEdgeMap rev_edge = get(edge_reverse, graph);
        // not used: ResidualCapacityMap res_capacity = get(edge_residual_capacity, graph);
        int source = 2 * intersection_count;
        int sink = 2 * intersection_count + 1;
        // read in where police stations are located and connect them to source/sink
        for(int station_index = 0; station_index < station_count; station_index++) {</pre>
             int station_loc;
             cin >> station_loc;
             // source to police station with weight 1 as each station has only one officer
             addEdge(source, station_loc, 1, capacity, rev_edge, graph);
             // police station to sink with weight 1 as each station can only hold one photograph,
// ATTENTION here police station is in the accordance.
             addEdge(intersection_count + station_loc, sink, 1, capacity, rev_edge, graph);
        // read where photographs are stored and connect this location from our first set (where policemen reach the
             location)
        // to our second set (where policement can only use a street once to get beck to a station)
        for(int photo_index = 0; photo_index < photograph_count; photo_index++) {</pre>
            int photo_loc;
             cin >> photo_loc;
             addEdge(photo_loc, intersection_count + photo_loc, 1, capacity, rev_edge, graph);
         // read where the streets are
        for(int street_index = 0; street_index < street_count; street_index++) {</pre>
            int from, to;
             cin >> from >> to;
             // first add street with unbound traffic to the first set, as all policemen are free to move multiple times
             // through the same street without a photograph
             addEdge(from, to, numeric_limits < int >:: max(), capacity, rev_edge, graph);
             // now we add the same street, but it can be used only once as now it is used by policemen
             // with photographs
addEdge(from + intersection_count, to + intersection_count, 1, capacity, rev_edge, graph);
      long flowValue = push_relabel_max_flow(graph, source, sink);
      cout <<flowValue<< endl;</pre>
  return 0;
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <map>
#include <string>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/dijkstra_shortest_paths.hpp>
#include <boost/graph/kruskal_min_spanning_tree.hpp>
#include <boost/property_map/transform_value_property_map.hpp>
#include <boost/graph/boyer_myrvold_planar_test.hpp>
#include <boost/graph/max_cardinality_matching.hpp>
#include <boost/graph/push_relabel_max_flow.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, directedS> Traits;
typedef adjacency_list<vecS, vecS, directedS, no_property, property<edge_capacity_t, long, property<
edge_residual_capacity_t, long, property<edge_reverse_t, Traits::edge_descriptor>>>> Graph;
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
typedef property_map<Graph, edge_capacity_t>::type EdgeCapacityMap;
typedef property_map<Graph, edge_reverse_t>::type ReverseEdgeMap;
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    {\tt int} \  \, {\tt nr\_intersections} \, , \, \, {\tt nr\_streets} \, , \, \, {\tt nr\_police\_stations} \, , \, \, {\tt nr\_photographs} \, ; \, \,
    cin >> nr_intersections >> nr_streets >> nr_police_stations >> nr_photographs;
    Graph g(nr_intersections * 2 + 2);
    int source = nr_intersections * 2;
int sink = nr_intersections * 2 + 1;
    EdgeCapacityMap capacity = get(edge_capacity, g);
ReverseEdgeMap rev_edge = get(edge_reverse, g);
    for (int i = 0; i < nr_police_stations; i++) {</pre>
       int station_location;
       cin >> station_location;
       Edge e, rev_e;
       bool success;
       tie(e, success) = add_edge(source, station_location, g);
       tie(rev_e, success) = add_edge(station_location, source, g);
       capacity[e] = 1;
       capacity[rev_e] = 0;
rev_edge[e] = rev_e;
       rev_edge[rev_e] = e;
       tie(e, success) = add_edge(station_location + nr_intersections, sink, g);
       tie(rev_e, success) = add_edge(sink, station_location + nr_intersections, g);
       capacity[e] = 1;
       capacity[rev e] = 0:
       rev_edge[e] = rev_e;
       rev_edge[rev_e] = e;
    for (int i = 0; i < nr_photographs; i++) {</pre>
       int photgraph_location;
       cin >> photgraph_location;
       Edge e, rev_e;
       bool success;
       tie(e, success) = add_edge(photgraph_location, photgraph_location + nr_intersections, g);
tie(rev_e, success) = add_edge(photgraph_location + nr_intersections, photgraph_location, g);
       capacity[e] = 1;
       capacity[rev_e] = 0;
       rev_edge[e] = rev_e;
       rev_edge[rev_e] = e;
    vector < pair < int , int > > streets(nr_streets);
    for (int i = 0; i < nr_streets; i++) {</pre>
       int from, to;
       cin >> from >> to;
       Edge e. rev e:
       bool success;
       tie(e, success) = add_edge(from, to, g);
```

```
tie(rev_e, success) = add_edge(to, from, g);
    capacity[e] = nr_police_stations;
    capacity[rev_e] = 0;
    rev_edge[e] = rev_e;
    rev_edge[rev_e] = e;

    tie(e, success) = add_edge(from + nr_intersections, to + nr_intersections, g);
    tie(rev_e, success) = add_edge(to + nr_intersections, from + nr_intersections, g);
    capacity[e] = 1;
    capacity[rev_e] = 0;
    rev_edge[e] = rev_e;
    rev_edge[e] = rev_e;
    rev_edge[rev_e] = e;
}

int max = push_relabel_max_flow(g, source, sink);
    cout << max << endl;
}

return 0;
}</pre>
```

5 CGAL Introduction

5.1 Hit?

Keywords: CGAL Segment, CGAL Ray, CGAL do_intersect

```
#include <CGAL/Exact_predicates_exact_constructions_kernel.h>
#include <iostream>
#include <stdexcept>
typedef CGAL::Exact_predicates_exact_constructions_kernel K;
typedef K::Point_2 Point;
typedef K::Segment_2 Segment;
typedef K::Ray_2 Ray;
using namespace std;
int main()
 while(true) {
   int obsticale count:
    cin >> obsticale_count;
    // kill switch for application
   if(obsticale_count == 0) {
     break;
    // get the laser
    double ray_start_x, ray_start_y, ray_other_x, ray_other_y;
    cin >> ray_start_x >> ray_start_y >> ray_other_x >> ray_other_y;
    Ray laser_ray = Ray(Point(ray_start_x, ray_start_y), Point(ray_other_x, ray_other_y));
    // read in obsticles and check if we hit them with the ray
    bool hit = false;
    for(int i = 0; i < obsticale_count; i++) {</pre>
      // read in and create obsticle
      double obsticle_start_x, obsticle_start_y, obsticle_end_x, obsticle_end_y;
      cin >> obsticle_start_x >> obsticle_start_y >> obsticle_end_x >> obsticle_end_y;
      // we know we hit something, read input but do nothing with it :)
      if(hit) {
       continue;
     Segment obsticle = Segment(Point(obsticle_start_x, obsticle_start_y), Point(obsticle_end_x, obsticle_end_y));
      // check if we hit it
      if(CGAL::do_intersect(laser_ray, obsticle)) {
       hit = true;
   if(hit) {
      cout << "yes" << endl;
   } else {
      cout << "no" << endl;
   }
 }
}
```

```
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
typedef K::Point_2 Point;
typedef K::Segment_2 Segment;
typedef K::Ray_2 Ray;
using namespace std;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int 1:
  for (cin >> 1; 1 != 0; cin >> 1) {
    long long x, y, a, b;
cin >> x >> y >> a >> b;
    Ray ray(Point(x, y), Point(a, b));
    bool found_intersect = false;
    for (int i = 0; i < 1; i++) {
  long long r, s, t, u;
      cin >> r >> s >> t >> u;
      if (CGAL::do_intersect(ray, Segment(Point(r, s), Point(t, u)))) {
        for (i++; i < 1; i++) {</pre>
```

```
cin >> r >> s >> t >> u;
}
    found_intersect = true;
}
if (found_intersect) {
    cout << "yes" << endl;
}
else {
    cout << "no" << endl;
}
}
return 0;
}</pre>
```

5.2 Antenna

Keywords: floor_to_double, ceil_to_double, Minimal Circle, CGAL sqrt

```
#include <iostream>
#include <cmath>
#include <CGAL/Exact_predicates_exact_constructions_kernel_with_sqrt.h>
#include <CGAL/Min_circle_2.h>
#include <CGAL/Min_circle_2_traits_2.h>
#include <CGAL/number_utils.h>
// typedefs
typedef CGAL::Exact_predicates_exact_constructions_kernel_with_sqrt K; // IMPORTANT!!!!! OTHERWISE NO SQRT!!!!!
typedef CGAL::Min_circle_2 traits_2 < K > Traits;
typedef CGAL::Min_circle_2 < Traits > Min_circle;
typedef K::Point_2 Point;
using namespace std;
// from slides, fun!
double floor_to_double(const K::FT& x)
  double a = std::floor(CGAL::to_double(x));
  while (a > x) a -= 1;
while (a+1 <= x) a += 1;
  return a:
double ceil_to_double(const K::FT& x)
  double a = std::ceil(CGAL::to_double(x));
  while (a < x) a += 1;
while (a-1 >= x) a -= 1;
  return a;
int main() {
  // some basic setup stuff
  cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  while(true) {
      int people_count;
cin >> people_count;
       // kill switch for application
       if(people_count == 0) {
         break;
       // collect all positions of people living at
       vector < Point > peoples (people_count);
       for(int i = 0; i < people_count; i++) {</pre>
         double person_x, person_y;
cin >> person_x >> person_y;
        peoples.at(i) = Point(person_x, person_y);
       // create the circle covering all people with minimal surface
      Min_circle min_circle(peoples.begin(), peoples.end(), true);
       // get radius
       cout << ceil_to_double(sqrt(min_circle.circle().squared_radius())) << endl;</pre>
  }
}
```

```
#include <CGAL/Exact_predicates_exact_constructions_kernel_with_sqrt.h>
#include <CGAL/Min_circle_2.h>
#include <CGAL/Min_circle_2_traits_2.h>
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
```

```
#include <queue>
#include <set>
#include <utility>
#include <cmath>
typedef CGAL::Exact_predicates_exact_constructions_kernel_with_sqrt K;
typedef CGAL::Min_circle_2_traits_2<K> Traits;
typedef CGAL::Min_circle_2<Traits> Min_circle;
typedef K::Point_2 Point;
using namespace std;
double floor_to_double(const K::FT& x)
  double a = std::floor(CGAL::to_double(x));
  while (a > x) a -= 1;
while (a + 1 <= x) a += 1;
  return a;
double ceil_to_double(const K::FT& x)
  double a = std::ceil(CGAL::to_double(x));
  while (a < x) a += 1;
while (a - 1 >= x) a -= 1;
  return a;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  for (cin >> n; n != 0; cin >> n) {
    vector < Point > points(n);
    for (int i = 0; i < n; i++) {
       double x, y;
       cin >> x >> y;
      points[i] = Point(x, y);
    Min_circle mc(points.begin(), points.end(), true);
cout << ceil_to_double(sqrt(mc.circle().squared_radius())) << endl;</pre>
  return 0;
7
```

5.3 First Hit

Keywords: CGAL randomise, CGAL intersection

```
#include <CGAL/Exact_predicates_exact_constructions_kernel.h>
#include <iostream>
#include <stdexcept>
typedef CGAL::Exact_predicates_exact_constructions_kernel K;
typedef K::Point_2 Point;
typedef K::Segment_2 Segment;
typedef K::Ray_2 Ray;
using namespace std;
// from slides, fun!
double floor_to_double(const K::FT& x)
 double a = std::floor(CGAL::to_double(x));
 while (a > x) a -= 1;
while (a+1 <= x) a += 1;
 return a;
}
double ceil_to_double(const K::FT& x)
  double a = std::ceil(CGAL::to_double(x));
  while (a < x) a += 1;
  while (a-1 >= x) a -= 1;
 return a;
inline void laser_obsticale_segment(Segment &lo_segment, CGAL::Object intersec_obj) {
 if (const Point* op = CGAL::object_cast<Point>(&intersec_obj)) {
    lo_segment = Segment(lo_segment.source(), *op);
 } else if(const Segment* os = CGAL::object_cast<Segment>(&intersec_obj)) {
   // ray hits a segment, three possibilities
    if(CGAL::collinear_are_ordered_along_line(lo_segment.source(), (*os).source(), (*os).target())) {
      // order is: laser source -> start of segment -> end of segment
      lo_segment = Segment(lo_segment.source(), (*os).source());
     lo_segment = Segment(lo_segment.source(), (*os).target());
 } else {
    throw runtime_error("Bad Wolf");
```

```
}
int main() {
  // some basic setup stuff
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  std::cout << std::setiosflags(std::ios::fixed) << std::setprecision(0);</pre>
  //cout << fixed << setprecision(0);</pre>
  while(true) {
    int obsticale_count;
    cin >> obsticale_count;
    // kill switch for application
    if(obsticale_count == 0) {
      break:
    // get the laser
    double ray_start_x, ray_start_y, ray_other_x, ray_other_y;
    cin >> ray_start_x >> ray_start_y >> ray_other_x >> ray_other_y;
    Ray laser_ray = Ray(Point(ray_start_x, ray_start_y), Point(ray_other_x, ray_other_y));
    vector < Segment > obsticle_segments(obsticale_count);
    // read in and create obsticle list
    for(int i = 0; i < obsticale_count; i++) {</pre>
      double obsticle_start_x, obsticle_start_y, obsticle_end_x, obsticle_end_y;
cin >> obsticle_start_x >> obsticle_start_y >> obsticle_end_x >> obsticle_end_y;
      obsticle_segments[i] = Segment(Point(obsticle_start_x, obsticle_start_y), Point(obsticle_end_x, obsticle_end_y));
    random_shuffle(obsticle_segments.begin(), obsticle_segments.end());
    // segment that starts at the source of the laser and ends, after our algo is done, at the point where the laser hits
    // obsticle
    // search for one intersaction between the laser ray and an obsticle, create a segment that starts at the laser
    source and ends \ensuremath{/\!/} at the point where the laser hits the obsticle
    bool hit_found = false;
    Segment lo_segment(laser_ray.source(), laser_ray.source());
    int obst_index = 0; // used to jump over already checked segments in the second for-loop
    for(; obst_index < obsticale_count; ++obst_index) {</pre>
      if(do_intersect(obsticle_segments[obst_index], laser_ray)) {
        hit_found = true;
        laser_obsticale_segment(lo_segment, intersection(obsticle_segments[obst_index], laser_ray));
        break;
      }
    // check if we hit something
    if(!hit_found) {
      cout << "no" << endl;
      continue;
    for(; obst_index < obsticale_count; ++obst_index) {</pre>
      if(do_intersect(lo_segment, obsticle_segments[obst_index])) {
        laser_obsticale_segment(lo_segment, intersection(obsticle_segments[obst_index], laser_ray));
    cout << floor_to_double(lo_segment.target().x()) << " " << floor_to_double(lo_segment.target().y()) << endl;</pre>
  }
}
```

```
#include <CGAL/Exact_predicates_exact_constructions_kernel.h>
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
typedef CGAL::Exact_predicates_exact_constructions_kernel K;
typedef K::Point_2 Point;
typedef K::Segment_2 Segment;
typedef K::Ray_2 Ray;
using namespace std;
double floor_to_double(const K::FT& x) {
  double a = floor(CGAL::to_double(x));
  while (a > x) a -= 1;
while (a + 1 <= x) a += 1;
  return a;
double ceil_to_double(const K::FT& x) {
```

```
double a = ceil(CGAL::to_double(x));
 while (a < x) a += 1;
while (a - 1 >= x) a -= 1;
  return a;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
 cout << setiosflags(ios::fixed) << setprecision(0);</pre>
  for (cin >> 1; 1 != 0; cin >> 1) {
    double x, y, a, b;
cin >> x >> y >> a >> b;
Point origin(x, y);
Ray ray(origin, Point(a, b));
    bool found_intersect = false;
    K::FT nearest_dist;
    Point nearest_point;
    for (int i = 0; i < 1; i++) {
  double r, s, t, u;</pre>
      cin >> r >> s >> t >> u;
       Segment seg(Point(r, s), Point(t, u));
       if (CGAL::do_intersect(ray, seg)) {
         auto o = CGAL::intersection(ray, seg);
         K::FT new_dist;
         Point new_point;
if (const Point* op = boost::get<Point>(&*o)) {
           new_dist = Segment(origin, *op).squared_length();
           new_point = *op;
         else if (const Segment* os = boost::get<Segment>(&*o)) {
           if (CGAL::collinear_are_ordered_along_line(origin, os->source(), os->target())) {
             new_dist = Segment(origin, os->source()).squared_length();
             new_point = os->source();
           else if (CGAL::collinear_are_ordered_along_line(origin, os->target(), os->source())) {
             new_dist = Segment(origin, os->target()).squared_length();
new_point = os->target();
             //segment going through ray origin point \rightarrow distance is 0
             new_dist = 0.0;
             new_point = origin;
           }
           throw runtime_error("strange segment intersection");
         if (!found_intersect) {
          nearest_dist = new_dist;
nearest_point = new_point;
           found_intersect = true;
           if (new_dist < nearest_dist) {</pre>
             nearest_dist = new_dist;
nearest_point = new_point;
        }
      }
   }
    if (found intersect) {
      cout << floor_to_double(nearest_point.x()) << " " << floor_to_double(nearest_point.y()) << endl;</pre>
      cout << "no" << endl;
   }
 return 0;
```

5.4 Almost Antenna

Keywords: CGAL qrt, Minimal Circle, floor_to_double, ceil_to_double

```
#include <iostream>
#include <cmath>
#include <unordered_set>

#include <CGAL/Exact_predicates_exact_constructions_kernel_with_sqrt.h>
#include <CGAL/Min_circle_2.h>
#include <CGAL/Min_circle_2_traits_2.h>
#include <CGAL/number_utils.h>

// typedefs
typedef CGAL::Exact_predicates_exact_constructions_kernel_with_sqrt K; // IMPORTANT!!!!! OTHERWISE NO SQRT!!!!!
typedef CGAL::Min_circle_2_traits_2 <K> Traits;
```

```
typedef CGAL::Min_circle_2<Traits>
                                             Min_circle;
typedef K::Point_2 Point;
using namespace std;
// from slides, fun!
double floor_to_double(const K::FT& x)
  double a = std::floor(CGAL::to_double(x));
  while (a > x) a -= 1;
while (a+1 <= x) a += 1;
  return a;
double ceil_to_double(const K::FT& x)
  double a = std::ceil(CGAL::to_double(x));
  while (a < x) a += 1;
while (a-1 >= x) a -= 1;
int main() {
  // some basic setup stuff
  cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  while(true) {
      int people_count;
cin >> people_count;
       // kill switch for application
       if (people_count == 0) {
        break;
       // collect all positions of people living at
       vector < Point > peoples (people_count);
       for(int i = 0; i < people_count; i++) {</pre>
         double person_x, person_y;
cin >> person_x >> person_y;
        peoples.at(i) = Point(person_x, person_y);
       // create the circle covering all people with minimal surface
       Min_circle min_circle(peoples.begin(), peoples.end(), true);
       // now we remove the support points, calculate the radius for the resulting min circles and choose the smallest one
             as the solution
       K::FT min_rad = sqrt(min_circle.circle().squared_radius());
       for(auto iter = min_circle.support_points_begin(); iter != min_circle.support_points_end(); iter++) {
  for(int i = 0; i < people_count; i++) {
    if(peoples.at(i) == *iter) {</pre>
              int add = i > 0 ? -1 : 1;
              peoples.at(i) = peoples.at(i + add);
              Min_circle almost_circ(peoples.begin(), peoples.end(), true);
              K::FT almost_rad = sqrt(almost_circ.circle().squared_radius());
              if(almost_rad < min_rad) {
  min_rad = almost_rad;</pre>
              peoples.at(i) = *iter;
              break:
      }
       // get radius
cout << ceil_to_double(min_rad) << endl;</pre>
 }
}
```

```
#include <CGAL/Exact_predicates_exact_constructions_kernel_with_sqrt.h>
#include <CGAL/Min_circle_2.h>
#include <iostream>
#include <vector>
#include #include #include #include #include #include #include #include <|
#include
```

```
double floor_to_double(const K::FT& x)
  double a = std::floor(CGAL::to_double(x));
  while (a > x) a -= 1;
while (a + 1 <= x) a += 1;
  return a;
double ceil_to_double(const K::FT& x)
  double a = std::ceil(CGAL::to_double(x));
  while (a < x) a += 1;
while (a - 1 >= x) a -= 1;
}
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  int n;
  for (cin >> n; n != 0; cin >> n) {
    vector < Point > points(n);
    for (int i = 0; i < n; i++) {
      double x, y;
cin >> x >> y;
points[i] = Point(x, y);
    Min_circle mc(points.begin(), points.end(), true);
double min_radius = ceil_to_double(sqrt(mc.circle().squared_radius()));
    for (auto sp_it = mc.support_points_begin(); sp_it != mc.support_points_end(); ++sp_it) {
       Point support_point = *sp_it;
       for (int i = 0; i < n; i++) {
  if (points[i] == support_point) {</pre>
           /*Min_circle almost_mc(points.begin(), points.begin()+i, true);
           if (i+1 < n) {
           almost_mc.insert(points.begin()+i+1, points.end());
           double new_radius = ceil_to_double(sqrt(almost_mc.circle().squared_radius()));
           if (new_radius < min_radius) {</pre>
           min_radius = new_radius;
            }*/
            if (i == 0) {
             if (n > 1) {
             points[i] = points[i + 1];
}
             points[i] = Point(0, 0);
}
              else {
           }
           else {
             points[i] = points[i - 1];
           Min_circle almost_mc(points.begin(), points.end(), true);
           points[i] = support_point;
double new_radius = ceil_to_double(sqrt(almost_mc.circle().squared_radius()));
           if (new_radius < min_radius) {</pre>
             min_radius = new_radius;
           break:
      }
    cout << min_radius << endl;</pre>
  return 0;
```

6 Proximity Structures

6.1 Graypes

Keywords: setprecision, Delaunay Triangulation, Finite edge iteration

```
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
#include <CGAL/Delaunay_triangulation_2.h>
typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
typedef CGAL::Delaunay_triangulation_2 < K > Triangulation;
typedef Triangulation::Edge_iterator Edge_iterator;
using namespace std;
// from slides, fun!
double floor_to_double(const K::FT& x)
  double a = std::floor(CGAL::to_double(x));
  while (a > x) a -= 1;
while (a+1 <= x) a += 1;</pre>
  return a;
double ceil_to_double(const K::FT& x)
  double a = std::ceil(CGAL::to_double(x));
  while (a < x) a += 1;
while (a-1 >= x) a -= 1;
  return a;
int main() {
  // some basic setup stuff
  cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  while(true) {
      int graype_count;
cin >> graype_count;
       // kill switch for application
      if(graype_count == 0) {
        break;
      // collect graype locations
      vector < K :: Point_2 > graype_locs;
      graype_locs.reserve(graype_count);
      for(int i = 0; i < graype_count; i++) {</pre>
        double graype_x, graype_y;
cin >> graype_x >> graype_y;
        graype_locs.push_back(K::Point_2(graype_x, graype_y));
       // construct triangulation
      Triangulation triang;
      triang.insert(graype_locs.begin(), graype_locs.end());
       // go trough apes, and search for shortest edge
      K::FT min_time;
      bool first = true:
      for (Edge_iterator edge = triang.finite_edges_begin(); edge != triang.finite_edges_end(); ++edge) {
        K::FT edge_time = triang.segment(edge).squared_length();
         if(edge_time < min_time || first) {</pre>
             first = false;
             min_time = edge_time;
        }
      \verb|cout| << ceil(sqrt(CGAL::to_double(min_time)) / 2.0 * 100.0) << endl; \\
}
```

```
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
#include <CGAL/Delaunay_triangulation_2.h>
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <cmath>

typedef CGAL::Exact_predicates_inexact_constructions_kernel K;

typedef CGAL::Delaunay_triangulation_2 <K> Triangulation;
typedef Triangulation::Edge_iterator Edge_iterator;
typedef Triangulation::Point Point;
```

```
typedef Triangulation::Segment Segment;
using namespace std;
double floor_to_double(const K::FT& x)
  double a = std::floor(CGAL::to_double(x));
  while (a > x) a -= 1;
while (a + 1 <= x) a += 1;
  return a;
double ceil_to_double(const K::FT& x)
  double a = std::ceil(CGAL::to_double(x));
 while (a < x) a += 1;
while (a - 1 >= x) a -= 1;
 return a;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  for (cin >> n; n != 0; cin >> n) {
    vector < Point > points;
    points.reserve(n);
    for (int i = 0; i < n; i++) {
      double x, y;
cin >> x >> y;
      points.push_back(Point(x, y));
    Triangulation t:
    t.insert(points.begin(), points.end());
    Segment shortest = t.segment(*(t.finite_edges_begin()));
    for (Edge_iterator e = t.finite_edges_begin(); e != t.finite_edges_end(); ++e) {
      Segment s = t.segment(*e);
      if (s.squared_length() < shortest.squared_length()) {</pre>
        shortest = s:
    cout << ceil(sqrt(CGAL::to_double(shortest.squared_length())) / 2.0*100.0) << endl;</pre>
 }
  return 0;
```

6.2 Bistro

Keywords: Delaunay Triangulation

```
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
#include <CGAL/Delaunay_triangulation_2.h>
{\tt typedef} \ {\tt CGAL::Exact\_predicates\_inexact\_constructions\_kernel} \ {\tt K};
using namespace std;
// from slides, fun!
double floor_to_double(const K::FT& x)
  double a = std::floor(CGAL::to_double(x));
  while (a > x) a -= 1;
  while (a+1 <= x) a += 1;
  return a;
double ceil_to_double(const K::FT& x)
  double a = std::ceil(CGAL::to_double(x));
 while (a < x) a += 1;
while (a-1 >= x) a -= 1;
 return a;
int main() {
  // some basic setup stuff
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
cout << fixed << setprecision(0);</pre>
  while(true) {
      int existing_count;
      cin >> existing_count;
      // kill switch for application
```

```
if(existing_count == 0) {
        break;
      }
      // collect existing restaurants
vector<K::Point_2> existing_locs;
      existing_locs.reserve(existing_count);
      for(int i=0; i < existing_count; i++) {</pre>
        double loc_x, loc_y;
cin >> loc_x >> loc_y;
        existing_locs.push_back(K::Point_2(loc_x, loc_y));
      // cosntruct triangulation
      Triangulation triang:
      triang.insert(existing_locs.begin(), existing_locs.end());
       // go through possible location
      int possible_count;
      cin >> possible_count;
      for(int i = 0; i < possible_count; i++) {</pre>
        int possible_x, possible_y
         cin >> possible_x >> possible_y;
        K::Point_2 possible_point = K::Point_2(possible_x, possible_y);
         // find nearest vertex and by that the nearest point
         K::Point_2 nearest = triang.nearest_vertex(possible_point)->point();
         cout << CGAL::to_double(CGAL::squared_distance(nearest, possible_point)) << endl;</pre>
      }
    7
}
```

```
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
#include <CGAL/Delaunay_triangulation_2.h>
#include <CGAL/squared_distance_2.h>
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
typedef CGAL::Delaunay_triangulation_2 < K > Triangulation;
typedef Triangulation::Edge_iterator Edge_iterator;
typedef Triangulation::Point Point;
typedef Triangulation::Segment Segment;
using namespace std;
double floor_to_double(const K::FT& x)
  double a = std::floor(CGAL::to_double(x));
  while (a > x) a -= 1;
  while (a + 1 <= x) a += 1;
 return a;
double ceil_to_double(const K::FT& x)
{
  double a = std::ceil(CGAL::to_double(x));
  while (a < x) a += 1;
  while (a - 1 >= x) a -= 1;
  return a;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  int n;
  for (cin >> n; n != 0; cin >> n) {
    vector < Point > points;
    points.reserve(n);
    for (int i = 0; i < n; i++) {
      double x, y;
      cin >> x >> y;
      points.push_back(Point(x, y));
    Triangulation t;
    t.insert(points.begin(), points.end());
    int m;
    cin >> m;
    for (int i = 0; i < m; i++) {</pre>
      double x, y;
```

```
cin >> x >> y;
  Point loc(x, y);
  K::FT sqaured_dist = CGAL::squared_distance(t.nearest_vertex(loc)->point(), loc);
  cout << CGAL::to_double(sqaured_dist) << endl;
}
}
return 0;
}</pre>
```

6.3 H1N1

Keywords: Delaunay Triangulation, CGAL Triangulation with DFS, Finite face iteration

```
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
#include <CGAL/Delaunay_triangulation_2.h>
#include <CGAL/squared_distance_2.h>
typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
typedef CGAL::Delaunay_triangulation_2 <K> Triangulation;
typedef Triangulation::Edge_iterator Edge_iterator;
using namespace std;
// from slides, fun!
double floor_to_double(const K::FT& x)
    double a = std::floor(CGAL::to_double(x));
    while (a > x) a -= 1;
while (a+1 <= x) a += 1;
    return a;
}
double ceil_to_double(const K::FT& x)
    double a = std::ceil(CGAL::to_double(x));
    while (a < x) a += 1;
    while (a-1 >= x) a -= 1;
    return a;
7
bool DFS(Triangulation &triang, double min_dist_for_edge, Triangulation::Face_handle &start, map<Triangulation::
    Face_handle, int> &visitor_map, int cur_iter) {
    // each infected person's point is connected to three edges, otherwise we wouldn't get triangle
    for(int edge_i = 0; edge_i < 3; edge_i++) {</pre>
         // get the segment representing the edge
Triangulation::Segment edge_segment = triang.segment(start, edge_i);
         // check if we are still far away from both endpoints of the segment while passing through
         double distance = CGAL::to_double(edge_segment.squared_length());
         if(distance >= min_dist_for_edge) {
              // get the neighboring face
              Triangulation::Face_handle neighbor_face_h = start->neighbor(edge_i);
              // check that we didn't visit it already
              if(visitor_map[neighbor_face_h] == cur_iter) {
                  continue; // use other edge
              // check if neighboring face is infinite, i.e. we found a way out
              if(triang.is_infinite(neighbor_face_h)) {
                   return true:
              // mark as visited by current iteration
              visitor_map[neighbor_face_h] = cur_iter;
              // recursion. DFS
              if(DFS(triang, min_dist_for_edge, neighbor_face_h, visitor_map, cur_iter)) {
         }
    7
    return false;
}
int main() {
    // some basic setup stuff
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    cout << fixed << setprecision(0);</pre>
    while(true) {
         int infected_count;
         cin >> infected_count;
            kill switch for application
         if(infected_count == 0) {
              break;
         // read in infected people's location
```

```
vector <K::Point_2> infected_locs;
         infected_locs.reserve(infected_count);
         for(int i = 0; i < infected_count; i++) {</pre>
              double infected_x, infected_y;
cin >> infected_x >> infected_y;
              infected_locs.push_back(K::Point_2(infected_x, infected_y));
         // create triangulation with the infected people
         Triangulation triang;
         triang.insert(infected_locs.begin(), infected_locs.end());
         // prepare a map mapping a face handle to an integer, the integer represents the DFS step in which the face was
         // visited already (to not visit multiple time the same face)
         map<Triangulation::Face_handle, int> visitor_map;
for (Triangulation::Face_iterator it = triang.finite_faces_begin(); it != triang.finite_faces_end(); it++) {
              visitor_map[it] = -1;
         // go trough people trying to escape
         int escapee_count;
         cin >> escapee_count;
         for(int i = 0; i < escapee_count; i++) {</pre>
              // read location of escapee and the minimum distance expected
              double escapee_x, escapee_y, min_dist;
              cin >> escapee_x >> escapee_y >> min_dist;
              K::Point_2 escapee_loc(escapee_x, escapee_y);
              // get nearst vertex's point in the triangulation
              Triangulation::Point nearest_vertex_point = triang.nearest_vertex(escapee_loc)->point();
              // check that we not already violate the distance condition
              if(CGAL::to_double(CGAL::squared_distance(escapee_loc, nearest_vertex_point)) < min_dist) {</pre>
                  cout << "n";
                   continue; // jump over the rest, we already know the escapee is near an infected person
              // find the face handle of our escapee
              Triangulation::Face_handle face_h = triang.locate(escapee_loc);
              // update for the face handle that we visited it in the current round
              visitor_map[face_h] = i;
              if(triang.is_infinite(face_h) || // face is already outside, escapee can escape, no DFS needed
   DFS(triang, min_dist * 4.0, face_h, visitor_map, i)) { // use DFS to find a way out, multiply by 4.0 (=
        2.0^2 (not squared distances)) as we must be min_dist away from one ende of an edge and min_dist
                        from the other, multiply by 2^2
                   cout << "y";
              } else {
                  cout << "n";
              }
         7
         cout << endl;
}
```

```
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
#include <CGAL/Delaunay_triangulation_2.h>
#include <CGAL/squared_distance_2.h>
#include <CGAL/Triangulation_face_base_with_info_2.h>
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility?
#include <cmath>
typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
typedef CGAL::Triangulation_vertex_base_2 < K > Vb;
typedef CGAL::Triangulation_face_base_with_info_2 < int , K > Fb;
typedef CGAL::Triangulation_data_structure_2 < Vb, Fb > Tds;
typedef CGAL::Delaunay_triangulation_2 < K, Tds > Triangulation;
typedef Triangulation::Edge_iterator Edge_iterator;
typedef Triangulation::Face_handle Face_handle;
typedef Triangulation::Face_iterator Face_iterator;
typedef Triangulation::All_faces_iterator All_faces_iterator;
typedef Triangulation::Point Point;
typedef Triangulation::Segment Segment;
using namespace std;
double floor_to_double(const K::FT& x)
  double a = std::floor(CGAL::to_double(x));
 while (a > x) a -= 1;
while (a + 1 <= x) a += 1;
 return a;
```

```
double ceil_to_double(const K::FT& x)
  double a = std::ceil(CGAL::to_double(x));
  while (a < x) a += 1;
while (a - 1 >= x) a -= 1;
 return a;
bool find_exit(Triangulation& t, Face_handle& face, K::FT& min_segment_squared_length, int current_id) {
 for (int i = 0; i < 3; i++) {
   Segment s = t.segment(face, i);</pre>
    if (s.squared_length() >= min_segment_squared_length) {
      Face_handle neighbor_face = face->neighbor(i);
      if (neighbor_face->info() == current_id) {
      if (t.is infinite(neighbor face)) {
        return true;
      neighbor_face->info() = current_id;
      if (find_exit(t, neighbor_face, min_segment_squared_length, current_id)) {
        return true;
   }
  return false;
}
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  for (cin >> n; n != 0; cin >> n) {
    vector < Point > points;
points.reserve(n);
    for (int i = 0; i < n; i++) {
      double x, y;
cin >> x >> y;
      points.push_back(Point(x, y));
    Triangulation t;
    t.insert(points.begin(), points.end());
    for (All_faces_iterator f = t.all_faces_begin(); f != t.all_faces_end(); ++f) {
      f \rightarrow info() = 0:
    int m;
    cin >> m;
    for (int i = 0; i < m; i++) {</pre>
      double x, v;
      K::FT distance, min_segment_squared_length;
      cin >> x >> y >> distance;
      Point loc(x, y);
      K::FT squared_dist = CGAL::squared_distance(t.nearest_vertex(loc)->point(), loc);
      Face_handle face = t.locate(loc);
      min_segment_squared_length = distance*4.0;
      face->info() = i + 1;
      if (squared_dist >= distance && (t.is_infinite(face) || find_exit(t, face, min_segment_squared_length, i + 1))) {
        cout << 'y';
      else {
        cout << 'n':
    cout << endl;</pre>
  return 0:
```

6.4 Germs

Keywords: Delaunay Triangulation, Finite vertices iteration, Finite edge iteration, Iteration over std::map

```
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
#include <CGAL/Delaunay_triangulation_2.h>
#include <CGAL/squared_distance_2.h>

typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
typedef CGAL::Delaunay_triangulation_2 <K > Triangulation;
typedef Triangulation::Edge_iterator Edge_iterator;

using namespace std;

// from slides, fun!
double floor_to_double(const K::FT& x)
{
    double a = std::floor(CGAL::to_double(x));
```

```
while (a > x) a -= 1;
while (a+1 <= x) a += 1;
    return a;
}
double ceil_to_double(const K::FT& x)
    double a = std::ceil(CGAL::to_double(x));
    while (a < x) a += 1;
    while (a-1 >= x) a -= 1:
    return a;
double hours(double distance) {
    double x = sqrt(distance) - 0.5; // first sqrt to get the distance ...
    double result;
if (x <= 0.0) {</pre>
        result = 0;
       result = ceil(sqrt(x)); // second sqrt because t^2 + 0.5 = x => t = <math>sqrt(x - 0.5);
    return result;
}
int main() {
    while(true) {
        int bacteria count:
        cin >> bacteria_count;
        // kill switch for application
        if(bacteria_count == 0) {
            break;
        7
        // read in boundaries of the dish
        double left_border, right_border, bottom_border, top_border;
        cin >> left_border >> bottom_border >> right_border >> top_border;
        // collect bacteria's center information
        vector <K::Point_2> bacteria_centers;
        bacteria_centers.reserve(bacteria_count);
        for(int i = 0; i < bacteria_count; i++) {</pre>
             double bacteria_x, bacteria_y;
             cin >> bacteria_x >> bacteria_y;
             bacteria centers.push back(K::Point 2(bacteria x. bacteria v)):
        }
         // create triangulation
        Triangulation triang;
        triang.insert(bacteria_centers.begin(), bacteria_centers.end());
        // keep track of the distances for each bacteria
        map < Triangulation:: Point, double > distances;
        //distances.reserve(bacteria_count);
         // calculate initial distance: distance between the bacteria and the nearest dish boundary
        for(Triangulation::Finite_vertices_iterator vertex_iter = triang.finite_vertices_begin(); vertex_iter != triang.
             finite_vertices_end(); ++vertex_iter) {
Triangulation::Point vertex = vertex_iter->point();
             distances[vertex] = min(
                 min(vertex.x() - left_border, right_border - vertex.x()), // left/right minimum
                 min(vertex.y() - bottom_border, top_border - vertex.y()) // top/bottom minimum
             ):
             distances[vertex] *= distances[vertex]; // square distance as we work with squared ones
         // compute distance to other two neighbours and update distance if it is smaller
        for(Triangulation::Finite_edges_iterator edge_iter = triang.finite_edges_begin(); edge_iter != triang.
             finite_edges_end(); ++edge_iter) {
             Triangulation::Vertex_handle vertex1 = edge_iter->first->vertex(triang.cw(edge_iter->second));
             Triangulation::Vertex_handle vertex2 = edge_iter->first->vertex(triang.ccw(edge_iter->second));
             Triangulation::Point vertex1_point = vertex1->point();
Triangulation::Point vertex2_point = vertex2->point();
             // calculate distance of the points of both vertex and half them (divide by 4 as distance is squared and 4 =
             double vertex_distance = CGAL::to_double(CGAL::squared_distance(vertex1_point, vertex2_point)) / 4;
             distances[vertex1_point] = min(distances[vertex1_point], vertex_distance);
distances[vertex2_point] = min(distances[vertex2_point], vertex_distance);
        // now we know the minimum distance for each bacteria to another one or the borders of the dish
        // extract distances into a vector and sort it
        vector < double > only_distances;
        only_distances.reserve(bacteria_count);
        for(map<Triangulation::Point, double>::iterator iter = distances.begin(); iter != distances.end(); ++iter) {
             only_distances.push_back(iter->second);
```

```
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
#include <CGAL/Delaunay_triangulation_2.h>
#include <CGAL/squared_distance_2.h>
#include <CGAL/Triangulation_face_base_with_info_2.h>
#include <CGAL/Triangulation_vertex_base_with_info_2.h>
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
typedef CGAL:: Exact predicates inexact constructions kernel K:
typedef CGAL::Triangulation_vertex_base_with_info_2 <K::FT, K> Vb;
typedef CGAL::Triangulation_face_base_2 < K > Fb;
{\tt typedef} \ {\tt CGAL::Triangulation\_data\_structure\_2 < Vb} \ , \ \ {\tt Fb>} \ \ {\tt Tds} \ ;
{\tt typedef} \ {\tt CGAL::Delaunay\_triangulation\_2 < K}, \ {\tt Tds > } \ {\tt Triangulation};
typedef Triangulation::Edge_iterator Edge_iterator;
typedef Triangulation::Face_handle Face_handle;
typedef Triangulation::Face_iterator Face_iterator;
typedef Triangulation::All_faces_iterator All_faces_iterator;
typedef Triangulation::Finite_vertices_iterator Finite_vertices_iterator;
typedef Triangulation::Finite_edges_iterator Finite_edges_iterator;
typedef Triangulation::Point Point;
typedef Triangulation::Segment Segment;
using namespace std;
double floor to double(const K::FT& x)
  double a = std::floor(CGAL::to_double(x));
  while (a > x) a -= 1;
while (a + 1 <= x) a += 1;
  return a;
double ceil_to_double(const K::FT& x)
  double a = std::ceil(CGAL::to_double(x));
  while (a < x) a += 1;
while (a - 1 >= x) a -= 1;
 return a;
double distance_to_time(K::FT distance) {
 double tmp = sqrt(CGAL::to_double(distance)) - 0.5;
return (tmp > 0.0) ? ceil(sqrt(tmp)) : 0.0;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0):</pre>
  int n;
  for (cin >> n; n != 0; cin >> n) {
    double 1, b, r, t;
    cin >> 1 >> b >> r >> t;
    vector < Point > points;
    points.reserve(n);
    for (int i = 0; i < n; i++) {
      double x, y;
      cin >> x >> y;
      points.push_back(Point(x, y));
    Triangulation bac;
    bac.insert(points.begin(), points.end());
    for (Finite_vertices_iterator it = bac.finite_vertices_begin(); it != bac.finite_vertices_end(); ++it) {
      Point& p = it->point();
      it->info() = min(min(p.x() - 1, r - p.x()), min(p.y() - b, t - p.y()));
it->info() *= it->info();
    for (Finite_edges_iterator it = bac.finite_edges_begin(); it != bac.finite_edges_end(); ++it) {
      Triangulation::Vertex_handle v1 = it->first->vertex((it->second + 1) % 3);
Triangulation::Vertex_handle v2 = it->first->vertex((it->second + 2) % 3);
      K::FT d = CGAL::squared_distance(v1->point(), v2->point()) / 4;
      v1->info() = min(v1->info(), d);
      v2->info() = min(v2->info(), d);
```

```
vector<K::FT> bac_expand_distances;
bac_expand_distances.reserve(n);
for (Finite_vertices_iterator it = bac.finite_vertices_begin(); it != bac.finite_vertices_end(); ++it) {
   bac_expand_distances.push_back(it->info());
}
sort(bac_expand_distances.begin(), bac_expand_distances.end());
cout << distance_to_time(bac_expand_distances[0]) << " " << distance_to_time(bac_expand_distances[n - 1]) << endl;
}
return 0;
}</pre>
```

6.5 Hiking Maps

Keywords: Delaunay Triangulation, CGAL turn function, CGAL right_turn, Scanline

```
#include <CGAL/Exact_predicates_exact_constructions_kernel.h>
#include <CGAL/Delaunay_triangulation_2.h>
#include <CGAL/squared_distance_2.h>
#include <CGAL/Triangulation_face_base_with_info_2.h>
#include <CGAL/Triangulation_vertex_base_with_info_2.h>
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
typedef CGAL::Exact_predicates_exact_constructions_kernel K;
typedef CGAL::Triangulation_vertex_base_2 < K > Vb;
typedef CGAL::Triangulation_face_base_with_info_2 < int, K> Fb;
typedef CGAL::Triangulation_data_structure_2 < Vb, Fb> Tds;
typedef CGAL::Delaunay_triangulation_2 < K, Tds > Triangulation;
typedef Triangulation::Edge_iterator Edge_iterator;
typedef Triangulation::Face_handle Face_handle;
typedef Triangulation::Face_iterator Face_iterator;
typedef Triangulation::All_faces_iterator All_faces_iterator;
typedef Triangulation::Finite_vertices_iterator Finite_vertices_iterator;
typedef Triangulation::Finite_edges_iterator Finite_edges_iterator;
typedef Triangulation::Point Point;
typedef Triangulation::Segment Segment;
typedef Triangulation::Line_face_circulator Line_face_circulator;
typedef K::Line_2 Line;
using namespace std;
double floor_to_double(const K::FT& x)
  double a = std::floor(CGAL::to_double(x));
  while (a > x) a -= 1;
  while (a + 1 <= x) a += 1;
  return a;
double ceil_to_double(const K::FT& x)
  double a = std::ceil(CGAL::to_double(x));
  while (a < x) a += 1;
  while (a - 1 >= x) a -= 1;
  return a;
}
inline bool containsSegment(const vector < Point > & triangle, const Point & s1, const Point & s2) {
  return !CGAL::right_turn(triangle[1], triangle[0], s1) &&
    !CGAL::right_turn(triangle[3], triangle[2], s1) &&
    !CGAL::right_turn(triangle[5], triangle[4], s1) && !CGAL::right_turn(triangle[1], triangle[0], s2) &&
    !CGAL::right_turn(triangle[3], triangle[2], s2) && !CGAL::right_turn(triangle[5], triangle[4], s2);
void print_array(vector<int>& a) {
 for (int i = 0; i < a.size(); i++) {
  cout << a[i] << " ";</pre>
  cout << endl;</pre>
}
int main() {
  cin.sync_with_stdio(false);
  cout.svnc with stdio(false):
  cout << fixed << setprecision(0);</pre>
  int nr_testcases;
  cin >> nr_testcases;
  for (int testcase = 0; testcase < nr_testcases; ++testcase) {</pre>
    int m, n;
```

```
cin >> m >> n;
     vector < Point > legs;
     legs.reserve(m);
     for (int i = 0; i < m; i++) {</pre>
      int x, y;
cin >> x >> y;
       legs.push_back(Point(x, y));
     vector<vector<Point> > triangles;
     triangles.reserve(n);
     for (int i = 0; i < n; i++) {</pre>
       vector<Point> triangle;
       triangle.reserve(6)
       int x0, y0, x1, y1, x2, y2, x3, y3, x4, y4, x5, y5; cin >> x0 >> y0 >> x1 >> y1 >> x2 >> y2 >> x3 >> y3 >> x4 >> y4 >> x5 >> y5; Point p0(x0, y0), p1(x1, y1), p2(x2, y2), p3(x3, y3), p4(x4, y4), p5(x5, y5);
       if (CGAL::left_turn(p2, p1, p0)) {
          triangle.push_back(p0);
          triangle.push_back(p1);
       else {
          triangle.push_back(p1);
          triangle.push_back(p0);
       if (CGAL::left_turn(p4, p3, p2)) {
  triangle.push_back(p2);
          triangle.push_back(p3);
          triangle.push_back(p3);
          triangle.push_back(p2);
       if (CGAL::left_turn(p0, p5, p4)) {
          triangle.push_back(p4);
          triangle.push_back(p5);
       else {
          triangle.push_back(p5);
          triangle.push_back(p4);
       triangles.push_back(triangle);
    vector<int> leg_to_triangle(m - 1, -1);
vector<int> triangle_contributions(n, 0);
     int found_legs = 0;
     int bound_max = 0;
     int i = 0;
     while (found_legs < m - 1 && i < n) {
  for (int j = 0; j < m - 1; j++) {</pre>
          if (containsSegment(triangles[i], legs[j], legs[j + 1])) {
            if (leg_to_triangle[j] == -1) {
              found_legs++;
            else {
              triangle_contributions[leg_to_triangle[j]]--;
//cout << "remove leg " << j << " covered by " << leg_to_triangle[j] << endl;</pre>
            leg_to_triangle[j] = i;
             //cout << "leg " << j << " covered by " << i << endl;
            triangle_contributions[i]++;
         }
       }
       bound_max = i;
       i++;
    }
     int bound_min = 0;
    while (triangle_contributions[bound_min] == 0) bound_min++;
int min_range = bound_max - bound_min;
     //cout << "min: " << bound_min << " max: " << bound_max << endl;
     while (i < n) {
       for (int j = 0; j < m - 1; j++) {
         if (containsSegment(triangles[i], legs[j], legs[j + 1])) {
            triangle_contributions[leg_to_triangle[j]]--;
            leg_to_triangle[j] = i;
            triangle_contributions[i]++;
         }
       bound_max = i;
       while (triangle_contributions[bound_min] == 0) bound_min++;
       min_range = min(min_range, bound_max - bound_min);
//cout << "min: " << bound_min << " max: " << bound_max << endl;</pre>
    cout << min_range + 1 << endl;</pre>
  return 0;
}
```

7 Linear/Quadratic Programming

7.1 What is the Maximum?

Keywords: Quadratic Program, ceil_to_double, floor_to_double

```
#include <iostream>
#include <cassert>
#include <CGAL/basic.h>
#include <CGAL/QP_models.h>
#include <CGAL/QP_functions.h>
// choose exact integral type
#ifdef CGAL_USE_GMP
#include <CGAL/Gmpz.h>
typedef CGAL::Gmpz ET;
#else
#include <CGAL/MP_Float.h>
typedef CGAL::MP_Float ET;
using namespace std;
// program and solution types
typedef CGAL::Quadratic_program <int > Program;
typedef CGAL::Quadratic_program_solution <ET> Solution;
const int var_x = 0; const int X = var_x;
const int var_y = 1; const int Y = var_y;
const int var_z = 2; const int Z = var_z;
int floor_to_double(const CGAL::Quotient<ET>& x) {
  double a = floor(CGAL::to_double(x));
  while (a > x) a -= 1;
while (a + 1 <= x) a += 1;
return a;</pre>
int ceil_to_double(const CGAL::Quotient<ET>& x) {
  double a = ceil(CGAL::to_double(x));
while (a < x) a += 1;
while (a - 1 >= x) a -= 1;
int main() {
  // some basic setup stuff
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  while(true) {
     int p, a, b;
cin >> p;
     // kill switch for application
     if(p == 0) {
       break;
     cin >> a >> b;
     if(p == 1) {
                                            v- set finite lower bound (x, y \ge 0), defaults to 0
                                                         v- no upper bound
       Program lp(CGAL::SMALLER, true, 0, false, 0);
       lp.set_a(var_x, 0, 1);
       lp.set_a(var_y, 0, 1);
lp.set_b(0, 4);
       lp.set_a(var_x, 1, 4);
lp.set_a(var_y, 1, 2);
lp.set_b(1, a * b);
       lp.set_a(var_x, 2, -1);
        lp.set_a(var_y, 2, 1);
       lp.set_b(2, 1);
       // maximize: by -ax^2 so we have to minimize -by + ax^2
lp.set_c(var_y, -b);
lp.set_d(var_x, var_x, 2*a);
        // solve it
       Solution s = CGAL::solve_nonnegative_quadratic_program(lp, ET());
       assert(s.solves_quadratic_program(lp));
       if(s.is_unbounded()) {
  cout << "unbounded" << endl;</pre>
        } else if(s.is_infeasible()) {
```

```
cout << "no" << endl;
       } else {
          cout << floor_to_double(-s.objective_value()) << endl;</pre>
     } else {
        // here we have an upper bound for the variables, but no lower bound
        Program lp(CGAL::LARGER, false, 0, false, 0);
        // bounds by benji
        //z >= 0
       lp.set_u(X, true, 0);
lp.set_u(Y, true, 0);
        lp.set_1(Z, true, 0);
        // x + y >= -4
        lp.set_a(var_x, 0, 1);
       lp.set_a(var_y, 0, 1);
lp.set_b(0, -4);
        // 4x + 2y + z^2 => -ab => we substitute z^2 by just z (don't forget to do the same for the minimized formula
             dingsi)
       lings1)
// i.e. we get 4x + 2y + z >= -ab
lp.set_a(var_x, 1, 4);
lp.set_a(var_y, 1, 2);
lp.set_a(var_z, 1, 1);
       lp.set_b(1, -(a*b));
        // -x + y >= -11
       lp.set_a(var_x, 2, -1);
lp.set_a(var_y, 2, 1);
lp.set_b(2, -1);
        // minimize ax^2 + by + z^4 \Rightarrow after our substitution: <math>ax^2 + by + z^2
       lp.set_d(var_x, var_x, 2*a);
lp.set_d(var_z, var_z, 2 * 1);
lp.set_c(var_y, b);
        // solve it
        Solution s = CGAL::solve_quadratic_program(lp, ET());
        assert(s.solves_quadratic_program(lp));
       if(s.is_unbounded()) {
  cout << "unbounded" << endl;</pre>
        } else if(s.is_infeasible()) {
          cout << "no" << endl;
       } else {
          cout << ceil_to_double(s.objective_value()) << endl;</pre>
       }
    }
  }
}
```

7.2 Diets

Keywords: Quadratic Program, Non-negative quadratic program

```
#include <iostream>
#include <cassert>
#include <CGAL/basic.h>
#include <CGAL/QP_models.h>
#include <CGAL/QP_functions.h>
// choose exact integral type
\verb|#ifdef CGAL_USE_GMP| \\
#include <CGAL/Gmpz.h>
typedef CGAL::Gmpz ET;
#else
#include <CGAL/MP_Float.h>
typedef CGAL::MP_Float ET;
#endif
using namespace std;
// program and solution types
typedef CGAL::Quadratic_program <int > Program;
typedef CGAL::Quadratic_program_solution <ET> Solution;
const int var_x = 0; const int X = var_x;
const int var_y = 1; const int Y = var_y;
const int var_z = 2; const int Z = var_z;
int floor_to_double(const CGAL::Quotient<ET>& x) {
  double a = floor(CGAL::to_double(x));
  while (a > x) a -= 1;
while (a + 1 <= x) a += 1;
  return a;
int ceil_to_double(const CGAL::Quotient<ET>& x) {
  double a = ceil(CGAL::to_double(x));
while (a < x) a += 1;</pre>
  while (a - 1 >= x) a -= 1;
```

```
return a;
int main() {
  // some basic setup stuff
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  while(true) {
    int nutrient_count, food_count;
    cin >> nutrient_count >> food_count;
    // kill switch for application
if(nutrient_count == 0 && food_count == 0) {
      break:
     // create linear programming application
    Program lp(CGAL::SMALLER, true, 0, false, 0);
    // read in nutrients
    vector<int> nutrient_min;
vector<int> nutrient_max;
    nutrient_min.reserve(nutrient_count);
    nutrient_max.reserve(nutrient_count);
    for(int i = 0; i < nutrient_count; i++) {</pre>
      int min_amount, max_amount;
      cin >> nutrient_min[i] >> nutrient_max[i];
    // read in foods and amount of nutrients
    vector<int> prices;
vector<vector<int> > nutrient_amount(food_count, vector<int>(nutrient_count));
    prices.reserve(food count):
    for(int i = 0; i < food_count; i++) {</pre>
      cin >> prices[i];
      for(int j = 0; j < nutrient_count; j++) {</pre>
        cin >> nutrient_amount[i][j];
    // vars: first food, then nutrients
    // set objective
    for(int i = 0; i < food_count; i++) {</pre>
      // we want to pay the minimum
// results in the sum of food_var * food_price
      lp.set_c(i, prices[i]);
    // set inequalities
    int eq_counter = 0;
    for(int nutrient_index = 0; nutrient_index < nutrient_count; nutrient_index++) {</pre>
      for(int food_index = 0; food_index < food_count; food_index++) {</pre>
        lp.set_a(food_index, eq_counter, nutrient_amount[food_index][nutrient_index]); // A := sum over: food * amount of
              nutrition
      lp.set_b(eq_counter, nutrient_max[nutrient_index]); // A <= maximum needed</pre>
      eq_counter++;
    for(int nutrient_index = 0; nutrient_index < nutrient_count; nutrient_index++) {</pre>
      for(int food_index = 0; food_index < food_count; food_index++) {</pre>
        lp.set_a(food_index, eq_counter, nutrient_amount[food_index][nutrient_index]); // B := sum over: food * amount of
              nutrition
      }
       // B >= minimum needed
      lp.set_b(eq_counter, nutrient_min[nutrient_index]);
      lp.set_r(eq_counter, CGAL::LARGER);
      eq_counter++;
    // find solution and print out
    Solution s = CGAL::solve_nonnegative_quadratic_program(lp, ET());
    if(s.is_optimal()) {
      cout << floor_to_double(s.objective_value()) << endl;</pre>
    } else {
      cout << "No such diet." << endl;</pre>
    }
 }
}
```

```
#include <iostream>
#include <cassert>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
```

```
#include <utility>
#include <cmath>
#include <CGAL/basic.h>
#include <CGAL/QP_models.h>
#include <CGAL/QP_functions.h>
// choose exact integral type
#ifdef CGAL_USE_GMP
#include <CGAL/Gmpz.h>
typedef CGAL::Gmpz ET;
#else
#include <CGAL/MP_Float.h>
typedef CGAL::MP_Float ET;
#endif
// program and solution types
typedef CGAL::Quadratic_program <int> Program;
typedef CGAL::Quadratic_program_solution <ET> Solution;
using namespace std;
int floor_to_double(const CGAL::Quotient <ET >& x) {
  double a = floor(CGAL::to_double(x));
while (a > x) a -= 1;
  while (a + 1 <= x) a += 1;
  return a;
int ceil_to_double(const CGAL::Quotient<ET>& x) {
  double a = ceil(CGAL::to_double(x));
  while (a < x) a += 1;</pre>
  while (a - 1 >= x) a -= 1;
  return a;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  int n, m;
  for (cin >> n >> m; n != 0; cin >> m >> m) {
     Program lp(CGAL::SMALLER, true, 0, false, 0);
     for (int i = 0; i < n; i++) {</pre>
       int min_nut, max_nut;
        cin >> min_nut >> max_nut;
        lp.set_r(i, CGAL::LARGER);
       lp.set_b(i, min_nut);
lp.set_r(i + n, CGAL::SMALLER);
lp.set_b(i + n, max_nut);
     for (int i = 0; i < m; i++) {</pre>
        int price;
        cin >> price;
       lp.set_c(i, price); //add price to function to minimize
for (int j = 0; j < n; j++) {
  int nut_amount;</pre>
          cin >> nut_amount;
          lp.set_a(i, j, nut_amount);
lp.set_a(i, j + n, nut_amount);
     }
     Solution s = CGAL::solve_linear_program(lp, ET());
     assert(s.solves_linear_program(lp));
     if (s.is_infeasible() || s.is_unbounded()) {
  cout << "No such diet." << endl;</pre>
     else {
        cout << floor_to_double(s.objective_value()) << endl;</pre>
    }
  }
  return 0:
```

7.3 Portfolios

Keywords: Quadratic Program

```
#include <iostream>
#include <cassert>
#include <CGAL/basic.h>
#include <CGAL/QP_models.h>
#include <CGAL/QP_functions.h>
// choose exact integral type
```

```
#ifdef CGAL_USE_GMP
#include <CGAL/Gmpzf.h>
typedef CGAL::Gmpzf ET;
#else
#include <CGAL/MP_Float.h>
typedef CGAL::MP_Float ET;
using namespace std;
// program and solution types
typedef CGAL::Quadratic_program <int > Program;
typedef CGAL::Quadratic_program_solution <ET> Solution;
int floor_to_double(const CGAL::Quotient<ET>& x) {
  double a = floor(CGAL::to_double(x));
while (a > x) a -= 1;
  while (a + 1 <= x) a += 1;
  return a;
int ceil_to_double(const CGAL::Quotient<ET>& x) {
  double a = ceil(CGAL::to_double(x));
  while (a < x) a += 1;
  while (a - 1 >= x) a -= 1;
  return a;
int main() {
  // some basic setup stuff
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
cout << fixed << setprecision(0);</pre>
  while(true) {
    int asset_count, people_count;
    cin >> asset_count >> people_count;
    // kill switch for application
if(asset_count == 0 && people_count == 0) {
      break;
    \label{lem:containers} \mbox{\it for asset properties}
    vector < int > asset cost(asset count):
    vector < int > asset_expected_return(asset_count);
       read in asset properties
    for(int asset_index = 0; asset_index < asset_count; asset_index++) {</pre>
      cin >> asset_cost.at(asset_index) >> asset_expected_return.at(asset_index);
    // read and store covariance
    vector<vector<int> > covariance(asset_count, vector<int>(asset_count));
    for(int assetA = 0; assetA < asset_count; assetA++) {
  for(int assetB = 0; assetB < asset_count; assetB++) {</pre>
         cin >> covariance.at(assetA).at(assetB);
    // go trough each investor and calculate for him/her the result
    for(int person_index = 0; person_index < people_count; person_index++) {</pre>
       int max_cost, min_return, max_variance;
       cin >> max_cost >> min_return >> max_variance;
      // by default, we have a nonnegative QP with Ax >= b
Program qp (CGAL::LARGER, true, 0, false, 0);
       // equation counter
       int eq_counter = 0;
       // add inequastion for expected return
       for(int asset_index = 0; asset_index < asset_count; asset_index++) {</pre>
         // sum of each asset amount times its expected return
         qp.set_a(asset_index, eq_counter, asset_expected_return[asset_index]);
       // ... >= investor's expected minimal return
qp.set_b(eq_counter, min_return);
       eq_counter++;
       // add inequastion for max cost for the investor
       for(int asset_index = 0; asset_index < asset_count; asset_index++) {</pre>
         // sum of each asset's cost times how many of them we buy
         qp.set_a(asset_index, eq_counter, asset_cost[asset_index]);
              <= investor's maximum cost
       qp.set_b(eq_counter, max_cost);
       qp.set_r(eq_counter, CGAL::SMALLER);
       eq_counter++:
       // objective function
       for(int assetA = 0; assetA < asset_count; assetA++) {</pre>
         for(int assetB = 0; assetB < asset_count; assetB++) {</pre>
           qp.set_d(assetA, assetB, 2 * covariance[assetA][assetB]);
```

```
}

// calculate
Solution s = CGAL::solve_nonnegative_quadratic_program(qp, ET());
assert(s.solves_quadratic_program(qp));

// Output
if (s.is_optimal() && s.objective_value() <= max_variance) {
    cout << "Yes." << endl;
} else {
    cout << "No." << endl;
}
}

}
</pre>
```

```
#include <iostream>
#include <cassert>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
// choose exact integral type
#ifdef CGAL_USE_GMP
#include <CGAL/Gmpz.h>
typedef CGAL::Gmpz ET;
#else
#include <CGAL/MP_Float.h>
typedef CGAL::MP_Float ET;
#endif
// program and solution types
typedef CGAL::Quadratic_program<int> Program;
typedef CGAL::Quadratic_program_solution<ET> Solution;
using namespace std;
\verb|int floor_to_double(const CGAL::Quotient<ET>\& x) \{|
  double a = floor(CGAL::to_double(x));
while (a > x) a -= 1;
while (a + 1 <= x) a += 1;</pre>
int ceil_to_double(const CGAL::Quotient<ET>& x) {
  double a = ceil(CGAL::to_double(x));
while (a < x) a += 1;
while (a - 1 >= x) a -= 1;
  return a;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  //n = Total assets
  //m = number of people
   int n, m;
  for (cin >> n >> m; n != 0; cin >> n >> m) {
     Program qp(CGAL::LARGER, true, 0, false, 0);
qp.set_r(0, CGAL::SMALLER); //cost
qp.set_r(1, CGAL::LARGER); //expectet return
     //read cost and expected return of assets
     for (int i = 0; i < n; i++) {
  int cost, expected_return;</pre>
       cin >> cost >> expected_return;
qp.set_a(i, 0, cost);
qp.set_a(i, 1, expected_return);
     //read covariance matrix
     for (int i = 0; i < n; i++) {</pre>
       for (int j = 0; j < n; j++) {</pre>
          int covar;
cin >> covar;
          if (j <= i) {</pre>
            qp.set_d(i, j, covar * 2);
          }
       }
     for (int i = 0; i < m; i++) {
  int C, R, V;</pre>
        cin >> C >> R >> V;
```

```
qp.set_b(0, C);
qp.set_b(1, R);

Solution s = CGAL::solve_nonnegative_quadratic_program(qp, ET());
assert(s.solves_quadratic_program(qp));

if (s.is_infeasible() || s.is_unbounded() || s.objective_value() > V) {
    cout << "No." << endl;
}
else {
    cout << "Yes." << endl;
}
}
return 0;
}</pre>
```

7.4 Inball

Keywords: Quadratic Program, Quadratic Program: Maximize

```
#include <iostream>
#include <cassert>
#include <CGAL/basic.h>
#include <CGAL/QP_models.h>
#include <CGAL/QP_functions.h>
// choose exact integral type
#ifdef CGAL_USE_GMP
#include <CGAL/Gmpz.h>
typedef CGAL::Gmpz ET;
#include <CGAL/MP_Float.h>
typedef CGAL::MP_Float ET;
#endif
using namespace std;
// program and solution types
typedef CGAL::Quadratic_program <int> Program;
typedef CGAL::Quadratic_program_solution <ET> Solution;
int floor_to_double(const CGAL::Quotient<ET>& x) {
   double a = floor(CGAL::to_double(x));
  while (a > x) a -= 1;
while (a + 1 <= x) a += 1;
  return a;
int ceil_to_double(const CGAL::Quotient <ET >& x) {
  double a = ceil(CGAL::to_double(x));
while (a < x) a += 1;
while (a - 1 >= x) a -= 1;
  return a;
int main() {
  // some basic setup stuff
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  while(true) {
     int inequality_count;
     cin >> inequality_count;
     // kill switch for application
     if(inequality_count == 0) {
       break;
     int dimension;
     cin >> dimension;
     // create linear programming application
     Program lp(CGAL::SMALLER, false, 0, false, 0);
     // set our target of maximixing the radius, i.e. we take the negative of the radius and minimize the whole thing
int var_radius = dimension; // everything below 'dimension' is a variable for the dimensions (?)
lp.set_c(var_radius, -1); // maximize by minimizing the negative
     // \  \, {\tt add} \  \, {\tt constraints} \  \, {\tt from} \  \, {\tt input}
     for(int constraint_index = 0; constraint_index < inequality_count; constraint_index++) {</pre>
       int distance = 0:
        for(int dim_var_index = 0; dim_var_index < dimension; dim_var_index++) {</pre>
          cin >> a_i;
          lp.set_a(dim_var_index, constraint_index, a_i);
```

```
lp.set_a(dim_var_index, constraint_index + inequality_count, a_i);
       distance += a_i * a_i;
     lp.set_a(var_radius, constraint_index, sqrt(distance));
     cin >> b i:
    lp.set_b(constraint_index, b_i);
lp.set_b(constraint_index + inequality_count, b_i);
   // find solution and print out
  Solution s = CGAL::solve_linear_program(lp, ET());
   assert(s.solves_linear_program(lp));
   if(s.is_optimal()) {
    cout << -1 * ceil_to_double(s.objective_value()) << endl;</pre>
  } else if (s.is_unbounded()) {
     cout << "inf" << endl;</pre>
  } else {
     cout << "none" << endl;</pre>
  }
}
```

```
#include <iostream>
#include <cassert>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
#include <CGAL/basic.h>
#include <CGAL/QP_models.h>
#include <CGAL/QP_functions.h>
// choose exact integral type
#ifdef CGAL_USE_GMP
#include <CGAL/Gmpz.h>
typedef CGAL::Gmpz ET;
#else
#include <CGAL/MP_Float.h>
typedef CGAL::MP_Float ET;
#endif
typedef CGAL::Quadratic_program <int> Program;
typedef CGAL::Quadratic_program_solution <ET> Solution;
using namespace std;
int floor_to_double(const CGAL::Quotient<ET>& x) {
  double a = floor(CGAL::to_double(x));
while (a > x) a -= 1;
  while (a + 1 <= x) a += 1;
  return a;
int ceil_to_double(const CGAL::Quotient <ET > & x) {
  double a = ceil(CGAL::to_double(x));
  while (a < x) a += 1;</pre>
  while (a - 1 >= x) a -= 1;
  return a;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  for (cin >> n; n != 0; cin >> n) {
    int dimensions;
    cin >> dimensions;
    Program lp(CGAL::LARGER, false, 0, false, 0);
for (int i = 0; i < n; ++i) {
  int sum = 0;</pre>
       for (int j = 0; j < dimensions; ++j) {
        int ai;
         cin >> ai;
         lp.set_a(j, i, ai);
        sum += pow(ai, 2);
       lp.set_a(dimensions, i, -static_cast<long>(sqrt(sum)));
      int bi;
cin >> bi;
      lp.set_b(i, -bi);
    lp.set_l(dimensions, true, 0);
    lp.set_c(dimensions, -1);
```

```
Solution s = CGAL::solve_linear_program(lp, ET());
assert(s.solves_linear_program(lp));
if (s.status() == CGAL::QP_OPTIMAL){
    cout << -1 * ceil_to_double(s.objective_value()) << endl;
}
else if (s.status() == CGAL::QP_UNBOUNDED) {
    cout << "inf" << endl;
}
else {
    cout << "none" << endl;
}
}
return 0;
}</pre>
```

7.5 Collisions

Keywords: Point set, Delaunay Triangulation, Finite edge iteration, Triangulation with info()

```
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
#include <CGAL/Delaunay_triangulation_2.h>
#include <CGAL/Point_set_2.h>
typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
typedef CGAL::Triangulation_vertex_base_with_info_2 <int, K> Vb;
typedef CGAL::Triangulation_face_base_2<K> Fb;
typedef CGAL::Triangulation_data_structure_2 < Vb, Fb > Tds;
typedef CGAL::Delaunay_triangulation_2 < K, Tds > Triangulation;
typedef Triangulation::Edge_iterator Edge_iterator;
typedef Triangulation::Face_handle Face_handle;
typedef Triangulation::Face_iterator Face_iterator;
typedef Triangulation::All_faces_iterator All_faces_iterator;
typedef Triangulation::Finite_vertices_iterator Finite_vertices_iterator;
typedef Triangulation::Finite_edges_iterator Finite_edges_iterator;
typedef Triangulation::Point Point;
typedef Triangulation::Segment Segment;
{\tt typedef} \  \, {\tt Triangulation::Vertex\_handle} \  \, {\tt Vertex\_handle};
using namespace std;
int main() {
     some basic setup stuff
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  int test_count;
  cin >> test_count;
  for(int test = 0; test < test_count; test++) {</pre>
    int airplane_count:
    cin >> airplane_count;
     // read minimum distance
    K::FT input_dist;
    cin >> input_dist;
    K::FT min_dist = input_dist * input_dist;
    // read in airplane location
    vector<pair<Point, int> > airplanes;
    airplanes.reserve(airplane_count);
    for(int airplane_index = 0; airplane_index < airplane_count; airplane_index++) {</pre>
      int x, y;
cin >> x >> y;
       airplanes.push_back(make_pair(Point(x, y), airplane_index));
    // keeps track of planes on collision course
    vector < bool > collisions(airplane_count, false);
     // triangulate planes
    Triangulation airplane_triang;
    airplane_triang.insert(airplanes.begin(), airplanes.end());
       iterate trough all edges
    for(Finite_edges_iterator edge_iter = airplane_triang.finite_edges_begin();
      edge_iter != airplane_triang.finite_edges_end();
       ++edge_iter) {
       // get the airplanes
      Vertex_handle plane1_vertex = edge_iter->first->vertex((edge_iter->second + 1) % 3);
Vertex_handle plane2_vertex = edge_iter->first->vertex((edge_iter->second + 2) % 3);
      Point plane1 = plane1_vertex->point();
      Point plane2 = plane2_vertex->point();
      //cout << "plane1: " << plane1 << ", plane2: " << plane2 << endl;
      int plane1_index = plane1_vertex->info();
```

```
int plane2_index = plane2_vertex->info();
    //cout << "\tindex: plane1: " << plane1_index << ", plane2: " << plane2_index << endl;

    // check if distance is not violated
    K::FT plane_dist = CGAL::squared_distance(plane1, plane2);
    //cout << "\tdist: " << plane_dist << endl;

if (plane_dist < min_dist) {
    collisions.at(plane1_index) = true;
    collisions.at(plane2_index) = true;
}

// calculate how many airplanes have a plane not far enough away
int planes_in_danger = 0;
for(int plane_index = 0; plane_index < airplane_count; plane_index++) {
    if(collisions.at(plane_index)) {
        planes_in_danger++;
    }
}

cout << planes_in_danger << endl;
}

return 0;
}
</pre>
```

```
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
#include <CGAL/Delaunay_triangulation_2.h>
#include <CGAL/squared_distance_2.h>
#include <CGAL/Triangulation_face_base_with_info_2.h>
#include <CGAL/Triangulation_vertex_base_with_info_2.h>
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
typedef CGAL:: Exact predicates inexact constructions kernel K:
typedef CGAL::Triangulation_vertex_base_with_info_2 < bool, K > Vb;
typedef CGAL::Triangulation_face_base_2 < K > Fb;
typedef CGAL::Triangulation_data_structure_2 < Vb , Fb > Tds;
typedef CGAL::Delaunay_triangulation_2 < K, Tds > Triangulation;
typedef Triangulation::Edge_iterator Edge_iterator;
typedef Triangulation::Face_handle Face_handle;
typedef Triangulation::Face_iterator Face_iterator;
typedef Triangulation::All_faces_iterator All_faces_iterator;
typedef Triangulation::Finite_vertices_iterator Finite_vertices_iterator;
typedef Triangulation::Finite_edges_iterator Finite_edges_iterator;
typedef Triangulation::Point Point;
typedef Triangulation::Segment Segment;
using namespace std;
double floor_to_double(const K::FT& x)
  double a = std::floor(CGAL::to_double(x));
  while (a > x) a -= 1;
  while (a + 1 <= x) a += 1;
  return a;
double ceil_to_double(const K::FT& x)
  double a = std::ceil(CGAL::to_double(x));
 while (a < x) a += 1;
while (a - 1 >= x) a -= 1;
 return a;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
 cout << fixed << setprecision(0);</pre>
  int nr_testcases;
  cin >> nr_testcases;
  for (int testcase = 0; testcase < nr_testcases; testcase++) {</pre>
    int nr_planes;
    K::FT min_distance;
    cin >> nr_planes >> min_distance;
    K::FT min_distance_squared = min_distance*min_distance;
    vector < Point > points;
points.reserve(nr_planes);
    for (int i = 0; i < nr_planes; i++) {</pre>
      int x, y;
cin >> x >> y;
      points.push_back(Point(x, y));
```

```
Triangulation t;
t.insert(points.begin(), points.end());

for (Finite_vertices_iterator it = t.finite_vertices_begin(); it != t.finite_vertices_end(); ++it) {
    it->info() = false;
}

for (Finite_edges_iterator it = t.finite_edges_begin(); it != t.finite_edges_end(); ++it) {
    Triangulation::Vertex_handle vi = it->first->vertex((it->second + 1) ¼ 3);
    Triangulation::Vertex_handle v = it->first->vertex((it->second + 2) ¼ 3);
    K::FT d = CGAL::squared_distance(v1->point(), v2->point());
    if (d < min_distance_squared) {
        v1->info() = true;
        v2->info() = true;
    }
}

int colliding_planes = 0;
for (Finite_vertices_iterator it = t.finite_vertices_begin(); it != t.finite_vertices_end(); ++it) {
    if (it->info()) {
        colliding_planes << endl;
}

cout << colliding_planes << endl;
}

return 0;
}
</pre>
```

8 Exam Preparation

8.1 TheeV

Keywords: CGAL, Minimal Circle, Custom compare, Compare function, Binary search

```
#include <iostream>
#include <cmath>
#include <unordered_set>
#include <CGAL/Exact_predicates_exact_constructions_kernel.h>
#include <CGAL/Min_circle_2.h>
#include <CGAL/Min_circle_2_traits_2.h>
#include <CGAL/number_utils.h>
// typedefs
typedef CGAL::Exact_predicates_exact_constructions_kernel K;
typedef CGAL::Min_circle_2_traits_2<K> Traits;
typedef CGAL::Min_circle_2<Traits>
                                            Min_circle;
typedef K::Point_2 Point;
using namespace std;
// global vars, needed by multiple functions
Point capital;
vector < Point > cities;
vector <K::FT> distances;
   from slides, fun!
double floor_to_double(const K::FT& x)
  double a = std::floor(CGAL::to_double(x));
  while (a > x) a -= 1;
  while (a+1 <= x) a += 1;
  return a;
double ceil_to_double(const K::FT& x)
  double a = std::ceil(CGAL::to_double(x));
  while (a < x) a += 1;
  while (a-1 >= x) a -= 1;
  return a;
bool city_order(Point cityA, Point cityB) {
  return squared_distance(cityA, capital) > squared_distance(cityB, capital);
int main() {
  // some basic setup stuff
  cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  int test_count;
  cin >> test_count;
  for(int t = 0; t < test_count; t++) {</pre>
    int city_count;
    cin >> city_count;
     // check for early termination
    if(city_count <= 2) {</pre>
      int ignore;
      // read in not needed information
      cin >> ignore >> ignore;
if(city_count == 2) {
        cin >> ignore >> ignore;
       // put in each of the cities one antenna with radius 0, done.
      cout << 0 << endl;
      continue;
    // read in capital city
    double capital_x, capital_y;
cin >> capital_x >> capital_y;
    capital = Point(capital_x, capital_y);
    // create vector containing all non-capital cities
    cities = vector < Point > (city_count - 1); // capital not part of it
    // read in city coordinates
    for(int city_index = 1; city_index < city_count; city_index++) { // capital already read, so start with 1, i.e.</pre>
         second city
      double city_x, city_y;
cin >> city_x >> city_y;
      cities.at(city_index - 1) = Point(city_x, city_y);
    // sort cities by descending distance from the capital
```

```
sort(cities.begin(), cities.end(), city_order);
    // create vector with all distances for each city from the capital
distances = vector<K::FT>(city_count - 1);
for(int i = 0; i < city_count - 1; i++) {</pre>
      distances.at(i) = squared_distance(cities.at(i), capital);
    // initiate radius temporary information
    K::FT radius1 = distances[1]; // currently the first antenna has maximal radius to contain in the furthest city
    K::FT old_radius1 = radius1;
    K::FT radius2 = 0.0; // second antenno has no radius yet
    K::FT old_radius2 = 0.0;
     // create min circle for all cities
    Min_circle min_circ_antenna2(cities.begin(), ++cities.begin(), true); // antenna 2 contains only the city farthest
         away from first anntena as a start
    Traits::Circle circ2;
    int cur_index = 1;
    // make first antenna's radius smaller and second antenna's radius larger to find an optimum
while(radius2 < radius1) { // iterate as long as the second antenna is still smaller as the first one</pre>
       // move current radius to old radius
       old_radius1 = radius1;
       old_radius2 = radius2;
      // add next outmost city to antenna 2's reach
      min_circ_antenna2.insert(cities[cur_index]);
       // get the circle of the min circ to get information about the radius
       circ2 = min_circ_antenna2.circle();
       // update radius
      radius1 = distances[cur_index + 1]; // first antenna only has to reach one city less as the one after that is now
           covered by the second antenna
       radius2 = circ2.squared_radius();
       // update index, maybe we add another city to second antenna's reach
       cur_index++;
    // we updates all four radius variables, now extract the optimum K\colon\colon FT result = min( // we're interested in the minimum radius needed
      max(radius1, radius2), // we must take the maximum of both, as both antenna have to have the same radius!
       max(old_radius1, old_radius2) // same reason as before
    cout << ceil_to_double(result) << endl;</pre>
 }
}
```

```
#include <CGAL/Exact_predicates_exact_constructions_kernel.h>
#include <CGAL/Min_circle_2.h>
#include <CGAL/Min_circle_2_traits_2.h>
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
typedef CGAL::Exact_predicates_exact_constructions_kernel K;
typedef CGAL::Min_circle_2_traits_2<K> Traits;
typedef CGAL::Min_circle_2<Traits> Min_circle;
typedef K::Point_2 Point;
using namespace std;
double floor_to_double(const K::FT& x)
 double a = std::floor(CGAL::to_double(x));
 while (a > x) a -= 1;
  while (a + 1 <= x) a += 1;
double ceil_to_double(const K::FT& x)
  double a = std::ceil(CGAL::to_double(x));
 while (a < x) a += 1;
while (a - 1 >= x) a -= 1;
 return a;
int main() {
 cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  int nr_testcases;
  cin >> nr_testcases;
  for (int testcase = 0; testcase < nr_testcases; testcase++) {</pre>
```

```
cin >> n;
  vector < Point > points(n);
vector < K::FT > distances(n);
  for (int i = 0; i < n; i++) {</pre>
    int x, y;
cin >> x >> y;
    points[i] = Point(x, y);
     distances[i] = CGAL::squared_distance(points[0], points[i]);
  vector <K::FT> distances_sorted = distances;
  sort(distances_sorted.begin(), distances_sorted.end());
  int min_bound = 0;
  int max_bound = distances_sorted.size() - 1;
  while (min_bound != max_bound) {
     int half = (min_bound + max_bound) / 2;
    K::FT squared_dist = distances_sorted[half];
//cout << "min = " << min_bound << " max = " << max_bound << " half = " << half << " squared_dist = " <<</pre>
          squared_dist << endl;
     vector < Point > uncovered_points;
     for (int i = 0; i < n; i++) {
  if (distances[i] > squared_dist) {
    //cout << "adding point" << points[i] << endl;</pre>
         uncovered_points.push_back(points[i]);
     //cout << uncovered_points.size() << endl;</pre>
    Min_circle mc(uncovered_points.begin(), uncovered_points.end(), true);
//cout << "valid = " << mc.is_valid() << endl;</pre>
     K::FT second_rad_squared = mc.circle().squared_radius();
     //cout << "second_rad_squared = " << second_rad_squared << endl;</pre>
     if (second_rad_squared > squared_dist) {
       //cout << "increase lower bound" << endl;</pre>
       if (second_rad_squared < distances_sorted[half + 1]) {</pre>
         max_bound = min_bound = half;
       else {
         min_bound = half + 1;
       }
     else {
       //cout << "decrease upper bound" << endl;</pre>
       max_bound = half;
  }
  K::FT squared_dist = distances_sorted[min_bound];
  vector < Point > uncovered_points;
  for (int i = 0; i < n; i++) {
    if (distances[i] > squared_dist) {
       uncovered_points.push_back(points[i]);
    }
  Min_circle mc(uncovered_points.begin(), uncovered_points.end(), true);
  K::FT second_rad_squared = mc.circle().squared_radius();
  cout << ceil_to_double(max(squared_dist, second_rad_squared)) << endl;</pre>
return 0;
```

8.2 Algocoön Group

Keywords: BGL, Graph with edge capacity, Graph with residual capacity, Graph with reverse edges, Max-flow

```
#include <iostream>
#include <vector>
#include <queue>
#include <tuple>
#include <cmath>
#include <climits>
#include <algorithm>
#include <climits>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/push_relabel_max_flow.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list_traits<vecS, vecS, directedS> Traits;
typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
    property < edge_capacity_t , int ,</pre>
    property < edge_residual_capacity_t, int,</pre>
    property<edge_reverse_t, Traits::edge_descriptor> > > Graph;
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
typedef property_map < Graph, edge_capacity_t >:: type EdgeCapacityMap;
```

```
typedef property_map <Graph, edge_residual_capacity_t>::type ResidualCapacityMap;
typedef property_map < Graph , edge_reverse_t >:: type ReverseEdgeMap;
int main(void)
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test_count;
    cin >> test_count;
    for(int test_index = 0; test_index < test_count; test_index++) {</pre>
        int figure_count, limb_count;
        cin >> figure_count >> limb_count;
        // create graph
        Graph graph(figure_count);
         // get graph's properties
        EdgeCapacityMap capacity = get(edge_capacity, graph);
        ReverseEdgeMap reverse_edge_map = get(edge_reverse, graph);
ResidualCapacityMap res_capacity = get(edge_residual_capacity, graph);
        // read in limbs
        for(int limb_index = 0; limb_index < limb_count; limb_index++) {</pre>
             int from, to, cost;
             cin >> from >> to >> cost;
             Edge edge;
             Edge rev_edge;
             tie(edge, tuples::ignore) = add_edge(from, to, graph);
             tie(rev_edge, tuples::ignore) = add_edge(to, from, graph);
             capacity[edge] = cost;
             capacity[rev_edge] = 0;
             reverse_edge_map[edge] = rev_edge;
             reverse_edge_map[rev_edge] = edge;
        // find bist source and sink
        int best_source = -1;
        int best_sink = -1;
        int best_value = numeric_limits < int >:: max();
         // attention: start at 1, otherwise assertion because sink == source
        for(int figure_index = 1; figure_index < figure_count; figure_index++) {</pre>
             // search for best sink
int max_flow = push_relabel_max_flow(graph, 0, figure_index);
             if(max_flow < best_value) {</pre>
                 best_value = max_flow;
                 best_source = 0;
                 best_sink = figure_index;
             }
             // search for best source
             max_flow = push_relabel_max_flow(graph, figure_index, 0);
if(max_flow < best_value) {</pre>
                 best_value = max_flow;
                 best_source = figure_index;
                 best_sink = 0;
            }
        // rerun for found best sink and source
        push_relabel_max_flow(graph, best_source, best_sink);
        std::queue < int > Q;
        Q.push(best_source);
        vector < bool > visited(figure_count, false);
        visited.at(best_source) = true;
        while(!Q.empty()) {
             const int figure = Q.front();
             Q.pop();
             graph_traits < Graph >:: out_edge_iterator out_iter, out_end;
             for(tie(out_iter, out_end) = out_edges(figure, graph); out_iter != out_end; ++out_iter) {
                 const int edge_end_v = target(*out_iter, graph);
                 if(res_capacity[*out_iter] == 0 || visited[edge_end_v]) {
                      continue:
                 visited[edge_end_v] = true;
                 Q.push(edge_end_v);
            }
        cout << best_value << endl << count(visited.begin(), visited.end(), true);</pre>
        for(int i = 0; i < figure_count; i++) {</pre>
            if(visited[i]) {
    cout << " " << i;</pre>
        cout << endl;
```

```
return 0;
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <map>
#include <string>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/push_relabel_max_flow.hpp>
#include <boost/graph/connected_components.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, directedS> Traits;
typedef adjacency_list<vecS, vecS, directedS, no_property, property<edge_capacity_t, long, property<
    edge_residual_capacity_t, long, property<edge_reverse_t, Traits::edge_descriptor> > > S Graph;
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits<Graph>::vertex_descriptor Vertex;
typedef property_map < Graph , edge_capacity_t >: : type EdgeCapacityMap;
typedef property_map < Graph, edge_reverse_t >: : type ReverseEdgeMap;
typedef property_map < Graph, edge_residual_capacity_t >: : type ResidualMap;
inline void add_flow_edge(int start, int end, int c, EdgeCapacityMap& capacity, ReverseEdgeMap& rev_edge, Graph& g) {
  Edge e, rev_e;
  bool success:
  tie(e, success) = add_edge(start, end, g);
  if (success) {
     tie(rev_e, success) = add_edge(end, start, g);
     capacity[e] = c;
     capacity[rev_e] = 0;
    rev_edge[e] = rev_e;
    rev_edge[rev_e] = e;
  else {
    capacity[e] += c;
  }
}
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_figures, nr_limbs;
     cin >> nr_figures >> nr_limbs;
    Graph g(nr_figures);
    EdgeCapacityMap capacity = get(edge_capacity, g);
ReverseEdgeMap rev_edge = get(edge_reverse, g);
     ResidualMap residual_map = get(edge_residual_capacity, g);
    for (int i = 0; i < nr_limbs; i++) {</pre>
       int from, to, cost;
cin >> from >> to >> cost;
       add_flow_edge(from, to, cost, capacity, rev_edge, g);
     int best_sink;
     int best_source;
     int min_flow = numeric_limits < int >:: max();
     for (int i = 1; i < nr_figures; i++) {</pre>
       int flow = push_relabel_max_flow(g, 0, i);
       if (flow < min_flow) {</pre>
         min_flow = flow;
         best_source = 0;
best_sink = i;
       flow = push_relabel_max_flow(g, i, 0);
       if (flow < min_flow) {</pre>
         min_flow = flow;
         best_source = i;
         best_sink = 0;
     min_flow = push_relabel_max_flow(g, best_source, best_sink);
     vector<int> vis(nr_figures, false);
     vis[best_source] = true;
     std::queue < int > to_visit;
     to_visit.push(best_source);
```

```
while (!to_visit.empty()) {
     const int u = to_visit.front();
     to_visit.pop();
     graph_traits < Graph > :: out_edge_iterator ebeg, eend;
     for (tie(ebeg, eend) = out_edges(u, g); ebeg != eend; ++ebeg) {
  const int v = target(*ebeg, g);
  if (residual_map[*ebeg] == 0 || vis[v]) {
          continue;
       vis[v] = true;
       to_visit.push(v);
  }
  cout << min_flow << endl;</pre>
  cout << count(vis.begin(), vis.end(), true);</pre>
  for (int i = 0; i < nr_figures; ++i) {</pre>
    if (vis[i]) {
   cout << " " << i;
  }
  cout << endl;
return EXIT_SUCCESS;
```

8.3 Monkey Island

Keywords: BGL, Strong component, Edge iteration, Uses class, Custom compare, Compare function, Greedy, DFS (Graph)

```
#include <iostream>
#include <vector>
#include <queue>
#include <tuple>
#include <cmath>
#include <climits>
#include <algorithm>
#include <climits>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/strong_components.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, directedS, no_property, no_property> Graph;
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits<Graph>::vertex_descriptor Vertex;
typedef graph_traits < Graph > :: edge_iterator EdgeIterator;
int main (void)
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test_cases;
    cin >> test_cases;
    for(int i = 0; i < test_cases; i++) {</pre>
         int location_count, road_count;
         cin >> location_count >> road_count;
         // create graph
         Graph graph(location_count);
         // read in directed roads and create edges for them
         for(int j = 0; j < road_count; j++) {</pre>
             // read vertices information
             int from, to;
             cin >> from >> to:
             // locations start at 1, inside our graph at 0
             from -= 1;
             to -= 1;
             // create edge
             add_edge(from, to, graph);
         // read in costs for building police station at a vertex
         vector<int> costs(location_count);
         for(int j= 0; j < location_count; j++) {</pre>
             cin >> costs.at(j);
//cout << "-> " << costs.at(j) << endl;;</pre>
         // retrieve strong components (maximum set of vertices for which we have a path from any pair in this set).
```

```
// records which strong component set has an incoming edge from an other strong component set
    vector < bool > incoming(scc_count, false);
    // iterate over all graph edges
    EdgeIterator edge_iter, edge_end;
    for(tie(edge_iter, edge_end) = edges(graph); edge_iter != edge_end; ++edge_iter) {
        // get vertices connected by the edge
        int from_vertex = source(*edge_iter, graph);
        int to_vertex = target(*edge_iter, graph);
           check that both vertices are not part of the same strong component
        if(scc[from_vertex] != scc[to_vertex]) {
             // ok, so both vertices don't have edges in both directions.
// furthermore we have a *directed* edge from the strong component set of from_vertex to the one of
                 to_vertex, record that we have an incoming
             // edge.
             incoming[scc[to_vertex]] = true;
    }
    // so, now we know which strong component set has incoming edges from other sets. Therefore we don't have to
    build a police station inside a strong component

// set that has an incoming edge! Reason: we can build one in the strong component set that has an edge to the
other set and with that we reach all vertices in
    // both strong component sets.
    // keeps track of minimum costs needed
    vector<int> min_costs(scc_count, numeric_limits<int>::max());
    // iterate over all locations
    for(int location_index = 0; location_index < location_count; location_index++) {</pre>
        if(!incoming[scc[location_index]]) {
            // the strong component set the location belongs to has *no* incoming edge.
             // assign the minimum cost for the strong component set the current location belongs to is defined
             // by the smaller number from the set {already known minimum, cost to build in the current location a
                 police station}
            min_costs[scc[location_index]] = min(min_costs[scc[location_index]], costs[location_index]);
        }
    // sum up the costs for all police stations, jumping over strong component sets with incoming edges!
    int cost_sum = 0;
for(int scc_index = 0; scc_index < scc_count; scc_index++) {</pre>
        if(!incoming[scc_index]) {
    //cout << "==> " << cost_sum << " + " << min_costs[scc_index] << " = ";</pre>
             cost_sum += min_costs[scc_index];
             //cout << cost_sum << endl;</pre>
        }
    // out with result
    cout << cost_sum << endl;</pre>
return 0;
```

```
#include <iostream>
#include <vector>
#include <algorithm>
#include <iomanip>
#include <queue>
#include <limits>
#include <stack>
using namespace std;
class Location {
public:
 int cost, id;
  bool visited:
  vector < Location *> roads;
 Location(int id)
    : cost(0), id(id), visited(false), roads(vector < Location *>()) {}
bool sortLocations(const Location* lhs, const Location* rhs) {
 return lhs->cost < rhs->cost;
int main(void) {
  int cases;
  cin >> cases;
  for (int c = 0; c < cases; c++) {</pre>
   int nr_locations;
    cin >> nr_locations;
    int nr_roads;
    cin >> nr_roads;
```

}

```
vector < Location *> locations (nr_locations, NULL);
    for (int i = 0; i < nr_locations; i++) {</pre>
      locations[i] = new Location(i + 1);
    for (int i = 0; i < nr_roads; i++) {</pre>
      int from, to;
      cin >> from >> to;
      locations[from - 1]->roads.push_back(locations[to - 1]);
    for (int i = 0; i < nr_locations; i++) {</pre>
      int cost;
      cin >> cost;
      locations[i]->cost = cost;
    sort(locations.begin(), locations.end(), sortLocations);
    int cost = 0;
for (int i = 0; i < nr_locations; i++) {</pre>
      Location* currentLoc = locations[i];
//cout << "Location " << currentLoc->id << " with cost " << currentLoc->cost << endl;
       if (!currentLoc->visited) {
         cost += currentLoc->cost;
         int tmpCost = currentLoc->cost;
         stack < Location *> locToVisit;
         locToVisit.push(currentLoc);
         vector < bool > vis(nr_locations, false);
         while (!locToVisit.empty()) {
           Location* nextLocation = locToVisit.top();
           locToVisit.pop();
           if (!vis[nextLocation->id]) {
             if (nextLocation->visited)
               if (nextLocation->cost > 0) {
                 //cout << "Reducing cost by " << nextLocation->cost << endl;
cost -= nextLocation->cost;
                 nextLocation -> cost = 0:
               }
             else {
               nextLocation -> visited = true;
               nextLocation -> cost = 0;
             vis[nextLocation->id] = true;
             for (unsigned int j = 0; j < nextLocation->roads.size(); j++) {
               locToVisit.push(nextLocation->roads[j]);
             }
          7
        currentLoc->cost = tmpCost;
    cout << cost << endl;
for (int i = 0; i < nr_locations; i++) {</pre>
      delete locations[i];
 }
}
```

8.4 Odd Route

Keywords: ACM, BFS (Graph), Custom BFS

```
#include <iostream>
#include <algorithm>
#include <vector>
#include <queue>
using namespace std;
int main() {
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test_cases;
    cin >> test_cases;
    for(int test = 0; test < test_cases; test++) {</pre>
        // get graph properties
        int vertex_count, edge_count;
cin >> vertex_count >> edge_count;
        // get start and target vertices
        int start_vertex, target_vertex;
        cin >> start_vertex >> target_vertex;
        // read in vertices
        vector < Vertex > vertices(vertex_count);
        for(int edge_index = 0; edge_index < edge_count; edge_index++) {</pre>
             int from, to, weight;
             cin >> from >> to >> weight;
             vertices.at(from).edges.push_back(make_pair(to, weight));
```

```
}
        priority_queue < NextMove , vector < NextMove > , MoveCompare > to_visit;
        to_visit.push(NextMove(start_vertex, 0, 0));
        int shortest_weight_sum = numeric_limits<int>::max();
        while(!to_visit.empty()) {
             NextMove cur_move = to_visit.top();
             to_visit.pop();
             if(cur_move.is_odd_weight()) {
                 if(cur_move.is_odd_length()) {
                         odd weight, odd length
                      if(vertices.at(cur_move.current_vertex).visited_odd_edges_odd_weight) {
                          // next edge was already visited with odd weight and odd length, do not revisit
                          continue:
                      } else {
                          if(cur_move.current_vertex == target_vertex) {
                              // found the end with searched configuration, update shortest weight shortest_weight_sum = cur_move.weight_sum;
                              break;
                          }
                          // visited it now with the configuration
                          vertices[cur_move.current_vertex].visited_odd_edges_odd_weight = true;
                 } else {
                      // odd weight, even length
                      if(vertices.at(cur_move.current_vertex).visited_even_edges_odd_weight) {
                          // already visited with that configuration
                          continue;
                      } else {
                          vertices.at(cur_move.current_vertex).visited_even_edges_odd_weight = true;
                 }
             } else {
                 if(cur_move.is_odd_length()) {
                         even weight, odd length
                      if(vertices.at(cur_move.current_vertex).visited_odd_edges_even_weight) {
                          \ensuremath{//} already visited with that configuration
                          continue:
                      } else {
                          vertices.at(cur_move.current_vertex).visited_odd_edges_even_weight = true;
                      }
                 } else {
                      // even weight, even length
                      if(vertices.at(cur_move.current_vertex).visited_even_edges_even_weight) {
                          // already visited with that configuration
                          continue;
                      } else {
                          vertices.at(cur_move.current_vertex).visited_even_edges_even_weight = true;
                      }
                 }
             }
             // ok, if we reach this point, we found an edge that we didn't visit in the current configuration,
             // have to visit it with current configuration
vector<pair<int, int> >& edges = vertices.at(cur_move.current_vertex).edges;
             for(int next_edge = 0; next_edge < edges.size(); next_edge++) {
    to_visit.push(NextMove(edges.at(next_edge).first, // use the next vertex that can be reached by current</pre>
                      vertex
                      cur_move.weight_sum + edges.at(next_edge).second, // add weight of the edge we would follow
                      cur_move.edges_length + 1)); // we use an edge more, wow!
             }
        if(shortest_weight_sum == numeric_limits<int>::max()) {
             cout << "no"
                           << endl;
        } else {
             cout << shortest_weight_sum - 1 << endl;</pre>
    }
    return 0;
}
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>

using namespace std;

class Vertex {
public:
   bool v_even_edges_even_weight;
   bool v_even_edges_odd_weight;
   bool v_odd_edges_even_weight;
   bool v_odd_edges_odd_weight;
   bool v_odd_edges_odd_weight;
   vector<pair<int, int> > edges;
```

```
Vertex() {
    v_even_edges_even_weight = false;
    v_even_edges_odd_weight = false;
v_odd_edges_even_weight = false;
    v_odd_edges_odd_weight = false;
  }
};
class Move {
public:
  int current_vertex;
  int weight_sum;
  int edges_sum;
  Move(int current_vertex, int weight_sum, int edges_sum)
    : current_vertex(current_vertex), weight_sum(weight_sum), edges_sum(edges_sum)
  bool is_odd_weight() { return weight_sum % 2; }
bool is_odd_edges() { return edges_sum % 2; }
}:
struct MoveComparator {
  bool operator() (const Move& lhs, const Move& rhs) {
    return lhs.weight_sum > rhs.weight_sum;
};
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test case = 0: test case < nr test cases: test case++) {</pre>
    int nr_vertices, nr_edges;
    cin >> nr_vertices >> nr_edges;
    vector < Vertex > vertices(nr_vertices);
    int start, end;
    cin >> start >> end;
    for (int i = 0; i < nr_edges; i++) {</pre>
      int from, to, weight;
cin >> from >> to >> weight;
       vertices[from].edges.push_back(make_pair(to, weight));
    priority_queue < Move, vector < Move>, MoveComparator > to_visit;
    to_visit.push(Move(start, 0, 0));
int shortest_weight_sum = -1;
    while (!to_visit.empty()) {
  Move cur_move = to_visit.top();
       to_visit.pop();
       if (cur_move.is_odd_weight()) {
         if (cur_move.is_odd_edges()) {
           if (vertices[cur_move.current_vertex].v_odd_edges_odd_weight) {
             continue;
           }
           else {
             if (cur_move.current_vertex == end) {
               shortest_weight_sum = cur_move.weight_sum;
             }
             vertices[cur_move.current_vertex].v_odd_edges_odd_weight = true;
           }
           if (vertices[cur_move.current_vertex].v_even_edges_odd_weight) {
           7-
           else {
             vertices[cur_move.current_vertex].v_even_edges_odd_weight = true;
        }
      }
       else {
         if (cur_move.is_odd_edges()) {
           if (vertices[cur_move.current_vertex].v_odd_edges_even_weight) {
             continue;
           }
             vertices[cur_move.current_vertex].v_odd_edges_even_weight = true;
         }
         else {
           if (vertices[cur_move.current_vertex].v_even_edges_even_weight) {
             continue;
           }
           else {
             vertices[cur_move.current_vertex].v_even_edges_even_weight = true;
       vector < pair < int , int > >& edges = vertices[cur_move.current_vertex].edges;
```

```
for (int i = 0; i < edges.size(); i++) {
    to_visit.push(Move(edges[i].first, cur_move.weight_sum + edges[i].second, cur_move.edges_sum + 1));
}

if (shortest_weight_sum == -1) {
    cout << "no" << endl;
}
else {
    cout << shortest_weight_sum << endl;
}
}

return 0;
}</pre>
```

8.5 Divisor Distance

Keywords: Prime Sieve, Next Prime, ACM

```
#include <iostream>
#include <algorithm>
#include <vector>
#include <queue>
#include <bitset>
using namespace std;
#define MAX PRIM 10000000
bitset < MAX_PRIM > is_prime;
void prime_sieve() {
  is_prime.set(); // sets all to true
  // 0, 1 not prime
  is_prime.reset(0);
  is_prime.reset(1);
  for(int prime = 2; prime * prime <= MAX_PRIM; prime++) {
  if(is_prime.test(prime)) {</pre>
      \ensuremath{//} is a prime number, so all multiples of it are not
      for(int multiple = prime + prime; multiple < MAX_PRIM; multiple += prime) {</pre>
         is_prime.reset(multiple); // set multiple to false, as it is not prime
      }
 }
}
int get_next_prime(int cur) {
  for(int i = cur + 1; i * i < MAX_PRIM; i ++) {
    if(is_prime.test(i)) {</pre>
      return i;
    }
 }
  return 0;
int main() {
  cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test cases:
    cin >> test_cases;
    prime_sieve();
    for(int test = 0; test < test_cases; test++) {</pre>
       int max_nr, vertices_pair_count;
       cin >> max_nr >> vertices_pair_count;
      for(int vertices_pair_index = 0; vertices_pair_index < vertices_pair_count; vertices_pair_index++) {</pre>
         int from, to;
         cin >> from >> to;
         int length = 0;
         int a_factor = 2;
         int b_factor = 2;
         // divise 'from' and 'to' with prime numbers as long as they do not match
         while(from != to) {
              always lower the current "maximum" of 'from' and 'to'
           if(from > to) {
             if(is_prime.test(from)) {
               from = 1;
             } else {
               // find a divisor for current 'from'
while(from % a_factor != 0) {
                 a_factor = get_next_prime(a_factor);
                // found a divisor for 'from', " " remove " " it
               from = from / a_factor;
```

```
#include <iostream>
#include <vector>
#include <algorithm>
#include <iomanip>
#include <queue>
#include <limits>
#include <cmath>
using namespace std;
int main(void) {
  ios_base::sync_with_stdio(false);
   const int max_n = 10000000;
   const int sqrt_max_n = sqrt(max_n) + 1;
   vector < bool > is_prime(max_n, true);
   vector < int > primes;
   //cout << "Calculating primes" << endl;</pre>
   is_prime[0] = false;
is_prime[1] = false;
for (int i = 2; i <= sqrt_max_n; i++) {</pre>
     if (is_prime[i]) {
  for (int j = 2 * i; j <= max_n; j += i) {
    is_prime[j] = false;
}</pre>
     }
  }
  //cout << "Adding primes to vector" << endl;
for (int i = 0; i <= max_n; i++) {
  if (is_prime[i]) {</pre>
        primes.push_back(i);
     }
  }
   int tests:
   cin >> tests;
   //cout << "Starting tests" << endl;</pre>
   for (int test = 0; test < tests; test++) {</pre>
     int n, cases;
cin >> n >> cases;
      for (int c = 0; c < cases; c++) {</pre>
        int v1, v2, hops = 0;
         int v1, v2, hops = 0,
cin >> v1 >> v2;
while (v1 != v2) {
   if (v1 > v2) {
      //cout << "Changing " << v1 << " to " << largest_div[v1] << endl;
      if (is_prime[v1]) {
            v1 = 1.</pre>
              v1 = 1;
}
               else {
                 for (unsigned int j = 0; j < primes.size(); j++) {
  if (v1 % primes[j] == 0) {
    v1 = v1 / primes[j];</pre>
                      break;
                    }
                 }
              }
               //v1 = largest_div[v1];
              hops++;
               //cout << "Changing " << v2 << " to " << largest_div[v2] << endl; if (is_prime[v2]) {
                 v2 = 1;
              }
                 for (unsigned int j = 0; j < primes.size(); j++) {
  if (v2 % primes[j] == 0) {</pre>
```

```
v2 = v2 / primes[j];
break;
}
}

//v2 = largest_div[v2];
hops++;
}
cout << hops << endl;
}
}</pre>
```

8.6 Portfolios Revisited

Keywords: CGAL, Quadratic Program, Non-negative quadratic program, Exponential bound search, Binary search

```
#include <iostream>
#include <cassert>
#include <CGAL/basic.h>
#include <CGAL/QP_models.h>
#include <CGAL/QP_functions.h>
// choose exact integral type
#ifdef CGAL_USE_GMP
#include <CGAL/Gmpzf.h>
typedef CGAL::Gmpzf ET;
#else
#include <CGAL/MP Float.h>
typedef CGAL::MP_Float ET;
#endif
using namespace std;
// program and solution types
typedef CGAL::Quadratic_program<int> Program;
typedef CGAL::Quadratic_program_solution <ET> Solution;
int floor_to_double(const CGAL::Quotient <ET >& x) {
  double a = floor(CGAL::to_double(x));
while (a > x) a -= 1;
while (a + 1 <= x) a += 1;</pre>
  return a;
int ceil_to_double(const CGAL::Quotient<ET>& x) {
  double a = ceil(CGAL::to_double(x));
while (a < x) a += 1;</pre>
  while (a - 1 >= x) a -= 1;
}
bool feasible(int asset_count, int max_cost, int max_covar, int expected_return, vector<int>& asset_costs, vector<int>&
    asset_returns, vector<vector<int> >& asset_covar) {
  // use quadratic programming to check if given parameters result in a feasable result, i.e. given parameters result in
       a possible solution
  // create QP program: lower bound is 0 for amount of assets bough and generally we're interested in <= inequastions
  Program qp(CGAL::SMALLER, true, 0, false, 0);
    restrict total cost
  for(int asset_index = 0; asset_index < asset_count; asset_index++) {</pre>
   qp.set_a(asset_index, 0, asset_costs.at(asset_index)); // sum of all asset's cost that were bought must be ...
  qp.set_b(0, max_cost); // ... <= maximum cost investor is ready to pay
  // restrict how much expected return we expect, be careful as our general operation is '<=', we have to switch it here,
        as we wan't at least some amount of
  // expected return
  for(int asset_index = 0; asset_index < asset_count; asset_index++) {</pre>
    qp.set_a(asset_index, 1, asset_returns[asset_index]); // sum of all asset's expected return that were bought must be
  qp.set_r(1, CGAL::LARGER); // ... >= ...
qp.set_b(1, expected_return); // the expected return
  // set the objective function:
    total portfolio variance must be not too large
  for(int assetA_index = 0; assetA_index < asset_count; assetA_index++) {</pre>
    for(int assetB_index = 0; assetB_index <= assetA_index; assetB_index++) { // careful: '<= assetA_index'!</pre>
      qp.set_d(assetA_index, assetB_index, 2 * asset_covar.at(assetA_index).at(assetB_index)); // careful: don't forget
           the 2 \ast because of how the matrix works..
   }
  }
  Solution sol = CGAL::solve_nonnegative_quadratic_program(qp, ET());
  return sol.is_optimal() && sol.objective_value() <= max_covar;</pre>
}
```

```
int main() {
  // some basic setup stuff
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  while(true) {
    int asset_count, friend_count;
    cin >> asset_count >> friend_count;
      kill switch
    if(asset_count == 0 && friend_count == 0) {
    }
    // collect asset costs and risk factors
    vector <int > asset_costs(asset_count);
    vector <int> asset_returns(asset_count);
    for(int asset_index = 0; asset_index < asset_count; asset_index++) {</pre>
      cin >> asset_costs.at(asset_index) >> asset_returns.at(asset_index);
    // collect covariance between two assets
    vector<vector<int > > asset_covar(asset_count, vector<int>(asset_count));
    for(int assetA_index = 0; assetA_index < asset_count; assetA_index++) {</pre>
     for(int assetB_index = 0; assetB_index < asset_count; assetB_index++) {</pre>
        cin >> asset_covar.at(assetA_index).at(assetB_index);
      }
    // go trough investors and calculate maximum expected outcome for given conditions
    for(int investor_index = 0; investor_index < friend_count; investor_index++) {</pre>
      int max_cost, max_covar;
      cin >> max_cost >> max_covar;
      // search for upper bound for return, so we don't have to search through every possible combination
      int r = 1;
      while(feasible(asset_count, max_cost, max_covar, r, asset_costs, asset_returns, asset_covar)) {
       r *= 2;
      // now we know in which range ([r/2, r]) to search for the maximum
      // use binary search to find it
      int ok = r / 2;
      int low = r / 2;
      int high = r:
      while(low <= high) {
   r = (high - low) / 2 + low;</pre>
        if(feasible(asset_count, max_cost, max_covar, r, asset_costs, asset_returns, asset_covar)) {
          low = r + 1;
        } else {
          high = r - 1;
        }
      cout << ok << endl;</pre>
   }
 }
}
```

```
#include <cassert>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
#include <CGAL/basic.h>
#include <CGAL/QP_models.h>
#include <CGAL/QP_functions.h>
// choose exact integral type
\verb|#ifdef CGAL_USE_GMP| \\
#include <CGAL/Gmpz.h>
typedef CGAL::Gmpz ET;
#else
#include <CGAL/MP_Float.h>
typedef CGAL::MP_Float ET;
#endif
// program and solution types
typedef CGAL::Quadratic_program <int > Program;
typedef CGAL::Quadratic_program_solution <ET> Solution;
using namespace std;
int floor_to_double(const CGAL::Quotient <ET>& x) {
  double a = floor(CGAL::to_double(x));
  while (a > x) a -= 1;
  while (a + 1 <= x) a += 1;
```

```
}
int ceil_to_double(const CGAL::Quotient <ET > & x) {
  double a = ceil(CGAL::to_double(x));
while (a < x) a += 1;</pre>
  while (a - 1 >= x) a -= 1;
  return a;
}
bool is_possible(Program& qp, int expected_return, int max_variance) {
  qp.set_b(1, expected_return);
  Solution s = CGAL::solve_nonnegative_quadratic_program(qp, ET());
  assert(s.solves_quadratic_program(qp));
  return !(s.is_infeasible() || s.is_unbounded() || s.objective_value() > max_variance);
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0):
  int nr_assets, nr_friends;
  for (cin >> nr_assets >> nr_friends; nr_assets != 0 && nr_friends != 0; cin >> nr_assets >> nr_friends) {
    Program qp(CGAL::LARGER, true, 0, false, 0);
qp.set_r(0, CGAL::SMALLER); //cost
     qp.set_r(1, CGAL::LARGER); //expectet return
    for (int i = 0; i < nr_assets; ++i) {</pre>
       int asset_cost, asset_return;
       cin >> asset_cost >> asset_return;
       qp.set_a(i, 0, asset_cost);
       qp.set_a(i, 1, asset_return);
    for (int i = 0; i < nr_assets; ++i) {</pre>
       for (int j = 0; j < nr_assets; ++j) {</pre>
         int asset_covariance;
         cin >> asset_covariance;
if (j <= i) {</pre>
           qp.set_d(i, j, asset_covariance * 2);
    7
     for (int friend_id = 0; friend_id < nr_friends; ++friend_id) {</pre>
       int max_invest, max_variance;
cin >> max_invest >> max_variance;
       qp.set_b(0, max_invest);
       int expected_return = 1;
       while (is_possible(qp, expected_return, max_variance)) {
   expected_return *= 2;
       int ok = expected_return / 2;
       int min_bound = expected_return / 2;
int max_bound = expected_return;
       while (min_bound <= max_bound) {
  int middle = (max_bound - min_bound) / 2 + min_bound;</pre>
         if (is_possible(qp, middle, max_variance)) {
            ok = middle;
           min_bound = middle + 1;
         else {
           max_bound = middle - 1;
       cout << ok << endl;
    }
  }
  return 0;
```

8.7 Tetris

Keywords: BGL, Graph with edge capacity, Graph with residual capacity, Graph with reverse edges, Max-flow

```
#include <iostream>
#include <vector>
#include <queue>
#include <tuple>
#include <cmath>
#include <climits>
#include <algorithm>
#include <climits>
#include <climits>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/push_relabel_max_flow.hpp>
using namespace std;
```

```
using namespace boost;
typedef adjacency_list_traits<vecS, vecS, directedS> Traits;
typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
           property<edge_capacity_t, unsigned int,</pre>
           property < edge_residual_capacity_t, unsigned int,
           property<edge_reverse_t, Traits::edge_descriptor> > > Graph;
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
typedef property_map <Graph, edge_capacity_t>::type EdgeCapacityMap;
typedef property_map <Graph, edge_residual_capacity_t>::type ResidualCapacityMap;
typedef property_map <Graph, edge_reverse_t >:: type ReverseEdgeMap;
int main(void)
           cin.sync_with_stdio(false);
           cout.sync_with_stdio(false);
           int test_cases;
           cin >> test_cases;
          for(int test_index = 0; test_index < test_cases; test_index++) {
   int game_width, brick_count;</pre>
                       cin >> game_width >> brick_count;
                       // define index of source and sink vertex
                       int source_index = game_width + 1;
                       int sink_index = game_width;
                        // create graph, don't forget we need a source and sink too
                       Graph graph(game_width * 2 + 1);
                       // get graph's properties
                       EdgeCapacityMap capacity = get(edge_capacity, graph);
                      ReverseEdgeMap rev_edge = get(edge_reverse, graph);
// not used: ResidualCapacityMap res_capacity = get(edge_residual_capacity, graph);
                       // create edges for splits, as only one can exist at any location. So add edges with weight 1
                       for(int game_location = 0; game_location < game_width; game_location++) {</pre>
                                  bool new_edge;
                                  Edge edge, reverse_edge;
                                 tie(edge, new_edge) = add_edge(game_location, game_width + game_location + 1, graph);
tie(reverse_edge, new_edge) = add_edge(game_width + game_location + 1, game_location, graph);
                                 capacity[edge] = 1;
capacity[reverse_edge] = 0;
                                  rev_edge[edge] = reverse_edge;
                                  rev_edge[reverse_edge] = edge;
                       // read in widths of blocks
                       for(int brick_index = 0; brick_index < brick_count; brick_index++) {</pre>
                                 int start, end;
                                  cin >> start >> end;
                                  // make sure we get expected order
if(start > end) {
                                             int tmp = end;
                                             end = start;
                                             start = tmp;
                                 }
                                  // check if we stay inside the game field
                                  if(end > game_width) {
                                             continue;
                                  // add edge for brick % \frac{1}{2}\left( \frac{1}{2}\right) =\frac{1}{2}\left( \frac{1}{2}\right) =\frac{1}
                                  bool new_edge;
                                  Edge edge, reverse_edge;
                                  tie(edge, new_edge) = add_edge(start + game_width + 1, end, graph);
                                  tie(reverse_edge, new_edge) = add_edge(end, start + game_width + 1, graph);
                                  capacity[edge] = 1;
                                 capacity[reverse_edge] = 0;
rev_edge[edge] = reverse_edge;
rev_edge[reverse_edge] = edge;
                      long max_flow = push_relabel_max_flow(graph, source_index, sink_index);
cout << max_flow << endl;</pre>
           return 0;
}
```

```
#include <iostream>
#include <cassert>
#include <vector>
#include <limits>
#include <algorithm>
```

```
#include <queue>
#include <set>
#include <utility>
#include <cmath>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/dijkstra_shortest_paths.hpp>
#include <boost/graph/kruskal_min_spanning_tree.hpp>
#include <boost/property_map/transform_value_property_map.hpp>
#include <boost/graph/boyer_myrvold_planar_test.hpp>
#include <boost/graph/max_cardinality_matching.hpp>
#include <boost/graph/push_relabel_max_flow.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, directedS> Traits;
typedef adjacency_list<vecS, vecS, directedS, no_property, property<edge_capacity_t, long, property<
    edge_residual_capacity_t, long, property<edge_reverse_t, Traits::edge_descriptor> > > Graph;
typedef graph_traits < Graph > :: edge_descriptor Edge;
typedef graph_traits < Graph > :: vertex_descriptor Vertex;
typedef property_map<Graph, edge_capacity_t>::type EdgeCapacityMap;
typedef property_map<Graph, edge_reverse_t>::type ReverseEdgeMap;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  //cout << fixed << setprecision(0);</pre>
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int width, nr_bricks;
    cin >> width >> nr_bricks;
    Graph g(width * 2 + 1);
    int source = width + 1;
int sink = width;
    EdgeCapacityMap capacity = get(edge_capacity, g);
    ReverseEdgeMap rev_edge = get(edge_reverse, g);
    Edge e, rev_e;
    bool success;
    for (int i = 1; i < width; i++) {</pre>
      tie(e, success) = add_edge(i, width + i + 1, g);
      tie(rev_e, success) = add_edge(width + i + 1, i, g);
       capacity[e] = 1;
      capacity[rev_e] = 0;
rev_edge[e] = rev_e;
      rev_edge[rev_e] = e;
    for (int i = 0; i < nr_bricks; i++) {</pre>
      int first_end, second_end;
      cin >> first_end >> second_end;
if (first_end > second_end) {
  int tmp = first_end;
         first_end = second_end;
        second_end = tmp;
      tie(e, success) = add_edge(width + 1 + first_end, second_end, g);
      tie(rev_e, success) = add_edge(second_end, width + 1 + first_end, g);
capacity[e] = 1;
      capacity[rev_e] = 0;
      rev_edge[e] = rev_e;
      rev_edge[rev_e] = e;
    int flow = push_relabel_max_flow(g, source, sink);
    cout << flow << endl;</pre>
  return 0;
```

8.8 Stamp Exhibition

Keywords: CGAL, Quadratic Program

```
#include <iostream>
#include <cassert>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <set>
#include <caset>
#include <algorithm>
#include <al
```

```
#include <CGAL/basic.h>
#include <CGAL/Exact_predicates_exact_constructions_kernel.h>
#include <CGAL/QP_models.h>
#include <CGAL/QP_functions.h>
#ifdef CGAL_USE_GMP
#include <CGAL/Gmpz.h>
typedef CGAL::Gmpzf ET;
#else
#include <CGAL/MP Float.h>
typedef CGAL::MP_Float ET;
#endif
typedef CGAL::Exact_predicates_exact_constructions_kernel K;
typedef K::Point_2 Point;
typedef K::Segment_2 Segment;
typedef CGAL::Quadratic_program <ET> Program;
typedef CGAL::Quadratic_program_solution<ET> Solution;
using namespace std;
using namespace CGAL;
int floor_to_double(const CGAL::Quotient<ET>& x) {
  double a = floor(CGAL::to_double(x));
  while (a > x) a -= 1;
  while (a + 1 <= x) a += 1;
 return a;
int ceil_to_double(const CGAL::Quotient<ET>& x) {
  double a = ceil(CGAL::to_double(x));
while (a < x) a += 1;</pre>
  while (a - 1 >= x) a -= 1;
  return a:
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  //cout << fixed << setprecision(0);</pre>
  int test_count;
  cin >> test_count;
  for (int test = 0; test < test_count; test++) {</pre>
    int lamp_count, stamp_count, wall_count;
    cin >> lamp_count >> stamp_count >> wall_count;
    // read in lamps
    vector < Point > lamps;
    lamps.reserve(lamp_count);
    for(int lamp_index = 0; lamp_index < lamp_count; lamp_index++) {</pre>
      int lamp_x, lamp_y;
cin >> lamp_x >> lamp_y;
      lamps.push_back(Point(lamp_x, lamp_y));
    \ensuremath{//} collect lamps and the maximum light they are allowed to get
    vector < Point > stamps;
    stamps.reserve(stamp_count);
    vector<int> stamp_max_light;
    stamp_max_light.reserve(stamp_count);
    for(int stamp_index = 0; stamp_index < stamp_count; stamp_index++) {</pre>
      int stamp_x, stamp_y, max_light;
      cin >> stamp_x >> stamp_y >> max_light;
      stamps.push_back(Point(stamp_x, stamp_y));
      stamp_max_light.push_back(max_light);
    // read in walls
    vector < Segment > walls;
    walls.reserve(wall count):
    for(int wall_index = 0; wall_index < wall_count; wall_index++) {</pre>
      int wall_start_x, wall_start_y, wall_end_x, wall_end_y;
      cin >> wall_start_x >> wall_start_y >> wall_end_x >> wall_end_y;
      walls.push_back(Segment(Point(wall_start_x, wall_start_y), Point(wall_end_x, wall_end_y)));
    // Create quadratic programming instance
    Program qp(CGAL::SMALLER, true, 1, true, 4096);
    for(int stamp_index = 0; stamp_index < stamp_count; stamp_index++) {
  for(int lamp_index = 0; lamp_index < lamp_count; lamp_index++) {</pre>
        Segment light_to_stamp(lamps.at(lamp_index), stamps.at(stamp_index));
        // check if a wall blocks the light beam from lamp to stamp
        bool light_blocked = false;
        for(int wall_index = 0; wall_index < wall_count; wall_index++) {</pre>
```

```
if(do_intersect(light_to_stamp, walls.at(wall_index))) {
              light_blocked = true;
              break;
         if(!light_blocked) {
            double d = CGAL::to_double(1 / light_to_stamp.squared_length());
            qp.set_a(lamp_index, stamp_index, d);
            qp.set_a(lamp_index, stamp_count + stamp_index, d);
       qp.set_b(stamp_index, stamp_max_light.at(stamp_index));
qp.set_b(stamp_count + stamp_index, 1);
qp.set_r(stamp_count + stamp_index, CGAL::LARGER);
     // get solution
    Solution sol = solve_linear_program(qp, ET());
    if(sol.is_infeasible()) {
       cout << "no" << endl;
      else {
       cout << "yes" << endl;
  }
  return 0:
}
```

```
#include <iostream>
#include <cassert>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
#include <CGAL/basic.h>
#include <CGAL/Exact_predicates_exact_constructions_kernel.h>
#include <CGAL/QP_models.h>
#include <CGAL/QP_functions.h>
#ifdef CGAL_USE_GMP
#include <CGAL/Gmpz.h>
typedef CGAL::Gmpzf ET;
#else
#include <CGAL/MP_Float.h>
typedef CGAL::MP_Float ET;
#endif
typedef CGAL::Exact_predicates_exact_constructions_kernel K;
typedef K::Point_2 Point;
typedef K::Segment_2 Segment;
typedef CGAL::Quadratic_program <ET> Program;
typedef CGAL::Quadratic_program_solution <ET> Solution;
using namespace std;
using namespace CGAL;
int floor_to_double(const CGAL::Quotient<ET>& x) {
  double a = floor(CGAL::to_double(x));
while (a > x) a -= 1;
while (a + 1 <= x) a += 1;</pre>
  return a;
}
int ceil_to_double(const CGAL::Quotient<ET>& x) {
  double a = ceil(CGAL::to_double(x));
while (a < x) a += 1;</pre>
  while (a - 1 >= x) a -= 1;
  return a;
}
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  //cout << fixed << setprecision(0);</pre>
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_lights, nr_stamps, nr_walls;
    cin >> nr_lights >> nr_stamps >> nr_walls;
    vector < Point > lights;
    lights.reserve(nr_lights);
for (int i = 0; i < nr_lights; i++) {
  int light_x, light_y;</pre>
       cin >> light_x >> light_y;
```

```
lights.push_back(Point(light_x, light_y));
    vector < Point > stamps;
    vector < int > stamps_max_int;
    stamps.reserve(nr_stamps);
    stamps_max_int.reserve(nr_stamps);
    for (int i = 0; i < nr_stamps; i++) {</pre>
      int stamp_x, stamp_y, stamp_max_light_intensity;
       cin >> stamp_x >> stamp_y >> stamp_max_light_intensity;
       stamps.push_back(Point(stamp_x, stamp_y));
       stamps_max_int.push_back(stamp_max_light_intensity);
    vector < Segment > walls;
    walls.reserve(nr_walls);
    for (int i = 0; i < nr_walls; i++) {</pre>
      int wall_start_x, wall_start_y, wall_end_x, wall_end_y;
cin >> wall_start_x >> wall_start_y >> wall_end_x >> wall_end_y;
      walls.push_back(Segment(Point(wall_start_x, wall_start_y), Point(wall_end_x, wall_end_y)));
    Program qp(CGAL::SMALLER, true, 1, true, 4096);
for (int i = 0; i < nr_stamps; i++) {
  for (int j = 0; j < nr_lights; j++) {</pre>
         Segment light_to_stamp(lights[j], stamps[i]);
         bool blocked = false;
         for (int k = 0; k < nr_walls; k++) {</pre>
           if (do_intersect(light_to_stamp, walls[k])) {
             blocked = true;
             break;
         if (!blocked) {
           double d = CGAL::to_double(1 / light_to_stamp.squared_length());
           qp.set_a(j, i, d);
           qp.set_a(j, nr_stamps + i, d);
        }
       qp.set_b(i, stamps_max_int[i]);
      qp.set_b(nr_stamps + i, 1);
qp.set_r(nr_stamps + i, CGAL::LARGER);
    Solution sol = solve_linear_program(qp, ET());
    assert(sol.solves_linear_program(qp));
    if (sol.is_infeasible())
       cout << "no" << endl;
    else {
       cout << "yes" << endl;
  return 0;
}
```

8.9 Placing Knights

Keywords: BGL, Matching

```
#include <iostream>
#include <vector>
#include <queue>
#include <tuple>
#include <cmath>
#include <climits>
#include <algorithm>
#include <climits>
#include <string>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/max_cardinality_matching.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, undirectedS> Graph;
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
int main(void)
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test_cases;
    cin >> test_cases;
    for(int test = 0; test < test_cases; test++) {</pre>
        int width;
        cin >> width;
        // 2D vector indicating if the field is not a hole
vector<bool> can_occupy(width * width);
```

```
int hole_count = 0;
     for(int row = 0; row < width; row++) {</pre>
           for(int column = 0; column < width; column++) {</pre>
                int indicator:
                 cin >> indicator;
                 if(indicator == 1) {
                      can_occupy.at(row + column * width) = true;
                 } else {
                      hole_count++;
                      can_occupy.at(row + column * width) = false;
          }
     }
     // create graph for game field
Graph graph(width * width);
      // create edges
     for(int row = 0; row < width; row++) {
    for(int column = 0; column < width; column++) {
        int field_index = row + column * width;
}</pre>
                 if(!can_occupy.at(field_index)) {
                      continue;
                 }
                // i = row, j = column
// [i - 1, j - 2]
if(row - 1 >= 0 && column - 2 >= 0 && can_occupy.at((row - 1) + (column - 2) * width)) {
   add_edge(field_index, (row - 1) + (column - 2) * width, graph);
}
                // [i - 1, j + 2]
if(row - 1 >= 0 && column + 2 < width && can_occupy.at((row - 1) + (column + 2) * width)) {
   add_edge(field_index, (row - 1) + (column + 2) * width, graph);</pre>
                 // [i + 1, j - 2] if (row + 1 < width && column - 2 >= 0 && can_occupy.at((row + 1) + (column - 2) * width)) {
                      add_edge(field_index, (row + 1) + (column - 2) * width, graph);
                 if(row + 1 < width && column + 2 < width && can_occupy.at((row + 1) + (column + 2) * width)) {
                      add_edge(field_index, (row + 1) + (column + 2) * width, graph);
                 // [i - 2, j - 1]
if(row - 2 >= 0 && column - 1 >= 0 && can_occupy.at((row - 2) + (column - 1) * width)) {
    add_edge(field_index, (row - 2) + (column - 1) * width, graph);
.
                 // [i - 2, j + 1] if(row - 2 >= 0 && column + 1 < width && can_occupy.at((row - 2) + (column + 1) * width)) {
                      add_edge(field_index, (row - 2) + (column + 1) * width, graph);
                // [i + 2, j - 1]
if(row + 2 < width && column - 1 >= 0 && can_occupy.at((row + 2) + (column - 1) * width)) {
    add_edge(field_index, (row + 2) + (column - 1) * width, graph);
.
                // [i + 2, j + 1]
if(row + 2 < width && column + 1 < width && can_occupy.at((row + 2) + (column + 1) * width)) {
   add_edge(field_index, (row + 2) + (column + 1) * width, graph);</pre>
          }
     // max cardinality
     vector < Vertex > mate(width * width);
     \tt checked\_edmonds\_maximum\_cardinality\_matching(graph\,,\,\,\&mate[0])\,;
     int matches = matching_size(graph, &mate[0]);
     //cout << "-> " << matches << endl;
     cout << ((width * width) - hole_count) - matches << endl;</pre>
return 0;
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <set>
#include <set
#include <set
#include <county>
#include <map>
#include <string>
#include <boost/config.hpp>
```

}

```
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/dijkstra_shortest_paths.hpp>
#include <boost/graph/kruskal_min_spanning_tree.hpp>
#include <boost/property_map/transform_value_property_map.hpp>
#include <boost/graph/boyer_myrvold_planar_test.hpp>
#include <boost/graph/max_cardinality_matching.hpp>
#include <boost/graph/push_relabel_max_flow.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, undirectedS> Graph;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  vector<pair<int, int> > moves;
  moves.reserve(8):
  moves.push_back(make_pair(-1, -2));
 moves.push_back(make_pair(-1, 2));
moves.push_back(make_pair(1, -2));
  moves.push_back(make_pair(1, 2));
  moves.push_back(make_pair(-2, -1));
 moves.push_back(make_pair(-2, 1));
moves.push_back(make_pair(2, -1));
  moves.push_back(make_pair(2, 1));
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int board_side_length;
    cin >> board_side_length;
    vector<vector<int> > board(board_side_length, vector<int>(board_side_length, -1));
    int vertex_id = 0;
    for (int i = 0; i < board_side_length; ++i) {</pre>
      for (int j = 0; j < board_side_length; ++j) {</pre>
        int field_status;
         cin >> field status:
         if (field_status == 1) {
           //add_vertex(g);
           board[i][j] = vertex_id++;
        }
      }
    }
    int nr_vertices = vertex_id;
    Graph g(nr_vertices);
    for (int i = 0; i < board_side_length; ++i) {</pre>
      for (int j = 0; j < board_side_length; ++j) {
   if (board[i][j] != -1) {
     for (int k = 0; k < moves.size(); ++k) {</pre>
             int x_cord = i + moves[k].first;
             int y_cord = j + moves[k].second;
             if (x_cord >= 0 && x_cord < board_side_length && y_cord >= 0 && y_cord < board_side_length && board[x_cord][ y_cord] != -1) {
               add_edge(board[i][j], board[x_cord][y_cord], g);
            }
          }
        }
      }
    1
    vector < Vertex > mate(nr vertices):
    edmonds_maximum_cardinality_matching(g, &mate[0]);
    int m_size = matching_size(g, &mate[0]);
    cout << m_size << endl;</pre>
    cout << nr_vertices - m_size << endl;</pre>
 return 0;
```

8.10 Beach Bar

Keywords: ACM, Scanline

```
#include <iostream>
#include <vector>
#include <algorithm>
#include <liimits>
#include <utility>
#include <set>
#include <limits>

using namespace std;

#define MAX_BAR_RANGE 200

int main() {
```

```
cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
int test count:
cin >> test_count;
for(int test = 0; test < test_count; test++) {</pre>
  int parasols_count;
  cin >> parasols_count;
  \begin{subarray}{lll} \end{subarray} // \end{subarray} read in parasol locations
  vector <int> parasols_locs(parasols_count);
  for(int parasol_index = 0; parasol_index < parasols_count; parasol_index++) {</pre>
    cin >> parasols_locs.at(parasol_index);
  // first sort parasols, so we can start from the one furthest away in negative direction
sort(parasols_locs.begin(), parasols_locs.end());
  // keep track of the maximum amount of parasols
  int max_parasols = 0;
  int cur_parasol_count = 0;
  // keep track of 'parasols_locs' indexes resulting in a ranges in which we can build a bar
  vector<pair<int, int> > bar_ranges;
  // keeps track of current start/stop index
  int start index = 0:
  int stop_index = 0;
  bar_ranges.push_back(make_pair(start_index, stop_index));
  // iterate through parasols and collect bar ranges
  for(int parasol_index = 0; parasol_index < parasols_count; parasol_index++) {</pre>
    // if the current parasol is too far away from the previous one (defined by 'start_index'), remove 
// parasols as long as there are more between the original 'start_index' and current one until we're
     // back in the range of a bar
    for(; parasols_locs.at(parasol_index) - parasols_locs.at(start_index) > MAX_BAR_RANGE; start_index++) {
       cur_parasol_count --;
    stop_index = parasol_index; // new "last" parasol in range of the bar
cur_parasol_count++; // as we added the current parasol, increase the amount
    if(max_parasols < cur_parasol_count) {</pre>
       // we found a range with more parasols as before!
max_parasols = cur_parasol_count;
       // as we found a better range, remove the previously found ones
       bar_ranges.clear();
       // ... and add the better one
       bar_ranges.push_back(make_pair(start_index, stop_index));
    } else if(max_parasols == cur_parasol_count) {
       /\!/ found another location for the bar with equal amount of reached parasols /\!/ we add it to our list of possible locations
       bar_ranges.push_back(make_pair(start_index, stop_index));
  // so, now we have a list of parisol ranges where we can build a bar in the middle and reach maximum // amount of customers. Next we have to find the one bar with the minimum distance.
  set < int > bar_locs;
  int min_distance_found = numeric_limits<int>::max();
  for(int range_index = 0; range_index < bar_ranges.size(); range_index++) {</pre>
    // stupid name, but basically 'added_range / 2' is the location of the bar :-)
int added_range = parasols_locs[bar_ranges.at(range_index).first] +
       parasols_locs[bar_ranges.at(range_index).second];
    int diff = (parasols_locs[bar_ranges.at(range_index).second] -
       parasols_locs[bar_ranges.at(range_index).first] + 1) / 2; // +1 because of rounding
    if(diff > min_distance_found) {
      // we found something with a better minimal distance, so ignore this bar!
       continue;
    } else if(diff < min_distance_found) {</pre>
       \ensuremath{//} oh, we found a better minimum, replace everything
       min_distance_found = diff;
       bar locs.clear():
     // now add the current bar to our bar location collection, as we know it is the best one
    // or as good as the best we not till now
if(added_range % 2 == 0) {
       // even distance
       bar_locs.insert(added_range / 2);
    } else {
       bar_locs.insert((added_range - 1) / 2);
       bar_locs.insert((added_range - 1) / 2 + 1);
  // output basic information
  cout << max_parasols << " " << min_distance_found << endl;</pre>
```

```
// output bar location in order: it is, we use a set!

set <int >:: iterator loc_iter = bar_locs.begin();
cout << *loc_iter++;
for(; loc_iter != bar_locs.end(); ++loc_iter) {
   cout << " " << *loc_iter;
}

cout << endl;
}
</pre>
```

```
#include <cassert>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
#include <stack>
using namespace std:
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_parasols;
    cin >> nr_parasols;
    vector<int> parasols;
    parasols.reserve(nr_parasols);
    for (int i = 0; i < nr_parasols; i++) {
      int location;
      cin >> location;
      parasols.push_back(location);
    sort(parasols.begin(), parasols.end());
    queue < int > covered_parasols;
    int best_nr_covered = 0;
    int best_min_distance = 0;
    set < int > best_locations;
    for (int i = 0; i < nr_parasols; i++) {</pre>
      int cur = parasols[i];
       covered_parasols.push(cur);
      while (covered_parasols.front() < cur - 200) {</pre>
         covered_parasols.pop();
      int min_distance = ceil((cur - covered_parasols.front()) / 2.0);
      if (covered_parasols.size() > best_nr_covered) {
         best_nr_covered = covered_parasols.size();
         best_min_distance = min_distance;
         best_locations.clear();
//add location
         int added = cur + covered_parasols.front();
         if (added % 2 == 0)
           best_locations.insert(added / 2);
         else {
          best_locations.insert((added - 1) / 2);
best_locations.insert((added - 1) / 2 + 1);
      else if (covered_parasols.size() == best_nr_covered) {
         if (min_distance < best_min_distance) {</pre>
           best_min_distance = min_distance;
           best_locations.clear();
           //add location
           int added = cur + covered_parasols.front();
if (added % 2 == 0)
             best_locations.insert(added / 2);
           else {
             best_locations.insert((added - 1) / 2);
best_locations.insert((added - 1) / 2 + 1);
         else if (min_distance == best_min_distance) {
           //add location
           int added = cur + covered_parasols.front();
if (added % 2 == 0)
             best_locations.insert(added / 2);
             best_locations.insert((added - 1) / 2);
best_locations.insert((added - 1) / 2 + 1);
   } }
```

```
cout << best_nr_covered << " " << best_min_distance << endl;
set <int>::iterator it = best_locations.begin();
cout << *it;
for (++it; it != best_locations.end(); ++it) {
   cout << " " << *it;
}
cout << endl
}
return 0;
}</pre>
```

8.11 Light the Stage

Keywords: CGAL, Point set, Triangulation with info()

```
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
#include <CGAL/basic.h>
#include <CGAL/squared_distance_2.h>
#include <CGAL/Triangulation_vertex_base_with_info_2.h>
#include <CGAL/Point_set_2.h>
typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
typedef K::Point_2 Point;
typedef K::Circle_2 Circle;
typedef CGAL::Triangulation_vertex_base_with_info_2 < int, K > Vb;
{\tt typedef} \ {\tt CGAL::Triangulation\_data\_structure\_2 < Vb > \ Tds;}
typedef CGAL::Point_set_2<K, Tds> PSet;
typedef CGAL::Point_set_2<K, Tds>::Vertex_handle Vertex_handle;
using namespace std;
int main() {
    some basic setup stuff
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  int test_count;
  cin >> test_count;
  for(int test = 0; test < test_count; test++) {</pre>
    int participant_count, lamp_count;
    cin >> participant_count >> lamp_count;
    // read in participants
    vector<K::Point_2> participant_locations(participant_count);
    rector<int> participant_radi(participant_count, -1);
for(int participant_index = 0; participant_index < participant_count; participant_index++) {</pre>
      double p_x, p_y, p_r;
      cin >> p_x >> p_y >> p_r;
      participant_locations.at(participant_index) = K::Point_2(p_x, p_y);
      participant_radi.at(participant_index) = p_r;
    // read in lamp information
    int lamp_height;
    cin >> lamp_height;
    // make it a vector of a pair. The moment we feed it in to Point_set_2 we can access the second
    // member of the pair by accessing ->info() :-)
    vector < pair < K :: Point_2, int > > lamp_locations(lamp_count);
    for(int lamp_index = 0; lamp_index < lamp_count; lamp_index++) {</pre>
      double 1_x, 1_y;
cin >> 1_x >> 1_y;
      lamp_locations.at(lamp_index) = make_pair(K::Point_2(l_x, l_y), lamp_index);
    // create a triangulation of the lamps using Point_set_2
    PSet lamps_triang(lamp_locations.begin(), lamp_locations.end());
    // contains the ID of the light that hit a participant first, or MAX if he survived till the end
    vector < int > min_light_hit(participant_count, numeric_limits < int >:: max());
    // keeps track of the max light that hit someone
    int max_light_hit = -1;
    // now we iterate over each person and find out which lamp hits each person first, i.e. how
    for(int participant_index = 0; participant_index < participant_count; participant_index++) {
   K::Point_2 participant_point = participant_locations.at(participant_index); // we need it more than once :-)</pre>
       // get nearest lamp
      Vertex_handle lamp_vertex = lamps_triang.nearest_neighbor(participant_point);
       * We know that the light is a cone with given height and it's a 90 degree one:
                          x <---- lamp point
```

```
g h g
                        ^- 'h' and the bottom have a 90 degree, therefore the triangle on the left/right (h, g and half
          of the bottom)
     * have a 90 degree and two 45 degrees, i.e. we can find out what the length of the bottom is (twice the bottom
          part of the triangle)
     * which is in this case 2 * 'h' (bottom is of 2 * 'h' length).
    // calculate the distance from our participant that still could be hit by light to "kill" the
    // participant. // do it ^2 (squared) because we compare it to a squared distance
    double max_dist_to_kill = pow(participant_radi.at(participant_index) + lamp_height, 2);
    // if the nearest lamp is already too far away, we don't have to search for other lamps,
       as they will even farther away
    if(max_dist_to_kill <= squared_distance(lamp_vertex->point(), participant_point)) {
    // iterate over all lamps in the search for one that hits the participant first
    for(int check_lamp_index = 0; check_lamp_index < lamp_count; check_lamp_index++) {
      if(max_dist_to_kill > squared_distance(lamp_locations.at(check_lamp_index).first, participant_point)) {
         // found such a lamp, stop searching as we only interested in the minimum! min_light_hit.at(participant_index) = lamp_locations.at(check_lamp_index).second;
         max_light_hit = max(max_light_hit, lamp_locations.at(check_lamp_index).second);
         break;
    /* nice idea, but too slow...
    // create a circle in which every light source would kill the current participant
K::Circle_2 circle_of_death = K::Circle_2(participant_point, max_dist_to_kill);
    // create a vector of vertex handles that represent our lights that are inside the circle_of_death
    vector < Vertex_handle > lights_hitting_participant;
    // so, micro optimizing stuff: don't do the rest of the algorithm if the lamp ID is higher than the
       already found one
    if(min_light_hit.at(participant_index) < lamp_vertex->info()) {
      continue;
    // collect the lights "of death" :-)
    lamps_triang.range_search(circle_of_death, back_inserter(lights_hitting_participant));
       iterate over the bad lights and write down the smallest light hitting
    for(vector<Vertex_handle>::iterator iter = lights_hitting_participant.begin();
      iter != lights_hitting_participant.end();
      ++iter) {
      int lamp_id = (*iter)->info();
      if(circle_of_death.has_on_boundary((*iter)->point())) {
         // point is on boundary, this is not a hit according to the exercise
         continue;
      min_light_hit.at(participant_index) = min(min_light_hit.at(participant_index), lamp_id);
      max_light_hit = max(max_light_hit, lamp_id);
  1
  // now we have to extract for each light who survived the longest
  vector<int> rank_list;
  // first we search for participants which were not hit by a light
  for(int participant_index = 0; participant_index < participant_count; participant_index++) {</pre>
    if(min_light_hit.at(participant_index) == numeric_limits<int>::max()) {
      rank_list.push_back(participant_index);
    }
  // if all participants were hit, we have to search for the ones that were hit last
  if(rank_list.size() <= 0) {</pre>
    for(int participant_index = 0; participant_index < participant_count; participant_index++) {</pre>
      if(min_light_hit.at(participant_index) == max_light_hit) {
        rank_list.push_back(participant_index);
      }
    }
  }
  // print out rank in sorted order
  sort(rank_list.begin(), rank_list.end());
for(int i = 0; i < rank_list.size(); i++) {</pre>
    cout << rank_list.at(i) << " ";</pre>
  cout << endl:
}
```

#include <iostream>

}

```
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
#include <CGAL/basic.h>
#include <CGAL/squared_distance_2.h>
#include <CGAL/Triangulation_vertex_base_with_info_2.h>
#include <CGAL/Point_set_2.h>
typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
typedef K::Point_2 Point;
typedef K::Circle_2 Circle;
typedef CGAL::Triangulation_vertex_base_with_info_2<int, K> Vb;
typedef CGAL::Triangulation_data_structure_2 < Vb > Tds;
typedef CGAL::Point_set_2<K, Tds> PSet;
typedef CGAL::Point_set_2<K, Tds>::Vertex_handle Vertex_handle;
using namespace std;
double floor_to_double(const K::FT& x)
  double a = std::floor(CGAL::to_double(x));
  while (a > x) a -= 1;
  while (a + 1 <= x) a += 1;
  return a;
double ceil to double(const K::FT& x)
  double a = std::ceil(CGAL::to_double(x));
  while (a < x) a += 1;
while (a - 1 >= x) a -= 1;
  return a;
}
class CompareVertex {
  bool operator()(const Vertex_handle& lhs, const Vertex_handle& rhs) {
  return lhs->info() < rhs->info();
  }
};
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_players, nr_lights;
cin >> nr_players >> nr_lights;
     vector < Point > players;
     vector < K :: FT > players_r;
     players.reserve(nr_players);
    players_r.reserve(nr_players);
for (int i = 0; i < nr_players; i++) {
  int player_x, player_y, player_r;</pre>
       cin >> player_x >> player_y >> player_r;
       players.push_back(Point(player_x, player_y));
       players_r.push_back(player_r);
     K::FT light_r;
     cin >> light_r;
     vector<pair<Point, int> > lights;
     lights.reserve(nr_lights);
    for (int i = 0; i < nr_lights; i++) {
  int light_x, light_y;
  cin >> light_x >> light_y;
       lights.push_back(make_pair(Point(light_x, light_y), i));
    PSet pset(lights.begin(), lights.end());
    vector(int) min_light_hit(nr_players, numeric_limits<int>::max());
for (int i = 0; i < nr_players; i++) {
   Point player = players[i];</pre>
       Vertex_handle light = pset.nearest_neighbor(player);
       double max_dist = pow(players_r[i] + light_r, 2);
       if (max_dist <= squared_distance(light->point(), player)) {
         continue;
       for (int j = 0; j < nr_lights; j++) {</pre>
```

```
if (max_dist > squared_distance(lights[j].first, player)) {
              min_light_hit[i] = lights[j].second;
              break;
           }
        }
      int max_light_hit = *max_element(min_light_hit.begin(), min_light_hit.end());
     for (int i = 0; i < nr_players; i++) {
   if (min_light_hit[i] == max_light_hit) {
           cout << i << " ";
      cout << endl;</pre>
      //Binary search would propably work...
      /*PSet pset(lights.begin(), lights.end());
     vector<int> player_death_time(nr_players, -1);
for (int i = 0; i < nr_players; i++) {
K::FT circle_squared_dist = pow(players_r[i] + light_r, 2);</pre>
     Circle c(players[i], circle_squared_dist);
vector<Vertex_handle> result;
     pset.range_search(c, back_inserter(result));
//cout << "player: " << i << " found: " << result.size() << endl;</pre>
      sort(result.begin(), result.end(), CompareVertex());
     for (int j = 0; j < result.size(); ++j) {
int death_time = result[j]->info();
if (player_death_time[i] == -1 || death_time < player_death_time[i]) {</pre>
      if (squared_distance(result[j]->point(), players[i]) < circle_squared_dist) {</pre>
      player_death_time[i] = death_time;
      break;
      int death_max = 0;
     for (int i = 0; i < nr_players; i++) {
  if (player_death_time[i] > death_max) {
    death_max = player_death_time[i];
}
      if (player_death_time[i] == -1) {
      death_max = -1;
     break:
     for (int i = 0; i < nr_players; i++) {</pre>
     if (player_death_time[i] == death_max) {
      cout << i << " ";
     cout << endl; */
   return 0;
}
```

8.12 Search Snippets

Keywords: ACM, Scanline, Custom compare, Compare in class

```
#include <iostream>
#include <algorithm>
#include <vector>
#include <queue>
#include <bitset>
using namespace std;
class PairCompare
public:
    bool operator() (pair<int, int>& lhs, pair<int, int>& rhs) {
        return lhs.first > rhs.first;
    }
ት :
int main() {
  cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test_cases;
    cin >> test cases:
    for(int test = 0; test < test_cases; test++) {</pre>
      int word_count;
        cin >> word_count;
        // read in how often each word occurs
```

```
vector<int> occurs(word_count, 0);
    for(int word_index = 0; word_index < word_count; word_index++) {</pre>
        cin >> occurs.at(word_index);
    // read in where it occurs
    priority_queue <pair <int, int>, vector <pair <int, int> >, PairCompare > locs;
    for(int word_index = 0; word_index < word_count; word_index++) {</pre>
        for(int i = 0; i < occurs.at(word_index); i++) {</pre>
            int 1:
            cin >> 1;
            locs.push(make_pair(1, word_index));
        }
    // find first range with all words
vector<int> first_set_loc(word_count, -1);
    set < pair < int , int > > words;
    int words_found = 0;
    int last_loc = numeric_limits < int >::min();
    while(!locs.empty() && words_found != word_count) {
        pair < int , int > cur = locs.top();
        locs.pop();
        if(first_set_loc.at(cur.second) == -1) {
            words_found++;
        } else {
            words.erase(make_pair(first_set_loc.at(cur.second), cur.second));
        }
        first_set_loc.at(cur.second) = cur.first;
        words.insert(cur);
        last_loc = cur.first;
    7
    //cout << "words_found: " << words_found << endl;</pre>
    //locs.push(make_pair(first_set_loc.at(x), x));
    //cout << "min: " << words.begin()->first << ", max: " << last_loc << endl;
    int min_dist = last_loc - words.begin()->first;
    while(!locs.empty()) {
        pair<int, int> cur = locs.top();
locs.pop();
        // modify location
        words.erase(make_pair(first_set_loc.at(cur.second), cur.second));
        words.insert(cur);
        first_set_loc.at(cur.second) = cur.first;
        // check range
        int d = cur.first - words.begin()->first;
        min_dist = min(min_dist, d);
    cout << min_dist + 1 << endl;</pre>
}
return 0;
```

```
#include <iostream>
#include <cassert>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
#define MOD_NUM 100003
using namespace std;
struct PairComparator {
 bool operator() (const pair < int, int > & lhs, const pair < int, int > & rhs) {
   return lhs.first > rhs.first;
}:
int main() {
 cin.sync_with_stdio(false);
 cout.sync_with_stdio(false);
  //cout << fixed << setprecision(0);</pre>
  int nr_test_cases;
 cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
```

```
int nr_words;
  cin >> nr_words;
  vector<int> nr_word_occurrences;
  nr_word_occurrences.reserve(nr_words);
  for (int i = 0; i < nr_words; ++i) {</pre>
    int nr_word_occurrence;
    cin >> nr_word_occurrence;
    nr_word_occurrences.push_back(nr_word_occurrence);
  priority_queue<pair<int, int>, vector<pair<int, int> >, PairComparator> words;
for (int i = 0; i < nr_words; ++i) {
   for (int j = 0; j < nr_word_occurrences[i]; ++j) {</pre>
      int word_occurrence;
      cin >> word_occurrence;
      words.push(make_pair(word_occurrence, i));
  // {\it find first valid range}
  set<pair<int, int> > max_word_occurrences_sorted;
  vector < int > max_word_occurences(nr_words, -1);
  int found_words = 0;
  int bound_max = 0;
  while (found_words < nr_words) {</pre>
    pair < int , int > word = words.top();
    words.pop();
    if (max_word_occurences[word.second] == -1) {
      //new word
      found_words++;
    else {
      //already inserted word
      max word occurrences sorted.erase(make pair(max word occurences[word.second]. word.second)):
    max_word_occurences[word.second] = word.first;
    max_word_occurrences_sorted.insert(word);
    bound_max = word.first;
  int min_range = bound_max - max_word_occurrences_sorted.begin()->first;
  while (!words.empty()) {
    pair<int, int> word = words.top();
    words.pop();
    \verb|max_word_occurrences_sorted.erase(make_pair(max_word_occurences[word.second]); word.second));|
    max_word_occurences[word.second] = word.first;
    max_word_occurrences_sorted.insert(word);
    bound_max = word.first;
    min_range = min(min_range, bound_max - max_word_occurrences_sorted.begin()->first);
  cout << min_range+1 << endl;</pre>
return 0;
```

8.13 Radiation Therapy

Keywords: CGAL, Quadratic Program, Exponential bound search, Binary search

```
#include <iostream>
#include <cassert>
#include <tuple>
#include <CGAL/basic.h>
#include <CGAL/QP_models.h>
#include <CGAL/QP_functions.h>
// choose exact integral type
#ifdef CGAL_USE_GMP
#include <CGAL/Gmpz.h>
typedef CGAL::Gmpz ET;
#include <CGAL/MP_Float.h>
typedef CGAL::MP_Float ET;
#endif
using namespace std;
// program and solution types
typedef CGAL::Quadratic_program <ET> Program;
typedef CGAL::Quadratic_program_solution <ET> Solution;
int floor_to_double(const CGAL::Quotient<ET>& x) {
  double a = floor(CGAL::to_double(x));
  while (a > x) a -= 1;
  while (a + 1 <= x) a += 1;
  return a;
```

```
int ceil_to_double(const CGAL::Quotient <ET > & x) {
  double a = ceil(CGAL::to_double(x));
while (a < x) a += 1;</pre>
  while (a - 1 >= x) a -= 1;
  return a;
bool can_solve(int dimension, vector<tuple<int, int, int> >& healthy, vector<tuple<int, int, int> >& cancer) {
   // use EQUAL, as we set it manually if we wish => or <=
   Program qp(CGAL::EQUAL, false, 0, false, 0);</pre>
  if(x_dim + y_dim + z_dim \le dimension) {
                double value = pow(get<0>(healthy.at(cell)), x_dim) *
                  pow(get<1>(healthy.at(cell)), y_dim) *
pow(get<2>(healthy.at(cell)), z_dim);
                qp.set_a(var_index, cell, value);
//cout << "value H: " << value << endl;</pre>
                var_index++;
             } else {
               break;
          }
       }
     qp.set_r(cell, CGAL::LARGER);
     qp.set_b(cell, 1);
  // add cancer cell inequations
for(int cell = 0; cell < cancer.size(); cell++) {
  int var_index = 0;
  for(int x_dim = 0; x_dim <= dimension; x_dim++) {</pre>
        for(int y_dim = 0; y_dim <= dimension; y_dim++) {</pre>
           for(int z_dim = 0; z_dim <= dimension; z_dim++) {</pre>
             if(x_dim + y_dim + z_dim \le dimension) {
                double value = pow(get<0>(cancer.at(cell)), x_dim) *
                  pow(get<1>(cancer.at(cell)), y_dim) *
pow(get<2>(cancer.at(cell)), z_dim);
                qp.set_a(var_index, cell + healthy.size(), value);
                //cout << "value C: " << value << endl;
                var_index++;
             } else {
               break;
            }
          }
       }
     qp.set_r(cell + healthy.size(), CGAL::SMALLER);
     qp.set_b(cell + healthy.size(), -1);
  1
      solve
  CGAL::Quadratic_program_options options;
  options.set_pricing_strategy(CGAL::QP_BLAND);
                                                                    // Bland's rule to avoid cycling...
  Solution s = CGAL::solve_linear_program(qp, ET(), options);
  //cout << s << endl:
  return !s.is_infeasible();
int main() {
  // some basic setup stuff
cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  int test_count;
  cin >> test_count;
  for(int test = 0; test < test_count; test++) {
  //cout << endl << endl;
  int healthy_count, cancer_count;</pre>
     cin >> healthy_count >> cancer_count;
     // read in healthy cell location
vector<tuple<int, int, int> > healthy(healthy_count);
for(int healthy_index = 0; healthy_index < healthy_count; healthy_index++) {</pre>
        int x, y, z;
cin >> x >> y >> z;
```

```
healthy.at(healthy_index) = make_tuple(x, y, z);
    // read in cancer cell location
vector<tuple<int, int, int> > cancer(cancer_count);
for(int cancer_index = 0; cancer_index < cancer_count; cancer_index++) {</pre>
       int x, y, z;
cin >> x >> y >> z;
       cancer.at(cancer_index) = make_tuple(x, y, z);
     // search upper lower
     int exp_value = 1;
     bool exp_found = false;
     do {
       exp_value = exp_value * 2;
       exp_found = true;
        //cout << "inc: for: " << exp_value << " is: " << can_solve(exp_value, healthy, cancer) << endl;
     } while(exp_value <= 30 && !can_solve(exp_value, healthy, cancer));</pre>
     // do binary search for the right dimension
     int min_d = 0;
     int max_d = 30;
     if(exp_found) {
       min_d = exp_value / 2 - 1;
       max_d = exp_value > 30 ? 30 : exp_value;
     //cout << "min set to " << min_d << " and max to " << max_d << endl;
     bool last_worked = false;
     while(min_d < max_d) {</pre>
       int mid_d = (min_d + max_d) / 2;
//cout << "binary search from: " << min_d << " to " << max_d << ", checking: " << mid_d << endl;
if(can_solve(mid_d, healthy, cancer)) {
    // [min_d, mid_d] contains the solution</pre>
          max_d = mid_d;
          last_worked = true;
          //cout << "\t0K" << endl;
       } else {
         /// [mid_d + 1, max_d] contains the solution
min_d = mid_d + 1;
          last_worked = false;
          //cout << "\tBAD!" << endl;
    if(min_d == 30 && !last_worked) {
       cout << "Impossible!" << endl;</pre>
       cout << min_d << endl;</pre>
    }
 }
}
```

```
#include <iostream>
#include <cassert>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
#include <CGAL/basic.h>
#include <CGAL/QP_models.h>
#include <CGAL/QP_functions.h>
// choose exact integral type
\verb|#ifdef CGAL_USE_GMP| \\
#include <CGAL/Gmpz.h>
typedef CGAL::Gmpz ET;
#else
#include <CGAL/MP_Float.h>
typedef CGAL::MP_Float ET;
#endif
// program and solution types
typedef CGAL::Quadratic_program <ET> Program;
typedef CGAL::Quadratic_program_solution <ET> Solution;
using namespace std;
int floor_to_double(const CGAL::Quotient <ET >& x) {
  double a = floor(CGAL::to_double(x));
while (a > x) a -= 1;
  while (a + 1 <= x) a += 1;
  return a;
int ceil_to_double(const CGAL::Quotient<ET>& x) {
  double a = ceil(CGAL::to_double(x));
while (a < x) a += 1;</pre>
  while (a - 1 >= x) a -= 1;
```

```
return a;
7
bool check_degree(vector<tuple<int, int, int> > cells, int nr_healthy, int degree) {
  //cout << "check with: " << degree << " ";
  Program qp(CGAL::LARGER, false, 0, false, 0);</pre>
        (int i = 0; i < cells.size(); i++) {
     int id = 0;
     tuple < int , int , int > & cell = cells[i];
     for (int x = 0; x <= degree; x++) {
  for (int y = 0; y <= degree; y++) {
    for (int z = 0; z <= degree; z++) {</pre>
            if (x + y + z <= degree) {
               qp.set_a(id, i, pow(get<0>(cell), x)*pow(get<1>(cell), y)*pow(get<2>(cell), z));
            }
            else {
              break;
            }
         }
       }
     if (i < nr_healthy) {</pre>
       qp.set_b(i, 1);
qp.set_r(i, CGAL::LARGER);
     else {
       qp.set_b(i, -1);
       qp.set_r(i, CGAL::SMALLER);
  {\tt CGAL}:: {\tt Quadratic\_program\_options} \ \ {\tt options};
   options.set_pricing_strategy(CGAL::QP_BLAND); // Bland's rule to avoid cycling...
  Solution s = CGAL::solve_linear_program(qp, ET(), options);
//cout << (s.is_optimal() == 1 ? "true" : "false") << endl;
  return !s.is_infeasible();
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_healthy, nr_tumor;
     cin >> nr_healthy >> nr_tumor;
     int nr_cells = nr_healthy + nr_tumor;
     vector<tuple<int, int, int> > cells;
     cells.reserve(nr_cells);
for (int i = 0; i < nr_cells; i++) {</pre>
       int cell_x, cell_y, cell_z;
cin >> cell_x >> cell_y >> cell_z;
        cells.push_back(make_tuple(cell_x, cell_y, cell_z));
     int exp_value = 0;
     while (exp_value < 30 && !check_degree(cells, nr_healthy, exp_value)) {
       exp_value = exp_value == 0 ? 1 : exp_value * 2;
     int min_bound = exp_value == 0 ? 0 : exp_value / 2 + 1;
     int max_bound = exp_value > 30 ? 30 : exp_value;
     //int min_bound = 0;
     //int max_bound = 30;
     bool last_check = false;
     while (min_bound < max_bound) {
  int test_degree = (min_bound + max_bound) / 2;</pre>
        //int test_degree = (min_bound*3 + max_bound) / 4;
        if (check_degree(cells, nr_healthy, test_degree)) {
         max_bound = test_degree;
last_check = true;
        else {
          min_bound = test_degree + 1;
          last_check = false;
    }
    if (min_bound == 30 && !last_check) {
  cout << "Impossible!" << endl;</pre>
     else {
        cout << min_bound << endl;</pre>
    7-
  return 0;
```

8.14 Island Hopping

Keywords: ACM, Dynamic Programming

```
#include <iostream>
#include <algorithm>
#include <vector>
#include <queue>
#include <cassert>
using namespace std;
int main() {
  cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test_cases;
    cin >> test_cases;
    for(int test = 0; test < test_cases; test++) {</pre>
        int island_count, attack_radius, attacker_strength_start;
        cin >> island_count >> attack_radius >> attacker_strength_start;
        // read in the defense strength
        vector<int> defense(island_count + 1, 0);
        for(int island_index = 1; island_index < island_count; island_index++) {</pre>
             cin >> defense.at(island_index);
        assert(defense.at(0) == 0);
        assert(defense.at(island_count) == 0);
        // keeps track of the path length
        vector<int> path_length(island_count + 1, numeric_limits<int>::max()); // first island is the attacker's island,
        this is just always -inf
path_length.at(0) = 0;
        // our DP table containing the resulting fighter strength left at an island
        vector<int> table(island_count + 1, 0);
        table.at(0) = attacker_strength_start;
        // DP algo
        for(int cur_island = 0; cur_island < island_count; cur_island++) {</pre>
            if(table.at(cur_island) <= 0) {</pre>
                 continue;
             for(int next_island = cur_island + 1;
                 next_island <= cur_island + attack_radius && next_island <= island_count;</pre>
                 next_island++) {
                 // calculate how many attackers are left if we send the people from island 'cur_island' to
                 // island 'next_island
                 int attackers left = table.at(cur island) - defense.at(next island):
                    if this is a greater number than the one already in our DP table, we found a better way
                 if(attackers_left > table.at(next_island)) {
                     table.at(next_island) = attackers_left;
                     // don't forget to keep track of the path
path_length.at(next_island) = path_length.at(cur_island) + 1;
                 } else if(attackers_left == table.at(next_island)) {
                     // maybe we found an other, better path with the same results
                     path_length.at(next_island) = min(path_length.at(cur_island) + 1, path_length.at(next_island));
                 }
            }
        if(table.at(island_count) <= 0) {</pre>
             cout << "safe" << endl;</pre>
        } else {
             cout << path_length.at(island_count) - 1 << " " << table.at(island_count) << endl;</pre>
  return 0;
}
```

```
#include <iostream>
#include <cassert>
#include <vector>
#include <liimits>
#include <queue>
#include <queue>
#include <set>
#include <cmath>
#include <cmath>
#include <stack>

using namespace std;

int main() {
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int nr_test_cases;
```

```
cin >> nr_test_cases;
for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
  int nr_islands, attack_radius, initial_strength;
  cin >> nr_islands >> attack_radius >> initial_strength;
  vector < int > defence_strengths;
  defence_strengths.reserve(nr_islands + 1);
  defence_strengths.push_back(0);
  for (int i = 1; i < nr_islands; i++) {</pre>
    int defence_strength;
    cin >> defence_strength;
    defence_strengths.push_back(defence_strength);
  defence_strengths.push_back(0);
  vector < int > max attack forces (nr islands + 1. 0):
  vector < int > min_islands (nr_islands + 1, 0);
  max_attack_forces[0] = initial_strength;
  for (int i = 0; i < nr_islands; i++)</pre>
     int current_attack_force = max_attack_forces[i];
     if (current_attack_force > 0) {
      for (int j = 1; j <= attack_radius; j++) {
   if (i + j <= nr_islands) {</pre>
           int new_attack_force = current_attack_force - defence_strengths[i + j];
           if (new_attack_force > max_attack_forces[i + j]) {
             max_attack_forces[i + j] = new_attack_force;
             min_islands[i + j] = min_islands[i] + 1;
           else if (new_attack_force == max_attack_forces[i + j]) {
             min_islands[i + j] = min(min_islands[i + j], min_islands[i] + 1);
           }
         }
         else {
           break:
        }
      }
    }
  }
  if (max_attack_forces[nr_islands] > 0) {
   cout << min_islands[nr_islands] - 1 << " " << max_attack_forces[nr_islands] << endl;</pre>
  else {
     cout << "safe" << endl;</pre>
  7
}
return 0;
```

8.15 Sweepers

Keywords: BGL, Graph with edge capacity, Graph with residual capacity, Graph with reverse edges, Max-flow, Euler circuit, Components

```
#include <iostream>
#include <algorithm>
#include <vector>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/push_relabel_max_flow.hpp>
#include <boost/graph/edmonds_karp_max_flow.hpp>
#include <boost/tuple/tuple.hpp>
#include <boost/graph/connected_components.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list_traits<vecS, vecS, directedS> Traits;
typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
   property < edge_capacity_t, long,
        property < edge_residual_capacity_t , long ,</pre>
            property < edge_reverse_t , Traits::edge_descriptor> > > Graph;
typedef adjacency_list<vecS, vecS, undirectedS, no_property, no_property> SimpleGraph;
typedef graph_traits < Graph > : : edge_descriptor
                                                         Edge;
// Custom add_edge, also creates reverse edges with corresponding capacities.
void addEdge(int u, int v, long c, EdgeCapacityMap &capacity, ReverseEdgeMap &rev_edge, Graph &G) {
    Edge e, reverseE;
    tie(e, tuples::ignore) = add_edge(u, v, G);
    tie(reverseE, tuples::ignore) = add_edge(v, u, G);
capacity[e] = c;
    capacity[reverseE] = 0;
    rev_edge[e] = reverseE;
    rev_edge[reverseE] = e;
```

```
1 }
int main() {
  cin.svnc with stdio(false):
     cout.sync_with_stdio(false);
     int test_cases;
     cin >> test_cases;
     for(int test = 0; test < test_cases; test++) {</pre>
       int room_count, corridor_count, sweeper_count;
          cin >> room_count >> corridor_count >> sweeper_count;
          int door_count = sweeper_count;
          // create graph for flow analysis
          Graph flow_graph(room_count + 2);
          EdgeCapacityMp capacity = get(edge_capacity, flow_graph);
ReverseEdgeMap rev_edge = get(edge_reverse, flow_graph);
          //ResidualCapacityMap res_capacity = get(edge_residual_capacity, flow_graph);
          // create graph with just the rooms, corridors
          SimpleGraph castle_graph(room_count);
          // define source and sink
          int source = room_count;
          int sink = room_count + 1;
          // keep track of vertices degrees
          vector < int > degrees (room_count, 0);
          vector < int > non_modified_degrees(room_count, 0);
          // read in location of sweepers
          vector<int> sweepers(room_count, 0);
          for(int sweeper_index = 0; sweeper_index < sweeper_count; sweeper_index++) {
   int location;</pre>
              cin >> location;
               // source -> sweeper location
              addEdge(source, location, 1, capacity, rev_edge, flow_graph);
              degrees.at(location)++:
              sweepers.at(location)++;
          // read in location of doors
for(int door_index = 0; door_index < door_count; door_index++) {</pre>
              int location:
              cin >> location;
              // door location -> sink
              addEdge(location, sink, 1, capacity, rev_edge, flow_graph);
              degrees.at(location) --:
          // read in corridors
          for(int corridor_index = 0; corridor_index < corridor_count; corridor_index++) {</pre>
              int from, to;
              cin >> from >> to;
              addEdge(from, to, 1, capacity, rev_edge, flow_graph);
              addEdge(to, from, 1, capacity, rev_edge, flow_graph);
              add_edge(from, to, castle_graph);
              degrees.at(from)++:
              degrees.at(to)++;
              non_modified_degrees.at(from)++;
              non_modified_degrees.at(to)++;
          // so now we have a basic graph, check if all sweepers can reach a door. // do this by doing a flow and check if flow result same as sweepers count
          int sweepers_exited = push_relabel_max_flow(flow_graph, source, sink);
          //cout << "sweepers exited: " << sweepers_exited << ", total sweepers: " << sweeper_count << endl;
if(sweepers_exited != sweeper_count) {</pre>
              cout << "no" << endl;
              continue:
          // check for euler circuit
          bool has_even_degree = true;
for(int vertex = 0; vertex < room_count; vertex++) {</pre>
              if(degrees.at(vertex) < 0 || degrees.at(vertex) % 2 != 0) {
   has_even_degree = false;</pre>
                   break;
              }
          7
          //cout << "even: " << has_even_degree << endl;</pre>
          if(!has_even_degree) {
              cout << "no" << endl;
               continue;
```

```
// make sure every edge, i.e. corridor, was visited at least once
    // first get the connected component information
    vector<int> component(room_count);
    {\tt connected\_components(castle\_graph\,,\,\,\&component[0])\,;}
    vector<int> cleaned_by_sweepers(room_count, 0);
int max_component_nr = 0;
    for(int room_index = 0; room_index < room_count; room_index++) {</pre>
        // we're interested that every component is cleaned, so we use this as the index. Keep track of
         // how many components we have
        int component_nr = component.at(room_index);
        max_component_nr = max(max_component_nr, component_nr);
         // if the room has no corridors attached, we assume it is cleaned (only corridors need cleaning,
         // no corridor, no cleaning needed)
        if(non_modified_degrees.at(room_index) == 0) {
             cleaned_by_sweepers.at(component_nr) = 1;
        } else {
            // the degree of the room might be 0, then there is no sweeper added to the component. If never one
             // is added, component not cleaned.
             cleaned_by_sweepers.at(component_nr) += sweepers.at(room_index);
        }
    }
    // make sure every component is cleaned, i.e. contains some sweepers. Other requirements make sure
       the component is cleaned if it contains sweepers
    bool components_cleaned = true;
    for(int i = 0; i <= max_component_nr; i++) {</pre>
        if(cleaned_by_sweepers.at(i) == 0) {
             components_cleaned = false;
             break;
        }
    if(components_cleaned) {
   cout << "yes" << endl;</pre>
     else {
        cout << "no" << endl;
}
return 0:
```

```
#include <iostream>
#include <cassert>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
#include <stack>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/push_relabel_max_flow.hpp>
#include <boost/graph/connected_components.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, directedS> Traits;
typedef adjacency_list<vecS, vecS, directedS, no_property, property<edge_capacity_t, long, property<
    edge_residual_capacity_t, long, property<edge_reverse_t, Traits::edge_descriptor> >> > Graph;
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
typedef property_map < Graph , edge_capacity_t >:: type EdgeCapacityMap;
typedef property_map < Graph , edge_reverse_t >:: type ReverseEdgeMap;
typedef adjacency_list < vecS , vecS , undirectedS , no_property , no_property > SimpleGraph;
inline void add_flow_edge(int start, int end, int c, EdgeCapacityMap& capacity, ReverseEdgeMap& rev_edge, Graph& g) {
  Edge e, rev_e;
  bool success;
  tie(e, success) = add_edge(start, end, g);
  if (success) {
    tie(rev_e, success) = add_edge(end, start, g);
    capacity[e] = c;
    capacity[rev_e] = 0;
    rev_edge[e] = rev_e;
    rev_edge[rev_e] = e;
  else {
    capacity[e] += c;
 }
1
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
```

```
int nr_test_cases;
cin >> nr_test_cases;
for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
  int nr_rooms, nr_corridors, nr_sweepers;
  cin >> nr_rooms >> nr_corridors >> nr_sweepers;
  //cout << endl;</pre>
  Graph g(nr_rooms + 2);
  SimpleGraph components_g(nr_rooms);
int source = nr_rooms;
  int sink = nr_rooms + 1;
  EdgeCapacityMap capacity = get(edge_capacity, g);
ReverseEdgeMap rev_edge = get(edge_reverse, g);
  vector<int> starting_locations(nr_rooms, 0);
  for (int i = 0; i < nr_sweepers; i++) {</pre>
    int starting_location;
    cin >> starting_location;
    add_flow_edge(source, starting_location, 1, capacity, rev_edge, g);
    starting_locations[starting_location]++;
  vector<int> outside_doors(nr_rooms, 0);
  for (int i = 0; i < nr_sweepers; i++) {</pre>
    int outside_door;
    cin >> outside_door;
     add_flow_edge(outside_door, sink, 1, capacity, rev_edge, g);
    outside_doors[outside_door]++;
  vector<int> vertex_degrees(nr_rooms, 0);
  for (int i = 0; i < nr_corridors; i++) {</pre>
    int end_one, end_two;
    cin >> end_one >> end_two;
    vertex_degrees[end_one]++;
    vertex_degrees[end_two]++;
    add_flow_edge(end_one, end_two, 1, capacity, rev_edge, g);
add_flow_edge(end_two, end_one, 1, capacity, rev_edge, g);
    add_edge(end_one, end_two, components_g);
  //check if all vertices have an even degree
  bool found_uneven = false;
for (int i = 0; i < nr_rooms; i++) {</pre>
    if ((vertex_degrees[i] + outside_doors[i] + starting_locations[i]) % 2 == 1) {
      found_uneven = true;
       break;
    }
  if (found_uneven) {
  //cout << "uneven degree found" << endl;</pre>
    cout << "no" << endl;
  //check if every component of the graph has at least one assigned sweeper
  vector<int> comp(nr_rooms);
  int num = connected_components(components_g, &comp[0]);
  vector < int > cleaned(num, 0);
for (int i = 0; i < nr_rooms; i++) {</pre>
    if (vertex_degrees[i] == 0) {
      cleaned[comp[i]] = 1;
    else {
      cleaned[comp[i]] += starting_locations[i];
  bool uncleaned_comp = false;
  for (int i = 0; i < num; i++) {
  if (cleaned[i] == 0) {</pre>
       uncleaned_comp = true;
    }
  }
  //cout << "no_sweeper: " << no_sweeper << endl;</pre>
  if (uncleaned_comp) {
    //cout << "component without sweeper" << endl;
cout << "no" << endl;</pre>
    continue;
  //check if all sweepers can flee
  int escaped_sweepers = push_relabel_max_flow(g, source, sink);
  if (escaped_sweepers < nr_sweepers) {</pre>
    //cout << "max flow to low" << endl;</pre>
```

```
cout << "no" << endl;
    continue;
}

cout << "yes" << endl;
}

return 0;
}</pre>
```

8.16 Clues

Keywords: BGL, CGAL, BGL with CGAL, CGAL with BGL, Point set, Triangulation with info(), Bipartite, Components

```
#include <cassert>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/bipartite.hpp>
#include <boost/graph/connected_components.hpp>
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
#include <CGAL/basic.h>
#include <CGAL/squared_distance_2.h>
#include <CGAL/Triangulation_vertex_base_with_info_2.h>
#include <CGAL/Point_set_2.h>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, undirectedS, no_property, no_property> Graph;
typedef graph_traits<Graph>::vertex_descriptor Vertex;
typedef graph_traits < Graph > :: edge_descriptor Edge;
typedef graph_traits < Graph >:: out_edge_iterator Edge_iterator;
typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
typedef K::Point_2 Point;
typedef K::Circle_2 Circle;
typedef CGAL::Triangulation_vertex_base_with_info_2 <int, K> Vb;
typedef CGAL::Triangulation_data_structure_2 < Vb > Tds;
typedef CGAL::Point_set_2<K, Tds> PSet;
typedef CGAL::Point_set_2<K, Tds>::Vertex_handle Vertex_handle;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  int test_count;
  cin >> test_count;
  for(int test = 0; test < test_count; test++) {</pre>
    int station_count, clue_count;
    K::FT range;
    cin >> station_count >> clue_count >> range;
    range = pow(range, 2); // work with squared distances
    // read in station location
    // pair.first: the point where the station is located
    // pair.second: the index of the station
    vector<pair<Point, int> > stations(station_count);
    for(int station_index = 0; station_index < station_count; station_index++) {</pre>
      int x, y;
cin >> x >> y;
      stations.at(station_index) = make_pair(Point(x, y), station_index);
    // read in clue location
    vector < pair < Point , Point > > clues(clue_count);
    for(int clue_index = 0; clue_index < clue_count; clue_index++) {</pre>
         read in from where to where we would like to go
      int start_x, start_y, target_x, target_y;
      cin >> start_x >> start_y >> target_x >> target_y;
      clues.at(clue_index) = make_pair(Point(start_x, start_y), Point(target_x, target_y));
    // create a graph that can be used to check for graph properties
    Graph graph(station_count);
    // calculate the point set so we can find the nearest one for a given point and all stations
```

```
// inside a circle of given radius
       PSet station_triang;
       station_triang.insert(stations.begin(), stations.end());
             go trough stations, search for stations that are inside the radius and process
                them.
       for(int stationA_index = 0; stationA_index < station_count; stationA_index++) {</pre>
             Point stationA = stations.at(stationA_index).first;
             Circle stationA_area = Circle(stationA, range);
              // collect all stations inside the circle
             vector < Vertex_handle > stations_in_range;
             station_triang.range_search(stationA_area, back_inserter(stations_in_range));
             // go trough found stations and make sure that each pair is at least 'range' away from each other
// as long as it's not our stationA one of the pair's stations
for(int i = 0; i < stations_in_range.size(); i++) {</pre>
                  for(int j = i + 1; j < stations_in_range.size(); j++) {
  int some_station_1 = stations_in_range.at(i) -> info();
                          int some_station_2 = stations_in_range.at(j)->info();
                         if(some_station_1 != stationA_index && some_station_2 != stationA_index) {
   if(CGAL::squared_distance(stations_in_range.at(i)->point(), stations_in_range.at(j)->point()) <= range) {
     // another pair of stations in reachable station, conflict!
     //cout << "blub" << endl;</pre>
                                     goto not_bipartit;
                              }
                        7
                 }
              // add edges
             for(int i = 0; i < stations_in_range.size(); i++) {</pre>
                   int to = stations_in_range.at(i)->info();
                   if(to != stationA_index) {
                        add_edge(stationA_index, to, graph);
                  }
           }
       // check if graph is not bipartit, if so, we can stop % \left( 1\right) =\left( 1\right) \left( 1\right)
       if(!is_bipartite(graph)) {
             //cout << "no blub" << endl;</pre>
              not_bipartit:
              for(int clue_index = 0; clue_index < clue_count; clue_index++) {</pre>
                   cout << "n";
             cout << endl:
       } else {
                     now we have to check which of the clues can be received
              // get connected components information, so we can find out if start and end of a clue is in the same
              // component and therefore reachable
             vector <int> in_component(station_count);
             connected_components(graph, &in_component[0]);
             for(int clue_index = 0; clue_index < clue_count; clue_index++) {</pre>
                   // get where the clue starts and should end
Point start = clues.at(clue_index).first;
                   Point target = clues.at(clue_index).second;
                   // check if start and target of the clue are near each other and communicate directly
if(range >= CGAL::squared_distance(start, target)) {
                        cout << "y";
                         continue;
                   // get nearest vertex to the start and check if we can reach it
Vertex_handle near_start_station = station_triang.nearest_vertex(start);
                   if(range < CGAL::squared_distance(start, near_start_station->point())) {
                         cout << "n"; // next station from start too far away
                         continue;
                    // now the same for the end station/clue location
                    Vertex_handle near_end_station = station_triang.nearest_vertex(target);
                   if(range < CGAL::squared_distance(target, near_end_station->point())) {
                         cout << "n";
                         continue;
                    // last part is to check if both are in the same component
                   if(in_component.at(near_start_station->info()) == in_component.at(near_end_station->info())) {
                         cout << "y";
                   } else {
                         cout << "n";
                  }
              cout << endl;
     }
}
return 0;
```

```
#include <iostream>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/bipartite.hpp>
#include <boost/graph/connected_components.hpp>
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
#include <CGAL/basic.h>
#include <CGAL/squared_distance_2.h>
#include <CGAL/Triangulation_vertex_base_with_info_2.h>
#include <CGAL/Point_set_2.h>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, undirectedS, no_property, no_property> Graph;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
typedef graph_traits < Graph > :: edge_descriptor Edge;
typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
typedef K::Point_2 Point;
typedef K::Circle_2 Circle;
typedef CGAL::Triangulation_vertex_base_with_info_2 <int, K> Vb;
typedef CGAL::Triangulation_data_structure_2 < Vb > Tds;
typedef CGAL::Point_set_2 < K, Tds > PSet;
typedef CGAL::Point_set_2 < K, Tds >::Vertex_handle Vertex_handle;
double floor_to_double(const K::FT& x)
  double a = std::floor(CGAL::to_double(x));
  while (a > x) a -= 1;
while (a + 1 <= x) a += 1;
  return a;
double ceil_to_double(const K::FT& x)
  double a = std::ceil(CGAL::to_double(x));
  while (a < x) a += 1;
  while (a - 1 >= x) a -= 1;
  return a;
7
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_stations, nr_clues, max_radius;
    cin >> nr_stations >> nr_clues >> max_radius;
    vector<pair<Point, int> > stations;
    stations.reserve(nr_stations);
    for (int i = 0; i < nr_stations; ++i) {</pre>
      int station_x, station_y;
       cin >> station_x >> station_y;
       stations.push_back(make_pair(Point(station_x, station_y), i));
    vector<pair<Point, Point> > clues;
     clues.reserve(nr_clues);
    for (int i = 0; i < nr_clues; ++i) {</pre>
       int from_x, from_y, to_x, to_y;
cin >> from_x >> from_y >> to_x >> to_y;
clues.push_back(make_pair(Point(from_x, from_y), Point(to_x, to_y)));
    PSet pset(stations.begin(), stations.end());
K::FT max_radius_squared = pow(max_radius, 2);
    Graph g(nr_stations);
for (int i = 0; i < nr_stations; ++i) {</pre>
       Circle c(stations[i].first, max_radius_squared);
       vector < Vertex_handle > result;
       pset.range_search(c, back_inserter(result));
       for (int j = 0; j < result.size(); ++j) {
  for (int k = j + 1; k < result.size(); ++k) {</pre>
           if (result[j]->info() != i && result[k]->info() != i) {
              if (CGAL::squared_distance(result[j]->point(), result[k]->point()) <= max_radius_squared) {</pre>
                goto not_bipartite;
```

```
}
     }
    for (int j = 0; j < result.size(); ++j) {</pre>
     int to = result[j]->info();
      if (to != i) {
       add_edge(i, to, g);
   }
  if (!is_bipartite(g)) {
    not_bipartite:
    for (int i = 0; i < nr_clues; i++) {</pre>
     cout << "n";
    cout << endl:
  else {
    vector < int > component(nr_stations);
    connected_components(g, &component[0]);
    for (int i = 0; i < nr_clues; i++) {</pre>
      if (CGAL::squared_distance(clues[i].first, clues[i].second) <= max_radius_squared) {</pre>
       cout << "y";
        continue;
      Vertex_handle start_p = pset.nearest_vertex(clues[i].first);
      if (CGAL::squared_distance(start_p->point(), clues[i].first) > max_radius_squared) {
       cout << "n";
       continue;
      Vertex_handle end_p = pset.nearest_vertex(clues[i].second);
      if (CGAL::squared_distance(end_p->point(), clues[i].second) > max_radius_squared) {
        cout << "n";
       continue:
      int start = start_p->info();
      int end = end_p->info();
      if (component[start] == component[end]) {
       cout << "y";
      else {
       cout << "n";
      }
    cout << endl:
 }
return 0;
```

8.17 Radiation 2

Keywords: CGAL, Delaunay Triangulation, Point set, Triangulation with info()

```
// ONLY FIRST TWO TEST CASES!
#include <CGAL/Exact_predicates_inexact_constructions_kernel.h>
#include <CGAL/Delaunay_triangulation_2.h>
#include <CGAL/Triangulation_vertex_base_with_info_2.h>
#include <CGAL/Point_set_2.h>
typedef CGAL::Exact_predicates_inexact_constructions_kernel K;
typedef CGAL::Delaunay_triangulation_2<K> Triangulation;
typedef Triangulation::Edge_iterator Edge_iterator;
typedef K::Point_2 Point;
typedef K::Circle_2 Circle;
typedef CGAL::Triangulation_vertex_base_with_info_2 < int , K > Vb;
typedef CGAL::Triangulation_data_structure_2 < Vb > Tds;
typedef CGAL::Point_set_2<K, Tds> PSet;
typedef CGAL::Point_set_2<K, Tds>::Vertex_handle PSVertex_handle;
typedef CGAL::Delaunay_triangulation_2 <K> Triangulation;
\label{typedef} \begin{tabular}{ll} type def & CGAL:: Delaunay\_triangulation\_2 < K > :: Vertex\_handle & TriangVertex\_handle; \\ \end{tabular}
using namespace std;
// from slides, fun!
double floor_to_double(const K::FT& x)
  double a = std::floor(CGAL::to_double(x));
  while (a > x) a -= 1;
while (a+1 <= x) a += 1;
  return a;
double ceil_to_double(const K::FT& x)
```

```
double a = std::ceil(CGAL::to_double(x));
  while (a < x) a += 1;
while (a-1 >= x) a -= 1;
  return a;
int main() {
  // some basic setup stuff
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  cout << fixed << setprecision(0);</pre>
  int test_count;
  cin >> test_count;
  for(int test = 0; test < test_count; test++) {</pre>
    int healthy count, cancer count:
    cin >> healthy_count >> cancer_count;
    // read in healthy and cancer cells
    vector < Point > cancer_cells;
    cancer_cells.reserve(cancer_count);
    vector < Point > healthy_cells;
    healthy_cells.reserve(healthy_count);
    for(int healthy_index = 0; healthy_index < healthy_count; healthy_index++) {</pre>
      double x, y;
      cin >> x >> y;
      healthy_cells.push_back(Point(x, y));
    for(int cancer_index = 0; cancer_index < cancer_count; cancer_index++) {</pre>
      double x, y;
cin >> x >> y;
      cancer_cells.push_back(Point(x, y));
    // create a point set of cancer cells, this allows us to find all cells inside a circle quickly (I hope!)
PSet cancer_triang(cancer_cells.begin(), cancer_cells.end());
    // create a triangulation of healthy cells to find quickly the nearest one to a cancer point
    Triangulation healthy_triang(healthy_cells.begin(), healthy_cells.end());
    // iterate over all cancer cells to search for the best radius
    unsigned long max_cells_killed = 0;
    for(int cancer_index = 0; cancer_index < cancer_count; cancer_index++) {
    // gett the point of the cancer cell
      Point cancer_cell = cancer_cells.at(cancer_index);
       ^{\prime\prime} get the nearest healthy cell, defining by that the radius
      TriangVertex_handle next_healthy = healthy_triang.nearest_vertex(cancer_cell);
       // create the circle which will be radiated
      Circle radiation_region = Circle(cancer_cell, CGAL::squared_distance(cancer_cell, next_healthy->point()));
      // get the cancer cells that would be eliminated
      vector < PSVertex_handle > killed_cancer_cells;
      cancer_triang.range_search(radiation_region, back_inserter(killed_cancer_cells));
      max_cells_killed = max(max_cells_killed, killed_cancer_cells.size());
    cout << max_cells_killed << endl;</pre>
 }
}
```

8.18 Knights

Keywords: BGL, Graph with edge capacity, Graph with residual capacity, Graph with reverse edges, Max-flow

```
typedef property_map <Graph, edge_residual_capacity_t>::type ResidualCapacityMap;
typedef graph_traits < Graph > :: edge_descriptor Edge;
void addEdge(int from, int to, int weight, Graph& graph, EdgeCapacityMap& capacity, ReverseEdgeMap& rev_edge) {
  Edge edge, r_edge;
  tie(edge, tuples::ignore) = add_edge(from, to, graph);
tie(r_edge, tuples::ignore) = add_edge(to, from, graph);
  capacity[edge] = weight;
  capacity[r_edge] = 0;
  rev_edge[edge] = r_edge;
 rev_edge[r_edge] = edge;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int test_count;
  cin >> test_count;
  for(int test = 0; test < test_count; test++) {</pre>
    int width, height, knight_count;
    cin >> width >> height >> knight_count;
    // create graph
    Graph graph(2 * width * height + 2 + knight_count); // don't forget source and sink
    EdgeCapacityMap capacity = get(edge_capacity, graph);
ReverseEdgeMap rev_edge = get(edge_reverse, graph);
    ResidualCapacityMap res_capacity = get(edge_residual_capacity, graph);
     * [0 .. knight_count - 1]: knights
     * [knight_count .. knight_count + width * height - 1]: intersections of set 1 with edges to set 2
* [knight_count + width * height .. knight_count + 2 * width * height - 1]: intersections of set 2 with edges to set
    // source / sink
    int source = 2 * width * height + knight_count;
    int sink = source + 1;
    // read in knight position
    for(int knight_index = 0; knight_index < knight_count; knight_index++) {</pre>
      int x, y;
cin >> x >> y;
       // source -> sink
      addEdge(source, knight_index, 1, graph, capacity, rev_edge);
       //cout << "source -> " << knight_index << endl;</pre>
       // knight -> starting position in first intersection set
addEdge(knight_index, knight_count + x + y * width, 1, graph, capacity, rev_edge);
       //cout << knight_index << " -> " << knight_count + x + y * width << endl;
    // add missing edges
    for(int edge_x = 0; edge_x < width; edge_x++) {</pre>
       for(int edge_y = 0; edge_y < height; edge_y++) {
  int intersection_offset = edge_x + edge_y * width;</pre>
         // edge from first intersection set to second one
addEdge(knight_count + intersection_offset, knight_count + width * height + intersection_offset, 1, graph,
              capacity, rev_edge);
         //cout << "first set to second set: " << intersection_offset << " -> " << intersection_offset << endl;</pre>
         // edge from second intersection set to all in set one that can be reached by a path of length 1 in the cave
         if(edge x - 1 >= 0) {
           \verb|addEdge(knight_count + width * height + intersection_offset, knight_count + edge_x - 1 + edge_y * width, 1, \\
           graph, capacity, rev_edge);
//cout << "A second set to first set: " << intersection_offset << " -> " << edge_x - 1 + edge_y * width << endl
         if(edge x + 1 < width) {
           addEdge(knight_count + width * height + intersection_offset, knight_count + edge_x + 1 + edge_y * width, 1,
           graph, capacity, rev_edge);
//cout << "B second set to first set: " << intersection_offset << " -> " << edge_x + 1 + edge_y * width << endl</pre>
         }
         if(edge_y - 1 >= 0) {
           addEdge(knight_count + width * height + intersection_offset, knight_count + edge_x + (edge_y - 1) * width, 1,
           graph, capacity, rev_edge);
//cout << "C second set to first set: " << intersection_offset << " -> " << edge_x + (edge_y - 1) * width <</pre>
                 endl;
         if(edge_y + 1 < height) {</pre>
           addEdge(knight_count + width * height + intersection_offset, knight_count + edge_x + (edge_y + 1) * width, 1,
                graph, capacity, rev_edge);
           //cout << "D second set to first set: " << intersection_offset << " -> " << edge_x + (edge_y + 1) * width <<
                endl:
         }
         // add sink edge to second intersection set
         if(edge_x == 0 || edge_x + 1 == width || edge_y == 0 || edge_y + 1 == height) {
           addEdge(knight_count + width * height + intersection_offset, sink, 1, graph, capacity, rev_edge);
```

```
//cout << knight_count + intersection_offset << " -> sink" << endl;
}
}
// do max flow
int max = push_relabel_max_flow(graph, source, sink);
cout << max << endl;
}
return 0;
}</pre>
```

```
#include <iostream>
#include <cassert>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/dijkstra_shortest_paths.hpp>
#include <boost/graph/kruskal_min_spanning_tree.hpp>
#include <boost/property_map/transform_value_property_map.hpp>
#include <boost/graph/boyer_myrvold_planar_test.hpp>
#include <boost/graph/max_cardinality_matching.hpp>
#include <boost/graph/push_relabel_max_flow.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, directedS> Traits;
typedef adjacency_list<vecS, vecS, directedS, no_property, property<edge_capacity_t, long, property<
    edge_residual_capacity_t, long, property<edge_reverse_t, Traits::edge_descriptor> > > > Graph;
typedef graph_traits < Graph > :: edge_descriptor Edge;
typedef graph_traits < Graph > :: vertex_descriptor Vertex;
typedef property_map < Graph , edge_capacity_t > :: type EdgeCapacityMap;
typedef property_map < Graph, edge_reverse_t >:: type ReverseEdgeMap;
inline void add_flow_edge(int start, int end, int c, EdgeCapacityMap& capacity, ReverseEdgeMap& rev_edge, Graph& g) {
  Edge e, rev_e;
  bool success;
  tie(e, success) = add_edge(start, end, g);
  if (success) {
    tie(rev_e, success) = add_edge(end, start, g);
capacity[e] = c;
    capacity[rev_e] = 0;
rev_edge[e] = rev_e;
    rev_edge[rev_e] = e;
  }
  else {
    capacity[e] += c;
  }
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  //cout << fixed << setprecision(0);</pre>
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int x_dim, y_dim, nr_knights;
cin >> x_dim >> y_dim >> nr_knights;
    int nr_intersections = x_dim*y_dim;
    int nr_nodes = nr_intersections * 2 + 2;
    int source = nr_intersections * 2;
int sink = nr_intersections * 2 + 1;
    Graph g(nr_nodes);
    EdgeCapacityMap capacity = get(edge_capacity, g);
    ReverseEdgeMap rev_edge = get(edge_reverse, g);
    for (int i = 0; i < x_dim; i++) {
  for (int j = 0; j < y_dim; j++) {
    int edge_id = j*x_dim + i;</pre>
         //add "only go through intersection once constraint"
         add_flow_edge(edge_id, edge_id + nr_intersections, 1, capacity, rev_edge, g);
         //add horizontal edges
         if (i == 0) {
           add_flow_edge(edge_id + nr_intersections, sink, 1, capacity, rev_edge, g);
```

```
add_flow_edge(edge_id + nr_intersections, edge_id-1, 1, capacity, rev_edge, g);
      if (i == x_dim - 1) {
       add_flow_edge(edge_id + nr_intersections, sink, 1, capacity, rev_edge, g);
       add_flow_edge(edge_id + nr_intersections, edge_id + 1, 1, capacity, rev_edge, g);
      //add vertical edges
      if (j == 0) {
       add_flow_edge(edge_id + nr_intersections, sink, 1, capacity, rev_edge, g);
      else {
       add_flow_edge(edge_id + nr_intersections, edge_id - x_dim, 1, capacity, rev_edge, g);
      if (j == y_dim - 1) {
       add_flow_edge(edge_id + nr_intersections, sink, 1, capacity, rev_edge, g);
      else {
       add_flow_edge(edge_id + nr_intersections, edge_id + x_dim, 1, capacity, rev_edge, g);
 }
 for (int i = 0; i < nr_knights; i++) {</pre>
   int knight_x, knight_y;
   cin >> knight_x >> knight_y;
    int edge_id = knight_y*x_dim + knight_x;
    add_flow_edge(source, edge_id, 1, capacity, rev_edge, g);
  int flow = push_relabel_max_flow(g, source, sink);
 cout << flow << endl;</pre>
return 0;
```

8.19 Tight Words

Keywords: ACM, Dynamic Programming

```
#include <iostream>
#include <cassert>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
#define MOD_NUM 100003
using namespace std;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  int test count:
  cin >> test_count;
  for(int test = 0; test < test_count; test++) {</pre>
     int max_word, max_length;
     cin >> max_word >> max_length;
    if(max_length > 0) {
       vector<vector<int> > table(max_word + 1, vector<int>(max_length + 1, 0));
       // init for length 1
       for(int word = 0; word <= max_word; word++) {</pre>
         table.at(word).at(1) = 1;
       // go trough length of the word
       for(int length = 2; length <= max_length; length++) {</pre>
         // go trough each additional word
         for(int word = 0; word <= max_word; word++) {</pre>
           // add current word to a string ending with the previous word
if(word - 1 >= 0) { // only if there is a "previous word" of course
  table.at(word).at(length) += table.at(word - 1).at(length - 1);
            // add current word to a string ending with the same word
            table.at(word).at(length) += table.at(word).at(length - 1);
```

```
// add current word to a string ending with the next word
if(word + 1 <= max_word) {
    table.at(word).at(length) += table.at(word + 1).at(length - 1);
}

table.at(word).at(length) = table.at(word).at(length) % MOD_NUM;
}

// now we have to count together all the words possible (it can end with any of the words)
int solution = 0;
for(int word = 0; word <= max_word; word++) {
    solution += table.at(word).at(max_length);
}

cout << solution % MOD_NUM << endl;
} else {
    cout << "1" << endl;
}

return 0;
}</pre>
```

```
#include <iostream>
#include <cassert>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
#define MOD_NUM 100003
using namespace std;
int main() {
  cin.sync_with_stdio(false);
  cout.sync_with_stdio(false);
  //cout << fixed << setprecision(0);</pre>
  int nr_test_cases;
  cin >> nr_test_cases;
  for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_letters, word_length;
    cin >> nr_letters >> word_length;
    if (word_length > 0) {
      vector < vector < int > > dp(word_length + 1, vector < int > (nr_letters + 1, 0));
      for (int i = 0; i <= nr_letters; i++) {
  dp[1][i] = 1;</pre>
      for (int i = 2; i <= word_length; i++) {</pre>
        //cout << "adding2: " << dp[i - 1][j] << endl;
          dp[i][j] += dp[i-1][j];
          if (j + 1 <= nr_letters) {
   //cout << "adding3: " << dp[i - 1][j + 1] << endl;
   dp[i][j] += dp[i - 1][j + 1];</pre>
           dp[i][j] = dp[i][j] % MOD_NUM;
          //cout << dp[i][j] << " ";
        }
        //cout << endl;
      int solution = 0;
      for (int i = 0; i <= nr_letters; i++) {</pre>
        solution += dp[word_length][i];
      solution = solution % MOD_NUM;
      cout << solution << endl;</pre>
      cout << 1 << endl;
 }
  return 0;
```

8.20 Cantonal Courier

Keywords: BGL, Graph with edge capacity, Graph with residual capacity, Graph with reverse edges, Max-flow

```
#include <iostream>
#include <vector>
#include <queue>
#include <tuple>
#include <cmath>
#include <climits>
#include <algorithm>
#include <climits>
#include <string>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/push_relabel_max_flow.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list_traits < vecS, vecS, directedS > Traits;
typedef adjacency_list<vecS, vecS, directedS, no_property,</pre>
    property < edge_capacity_t, int,</pre>
    property < edge_residual_capacity_t, int,</pre>
    property < edge_reverse_t, Traits::edge_descriptor> > > Graph;
typedef graph_traits < Graph > : : edge_descriptor Edge;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
typedef property_map < Graph , edge_capacity_t > :: type EdgeCapacityMap;
typedef property_map <Graph, edge_residual_capacity_t>::type ResidualCapacityMap;
typedef property_map < Graph , edge_reverse_t > :: type ReverseEdgeMap;
// Custom add_edge, also creates reverse edges with corresponding capacities. void addEdge(int u, int v, int c, EdgeCapacityMap &capacity, ReverseEdgeMap &rev_edge, Graph &G) {
    Edge e, reverseE;
    tie(e, tuples::ignore) = add_edge(u, v, G);
    tie(reverseE, tuples::ignore) = add_edge(v, u, G);
capacity[e] = c;
    capacity[reverseE] = 0;
    rev_edge[e] = reverseE;
    rev_edge[reverseE] = e;
}
int main(void)
    cin.sync_with_stdio(false);
    cout.sync_with_stdio(false);
    int test_cases;
    cin >> test_cases;
    for(int test = 0; test < test_cases; test++) {</pre>
         int zone_count, job_count;
         cin >> zone_count >> job_count;
         // create graph for flow analysis
Graph graph(zone_count + job_count + 2);
         // helper variables to find
         int zone_offset = 0;
         int job_offset = zone_count;
         int source = zone_count + job_count;
         int sink = source + 1;
         // get graph's properties
         EdgeCapacityMap capacity = get(edge_capacity, graph);
ReverseEdgeMap rev_edge = get(edge_reverse, graph);
         // read in the cost for a zone ticket
         for(int zone_index = 0; zone_index < zone_count; zone_index++) {</pre>
             int cost;
             cin >> cost;
             addEdge(zone_offset + zone_index, sink, cost, capacity, rev_edge, graph);
         // read in job rewards
         int total_reward = 0;
         for(int job_index = 0; job_index < job_count; job_index++) {</pre>
             int reward;
             cin >> reward;
             total_reward += reward;
             addEdge(source, job_offset + job_index, reward, capacity, rev_edge, graph);
         // read in needed zones
         for(int job_index = 0; job_index < job_count; job_index++) {</pre>
             int zones_needed_count;
             cin >> zones_needed_count;
             for(int col = 0; col < zones_needed_count; col++) {</pre>
                 int zone;
```

```
#include <iostream>
#include <cassert>
#include <vector>
#include <limits>
#include <algorithm>
#include <queue>
#include <set>
#include <utility>
#include <cmath>
#include <stack>
#include <boost/config.hpp>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/push_relabel_max_flow.hpp>
#include <boost/graph/connected_components.hpp>
using namespace std;
using namespace boost;
typedef adjacency_list<vecS, vecS, directedS> Traits;
typedef adjacency_list<vecS, vecS, directedS, no_property, property<edge_capacity_t, long, property<
edge_residual_capacity_t, long, property<edge_reverse_t, Traits::edge_descriptor> > > Graph;
typedef graph_traits<Graph>::edge_descriptor Edge;
typedef graph_traits < Graph >:: vertex_descriptor Vertex;
typedef property_map < Graph , edge_capacity_t > :: type EdgeCapacityMap;
typedef property_map < Graph, edge_reverse_t >:: type ReverseEdgeMap;
typedef adjacency_list<vecS, vecS, undirectedS, no_property, no_property> SimpleGraph;
inline void add_flow_edge(int start, int end, int c, EdgeCapacityMap& capacity, ReverseEdgeMap& rev_edge, Graph& g) {
  Edge e, rev_e;
  bool success;
  tie(e, success) = add_edge(start, end, g);
  if (success) {
    tie(rev_e, success) = add_edge(end, start, g);
    capacity[e] = c;
    capacity[rev_e] = 0;
    rev_edge[e] = rev_e;
    rev_edge[rev_e] = e;
  else {
    capacity[e] += c;
7
int main() {
 cin.svnc with stdio(false):
 cout.sync_with_stdio(false);
  int nr_test_cases;
  cin >> nr_test_cases;
 for (int test_case = 0; test_case < nr_test_cases; test_case++) {</pre>
    int nr_zones, nr_jobs;
    cin >> nr_zones >> nr_jobs;
    int nr_vertices = nr_zones + nr_jobs + 2;
    Graph g(nr_vertices);
int source = nr_vertices - 2;
int sink = nr_vertices - 1;
    EdgeCapacityMap capacity = get(edge_capacity, g);
    ReverseEdgeMap rev_edge = get(edge_reverse, g);
    for (int i = 0; i < nr_zones; ++i) {</pre>
      int ticket cost:
      cin >> ticket_cost;
      add_flow_edge(nr_jobs + i, sink, ticket_cost, capacity, rev_edge, g);
    int sum_job_reward = 0;
for (int i = 0; i < nr_jobs; ++i) {</pre>
      int job_reward;
cin >> job_reward;
      add_flow_edge(source, i, job_reward, capacity, rev_edge, g);
      sum_job_reward += job_reward;
```

```
for (int i = 0; i < nr_jobs; ++i) {
   int nr_tickets_for_job;
   cin >> nr_tickets_for_job;
   for (int j = 0; j < nr_tickets_for_job; ++j) {
      int ticket_id;
      cin >> ticket_id;
      ticket_id--;
      add_flow_edge(i, nr_jobs + ticket_id, numeric_limits<int>::max(), capacity, rev_edge, g);
   }
} int cost = push_relabel_max_flow(g, source, sink);

cout << sum_job_reward - cost << endl;
}
return 0;
}</pre>
```

9 Useful Snippets and Stuff

9.1 General remarks

• around 10'000'000 operations/iterations per second (ACM slide below claims its less, but oh well)

Asymptotic Running Time

- Rule of Thumb: Processor can do IM operations per second, Timelimit is 3 seconds.
- n < 1M: Algorithm should be O(n)
- n < 100K: Algorithm should be O(n log n)
- n < 1K: Algorithm should be $O(n^2)$
- n < 100: Algorithm should be $O(n^3)$
- n < 50: Algorithm should be $O(n^4)$
- n < 20: Algorithm should be $O(n^5)$ or $O(2^n)$
- n < 10: Algorithm should be $O(n^6)$ or O(n!)

9.2 Custom Sorting

```
// ATTENTION: be careful, each container has its own order!
#include <vector>
#include <algorithm>
 * #1: Define custom compare function
struct Edge {
 int from, to, weight;
bool compare(const Edge& lhs, const Edge& rhs) {
  return lhs.weight > rhs.weight;
vector < Edge > edges;
sort(edges.begin(), edges.end(), compare);
/* #2: Define the '<' operator for a struct/class
 * Generally, for some type T define 'bool operator<(T other) const {}'</pre>
struct Edge {
 int from, to, weight;
  bool operator < (Edge other) const {</pre>
    return weight > other.weight;
vector < Edge > edges;
sort(edges.begin(), edges.end());
 * #3: Define 'operator()'
struct Edge {
  int from, to, weight;
};
```

```
class Compares {
  int ref_weight;

public:
    Compares(const int& weight) : ref_weight(weight) {}

    bool operator()(const Edge& lhs, const Edge& rhs) const {
        return lhs.weight > rhs.weight && lhs.weight >= ref_weight;
    }
};

// ...
Compares comp(100);
// ...
vector < Edge > edges;
// ...
sort(edges.begin(), edges.end(), comp);
```

9.3 CMake Configuration

Add to CMakeLists.txt:

```
project( some-project_)

# ^^ start of the CMakeLists.txt ...

# enable C++11
add_definitions("-std=c++11")

# enable all warnings
set(CMAKE_CXX_FLAGS_DEBUG "${CMAKE_CXX_FLAGS_DEBUG} -Wall")
set(CMAKE_CXX_FLAGS_RELEASE "${CMAKE_CXX_FLAGS_RELEASE} -Wall")

# enable debug always
set(CMAKE_BUILD_TYPE "Debug")

# additional information regarding the makefile creation, not really useful I think
set(CMAKE_VERBOSE_MAKEFILE ON)

# ... rest of the CMakeLists.txt ...
cmake_minimum_required(VERSION 2.6.2)
```

Debugging can also be enabled by calling cmake -DCMAKE_BUILD_TYPE=Debug, however this adds only the -g flag!

9.4 CMake and CGAL

```
# Step 0: IMPORTANT: first, create the C++ source code file

# Step 1: call CGAL CMake script
cgal_create_cmake_script

# Step 2: modify CMakeLists.txt if needed (adding C++11 support, debugging, etc.)
vim CMakeLists.txt

# or
nano CMakeLists.txt
# or ...

# Step 3: call CMake, don't forget the dot
cmake .

# Step 4: from now on always enough to call make
make

# Step 5: execute application
```

9.5 BGL

URL for normal graph functions: https://judge.inf.ethz.ch/doc/boost/libs/graph/doc/graph_concepts.html. Also good starting point is the "A Quick Tour of the Boost Graph Library" (see TOC).

```
#include <climits>
#include <iostream>
#include <vector>

#include <boost/graph/adjacency_list.hpp>
#include <boost/tuple/tuple.hpp> // tuples::ignore

// BGL algo specific includes ...
#include <boost/graph/dijkstra_shortest_paths.hpp>
#include <boost/graph/strong_components.hpp>
// .. end

using namespace std;
using namespace boost;

// Directed graph with int weights on edges.
typedef adjacency_list<vecS, vecS, directedS, no_property, property<edge_weight_t, int> > Graph;
```

```
// \dots or one with multiple properties for some fancy algorithm
typedef adjacency_list<vecS, vecS, directedS, property<vertex_name_t, string,
property<vertex_distance_t, int> >> Graph;
  // and don't forget:
  typedef property_map < Graph , vertex_name_t > :: type NameMap;
// Edge type (edge descriptor in BGL speak).
typedef graph_traits<Graph>::edge_descriptor Edge;
// Edge iterator.
typedef graph_traits < Graph > :: edge_iterator EdgeIterator;
// Out Edge iterator (directed graph)
typedef graph_traits < Graph >:: out_edge_iterator OutEdgeIterator;
// Map edge -> weight.
typedef property_map < Graph , edge_weight_t >: : type WeightMap;
void main() {
   // create graph with 'n' vertices
  Graph graph(n);
  // accessing a property map
  NameMap name_map = get(vertex_name, graph_instance);
  // iterate over all outgoing (directed graph) edges
OutEdgeIterator out_edge_iterator, out_edge_end;
  for(tie(out_edge_iterator, out_edge_end) = out_edges(some_vertices, graph);
    out_edge_iterator != out_edge_end;
    ++out_edge_iterator) {
// get the other end's vertex
int other_vertex = target(*out_edge_iterator, graph);
 }
}
```

9.6 CGAL: Linear/Quadratic Programming

typedef CGAL::Quadratic_program<IT> P;
typedef CGAL::Quadratic_program_solution<ET> S;

- The input type IT
 - Typically int or double

The exact type ET

(check in the manual)

- Requirement: input type can be converted to exact type
- ▶ int / double (not recommended)
- ► GMP
 - ★ CGAL::Gmpz integral numbers
 - ★ CGAL::Gmpq rational numbers
 - ★ CGAL::Gmpzf "floating point" numbers
- CGAL::MP_Float "floating point" numbers
- The solution type CGAL::Quotient<ET>

Multiplication in CGAL::MP_Float has complexity $\Theta(n^2)$, multiplication for the GMP number types uses a faster algorithm (depends on the magnitude), asymptotic runtime $\approx n^{<1.5}$

QuadraticProgram

$$\min x^{T} Dx + c^{T} x + c_{0}$$
s.t. $Ax \leq b$

$$\ell \leq x \leq u$$

 ${\tt NonnegativeQuadraticProgram}$

$$\min x^T Dx + c^T x + c_0$$
s.t. $Ax \leq b$

$$x \geq 0$$

LinearProgram

$$\min c^T x + c_0$$
s.t. $Ax \leq b$

$$\ell < x < u$$

NonnegativeLinearProgram

$$\min c^{T}x + c_{0}$$
s.t. $Ax \leq b$

$$x \geq 0$$

The solvers

solve_nonnegative_{linear/quadratic}_program() will completely ignore any manually set lower or upper bounds ℓ or u.

Debugging:

- Check the dimensions: lp.get_n(), lp.get_m()
- OCGAL::print_linear_program(std::cerr, lp, "lp");

Change the pivot rule

Bland's pivot rule avoids cycling (but it is slower...)

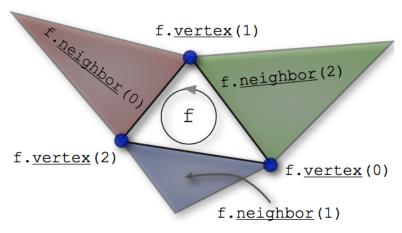
```
CGAL::Quadratic_program_options options;
options.set_pricing_strategy(CGAL::QP_BLAND);
Solution s = CGAL::SOLVER(program, ET(), options);
```

BUG - Don't Forget!

There is a bug in the assignment operator= for Solution objects...

9.7 CGAL: Approximation (Triangulation)

Nex image 'f' is a 'face handle'



Triangulation::Edge e;

// get the vertices of e

Triangulation::Vertex_handle v1 = e.first->vertex((e.second + 1) % 3);
Triangulation::Vertex_handle v2 = e.first->vertex((e.second + 2) % 3);

std::cout << "e = " << v1->point() << " <-> " << v2->point() << std::endl;

9.8 Matching

- Undirected graph G = (V, E)
- Is a subset $M \subseteq E$ of edges
- Each pair of edges of the matching set $(e_1, e_2 \in M)$ don't have a common vertices $v \in V$
- Or based on the vertices: Every pair of vertices $v_1, v_2 \in V$ aren't the start or end point of an edge $e \in M$
- Maximal Matching: If it's not possible to add another edge $e \in E$ M to M and M being a matching
- Maximum Matching/Maximum Cardinality Matching: A maximal matching with the largest amount of edges. There might exists multiple maximum matchings.

9.9 Vertex Cover

- Undirected graph G = (V, E)
- A vertex cover is a subset $V' \subseteq V$ such that for each edge $(u,v) =: e \in E \ u \in V'$ and/or $v \in V'$
- Minimal Vertex Cover: Generally NP-complete. Is the smallest possible vertex cover.

9.10 König's Theorem

- only for bipartite graphs
- The size of a maximum matching (maximum cardinality matching) is equal to the minimal vertex cover

Algorithm:

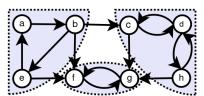
- 1. Let G = (V, E) be a undirected bipartite graph, i.e. $L \cup R = V \wedge L \cap R = \emptyset$
- 2. Calculate the Maximum Matching (Maximum Cardinality Matching), resulting in a matching $M \subseteq E$
- 3. Mark all vertices $v \in L$ that are not in M ($v \notin M$) as visited
- 4. Start at visited vertices and do a vertices search (DFS) from L to R along edges from V M and R to L along edges from M. Each such visited vertex is marked as visited
- 5. All unvisited vertices in L and all visited in R are part of the minimal vertex cover

9.11 Connected Component

- For undirected graphs
- Connected component is a subgraph of a graph where any two vertices in the subgraph are connected by a path, but no path exists to vertices to ones outside the subgraph

9.12 Strongly Connected Component

- For directed graphs
- Partitions a graph into subgraphs where each subgraph is strongly connected.
- Strongly Connected: A graph is strongly connected iff every vertex of the graph is reachable from every other vertex



From: https://commons.wikimedia.org/wiki/File:Scc.png

9.13 Biconnected Component / Articulation Points

See BGL documentation, it's pretty good. Otherwise this might help:

- **Biconnected Graph**: A connected graph is biconnected iff removing any single vertex (and all edges from/to this vertex) can't disconnect the graph. Such a graph doesn't contain *articulation points*!
- **Biconnected Components**: A subset of vertices where removing one of these vertices doesn't result in a disconnected graph inside the subgraph. Vertices can belong to multiple biconnected components!
- Articulation Points: These are the vertices that belong to more than one biconnected component. Such vertices are called *articulation points*. Removing such a articulation point would result in an increase of connected components (i.e. increase the number of graphs). No such articulation points means the graph is biconnected!

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