

▼ Postavka Julie u Google Colab

Potrebno je preuzeti ovaj notebook, upload-ovati ga i pokrenuti kôd ispod prilikom kreiranja notebook-a za sve vježbe. Nakon pokretanja, potrebno je restartovati notebook. U *Runtime* kliknite na *Change runtime type* i odaberite Juliu i GPU. Sada možete koristiti Juliu za sve što radite.

U slučaju da vam krene izbacivati greške radi gubitka trenutne sesije izvršite sve naredbe opet i restartujte notebook.

```
!curl -sSL "https://julialang-s3.julialang.org/bin/linux/x64/1.5/julia-1.5.2-linux
!tar -xzf julia.tar.gz -C /usr --strip-components 1
!rm -rf julia.tar.gz*
!julia -e 'using Pkg; pkg"add IJulia; precompile"'
!echo "DONE"
```

```
Installing known registries into `~/.julia`
##### 100
Added registry `General` to `~/.julia/registries/General`
Resolving package versions...
Installed ZeroMQ_jll v4.3.2+5
Installed Artifacts v1.3.0
Installed MbedTLS_jll v2.16.8+1
Installed VersionParsing v1.2.0
Installed ZMQ v1.2.1
Installed IJulia v1.23.0
Installed Parsers v1.0.12
Installed MbedTLS v1.0.3
Installed Conda v1.5.0
Installed SoftGlobalScope v1.1.0
Installed JLLWrappers v1.1.3
Installed JSON v0.21.1
Downloading artifact: ZeroMQ
##### 100
Downloading artifact: MbedTLS
##### 100
Updating `~/.julia/environments/v1.5/Project.toml`
[7073ff75] + IJulia v1.23.0
Updating `~/.julia/environments/v1.5/Manifest.toml`
[56f22d72] + Artifacts v1.3.0
[8f4d0f93] + Conda v1.5.0
[7073ff75] + IJulia v1.23.0
[692b3bcd] + JLLWrappers v1.1.3
[682c06a0] + JSON v0.21.1
[739be429] + MbedTLS v1.0.3
[c8ffd9c3] + MbedTLS_jll v2.16.8+1
[69de0a69] + Parsers v1.0.12
[b85f4697] + SoftGlobalScope v1.1.0
[81def892] + VersionParsing v1.2.0
[c2297ded] + ZMQ v1.2.1
[8f1865be] + ZeroMQ_jll v4.3.2+5
[2a0f44e3] + Base64
[ade2ca70] + Dates
[8ba89e20] + Distributed
[7b1f6079] + FileWatching
```

```

[b77e0a4c] + InteractiveUtils
[76f85450] + LibGit2
[8f399da3] + Libdl
[56ddb016] + Logging
[d6f4376e] + Markdown
[a63ad114] + Mmap
[44cfe95a] + Pkg
[de0858da] + Printf
[3fa0cd96] + REPL
[9a3f8284] + Random
[ea8e919c] + SHA
[9e88b42a] + Serialization
[6462fe0b] + Sockets
[8dfed614] + Test
[cf7118a7] + UUIDs
[4ec0a83e] + Unicode
Building Conda → `~/ .julia/packages/Conda/x5ml4/deps/build.log`
Building IJulia → `~/ .julia/packages/IJulia/ljYVo/deps/build.log`
Precompiling project...

```

LAB. VJEŽBA 45

```

using LinearAlgebra
function rijesi_simplex(A, b, c)
    if(A==nothing||b==nothing||c==nothing||size(b,1)!=size(A,1)||size(c,2)!=size(A,1))
        error("Doslo je do greske!")
    end
    pomb=Array{Float64}(b)
    push!(pomb,0)
    simplex=hcata(pomb,vcat(A,c));
    J=vcat(Matrix{I,size(A,1),size(b,1)},zeros(1,size(A,1)))
    simplex=hcata(simplex,J)
    vrijednostVarijabliX=Array{Float64,1}()

    while(true)
        iteracija=rijesi_iteraciju(simplex)
        if(iteracija==-1)
            break
        end
    end

    for i=2:size(simplex,2)
        provjera1=false
        for j=1:size(simplex,1)-1
            provjera2=true
            if(simplex[j,i]==1)
                for k=1:size(simplex,1)-1
                    if(k!=j && simplex[k,i]!=0)
                        provjera2=false
                    end
                end
                if(provjera2==true)
                    push!(vrijednostVarijabliX,simplex[j,1])
                    provjera1=true
                    j=size(simplex,1)-1
                end
            end
        end
    end
end

```

```

        end
    end
end
    if(provjera1==false)
        push!(vrijednostVarijabliX,0)
    end

end
display(simplex)
return simplex[size(simplex,1),1]*(-1),vrijednostVarijabliX

end

function rijesi_iteraciju(simplex)
    najveciURedu=0
    k=1
    kolona=0
    x=0
    for x in simplex[size(simplex,1),2:end]
        if(x > najveciURedu)
            najveciURedu=x;
            kolona=k
        end
        k=k+1
    end
    kolona=kolona+1

    if (najveciURedu==0)
        return -1
    end

    najveciUKoloni=-1
    najveciUKoloni,index1=findmax(simplex[1:end-1,kolona])

    if (najveciUKoloni<=0)
        return -1
    end

    i=1;
    minKol=100000
    imin=0
    while(i<=size(simplex,1)-1)
        if(simplex[i,1]/simplex[i,kolona]<minKol && simplex[i,1]/simplex[i,kolona]:
            minKol=simplex[i,1]/simplex[i,kolona]
            imin=i
        end
        i=i+1
    end

    pivot= simplex[imin,kolona]

    for i=1:size(simplex,1)
        if(i==imin)
            for j=1:size(simplex,2)
                simplex[i,j]=simplex[i,j]*(1/pivot)
            end
        end
    end
end

```

```

        end
    end
end

for i=1:size(simplex,1)
    el=simplex[i,kolona]
    if(i!=imin)
        for j=1:size(simplex,2)
            simplex[i,j]=simplex[i,j]-(el*simplex[imin,j])
        end
    end
end
return simplex
end

```

rijesi_iteraciju (generic function with 1 method)

PRIMJER 1

```

c = [150 40]
A = [3 0; 0 2; 9 4]
b = [36; 54; 144 ]
optimalnoZ,vrijednostiX=rijesi_simplex(A,b,c);
println("Optimalna vrijednost funkcije cilja Z: ", optimalnoZ)
println("Vrijednosti varijabli x: ")
for i=1:size(vrijednostiX,1)
    println("x",i,"=", round(vrijednostiX[i]))
end

```

```

4×6 Array{Float64,2}:
 12.0  1.0  0.0  0.333333  0.0  0.0
 36.0  0.0  0.0  1.5      1.0 -0.5
  9.0  0.0  1.0 -0.75    0.0  0.25
-2160.0 0.0  0.0 -20.0    0.0 -10.0
Optimalna vrijednost funkcije cilja Z: 2160.0
Vrijednosti varijabli x:
x1=12.0
x2=9.0
x3=0.0
x4=36.0
x5=0.0

```

PRIMJER 3.9

```

c1 = [3 1]
A1 = [0.5 0.3; 0.1 0.2]
b1 = [150; 60]
optimalnoZ1,vrijednostiX1=rijesi_simplex(A1,b1,c1);
println("Optimalna vrijednost funkcije cilja Z: ", optimalnoZ1)
println("Vrijednosti varijabli x: ")
for i=1:size(vrijednostiX1,1)
    println("x",i,"=", round(vrijednostiX1[i]))
end

```

```

3x5 Array{Float64,2}:
 300.0  1.0   0.6   2.0  0.0
  30.0  0.0   0.14 -0.2  1.0
-900.0  0.0  -0.8  -6.0  0.0
Optimalna vrijednost funkcije cilja Z: 900.0
Vrijednosti varijabli x:
x1=300.0
x2=0.0
x3=0.0
x4=30.0

```

PRIMJER 3.10

```

c2 = [800 1000]
A2 = [30 16; 14 19; 11 26; 0 1]
b2 = [22800; 14100; 15950; 550]
optimalnoZ2,vrijednostiX2=rijesi_simplex(A2,b2,c2);
println("Optimalna vrijednost funkcije cilja Z: ", optimalnoZ2)
println("Vrijednosti varijabli x: ")
for i=1:size(vrijednostiX2,1)
    println("x",i,"=", round(vrijednostiX2[i]))
end

```

```

5x7 Array{Float64,2}:
1550.0  0.0  0.0   0.447977  -1.74566   1.0  0.0
 250.0  0.0  0.0   0.0404624 -0.0867052  0.0  1.0
 600.0  1.0  0.0   0.0549133 -0.0462428  0.0  0.0
 300.0  0.0  1.0  -0.0404624  0.0867052  0.0  0.0
-780000.0  0.0  0.0  -3.46821  -49.711   0.0  0.0
Optimalna vrijednost funkcije cilja Z: 780000.0
Vrijednosti varijabli x:
x1=600.0
x2=300.0
x3=0.0
x4=0.0
x5=1550.0
x6=250.0

```

PRIMJER 3.11

```

c3 = [1 2]
A3 = [-2 1; 0 1]
b3 = [1; 3]
optimalnoZ3,vrijednostiX3=rijesi_simplex(A3,b3,c3);
println("Optimalna vrijednost funkcije cilja Z: ", optimalnoZ3)
println("Vrijednosti varijabli x: ")
for i=1:size(vrijednostiX3,1)
    println("x",i,"=", round(vrijednostiX3[i]))
end

```



```

3x5 Array{Float64,2}:
 3.0  0.0  1.0  0.0  1.0
 1.0  1.0  0.0 -0.5  0.5
-7.0  0.0  0.0  0.5 -2.5
Optimalna vrijednost funkcije cilja Z: 7.0
Vrijednosti varijabli x:
x1=1.0
x2=3.0

```

Rješenje 2

using DelimitedFiles

```

function simplex_method(A,b)
    a_row = size(A, 1) + 1      #redovi
    a_col = size(A, 2) + size(A, 1) + 1    #kolone
    a = zeros((a_row, a_col))
    m = size(A,1)
    n = size(A,2)
    for i = 1 : m
        for j = 1 : n
            a[i + 1,j + 1] = A[i, j]
        end
    end
    B = zeros{Int8, 1, m + 1}
    for i = 1 : m
        B[i] = n + i
        a[i + 1,1] = b[i]
        for j = n + 2 : n + m + 1
            a[i + 1,j] = 0
        end
        a[i + 1, n + i + 1] = 1
    end
    for i = 1 : n
        a[1,i + 1] = c[i]
    end
    for j = n + 2 : n + m + 1
        a[1,j] = 0
    end
    a[1,1] = 0
    optimal = false
    println("Unesena matrica je: ")
    writedlm(stdout, a)

    #ITERACIJE DOK SE NE DODJE DO OPTIMUMA
    while(!optimal)
        cmax = -1
        q = 2
        for j = 2 : n + m + 1
            if a[1,j] > 0 && a[1,j] > cmax
                cmax = a[1,j]
                q = j
            end
        end
        p = 2
    end
end

```

```

tmax = Inf
if cmax == -1
    optimal = true
else
    for i = 2 : m + 1
        if a[i, q] > 0
            if a[i, 1] / a[i,q] < tmax
                tmax = a[i,1] / a[i,q]
                p = i
            end
        end
    end
    if tmax == Inf
        println("Rješenje je neograničeno")
        break;
    end
    B[p] = q-1
    # println(q) vodeca kolona
    pivot = a[p,q]
    # println(p) vodeci red
    for j = 1 : m + n + 1      #svodjenje pivota na 1
        a[p,j] = a[p,j] / pivot
    end
    for i = 1 : m + 1
        if i != p
            factor = a[i,q]
            for j = 1 : n + m + 1
                a[i,j] = a[i,j] - factor * a[p,j]
            end
        end
    end
    end
    end
    end

x = zeros((1, n + m + 1))
for j = 2 : n + m + 1
    x[j] = 0
end

for i = 2 : m+1
    x[B[i]] = a[i,1]
end
Z = a[1,1]
return x, Z
end

# main dio / probni dio zadatak 1 sa zadace 1
A = [1 1 ; 3 6]
b = [29 145]
c = [18 22]
(x, Z) = simplex_method(A,b)
println("Optimalno rješenje: ")
for i = 1 : size(x,2)
    println(x[i])
end

```

```
println("Funkcija cilja: ")  
Z = (-1) * Z  
print(Z)
```

Unesena matrica je:

0.0	18.0	22.0	0.0	0.0
29.0	1.0	1.0	1.0	0.0
145.0	3.0	6.0	0.0	1.0

Optimalno rješenje:

9.666666666666664

19.333333333333336

0.0

0.0

0.0

Funkcija cilja:

599.3333333333334