

Hypothesis Testing

Hypothesis testing in statistics is a fundamental method used to make inferences or draw conclusions about a population based on sample data. It involves formulating and testing hypotheses, which are statements about a population parameter, such as the mean or proportion.

Steps

1 Formulation of Hypotheses:

- **Null Hypothesis (H_0):** This is the hypothesis that there is no significant effect or difference, and it represents a statement of "no change" or "no difference". It's the hypothesis that is initially assumed to be true.
- **Alternative Hypothesis (H_1 or H_a):** This is the hypothesis that indicates the presence of an effect or a significant difference that the researcher aims to prove.

Steps

2 Choice of Test Statistic:

A test statistic is a standardized value derived from sample data, used to decide whether to reject the null hypothesis. It's calculated based on the data and the type of test being performed (e.g., t-test, chi-square test, Z-test).

Steps

3 Significance Level (α):

The significance level, often set at 0.05 (5%), is the probability of rejecting the null hypothesis when it is actually true (Type I error). It's a threshold for determining whether the observed data is sufficiently extreme to reject the null hypothesis.

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4 Calculation and Decision:

- Calculate the test statistic and compare it against a critical value determined by the chosen significance level, or calculate the p-value (probability of observing the data if the null hypothesis is true) and compare it with α .
- If the test statistic is more extreme than the critical value, or if the p-value is less than α , the null hypothesis is rejected in favor of the alternative hypothesis.

Types of Hypothesis Tests:

There are several types of hypothesis tests, each suitable for different kinds of data and research questions. Here are some of the main types:

Name of Test	Use Case	Type of Data	Main Goal	Example
Z-Test	Large sample size, known population standard deviation	Quantitative	Test mean against known population mean	Comparing average test scores to national average
One-sample T-Test	Unknown population standard deviation, single group vs known mean	Quantitative	Test mean against known population mean	Testing the mean salary of a small company against the industry average
Independent two-sample T-Test	Compare means of two independent groups	Quantitative	Test difference in means	Comparing average blood pressure between two groups
Paired T-Test	Compare means of the same or paired groups	Quantitative	Test difference in means	Testing the effect of a drug before and after treatment in the same patients
Chi-Square Goodness of Fit Test	Test if sample matches a population distribution	Categorical	Test fit to expected distribution	Testing if dice are fair based on rolled numbers
Chi-Square Test for Independence	Test independence between two categorical variables	Categorical	Test for association/independence	Examining if there's a relationship between gender and voting preference
One-way ANOVA	Compare means across groups split on one variable	Quantitative	Test difference in means across multiple groups	Comparing test scores across different teaching methods
Two-way ANOVA	Compare means across groups split on two variables	Quantitative	Test difference in means across multiple groups	Examining the effect of diet and exercise on weight loss
F-Test	Compare two population variances	Quantitative	Test equality of variances	Comparing variances of test scores between schools
Mann-Whitney U Test	Compare two groups, non-normal distribution	Quantitative	Test difference in medians	Comparing reaction times of two different age groups
Wilcoxon Signed-Rank Test	Compare two related samples or repeated measurements	Quantitative	Test difference in medians	Assessing pain levels before and after treatment in the same patients
Kruskal-Wallis H Test	Compare medians of three or more groups, non-normal distribution	Quantitative	Test difference in medians across multiple groups	Comparing exam scores across different study groups with varying study habits
Fisher's Exact Test	Compare two groups, small sample size, categorical data	Categorical	Test independence	Examining the relationship between smoking status and lung cancer incidence

Consideration of Errors:

- **Type I Error (false positive):** Rejecting the null hypothesis when it is actually true.
- **Type II Error:** Failing to reject the null hypothesis when it is actually false(**false negative**). The probability of a Type II error is denoted by β , and $(1 - \beta)$ is known as the power of the test.